

# Interstellar Interceptors

Mission design for rendezvous with objects in hyperbolic orbits

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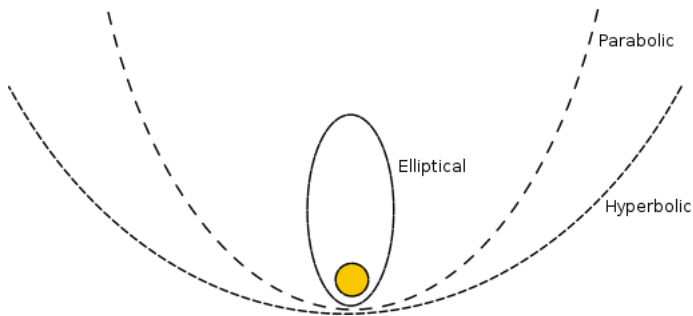
Universidad Internacional de Valencia

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# What are interstellar objects?

## Definition

Interstellar objects (ISOs) are asteroids, comets or planetary bodies moving through interstellar medium (ISM) without being gravitationally bound to a star.



ISOs follow hyperbolic orbits

# Why are interstellar objects important?

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- Exploring their physical and chemical composition
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## Motivation of this work

Design orbits for rendezvous with ISOs to study their physical properties.

# Discovered interstellar objects

There are two confirmed ISOs to this day:



1I/'Oumuamua

ESO's VLT and GST Telescopes

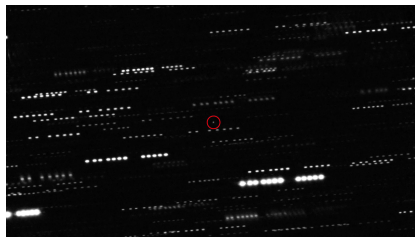


2I/Borisov

NASA Hubble Space Telescope

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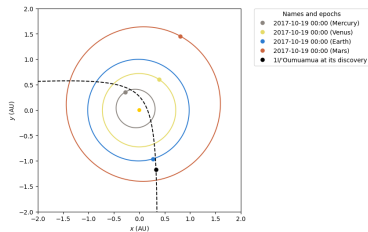
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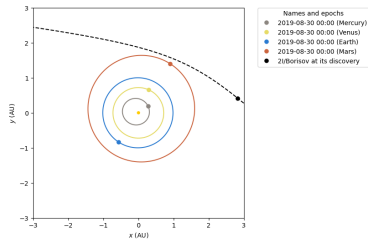
These interlopers present the following orbit attributes:

- Hyperbolic orbits
- High relative velocity w.r.t. the Sun
- Random inclination
- Discovered close to the direction of the Solar Apex

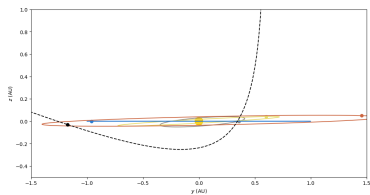
# Orbits of 1I/'Oumuamua and 2I/Borisov



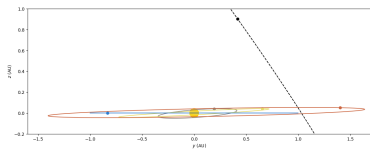
1I/'Oumuamua orbit top view



2I/Borisov orbit top view



1I/'Oumuamua orbit side view

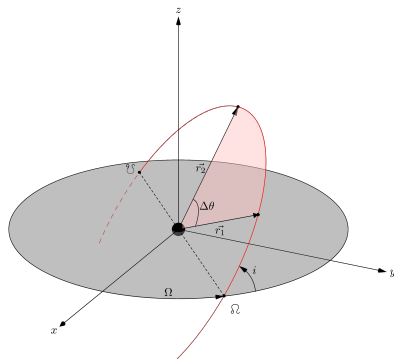


2I/Borisov orbit side view



# Navigating through space: the Lambert's problem

Lambert's problem is the Boundary Value Problem (BVP) in the context of the restricted two-body problem dynamics.

