

# Sorting Algorithms!

Lab 06



# Sorting Algorithms

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- ▶ This is one of the few times Wikipedia is your friend.
  - ▶ [https://en.wikipedia.org/wiki/Bubble\\_sort](https://en.wikipedia.org/wiki/Bubble_sort)
  - ▶ [https://en.wikipedia.org/wiki/Selection\\_sort](https://en.wikipedia.org/wiki/Selection_sort)
  - ▶ [https://en.wikipedia.org/wiki/Insertion\\_sort](https://en.wikipedia.org/wiki/Insertion_sort)
- ▶ YouTube and other sites also have lots of visualisations of sorting algorithms which will walk you through how they work



# Bubble Sort

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- ▶ It is called bubble sort because it looks like it is ‘bubbling’ larger numbers to the top (right) of a list
- ▶ Bubble Sort works by repeatedly looping through a list and swapping adjacent numbers which aren’t in order until the list is sorted
  - ▶ E.g. [ ..., 4, 2, ...] -> [ ..., 2, 4, ...]
- ▶ Every time we loop through the list swapping pairs of numbers, we bring the next largest number to its sorted place in the top of the list



# Bubble Sort – How it Works

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- ▶ Bubble Sort works by repeatedly looping through a list and swapping adjacent numbers which aren't in order until the list is sorted
  
- ▶ Given a list of numbers containing  $n$  items
  
- ▶ Repeat the following  $n-1$  times:
  - ▶ Loop through all pairs of adjacent numbers in a list except for the top  $i$  numbers in the list where  $i$  is the number of passes we have made through the list already:
  
  - ▶ If two adjacent numbers are out of order:  
Swap those two numbers in the numbers list



# Bubble Sort – Example

- ▶ Given a list of numbers containing 4 items
- ▶ Repeat the following 3 times: # 1<sup>st</sup> Pass
  - ▶ Loop through all pairs of adjacent numbers in a list except the top i numbers:
  - ▶ If two adjacent numbers are out of order:  
Swap those two numbers in the numbers list

|    |    |    |    |
|----|----|----|----|
| 29 | 10 | 37 | 13 |
|----|----|----|----|

Out of order so we swap them

|    |    |    |    |
|----|----|----|----|
| 10 | 29 | 37 | 13 |
|----|----|----|----|

|    |    |    |    |
|----|----|----|----|
| 10 | 29 | 37 | 13 |
|----|----|----|----|

In order so we don't do anything

|    |    |    |    |
|----|----|----|----|
| 10 | 29 | 37 | 13 |
|----|----|----|----|

Out of order so we swap them

|    |    |    |    |
|----|----|----|----|
| 10 | 29 | 13 | 37 |
|----|----|----|----|



# Bubble Sort – Example

- ▶ Given a list of numbers containing 4 items
- ▶ Repeat the following 3 times: # 2<sup>nd</sup> Pass
  - ▶ Loop through all pairs of adjacent numbers in a list except the top i numbers:
  - ▶ If two adjacent numbers are out of order:  
Swap those two numbers in the numbers list

|    |    |    |           |
|----|----|----|-----------|
| 10 | 29 | 13 | <u>37</u> |
|----|----|----|-----------|

In order so we don't do anything

|    |    |    |           |
|----|----|----|-----------|
| 10 | 29 | 13 | <u>37</u> |
|----|----|----|-----------|

Out of order so we swap them

|    |    |    |           |
|----|----|----|-----------|
| 10 | 13 | 29 | <u>37</u> |
|----|----|----|-----------|

|    |    |           |           |
|----|----|-----------|-----------|
| 10 | 13 | <u>29</u> | <u>37</u> |
|----|----|-----------|-----------|

We don't need to check the top number because we know it is in the correct position



# Bubble Sort – Example

- ▶ Given a list of numbers containing 4 items
- ▶ Repeat the following 3 times: # 3<sup>rd</sup> Pass
  - ▶ Loop through all pairs of adjacent numbers in a list except the top i numbers:
  - ▶ If two adjacent numbers are out of order:  
Swap those two numbers in the numbers list

|    |    |           |           |
|----|----|-----------|-----------|
| 10 | 13 | <u>29</u> | <u>37</u> |
|----|----|-----------|-----------|

In order so we don't do anything

|    |           |           |           |
|----|-----------|-----------|-----------|
| 10 | <u>13</u> | <u>29</u> | <u>37</u> |
|----|-----------|-----------|-----------|

We don't need to compare the top two numbers because we know they are in order

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <u>10</u> | <u>13</u> | <u>29</u> | <u>37</u> |
|-----------|-----------|-----------|-----------|

We know 10 must be sorted because the larger numbers are all above it on the last pass



