



SIGGRAPH 2008

Lighting and Material of Halo 3



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Talk Overview

- Introduction
- Halo3 Lighting
- Halo3 Material Model
- Results
- Conclusions
- Future Work

Motivation

- global illumination
- handle variety of environments
- consistent lighting everywhere
- render bump maps “correctly”
- complex materials under complex lighting
- HDR



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Related Work

- Irradiance Volume [GSHG98][Oat05]
- SH Irradiance Environment Map [RamamoorthiHanrahan01]
- Pre-computed Radiance Transfer [SKS02]
- SH Light Maps [GoodTaylor05]
- Sky and Atmosphere [PSS99][HoffmanPreetham02]
- Reflectance Models [CookTorrance81][Schlick94]
- Low Frequency Glossy Material [KSS02][SHHS03]
- Frequency Space Environment Map [RamamoorthiHanrahan02]

Rendering Equation

$$I(V) = \int [f(V, L)\ell(\omega) \cos(\theta)] d\omega$$

BRDF Distant Lighting ^{Incident angle}

Spherical Harmonics

- A complete set of orthogonal basis for L^2 functions on a unit sphere

$$Y_\ell^m(\theta, \varphi) = \sqrt{\frac{(2\ell+1)}{4\pi} \frac{\ell - |m|}{\ell + |m|}} P_\ell^{|m|}(\cos \theta) e^{im\varphi}$$

Orthogonality:

$$\int_{\varphi=0}^{2\pi} \int_{\theta=0}^{\pi} Y_\ell^m(\theta, \varphi) {Y_\ell^m}^*(\theta, \varphi) \sin \theta d\theta d\varphi = \delta_{\ell\ell'} \delta_{mm'}$$

Spherical Harmonics

- Real Spherical Harmonics $y_\ell^m(\theta, \varphi)$

$$y_\ell^m(\theta, \varphi) = \begin{cases} \sqrt{2} \operatorname{Re} [Y_\ell^m(\theta, \varphi)] , & m > 0 \\ Y_\ell^0(\theta, \varphi) , & m = 0 \\ \sqrt{2} \operatorname{Im} [Y_\ell^m(\theta, \varphi)] , & m < 0 \end{cases}$$

Spherical Harmonics

- SH expansion

$$f(\theta, \varphi) = \sum_{\ell, m} f_\ell^m y_\ell^m(\theta, \varphi)$$

where

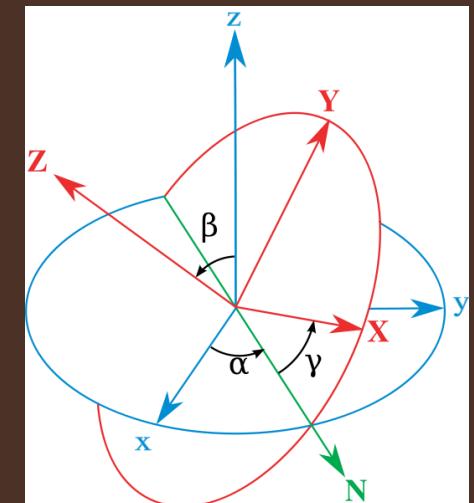
$$f_\ell^m = \int_{\theta=0}^{\pi} \int_{\varphi=0}^{2\pi} f(\theta, \varphi) y_\ell^m(\theta, \varphi) \sin \theta d\theta d\varphi$$

Spherical Harmonics

- SH Rotation by euler angles: α, β, γ

$$\begin{pmatrix} f_0^0 \\ f_1^{-1} \\ f_1^0 \\ f_1^1 \\ \vdots \end{pmatrix} = R_{SH}(\alpha, \beta, \gamma) \begin{pmatrix} f_0^0 \\ f_1^{-1} \\ f_1^0 \\ f_1^1 \\ \vdots \end{pmatrix}$$

[Green03]



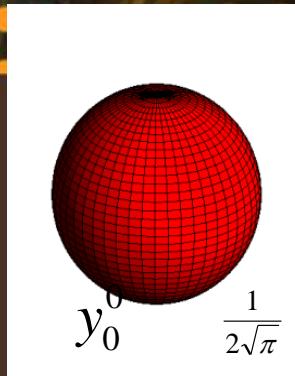
$$R_{SH}(\alpha, \beta, \gamma) = Z_\gamma X_{-90} Z_\beta X_{+90} Z_\alpha$$