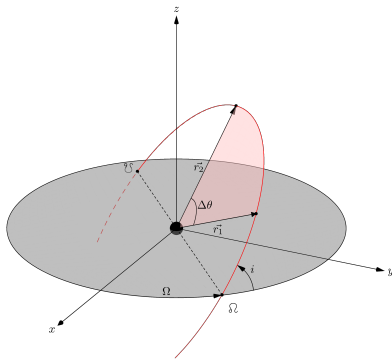


$$\ddot{\vec{r}} = -\frac{\mu}{r^3}\vec{r} \quad \left\{ \begin{array}{l} \vec{r}(t_1) = \vec{r}_1 \\ \vec{r}(t_2) = \vec{r}_2 \end{array} \right.$$

Geometry of the Lambert's problem

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Solve for the orbit which passes through  $\vec{r}_1$  and  $\vec{r}_2$  over a finite amount of time  $\Delta t = t_2 - t_1$ .

# Estimating the cost of the maneuver using the $C_3$ energy

Lambert's problem computes the initial velocity  $\vec{v}_1$  and final velocity  $\vec{v}_2$  of the orbit.

- First impulse:  $\Delta v_1 = \|\vec{v}_1 - \vec{v}_{\text{origin}}\|$
- Last impulse:  $\Delta v_2 = \|\vec{v}_2 - \vec{v}_{\text{iso}}\|$

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The total cost of the maneuver is  $\Delta v = \Delta v_1 + \Delta v_2$ . This relates with the fuel mass via the Tsiolkovsky rocket equation:

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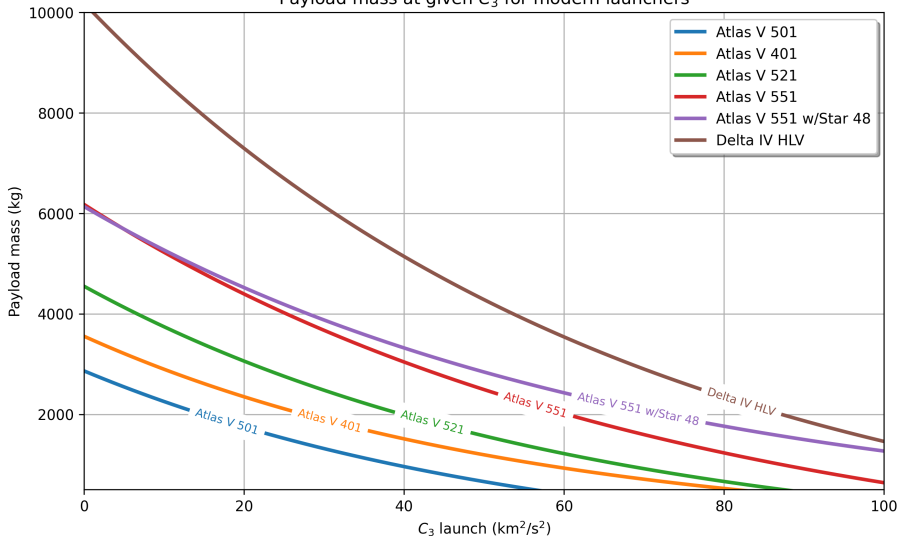
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The characteristic energy for hyperbolic orbits  $C_3$  is defined as:

$$C_3 = v_{\infty}^2$$

# Modern launching technologies

Payload mass at given  $C_3$  for modern launchers



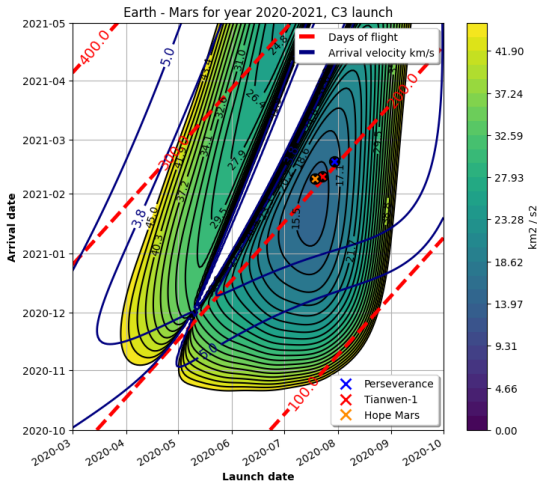
Maximum payload mass vs.  $C_3$  energy for different launchers

# Minimizing the cost of the maneuver

Porkchop plots are used to find the optimal launch and arrival dates by solving Lambert's problem for a variety of trajectories.

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Porkchop plot between Earth and Mars



# Analyzed scenarios

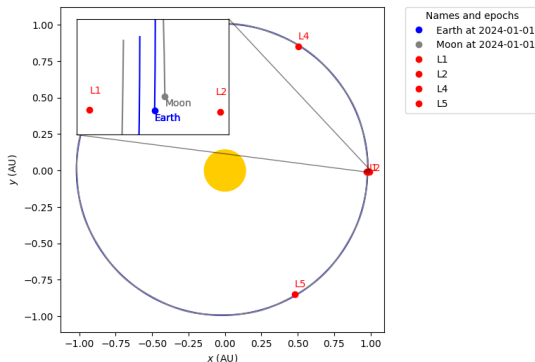
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- Direct transfer between the Earth and the ISO
- Direct transfer between the L2 point and the ISO

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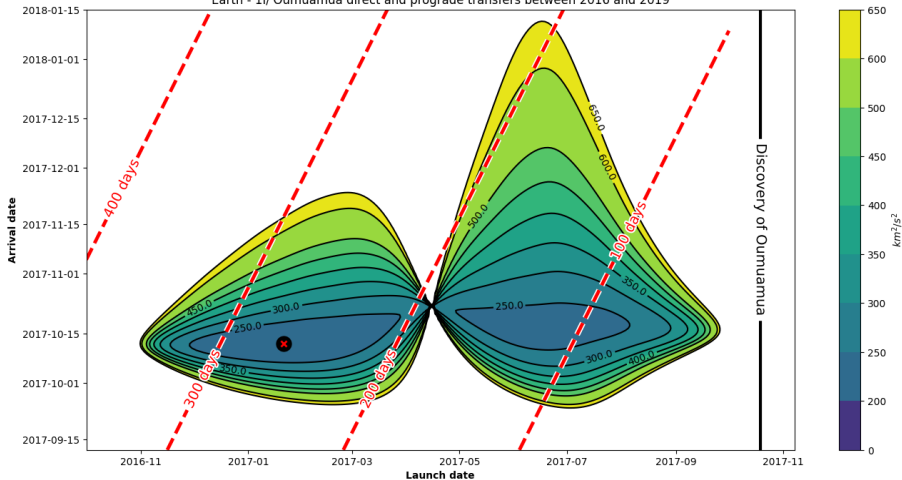
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Lagrange points for the Sun Earth-Moon system

