DS and Graph Compression

May 10, 2024

1 Path Visualizer

1.1 What is this?

This notebook accomplishes the following: 1) **Downloading** and **formatting** data in a form usable by the **Parallang Simulator**. 2) **Visualization** of the true shortest route between **any two points** on the graph. 3) **Reading** and **visualization** of the output of the **Parallang Simulator** for comparison.

1.2 How do I start?

Begin by **installing and importing the below modules**. Then, read the instructions in each section carefully to find what needs to be changed.

```
[]: !pip3 install matplotlib !pip3 install osmnx
```

```
[]: import matplotlib.pyplot as plt
import networkx as nx
import osmnx as ox
import os
import pprint
import random
from collections import defaultdict
```

1.3 Section 1: Downloading of Data

Set the below variables and run the rest of the blocks in this section before continuing.

```
[]: # CONSTANTS: Useful if you need something specific.

SOUTHERN_ENGLAND = ['Bristol, UK', 'Cornwall, UK', 'Devon, UK', 'Dorset, UK', \u00c4

\u00c4'Gloucestershire, UK', 'Somerset, UK', 'Wiltshire, UK', 'Berkshire, UK', \u00c4

\u00c4'Buckinghamshire, UK', 'West Sussex, UK', 'East Sussex, UK', 'Kent, UK', \u00c4

\u00c4'Oxfordshire, UK', 'Hampshire, UK', 'Isle of Wight, UK', 'Surrey, UK', 'City \u00c4

\u00c4of London, UK', 'Greater London, UK', 'Bedfordshire, UK', 'Cambridgeshire, \u00c4

\u00c4UK', 'Hertfordshire, UK', 'Essex, UK', 'Norfolk, UK', 'Suffolk, UK']
```

```
# CHANGE ME: Location to get data from.
    place_name = "Stroud, UK"
    # Optional (not recommended to change): Change me if you want a different type_
     ⇔of graph. Defaultly just paths you can drive.
    mode = None
    # Optional: It's a whitelist filter that filters out unwanted edges. For large \Box
     ⇒queries, consider implementing a motorway filter
    # All others: custom_filter = ___
     # Southern England: '["highway"~"motorway"]'
    # Sizes (post-compression):
         * Southern England (1351) <- 29795 (originally)
        * Gloucestershire (991) <- 17941
        * Bristol (762)
                                <- 8479
        * Southampton (455)
                                <- 7188
                                <- 3941
        * Cheltenham (267)
                                <- 3570
        * Stroud (110)
        * Bishop's Cleeve (50) <- 489
    custom_filter =
     - '["highway"~"primary|primary|link|secondary|secondary|link|tertiary|tertiary|link"]
    # Optional: Change me if you want a directed graph
    directed = False
    # Optional: Whether to apply graph compression
    apply_graph_compression = True & (not directed)
    # Optional: Whether to truncate
    truncate_to = 400000
    # Optional: Number of datasets to generate
    num datasets = 1
    # CHANGE ME: Location to store edge list in.
    filename = f"analyzed_datasets/{place_name}"
    # Optional: Whether to output verbosely.
    ox.settings.log_console = True
[]: # must set simplify to false, otherwise the simplification ratios of this.
     →technique will be terrible!
    graph = ox.graph_from_place(place_name, network_type=mode, simplify=not_
     →apply_graph_compression, custom_filter=custom_filter)
```

```
if not directed:
    graph = ox.utils_graph.get_undirected(graph)

nodes, edges = ox.graph_to_gdfs(graph)

print("Graph downloaded.")
```

```
[]: translations = {}
     nextid = 0
     shortest_direct_distances = {}