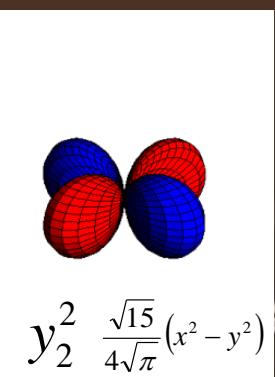
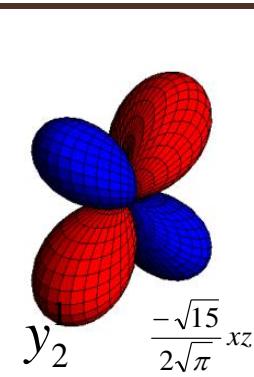
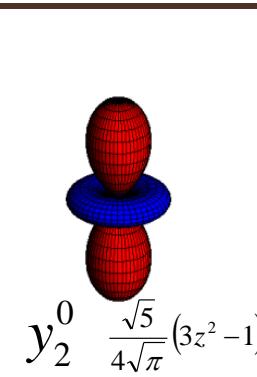
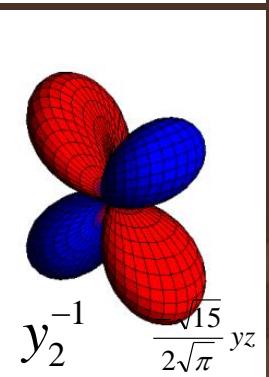
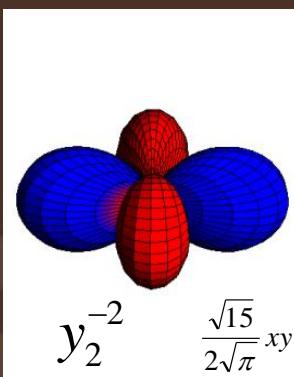
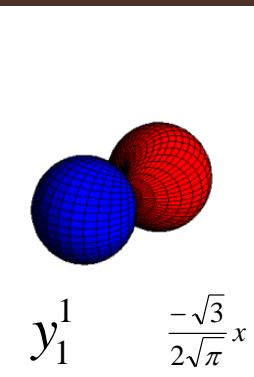
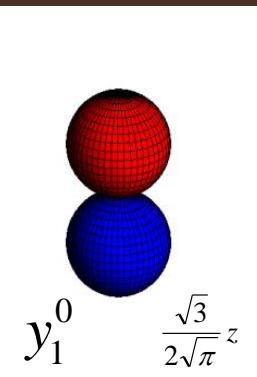
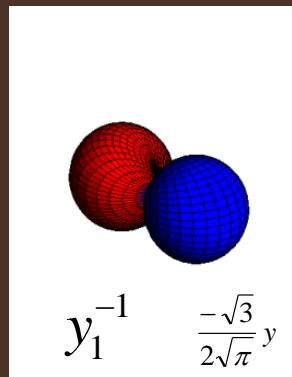
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Spherical Harmonics

- Order-3 Real Spherical Harmonics



[Sloan08]



Spherical Harmonics

- Order-3 Real SH
 - Rotation
- $$\mathbf{X}_{+20} = \begin{pmatrix} 1 & & & & & \\ & 00 & -10 & 00 & & & \\ & 101 & 00 & 00 & & & \\ & 00S & 00 & 1C & & & \\ & & & & 0c_2 & 0 & 0 & 0 & 0 + 1000s_2 \\ & & & & 00 & -1c & 0 & 0 & 0 + s00 \\ & & & & 00 & 0 & 0 & -\frac{1}{2} & 100 + \frac{\sqrt{3}}{2}0 \\ & & & & 00 & 0 & -s & 0 & 000 + c00 \\ & & & & -4s_2 & 0 & 0 & -\frac{\sqrt{3}}{2}0 & 0 - \frac{1}{2}c_2 \end{pmatrix}$$