# Selection Sort

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- ▶ We repeatedly loop through a list of numbers and select the  $n^{\text{th}}$  largest number and will swap that number with the number in the  $-n^{\text{th}}$  position in the list.
- ▶ E.g.
  - ▶ [2, 5, 4, 1, 3]  
5 is the 1<sup>st</sup> largest number in the list, so we swap it with the number in the -1<sup>st</sup> (last) position in the list  
-> [2, 3, 4, 1, 5]





# Selection Sort – How it Works

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- ▶ We repeatedly loop through a list of numbers and select the  $n^{\text{th}}$  largest number and swap that number with the number in the  $-n^{\text{th}}$  position in the list.
- ▶ Given a list of numbers containing  $n$  items
- ▶ Repeat the following  $n-1$  times:
  - ▶ Find the index of the largest number from the first  $n-i$  items (where  $i$  is the number of passes we have made through the list)
  - ▶ Swap that number with the number in the  $-(i+1)^{\text{th}}$  place in the list



# Selection Sort – Example

- ▶ Given a list of numbers containing  $n$  items
- ▶ Repeat the following  $n-1$  times: # 1<sup>st</sup> pass
  - ▶ Find the index of the largest number from the first  $n-i$  items
  - ▶ Swap that number with the number in the  $-(i+1)^{\text{th}}$  place in the list

|    |    |    |    |
|----|----|----|----|
| 29 | 10 | 37 | 13 |
|----|----|----|----|

37 is the 1st largest number

|    |    |    |           |
|----|----|----|-----------|
| 29 | 10 | 13 | <u>37</u> |
|----|----|----|-----------|

We swap 37 with the last number in the list



# Selection Sort – Example

- ▶ Given a list of numbers containing  $n$  items
- ▶ Repeat the following  $n-1$  times: # 2<sup>nd</sup> pass
  - ▶ Find the index of the largest number from the first  $n-i$  items
  - ▶ Swap that number with the number in the  $-(i+1)^{\text{th}}$  place in the list

|    |    |    |           |
|----|----|----|-----------|
| 29 | 10 | 13 | <u>37</u> |
|----|----|----|-----------|

29 is the 2nd largest number  
(or the largest number of the  
first 3 numbers)

|    |    |           |           |
|----|----|-----------|-----------|
| 13 | 10 | <u>29</u> | <u>37</u> |
|----|----|-----------|-----------|

We swap 29 with the second to  
last number in the list



# Selection Sort – Example

- ▶ Given a list of numbers containing  $n$  items
- ▶ Repeat the following  $n-1$  times: # 3<sup>rd</sup> pass
  - ▶ Find the index of the largest number from the first  $n-i$  items
  - ▶ Swap that number with the number in the  $-(i+1)^{\text{th}}$  place in the list

**13**    10    29    37

13 is the 3<sup>rd</sup> largest number  
(or the largest number of the  
first 2 numbers)

**10**    **13**    29    37

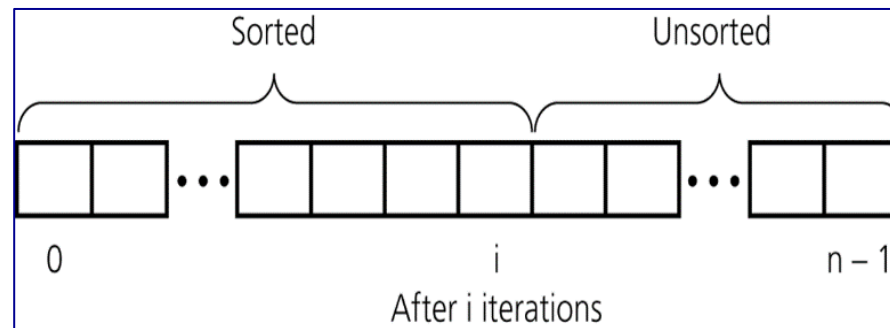
We swap 13 with the third to  
last number in the list

10    13    29    37

Like with bubble sort – we now  
know 10 is also in the right  
position

# Insertion Sort

- ▶ We slowly build up a list of sorted numbers by inserting the unsorted numbers from the input list into the correct position one at a time
- ▶ However, we do this by shifting numbers around in the same list and keeping track of what part is sorted and what part is unsorted





# Insertion Sort – How it Works

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- ▶ We slowly build up a list of sorted numbers by inserting the unsorted numbers from the input list into the correct position one at a time
- ▶ Given a list of numbers containing  $n$  items
- ▶ Repeat the following  $n-1$  times:
  - ▶ Divide list into sorted (left –  $i+1$  elements) and an unsorted part (right) where  $i$  is the number of passes we have currently done
  - ▶ In each pass take left most element from unsorted part and place it into correct position of sorted part