     # length is in meters
     lengths = edges[["osmid", "length"]]
     print("Formatting graph...")
     for u, u keyed df in lengths.groupby(level=0):
         for v, uv_keyed_df in u_keyed_df.groupby(level=1):
             if u not in translations:
                 translations[u] = nextid
                 nextid += 1
             if v not in translations:
                 translations[v] = nextid
                 nextid += 1
             for (i, length) in enumerate(uv_keyed_df["length"]):
                 shortest_direct_distances[(translations[u], translations[v])] = ___
      min(int(length*1000), shortest_direct_distances.get((u, v), float("inf")))
                 if not directed:
                     shortest_direct_distances[(translations[v], translations[u])] = ___
      ⇒shortest_direct_distances[(translations[u], translations[v])]
     inverted_translations = {v: k for (k, v) in translations.items()}
     two_valency_nodes = set()
     if apply_graph_compression:
         print("Beginning compression...")
         edge_list_dict = defaultdict(set)
         for ((e1, e2), d) in shortest_direct_distances.items():
             if e1 == e2: continue
             edge list dict[e1].add(e2)
             edge_list_dict[e2].add(e1)
         edge_list_dict = {k: list(v) for (k, v) in edge_list_dict.items()}
         # first, find the two valency nodes
         for n in edge_list_dict:
             if len(edge_list_dict[n]) == 2:
                 two_valency_nodes.add(n)
```

```
print(f"Found {len(two_valency_nodes)} two valency nodes, finding paths...")
  collapsed_paths = []
  i = 0
  visited = set()
  for n in two_valency_nodes:
      if n in visited:
           continue
      left search = []
      right search = []
      left_search = [n, edge_list_dict[n][0]]
      right_search = [edge_list_dict[n][1]]
      visited.add(n)
      for search in [left_search, right_search]:
          two_in_search = any(2 in s for s in [left_search, right_search])
          if not search:
              continue
          while search[-1] in two_valency_nodes and any(k not in visited for_
→k in edge_list_dict[search[-1]]):
              visited.add(search[-1])
              k = edge_list_dict[search[-1]][0]
              if k in visited:
                   k = edge_list_dict[search[-1]][1]
               search.append(k)
      collapsed_paths.append((list(reversed(right_search)) + left_search)[1:
-1])
  print(f"Collapsed to {len(collapsed_paths)} paths, compressing them...")
  better egress = {}
  path_length = {}
  node_to_path_id = {}
  collapsed_paths_dict = {}
  egresses_to_path_id = defaultdict(list)
  path_id_to_egresses = {}
  path_id = 0
  for p in collapsed_paths:
      # # don't resolve stand-alone cycles
      # if edge_list_dict[p[-1]] in edge_list_dict[p[0]]:
            continue
      collapsed_paths_dict[path_id] = p
      k = edge_list_dict[p[0]][0]
```

```
if k in visited:
           k = edge_list_dict[p[0]][1]
      j = edge_list_dict[p[-1]][0]
      # some paths will be one node.
      # in such a scenario, you need to
      # ensure differing endpoints are used
      # as p[-1] and p[0] will be the same
      # and hence the len(p) == 1 check
      if j in visited or len(p) == 1:
           j = edge_list_dict[p[-1]][1]
      egresses_to_path_id[(k, j)].append(path_id)
      path_id_to_egresses[path_id] = (k, j)
      for n in p:
          node_to_path_id[n] = path_id