$$c \equiv \cos(\alpha) \quad s \equiv \sin(\alpha)$$

$$c_2 \equiv \cos(2\alpha) \quad s_2 \equiv \sin(2\alpha)$$



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Spherical Harmonics

- A fast rotation code for pixel shader

```

/*
rotation [ r00 r01 r02 ] -> x-tagent of the local frame
matrix R = [ r10 r11 r12 ] -> y-tagent of the local frame
              [ r20 r21 r22 ] -> z/normal of the local frame

r[] = { r00, r01, r02, r10, r11, r12, r20, r21, r22 };

*/
void sh_rot( const double r[], const double pln[9], double pOut[9] )
{
    // DC
    pOut[0] = pln[0];

    // Linear
    pOut[1] = r[3]*pln[3] + r[4]*pln[1] + r[5]*(-pln[2]);
    pOut[2] = -(r[6]*pln[3] + r[7]*pln[1] + r[8]*(-pln[2]));
    pOut[3] = r[0]*pln[3] + r[1]*pln[1] + r[2]*(-pln[2]);

    // Quadratics
    pOut[4] = -(

        ( r[0]*r[4] + r[1]*r[3] ) * ( -pln[4] ) +
        ( r[1]*r[5] + r[2]*r[4] ) * ( pln[5] ) +
        ( r[2]*r[3] + r[0]*r[5] ) * ( pln[7] ) +
        ( r[0]*r[3] ) * ( -pln[8] ) +
        ( r[1]*r[4] ) * ( pln[8] ) +
        ( r[2]*r[5] ) * ( -v173*pln[6] ) );

```

```

pOut[5] = ( r[3]*r[7] + r[4]*r[6] ) * ( -pln[4] ) +
          ( r[4]*r[8] + r[5]*r[7] ) * ( pln[5] ) +
          ( r[5]*r[6] + r[3]*r[8] ) * ( pln[7] ) +
          ( r[3]*r[6] ) * ( -pln[8] ) +
          ( r[4]*r[7] ) * ( pln[8] ) +
          ( r[5]*r[8] ) * ( -v173*pln[6] );

pOut[7] = ( r[0]*r[7] + r[1]*r[6] ) * ( -pln[4] ) +
          ( r[1]*r[8] + r[2]*r[7] ) * ( pln[5] ) +
          ( r[2]*r[6] + r[0]*r[8] ) * ( pln[7] ) +
          ( r[0]*r[6] ) * ( -pln[8] ) +
          ( r[1]*r[7] ) * ( pln[8] ) +
          ( r[2]*r[8] ) * ( -v173*pln[6] );

pOut[6] = -v173*(( r[7]*r[6] ) * ( -pln[4] ) +
                  ( r[8]*r[7] ) * ( pln[5] ) +
                  ( r[6]*r[8] ) * ( pln[7] ) +
                  0.5f*( r[6]*r[6] ) * ( -pln[8] ) +
                  0.5f*( r[7]*r[7] ) * ( pln[8] ) +
                  0.5f*( r[8]*r[8] ) * ( -v173*pln[6] ) +
                  0.5f*( 1.f*3.f ) * ( v173*pln[6] ));

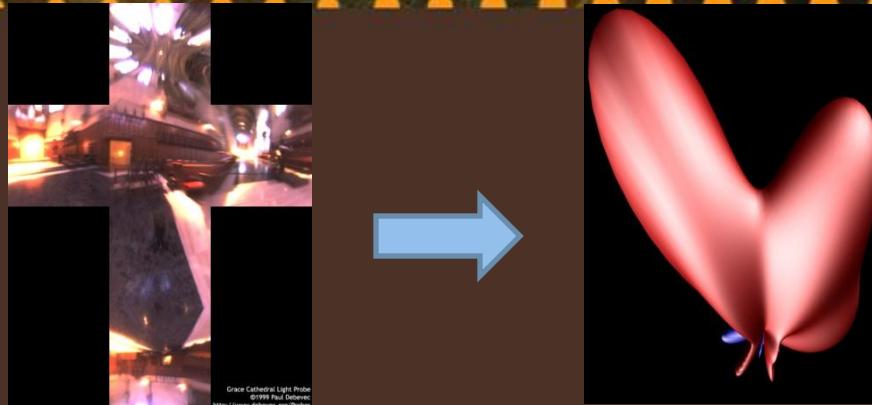
pOut[8] = -(

    ( r[1]*r[0] - r[4]*r[3] ) * ( -pln[4] ) +
    ( r[2]*r[1] - r[5]*r[4] ) * ( pln[5] ) +
    ( r[0]*r[2] - r[3]*r[5] ) * ( pln[7] ) +
    0.5f*( r[0]*r[0] - r[3]*r[3] ) * ( -pln[8] ) +
    0.5f*( r[1]*r[1] - r[4]*r[4] ) * ( pln[8] ) +
    0.5f*( r[2]*r[2] - r[5]*r[5] ) * ( -v173*pln[6] ));

}

