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<https://github.com/julianmak/academic-notes>

The repository principally contains the compiled products rather than the source for size reasons.

- ▶ Associated Python code (as Jupyter notebooks mostly) will be held on the same repository. The source data however might be big, so I am going to be naughty and possibly just refer you to where you might get the data if that is the case (e.g. JRA-55 data). I know I should make properly reproducible binders etc., but I didn't...
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OCES 3301 : basic Data Analysis in ocean sciences

Session 9: fun with maps

Outline

(Just overview here; for actual content see Jupyter notebooks)

- ▶ multi-dimensional arrays
 - documenting data varying in **space** (and in **time**)
 - basics of plotting (contours, animations) and statistics
- ▶ **GEBCO** and **WOA13** data
 - NetCDF and `xarray`, basic functionalities
 - vertical profiles, meridional sections
 - masking, basic statistics, **Hovmöller plots**

Recap: data so far

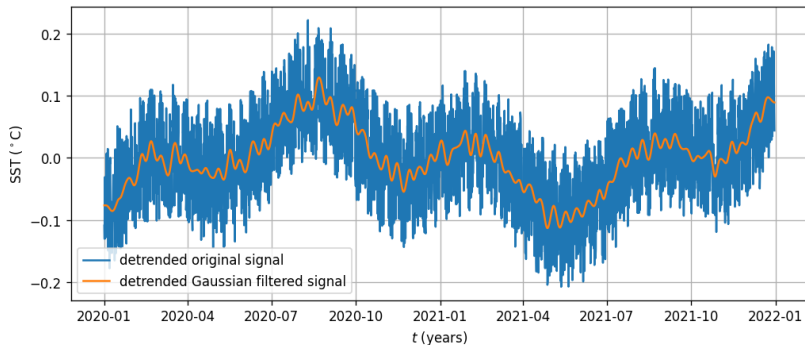


Figure: A detrended signal, as a 1d array varying in time.

Recap: data so far

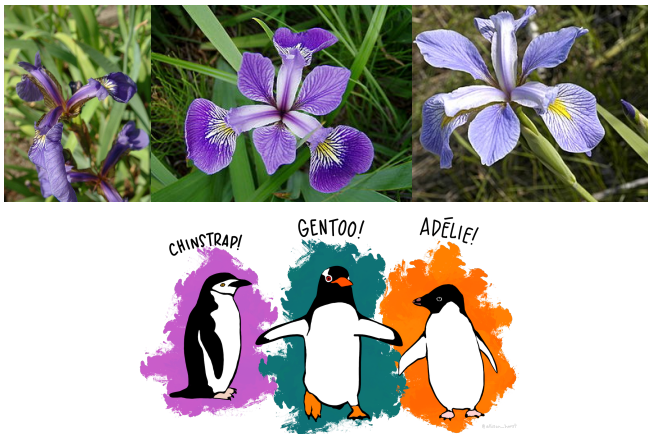


Figure: Analysis of data as 1d arrays against each other, but stored as **multi-dimensional arrays**.

Basic 2d array

Consider the function

$$f(x, y) = \sin(x) \cos(y)$$

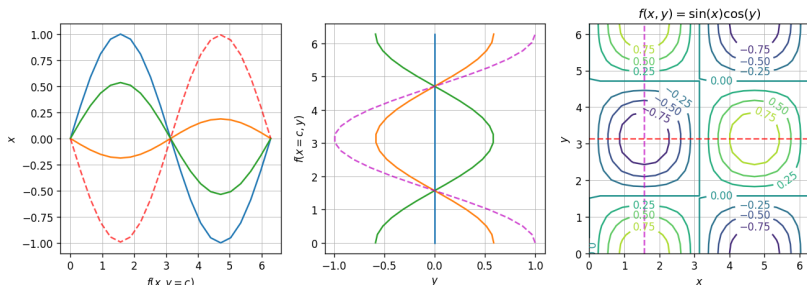


Figure: $f(x, y) = \sin(x) \cos(y)$ as lines at fixed y , fixed x , and contours in the (x, y) .