# Insertion Sort – Example

- ▶ Given a list of numbers containing  $n$  items
- ▶ Repeat the following  $n-1$  times: **# 1st pass**
  - ▶ Divide list into sorted (left –  $i+1$  elements) and an unsorted part (right) where  $i$  is the number of passes we have currently done
  - ▶ In each pass take left most element from unsorted part and place it into correct position of sorted part

29 | 10 37 13

10 is the first unsorted element

10 29 | 37 13

We insert 10 into the correct position in the sorted list



# Insertion Sort – Example

- ▶ Given a list of numbers containing  $n$  items
- ▶ Repeat the following  $n-1$  times: **# 2nd pass**
  - ▶ Divide list into sorted (left –  $i+1$  elements) and an unsorted part (right) where  $i$  is the number of passes we have currently done
  - ▶ In each pass take left most element from unsorted part and place it into correct position of sorted part

|           |           |  |    |    |
|-----------|-----------|--|----|----|
| <u>10</u> | <u>29</u> |  | 37 | 13 |
|-----------|-----------|--|----|----|

37 is the first unsorted element

|           |           |  |    |  |    |
|-----------|-----------|--|----|--|----|
| <u>10</u> | <u>29</u> |  | 37 |  | 13 |
|-----------|-----------|--|----|--|----|

We insert 37 into the correct position in the sorted list





# Insertion Sort – Example

- ▶ Given a list of numbers containing  $n$  items
- ▶ Repeat the following  $n-1$  times: **# 3rd pass**
  - ▶ Divide list into sorted (left –  $i+1$  elements) and an unsorted part (right) where  $i$  is the number of passes we have currently done
  - ▶ In each pass take left most element from unsorted part and place it into correct position of sorted part

|           |           |           |  |    |
|-----------|-----------|-----------|--|----|
| <u>10</u> | <u>29</u> | <u>37</u> |  | 13 |
|-----------|-----------|-----------|--|----|

13 is the first unsorted element

|           |           |           |           |  |
|-----------|-----------|-----------|-----------|--|
| <u>10</u> | <u>13</u> | <u>29</u> | <u>37</u> |  |
|-----------|-----------|-----------|-----------|--|

We insert 13 into the correct position in the sorted list



# Binary Search!

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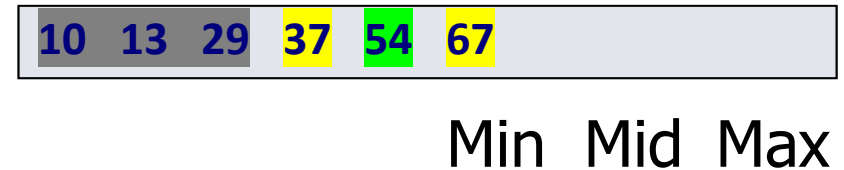
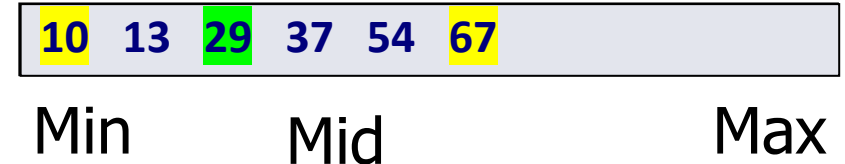
- ▶ Useful for searching through sorted data quickly ( $\log(n)$  time!!!)
- ▶ Pros: Quick
- ▶ Cons: Data has to be sorted



# Binary Search Example

- ▶ Given a sorted list of  $n$  items
- ▶ Set the current `max_index` to the last index
- ▶ Set the current `min_index` to the first index
- ▶ While the `max_index` is bigger than the `min_index`:
  - ▶ Calculate the `mid_index` by getting the average of the `max` and `min` indices
  - ▶ If the value at the `mid_index` == the search value we can return
  - ▶ If the value at the `mid_index` is less than the search value we know the search value is going to be above the `mid_index`.
    - ▶ Set the `min_index` to the index above the `mid_index`
  - ▶ Otherwise:
    - ▶ Set the `max_index` to one below the `mid_index`
- ▶ If we get outside the while loop the value is not in the list

Search Value = 54



We found our search value!



# CodeRunner

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- ▶ **Bubble Sort**
    - ▶ Test case
    - ▶ Implement the bubble sort
  - ▶ **Selection Sort**
    - ▶ Test case
    - ▶ Get the largest element
    - ▶ Implement the selection sort
  - ▶ **Insertion Sort**
    - ▶ Test case
    - ▶ Shifting elements
    - ▶ Implement the insertion sort
  - ▶ **Binary search function**
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# IMPORTANT CODERUNNER TIP!!

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- ▶ A lot of the code for these questions might be shorter than you think!
- ▶ It is *really really* helpful to get a pencil and paper and try doing these algorithms by hand thinking carefully about what operations you need to do in what order if you're not familiar with them
- ▶ If your code is starting to get super duper long – it might be time to rethink your approach