# 1I/'Oumuamua: direct prograde transfer from Earth

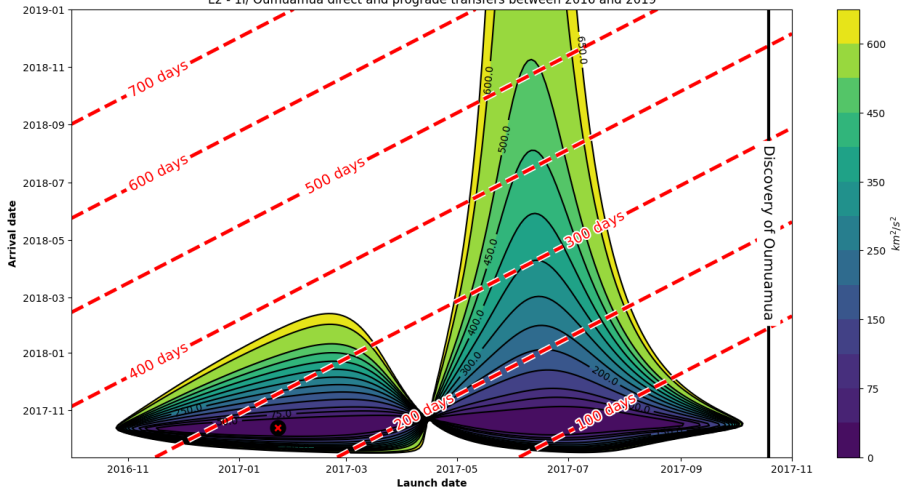
Detailed launch energy  $C_3$  and time of flight  
Earth - 1I/'Oumuamua direct and prograde transfers between 2016 and 2019



Direct transfer from Earth

# 1I/'Oumuamua: direct prograde transfer from L2

Detailed launch energy  $C_3$  and time of flight  
L2 - 1I/'Oumuamua direct and prograde transfers between 2016 and 2019



Direct transfer from L2

# 1I/'Oumuamua: summary of results

$\Delta v$ launch Earth [km/s]	$\Delta v$ launch L2 [km/s]	Reduction [%]
13.85	3.80	72.56

Launch energy comparison

$\Delta V$ arrival Earth [km/s]	$\Delta V$ arrival L2 [km/s]	Reduction [%]
62.33	61.46	1.40

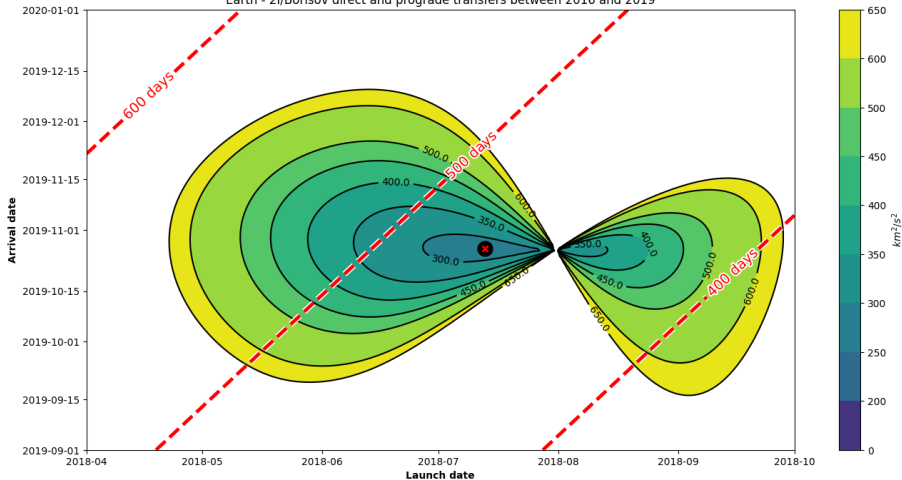
Arrival velocity comparison

$C_3$ launch Earth [km <sup>2</sup> /s <sup>2</sup> ]	$C_3$ launch L2 [km <sup>2</sup> /s <sup>2</sup> ]	Reduction [%]
192.00	14.41	92.51