- ▶ varying as sines in x and cosines in y
- ▶ circular 'blobs' in top-down view

Basic 2d array

$$f(x, y) = \sin(x) \cos(y)$$

Take

$$x = \begin{pmatrix} x_0 \\ x_1 \\ \vdots \\ x_{N_x} \end{pmatrix}, \quad y = \begin{pmatrix} y_0 \\ y_1 \\ \vdots \\ y_{N_y} \end{pmatrix}$$

and store as (see notebook to see how this would be generated)

$$f(x, y) = \begin{pmatrix} f(x_0, y_0) & f(x_1, y_0) & \cdots & f(x_{N_x}, y_0) \\ f(x_0, y_1) & f(x_1, y_1) & \cdots & f(x_{N_x}, y_1) \\ \vdots & \vdots & \ddots & \vdots \\ f(x_0, y_{N_y}) & f(x_1, y_{N_y}) & \cdots & f(x_{N_x}, y_{N_y}) \end{pmatrix}.$$

- Python plotting ‘prefers’ storage of arrays in ‘descending’ dimensions `f[t, z, y, x]` etc.

Basic 2d array

$$f(x, y) = \sin(x) \cos(y)$$

- view the **contour** (or **filled contour**) plots as ‘top-down’ views of 3d plot

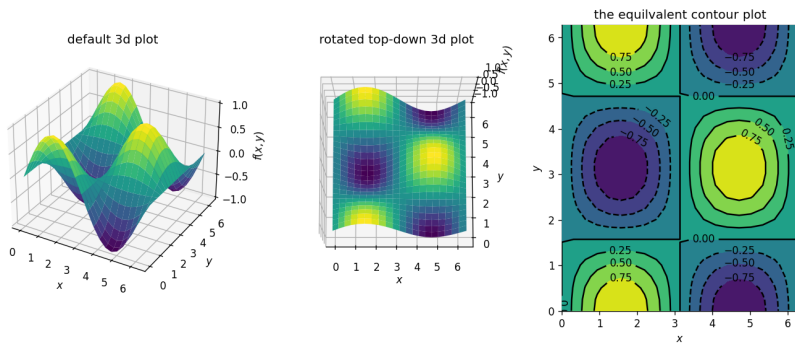


Figure: $f(x, y) = \sin(x) \cos(y)$ as 3d plots.

e.g. equation of state

- ▶ oceanography relevant 2d example: equation of state (EOS)

$$\rightarrow \rho = \rho(T, S, \dots)$$

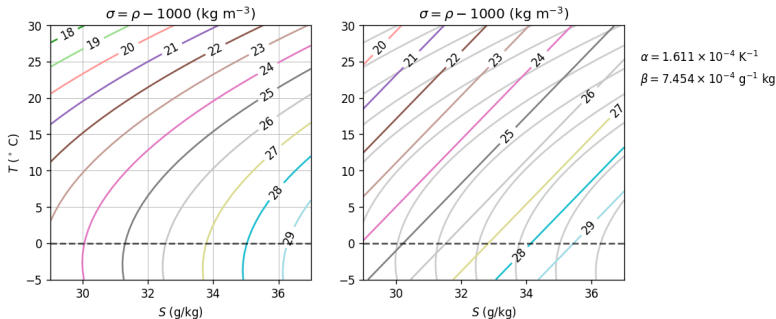


Figure: $\rho = \rho(T, S, \dots)$ over choices of T and S , for the nonlinear TEOS-10 and linear EOS for some choice of α and β .

Animations

- ▶ really just pictures transitioning quickly
 - think flipbooks
 - a few still images as **frames**
 - transitioning with a **frame rate** (fps = frames per second)
- (Humans perceive anything larger than about 16 fps as 'smooth', loosely speaking)

cursed beast most foul

$(2 + 1)$ d array

$$f(x, y) = \sin(x) \cos(y) \sin(t)$$

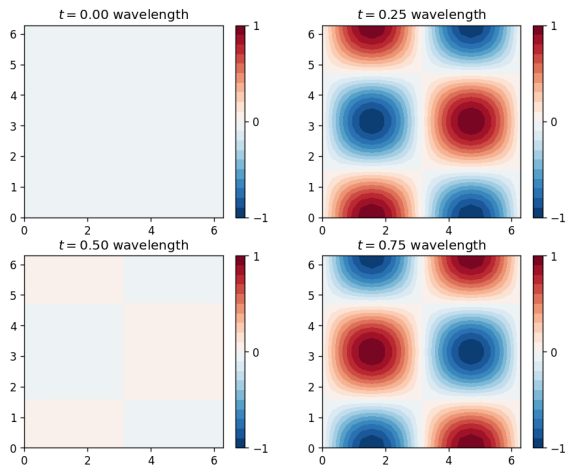


Figure: $f(x, y, t) = \sin(x) \cos(y) \sin(t)$ at some fixed times.