      length = sum(shortest direct distances[(a, b)] for (a, b) in zip(p[:
-1], p[1:]))
      right_escape = length + shortest_direct_distances[(p[-1], j)]
      left escape = shortest direct distances[(k, p[0])]
      for (a, b) in zip(p[:-1], p[1:]):
           if left_escape < right_escape:</pre>
               better_egress[a] = (k, left_escape)
           else:
               better_egress[a] = (j, right_escape)
           left_escape += shortest_direct_distances[(a, b)]
           right_escape -= shortest_direct_distances[(a, b)]
      if left_escape < right_escape:</pre>
           better_egress[p[-1]] = (k, left_escape)
      else:
           better_egress[p[-1]] = (j, right_escape)
      shortest_direct_distances[(k, j)] = shortest_direct_distances[(j, k)] =_u
min(shortest_direct_distances.get((k, j), float("inf")), right_escape +u
→left_escape)
      path_length[path_id] = right_escape + left_escape
      path_id += 1
  print(f"Shuffling down vertex numbers to account for removed nodes...")
  compressed_shortest_direct_distances = {}
  compressed_translations = {}
  inverted_compressed_translations = {}
  node id = 0
  for ((e1, e2), d) in shortest_direct_distances.items():
      if e1 in visited or e2 in visited:
           continue
      for e in (e1, e2):
           if e not in inverted_compressed_translations:
```

```
compressed_translations[node_id] = e
                inverted_compressed_translations[e] = node_id
                node id += 1
        e1_new = inverted_compressed_translations[e1]
        e2_new = inverted_compressed_translations[e2]
        compressed_shortest_direct_distances[(e1_new, e2_new)] = d
        compressed_shortest_direct_distances[(e2_new, e1_new)] = d
    # de-default-ify
    egresses_to_path_id = {k : v for (k, v) in egresses_to_path_id.items()}
dist_to_use = shortest_direct_distances if not apply_graph_compression else_u
 ⇔compressed_shortest_direct_distances
max_node_num = max(max(shortest_direct_distances, key=lambda t: max(t)))
max_node_num_compressed = max_node_num
if apply_graph_compression:
    max_node_num_compressed = max(max(compressed_shortest_direct_distances,_
 ⇔key=lambda t: max(t)))
for i in range(num_datasets):
    old_dist_to_use = dist_to_use
    if max_node_num_compressed > truncate_to:
        print(f"Going to truncate graph to {truncate_to}, currently⊔
 →{max_node_num_compressed+1} nodes")
        all_edges = (list(dist_to_use.items()) + list(((y, x), d) for ((x, y),_{\sqcup}

→d) in dist_to_use.items()))
        random.shuffle(all_edges)
        edge = random.choice(all_edges)
        nodes = set((edge[0][0], edge[0][1]))
        while len(nodes) < truncate_to:</pre>
            for ((v1, v2), dist) in all_edges:
                if v1 in nodes:
                    nodes.add(v2)
                if len(nodes) >= truncate_to:
                    break
        mappings = {v: i for (i, v) in enumerate(nodes)}
        dist_to_use = {(mappings[v1], mappings[v2]) : d for ((v1, v2), d) in_u
 dist_to_use.items() if v1 in nodes and v2 in nodes}
        print("Dropped", len(all_edges) - len(dist_to_use), "edges")
    filename = f"analyzed_datasets/{place_name}Trunc{truncate_to}_{i}.points"
    with open(filename, "w+") as F:
        drops = 0
        for i, (k, v) in enumerate(dist_to_use.items()):
            F.write(f''{i} {k[0]} {k[1]} {v}\n'')
    dist_to_use = old_dist_to_use
```

```
[]: fig, ax = ox.plot_graph(graph)
print(f"Visualization of {place_name}")
```