```

SH Irradiance Env Map



[Ramamoorthi00]

$$L_{lm} = \iint_{\theta, \phi} L(\theta, \phi) Y_{lm}(\theta, \phi) \sin(\theta) d\theta d\phi$$

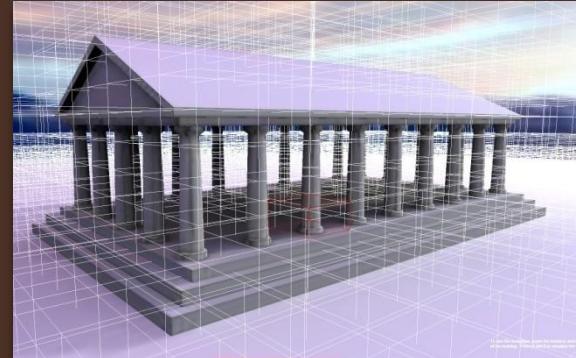
distant radiance
evaluated at given
direction solid
basis angle

Irradiance Volumes

[GSHG98]



[Oat05]



- Spatially divide volume into cells.
- irradiance volume per cell.
- Interpolate between samples.
- Sharp shadow boundaries?
- Bump maps?



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Spherical Harmonics Light Map

- Parameterize over geometry surface.
- Each texel is a SH Vector.
- 9 textures for quadratic SH.
- Highly compressed.