$(2 + 1)d$ array

$$f(x, y) = \sin(x) \cos(y) \sin(t)$$

- ▶ data stored as `f[t_k, y_j, x_i]`
- ▶ see code for how you might animate the above in Python/Jupyter

(I tend to output all frames in Python but assemble into animation externally)



wibbly wobbly timey wimey

(2 + 1)d array: statistics

$$f(x, y) = \sin(x) \cos(y) \sin(t)$$

- can compute averages, stds, rolling-averages etc.
 - over t (time average)
 - over space (spatial average)
 - over the longitude or x (zonal average)

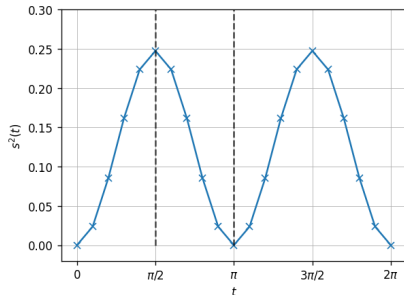
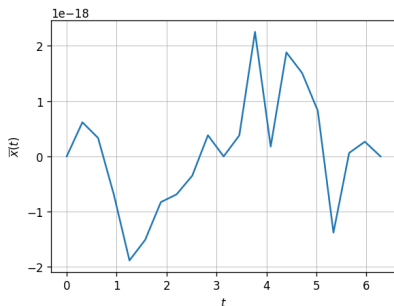


Figure: Spatial average and variance of $f(x, y, t) = \sin(x) \cos(y) \sin(t)$ as a function of time.

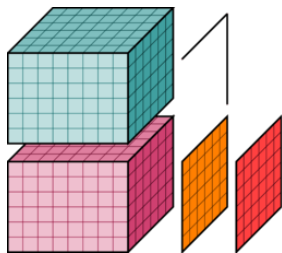
GEBCO and WOA13 data

More 'realistic' examples:

- ▶ **GEBCO** (The General Bathymetric Chart of the Oceans)
 - **topography** (above sea level) and **bathymetry** (below sea level) I will probably use them interchangeably
 - various **spatial resolutions**, time independent
 - `elev(lat, lon)`
- ▶ **WOA13** (World Ocean Atlas 2013)
 - various quantities, going to deal with T and S here
 - **climatology**, monthly ('average' monthly condition)
 - 1° spatial resolution (but will find denser interpolated versions)
 - `f(month, depth, lat, lon)`

GEBCO and WOA13 data

- ▶ going to use `xarray` to read NetCDF files
 - could think of it as a convenient front end for the Python NetCDF library
 - actually much more powerful than that (see notebook)



xarray

GEBCO and WOA13 data

- xarray returns a data frame **df**
 - cf. Pandas data frame
 - see co-ordinate variables, data variables, attributes etc.

```
<xarray.Dataset>
Dimensions: (lat: 451, lon: 901)
Coordinates:
  * lat      (lat) float64 -90.0 -89.6 -89.2 -88.8 -88.4 ... 88.8 89.2 89.6 90.0
  * lon      (lon) float64 -180.0 -179.6 -179.2 -178.8 ... 179.2 179.6 180.0
Data variables:
  elev      (lat, lon) float32 ...
Attributes:
  Conventions: CF-1.6
  title:       The GEBCO One Minute Grid - a continuous terrain model for ...
  institution: On behalf of the General Bathymetric Chart of the Oceans (G...
  source:      The grid is largely based on the bathymetric contours conta...
  history:     This is version 2.0 of the data set, released in November 2008
  references:  Information on the data set is available from the internet:...
  comment:     The data in the GEBCO One Minute Grid should not be used fo...
  node_offset: 0
```

Figure: Sample output from GEBCO read via xarray.