1.4 Section 2: Loading Simulator Output

Before progressing to this section, run the simulator on the output .points file. You can use the EdgesReader utility to load it into the system, and the MatrixDumper utility to dump the final results

```
translated_line.append(e)
        output.append(translated_line)
    return output
def safe_localize(node_l):
    safely resolves a global ID to a local one with graph compression
    if apply_graph_compression:
        node 1 = inverted compressed translations[node 1]
    return node_1
def path_from_successor(successor, start_l, fin_l):
    start_l = safe_localize(start_l)
    fin_l = safe_localize(fin_l)
    output = [start_1]
    prev_l = fin_l
    while successor[output[-1]][fin_1] != fin_1:
        if successor[output[-1]][fin_1] == output[-1]:
            return []
        output.append(successor[output[-1]][fin_1])
    output.append(fin_1)
    return list(map(lambda e: compressed translations[e], output))
    # return list(map(lambda e: l2g_ids[e], output))
def path_from_predecessor(predecessor, start_1, fin_1):
    start_l = safe_localize(start_l)
    fin_l = safe_localize(fin_l)
    output = [fin_1]
    prev_l = fin_l
    while predecessor[start_1][prev_1] != start_1:
        if prev_l == predecessor[start_l][prev_l]:
            return []
        output.append(predecessor[start_1][prev_1])
        prev_l = predecessor[start_l][prev_l]
    output.append(start_1)
    output.reverse()
    return list(map(lambda e: compressed translations[e], output))
    # return list(map(lambda e: l2g_ids[e], output))
def calculatePath(matrix, distance_matrix, start_g, fin_g, g2l_ids, l2g_ids):
    #print("Entry.")
```

```
if start_g == fin_g:
      return [start_g]
  strategy = path_from_successor if method == SUCCESSOR else_
→path_from_predecessor
  start_l = g2l_ids[start_g]
  fin 1 = g21 ids[fin g]
  start_c = None
  fin_c = None
  if start_l in inverted_compressed_translations:
      start_c = inverted_compressed_translations[start_1]
  if fin_l in inverted_compressed_translations:
      fin_c = inverted_compressed_translations[fin_1]
  if not apply_graph_compression:
      output = strategy(matrix, start_1, fin_1)
      return list(map(lambda e: 12g_ids[e], output))
  def ddash_within_path(a, b, pid):
      (a_egg, a_dist) = better_egress[a]
      (b_egg, b_dist) = better_egress[b]
      if a_egg == b_egg:
          return abs(a_dist - b_dist)
      return abs((path_length[pid] - a_dist) - b_dist)
  def ddash(a, egg, pid):
      if a not in better_egress:
          a, egg = egg, a
      (a_egg, a_dist) = better_egress[a]
      if a_egg == egg:
          return a_dist
      return abs((path_length[pid] - a_dist))
  def dc(a, b):
      return distance_matrix[a][b]
  # case 1: neither vertex removed
  →inverted_compressed_translations:
      #print("Case 1.")
      path = strategy(matrix, start_1, fin_1)
      output = []
      for (v1, v2) in zip(path[:-1], path[1:]):
          output.append(v1)
          if (v1, v2) in egresses_to_path_id or (v2, v1) in_
→egresses_to_path_id:
              f = lambda l: l
```

```
pathlist = []
               if (v2, v1) in egresses_to_path_id and (v1, v2) not in_
→egresses_to_path_id:
                   f = lambda 1: reversed(1)
                   pathlist = egresses_to_path_id[(v2, v1)]
               else:
                   pathlist = egresses_to_path_id[(v1, v2)]
              best_path = None
              best_dist = float("inf")
               for p in pathlist:
                   if path_length[p] < best_dist:</pre>
                       best_path = collapsed_paths_dict[p]
                       best_dist = path_length[p]
               output += list(f(best_path))
      output.append(v2)
      return list(map(lambda e: 12g_ids[e], output))
  # case 2: both removed, on same path
  if start_l in node_to_path_id and fin_l in node_to_path_id and_
anode_to_path_id[start_1] == node_to_path_id[fin_1]:
      #print("Case 2.")
      pid = node_to_path_id[fin_1]
      (s1, a_dist) = better_egress[start_1]
       (s2, b_dist) = better_egress[fin_1]
      s1c = inverted_compressed_translations[s1]
      s2c = inverted_compressed_translations[s2]
      candidate1 = ddash_within_path(start_1, fin_1, pid)
      candidate2 = ddash(start_1, s1, pid) + dc(s1c, s2c) + ddash(s2, fin_1,__
⊶pid)
      path = collapsed_paths_dict[pid]
      if candidate1 > candidate2:
           if path.index(start_1) < path.index(fin_1):</pre>
              path = list(reversed(path))
          first_portion = path[path.index(start_1):]
          last_portion = path[:path.index(fin_1)+1]