Characteristic energy comparison

# 2I/Borisov: direct prograde transfer from Earth

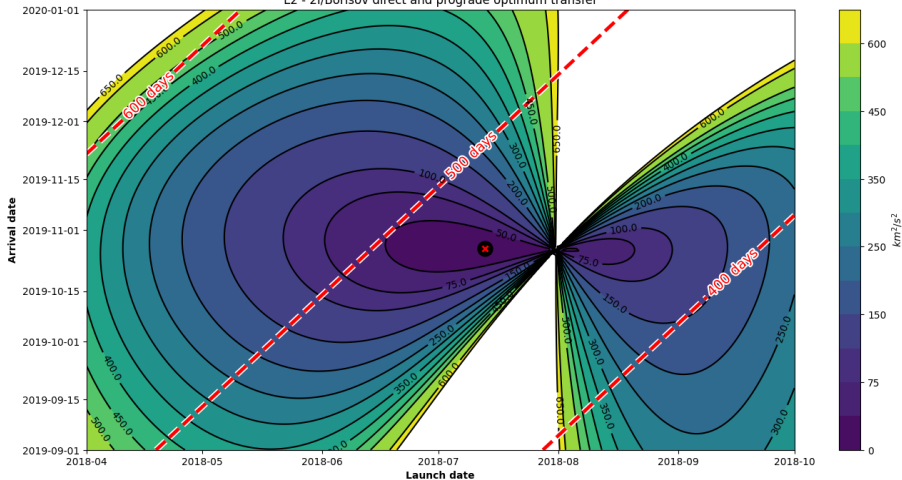
Detailed launch energy  $C_3$  and time of flight  
Earth - 2I/Borisov direct and prograde transfers between 2016 and 2019



Direct transfer from Earth

# 2I/Borisov: direct prograde transfer from L2

Detailed launch energy  $C_3$  and time of flight  
L2 - 2I/Borisov direct and prograde optimum transfer



Direct transfer from Earth

## 21/Borisov: summary of results

$\Delta v$ launch Earth [km/s]	$\Delta v$ launch L2 [km/s]	Reduction [%]
16.90	5.85	65.38

Launch energy comparison

$\Delta V$ arrival Earth [km/s]	$\Delta V$ arrival L2 [km/s]	Reduction [%]
33.00	33.02	-0.06

Arrival velocity comparison

$C_3$ launch Earth [km <sup>2</sup> /s <sup>2</sup> ]	$C_3$ launch L2 [km <sup>2</sup> /s <sup>2</sup> ]	Reduction [%]
286.00	34.30	88.08

Characteristic energy comparison



# Conclusions

## L2 as the optimal launching point

Launching an intercepting spacecraft from L2 is more fuel efficient. These results agree with the ones presented by the Comet Interceptor mission.

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## Need of increased vigilance in the search for ISOs

Both optimum transfer dates take place prior the discovery of 1I/'Oumuamua and 2I/Borisov. Surveillance of the sky is crucial to detect future ISOs.

# Future work

## Generating a synthetic population of ISOs

Synthetic orbits of ISOs can be generated by using Monte-Carlo simulations. This could allow to predict future ISO encounters.

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## Drafting optimum transfers

Optimum transfers can be solved for previous synthetic data. Solutions would be used by future missions parked at L2.

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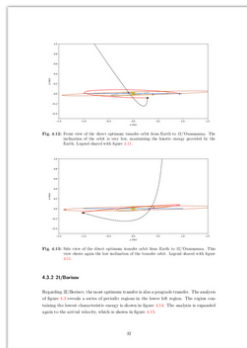
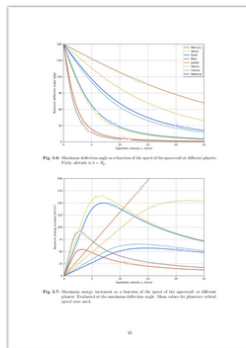
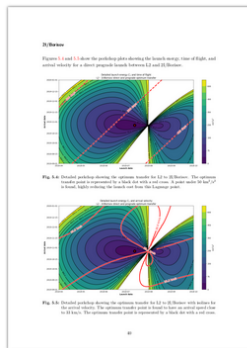
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## Trajectory optimization

A combination of multiple gravity assists and deep space maneuvers may allow for a more efficient transfer to an ISO, depending on the scenario.

# References

All this work is reproducible, including figures and results.