GEBCO and WOA13 data: surface plots

- ▶ xarray objects have **imbued** functions
→ `df["elev"].plot()` below with GEBCO data

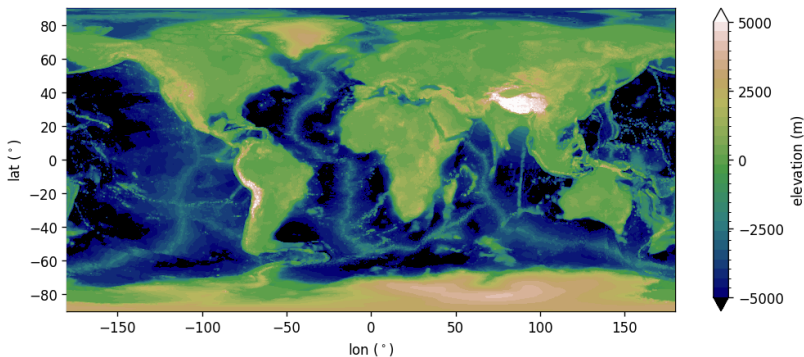


Figure: Sample output from GEBCO read via xarray.

GEBCO and WOA13 data: vertical profile

- xarray objects have **imbu**ed functions
→ `df["votemper"].sel().plot()` to pick out
lon/lat/time locations rather than specifying the index
explicitly, and doing `plot`

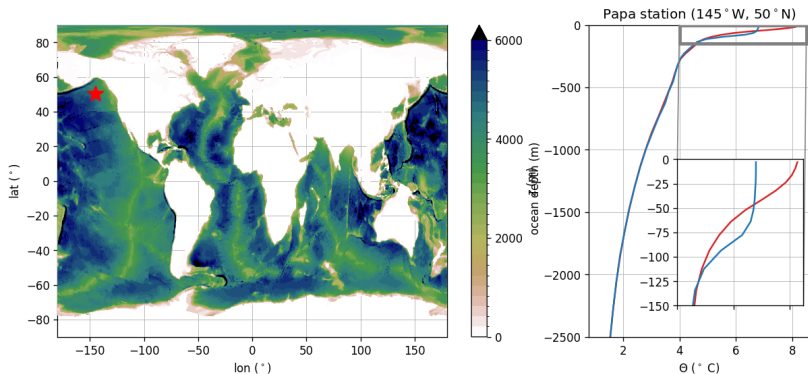


Figure: Vertical profile of WOA13 (conservative) temperature at summer and winter months at PAPA station.

GEBCO and WOA13 data: meridional section

- ▶ as previous, but for **meridional section**
 - fixed latitude, function of lon and depth
 - `.sel(lat=SOMETHING, method="nearest")`

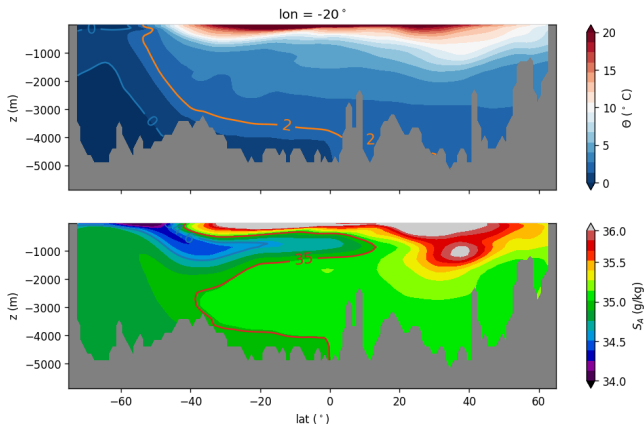


Figure: Meridional profile of time-averaged WOA13 (conservative) temperature and (absolute) salinity. Masking of based on GEBCO data.