          first_portion = list(map(lambda e: 12g_ids[e], first_portion))
          last_portion = list(map(lambda e: l2g_ids[e], last_portion))
          return first_portion + calculatePath(matrix, distance_matrix,_
inverted_translations[s1], inverted_translations[s2], g2l_ids, l2g_ids) + ∪
→last_portion
      else:
          if path.index(start_l) > path.index(fin_l):
              path = list(reversed(path))
          output = path[path.index(start_1):path.index(fin_1)+1]
          return list(map(lambda e: 12g_ids[e], output))
  # case 3a: start removed, but end is not
```

```
if start_l in node_to_path_id and fin_l not in node_to_path_id:
      print("Case 3a.")
      pid = node_to_path_id[start_1]
      (s1, s2) = path_id_to_egresses[pid]
      s1c = inverted_compressed_translations[s1]
      s2c = inverted_compressed_translations[s2]
      candidate1 = ddash(start_1, s1, pid) + dc(s1c, fin_c)
      candidate2 = ddash(start_1, s2, pid) + dc(s2c, fin_c)
      if candidate1 < candidate2:</pre>
          egress_begin = s1
      else:
          egress_begin = s2
      path = [s1] + collapsed_paths_dict[pid] + [s2]
      if path.index(start_l) > path.index(egress_begin):
          path = list(reversed(path))
      first_portion = path[path.index(start_l):-1]
      first_portion = list(map(lambda e: 12g_ids[e], first_portion))
      return first_portion + calculatePath(matrix, distance_matrix,_
inverted_translations[egress_begin], fin_g, g2l_ids, l2g_ids)
  # case 3b: start not removed, but end is
  if start_l not in node_to_path_id and fin_l in node_to_path_id:
      #print("Case 3b.")
      pid = node_to_path_id[fin_1]
      (s1, s2) = path_id_to_egresses[pid]
      s1c = inverted_compressed_translations[s1]
      s2c = inverted_compressed_translations[s2]
      candidate1 = dc(start_c, s1c) + ddash(s1, fin_l, pid)
      candidate2 = dc(start_c, s2c) + ddash(s2, fin_l, pid)
      if candidate1 < candidate2:</pre>
          egress end = s1
      else:
          egress_end = s2
      path = [s1] + collapsed_paths_dict[pid] + [s2]
      if path.index(fin_1) < path.index(egress_end):</pre>
          path = list(reversed(path))
      last_portion = path[1:path.index(fin_1)+1]
      last_portion = list(map(lambda e: 12g_ids[e], last_portion))
      return calculatePath(matrix, distance_matrix, start_g,_
winverted_translations[egress_end], g21_ids, l2g_ids) + last_portion
  # case 4: both removed but on different chains
  #print("Case 4.")
```

```
pid_start = node_to_path_id[start_1]
  pid_fin = node_to_path_id[fin_1]
  (s1_start, s2_start) = path_id_to_egresses[pid_start]
  s1c_start = inverted_compressed_translations[s1_start]
  s2c_start = inverted_compressed_translations[s2_start]
  (s1_fin, s2_fin) = path_id_to_egresses[pid_fin]
  s1c fin = inverted compressed translations[s1 fin]
  s2c_fin = inverted_compressed_translations[s2_fin]
  candidate1 = ddash(start_l, s1_start, pid_start) + dc(s1c_start, s1c_fin) +__

ddash(s1_fin, fin_l, pid_fin)

  candidate2 = ddash(start_1, s2_start, pid_start) + dc(s2c_start, s1c_fin) +

→ddash(s1_fin, fin_l, pid_fin)
  candidate3 = ddash(start_1, s1_start, pid_start) + dc(s1c_start, s2c_fin) +
→ddash(s2_fin, fin_l, pid_fin)
  candidate4 = ddash(start_1, s2_start, pid_start) + dc(s2c_start, s2c_fin) +

¬ddash(s2_fin, fin_l, pid_fin)
  best = min([candidate1, candidate2, candidate3, candidate4])
  #print(best)
  if best == candidate1:
      s_start = s1_start
      s_fin = s1_fin
  elif best == candidate2:
      s_start = s2_start
      s_fin = s1_fin
  elif best == candidate3:
      s_start = s1_start
      s_fin = s2_fin
  else: # best == candidate4
      s_start = s2_start
      s_fin = s2_fin
  start_path = [s1_start] + collapsed_paths_dict[pid_start] + [s2_start]
  if start_path.index(start_l) > start_path.index(s_start):
      start_path = list(reversed(start_path))
  first_portion = start_path[start_path.index(start_l):-1]
  first_portion = list(map(lambda e: l2g_ids[e], first_portion))
  fin_path = [s1_fin] + collapsed_paths_dict[pid_fin] + [s2_fin]
  if fin_path.index(fin_l) < fin_path.index(s_fin):</pre>
      fin_path = list(reversed(fin_path))
  last_portion = fin_path[1:fin_path.index(fin_1)+1]
  last_portion = list(map(lambda e: l2g_ids[e], last_portion))
```

```
return first_portion + \
calculatePath(matrix, distance_matrix, inverted_translations[s_start],
inverted_translations[s_fin], g2l_ids, l2g_ids) + \
last_portion
```

```
[]: matrix = parseMatrix(path_to_matrix, inverted_translations)
   distance_matrix = parseMatrix(path_to_distance_matrix, do_optimization=False)
   print("Simulator data loaded!")
```

