SymPy generated orbital functions

Orbitals are constructed in the following fashion:

$$\phi(\vec{r})_{n,l,m} = L^{2l+1}_{n-l-1}\left(\frac{2r}{n}k\right)S^m_l(\vec{r})e^{-\frac{r}{n}k}$$

where n is the principal quantum number, $k = \alpha Z$ with Z being the nucleus charge and α being the variational parameter.

$$l = 0,\ 1,\ ...,\ (n-1)$$

$$m = -l,\ (-l+1),\ ...,\ (l-1),\ l$$

$\phi_0 \rightarrow \phi_{1,0,0}$	
$\phi(\vec{r})$	1
$\vec{i} \cdot \nabla\phi(\vec{r})$	$-\frac{kx}{r}$
$\vec{j} \cdot \nabla\phi(\vec{r})$	$-\frac{ky}{r}$
$\vec{k} \cdot \nabla\phi(\vec{r})$	$-\frac{kz}{r}$
$\nabla^2\phi(\vec{r})$	$\frac{k(kr-2)}{r}$

Table 1: Orbital expressions hydrogenicOrbitals : 1, 0, 0. Factor e^{-kr} is omitted.

$\phi_1 \rightarrow \phi_{2,0,0}$	
$\phi(\vec{r})$	$kr - 2$
$\vec{i} \cdot \nabla\phi(\vec{r})$	$-\frac{kx(kr-4)}{2r}$
$\vec{j} \cdot \nabla\phi(\vec{r})$	$-\frac{ky(kr-4)}{2r}$
$\vec{k} \cdot \nabla\phi(\vec{r})$	$-\frac{kz(kr-4)}{2r}$
$\nabla^2\phi(\vec{r})$	$\frac{k(kr-8)(kr-2)}{4r}$

Table 2: Orbital expressions hydrogenicOrbitals : 2, 0, 0. Factor $e^{-\frac{1}{2}kr}$ is omitted.

$\phi_2 \rightarrow \phi_{2,1,0}$	
$\phi(\vec{r})$	z
$\vec{i} \cdot \nabla\phi(\vec{r})$	$-\frac{kxz}{2r}$
$\vec{j} \cdot \nabla\phi(\vec{r})$	$-\frac{kyz}{2r}$
$\vec{k} \cdot \nabla\phi(\vec{r})$	$-\frac{kz^2-2r}{2r}$
$\nabla^2\phi(\vec{r})$	$\frac{kz(kr-8)}{4r}$

Table 3: Orbital expressions hydrogenicOrbitals : 2, 1, 0. Factor $e^{-\frac{1}{2}kr}$ is omitted.

$\phi_3 \rightarrow \phi_{2,1,1}$	
$\phi(\vec{r})$	x
$\vec{i} \cdot \nabla \phi(\vec{r})$	$-\frac{kx^2-2r}{2r}$
$\vec{j} \cdot \nabla \phi(\vec{r})$	$-\frac{kxy}{2r}$
$\vec{k} \cdot \nabla \phi(\vec{r})$	$-\frac{kxz}{2r}$
$\nabla^2 \phi(\vec{r})$	$\frac{kx(kr-8)}{4r}$

Table 4: Orbital expressions hydrogenicOrbitals : 2, 1, 1. Factor $e^{-\frac{1}{2}kr}$ is omitted.

$\phi_4 \rightarrow \phi_{2,1,-1}$	
$\phi(\vec{r})$	y
$\vec{i} \cdot \nabla \phi(\vec{r})$	$-\frac{kxy}{2r}$
$\vec{j} \cdot \nabla \phi(\vec{r})$	$-\frac{ky^2-2r}{2r}$
$\vec{k} \cdot \nabla \phi(\vec{r})$	$-\frac{kyz}{2r}$
$\nabla^2 \phi(\vec{r})$	$\frac{ky(kr-8)}{4r}$

Table 5: Orbital expressions hydrogenicOrbitals : 2, 1, -1. Factor $e^{-\frac{1}{2}kr}$ is omitted.