GEBCO and WOA13 data: masking

- ▶ WOA13 data here is not **masked**
 - e.g. `f(month, depth, lat, lon)` contains co-ordinates at **land points**
 - wanted to exclude those points when doing calculations (e.g. averages)
- ▶ create a **mask** separately here from GEBCO data
 - boolean arrays of `True/False` or integer arrays of `1/0` to correspond to ocean/land points
 - using some conditional, e.g. `if df["elev"] < 0`
then 1 else 0

GEBCO and WOA13 data: masking

- ▶ mask is $(df["elev"] < 0)$ AND (lon and lat within some region)
→ 1 if true, 0 otherwise
- ▶ construct $T \times \text{mask}$
→ I actually used NaNs instead of 0

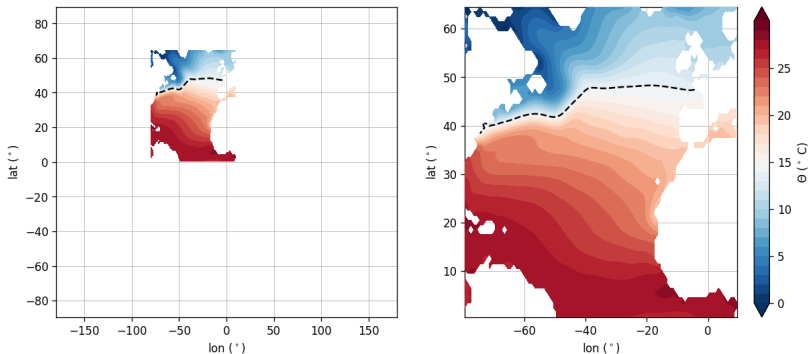


Figure: Mask created GEBCO data based on land, and within a certain region in the Atlantic. Plotting the surface WOA13 temperature on top of that.

GEBCO and WOA13 data: masking and stats

NaNs instead of zeroes might be preferably because

- ▶ plotting commands normally ignore NaNs (see above)
→ e.g. if zeroes, then contours of '0' will probably dominate
- ▶ there are routines to ignore NaNs in calculations (e.g. `np.nanmean`)
→ e.g.

$$\text{nanmean}\{1, 2, 3, \text{NaN}\} = \frac{1 + 2 + 3}{3} = 2$$

$$\text{mean}\{1, 2, 3, 0\} = \frac{1 + 2 + 3 + 0}{4} = 1.5$$

$$\text{mean}\{1, 2, 3, \text{NaN}\} = \frac{1 + 2 + 3 + \text{NaN}}{4} = ???$$

GEBCO and WOA13 data: masking and stats

Domain average (really just nanmean twice here) and **zonal average** (really just nanmean over longitude)

$$\langle \Theta \rangle = \frac{1}{A} \iint \Theta \, dA = \frac{1}{A} \iint \Theta \, dx \, dy \quad \bar{\Theta} = \frac{1}{L_x} \int \Theta \, dx.$$

► $\langle \Theta \rangle$ is a function of t only, while $\bar{\Theta}$ is a function of t and y

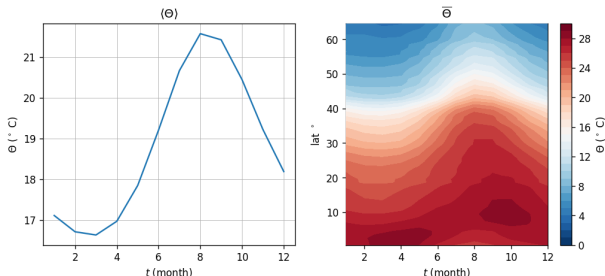


Figure: Domain and zonal average of WOA13 surface temperature over the Atlantic, as a time-series and a Hovmöller diagram.

Jupyter notebook

go to 09 Jupyter notebook to get some code practise

- ▶ try analyses on some sample data from a numerical simulation also

→ surface current speed from NEMO ORCA0083-N01

→ 1 year, every 5 days, nominally $1/12^\circ$ horizontal resolution

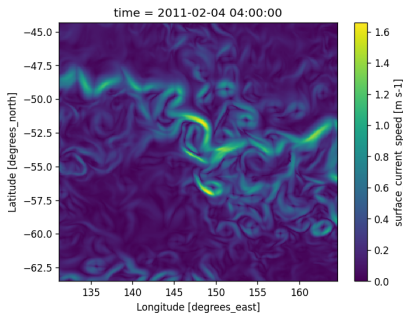


Figure: Surface current speed from NEMO ORCA0083-N01 somewhere in the Southern Ocean (ask me for more data if you want).