1.5 Section 3: Comparison of Outputs

To visualize paths, choose two nodes below and see the results.

```
[]: calcr1 = calculatePath(matrix, distance matrix, orig1, dest1, translations,
      →inverted_translations)
     calcr2 = calculatePath(matrix, distance_matrix, orig2, dest2, translations,__
     ⇒inverted translations)
     calcr3 = calculatePath(matrix, distance_matrix, orig3, dest3, translations,__
      ⇒inverted translations)
     calcr4 = calculatePath(matrix, distance_matrix, orig4, dest4, translations,_
      ⇔inverted translations)
     fig, ax = ox.plot_graph_routes(graph, [calcr1, calcr2, calcr3, calcr4],_u
      →route_colors=rc, route_linewidth=6, node_size=0)
     print("Simulator shortest paths")
[]: print("Do they agree on path 1? " + "Yes!" if calcr1 == route1 else f"No:

¬\n{calcr1} \n{route1}")
     print("Do they agree on path 2? " + "Yes!" if calcr2 == route2 else f"No:⊔

¬\n{calcr2} \n{route2}")
     print("Do they agree on path 3?" + "Yes!" if calcr3 == route3 else f"No:

¬\n{calcr3} \n{route3}")
     print("Do they agree on path 4? " + "Yes!" if calcr4 == route4 else f"No:

¬\n{calcr4} \n{route4}")
     # nx.shortest_path_length(graph, orig2, dest2, weight='length')
[]: nodes = list(graph.nodes())
     for start in nodes:
         for end in nodes:
             route = nx.shortest_path(graph, start, end, weight='length')
             try:
                 calcr = calculatePath(matrix, distance_matrix, start, end,__
      ⇔translations, inverted translations)
             except BaseException as e:
                 print(start)
                 print(end)
                 raise e
             try:
                 assert(route == calcr)
             except AssertionError as e:
                 # IMPORTANT NOTE: Any failed cases require manual investigation.
      → The model solution will sometimes differ if there are multiple shortest
      \rightarrow paths.
                                   This is rare, but does occurs thanks to the many
      ⇔roundabouts in Britain.
                 print("Consider checking", start, end)
     print("Test successful!")
```