Document and figures generated via LaTeX and Python

Official repository

All source code is hosted in <https://github.com/jorgepiloto/tfm>

# Additional materials: 1I/'Oumuamua shape

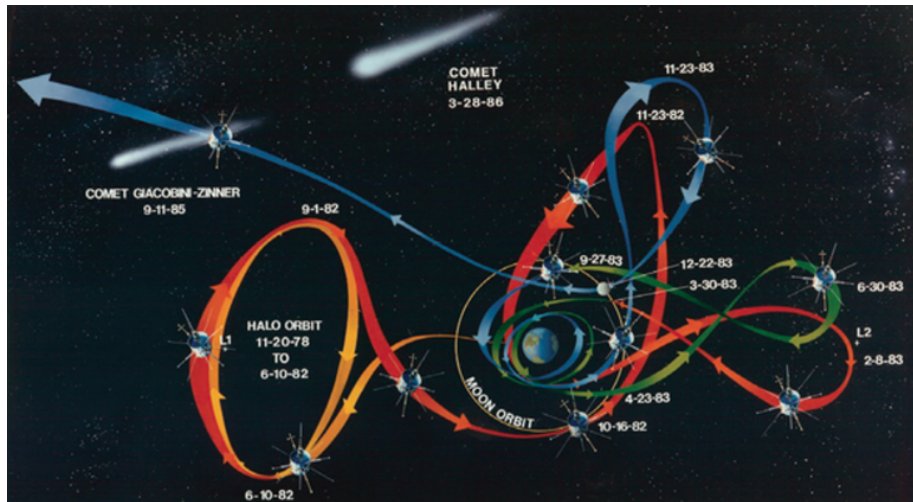


1I/'Oumuamua shape

Illustration by William Hartmann/Michael Belton/AP

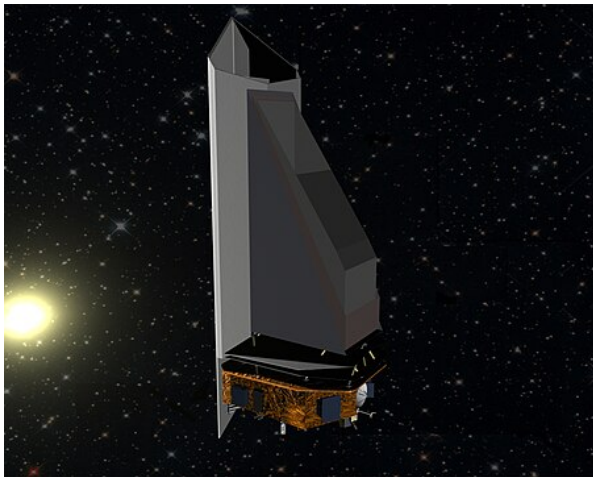


# Additional materials: ISEE-3 mission



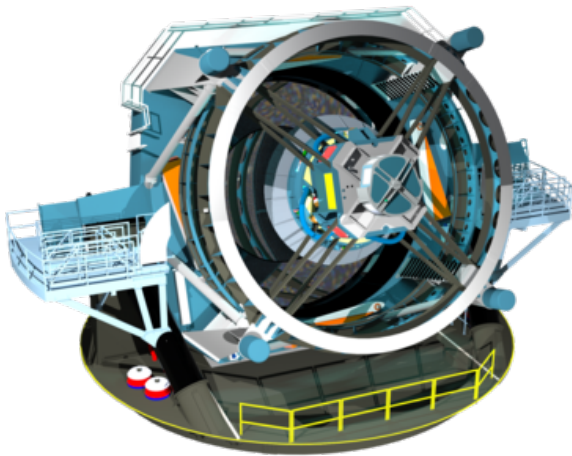
ISEE-3 mission  
Illustration by NASA

# Additional materials: NEO surveyor



NEO surveyor  
Illustration by NASA

# Additional materials: Large Synoptic Survey Telescope



LSST

Illustration by LSST Project Office