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Halo3 Lighting Pipeline



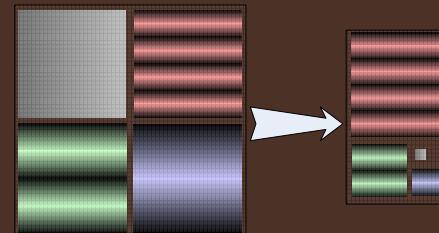
Parameterize



GI Solver



Rendering



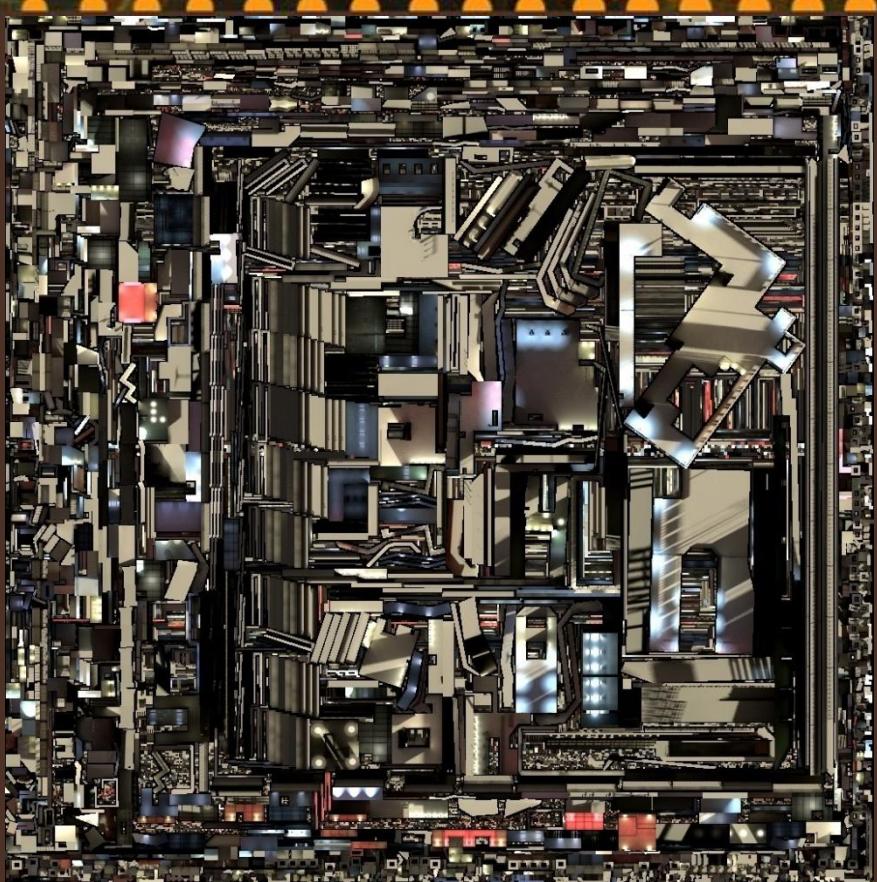
Compression



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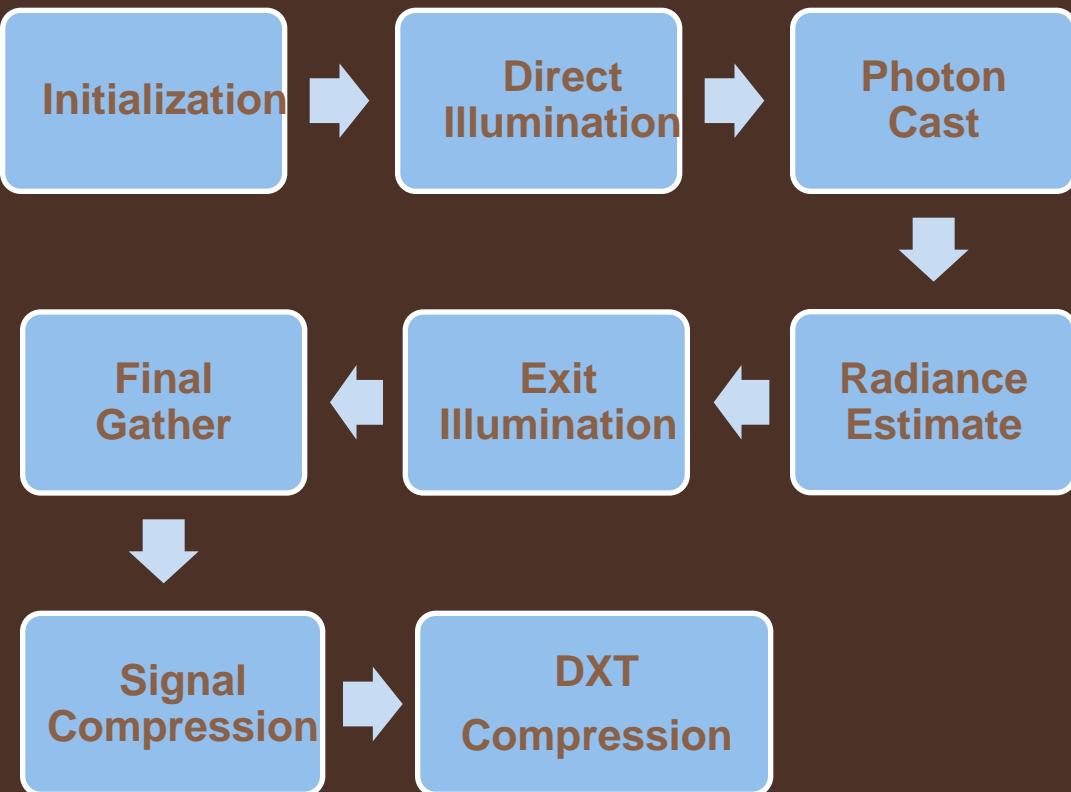
Parameterization

- UVAtlas (MSRA)
- Small Charts
- Long and thin charts
- > 80% utilization.
- Vastly improved over Halo2.



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Photon Mapping

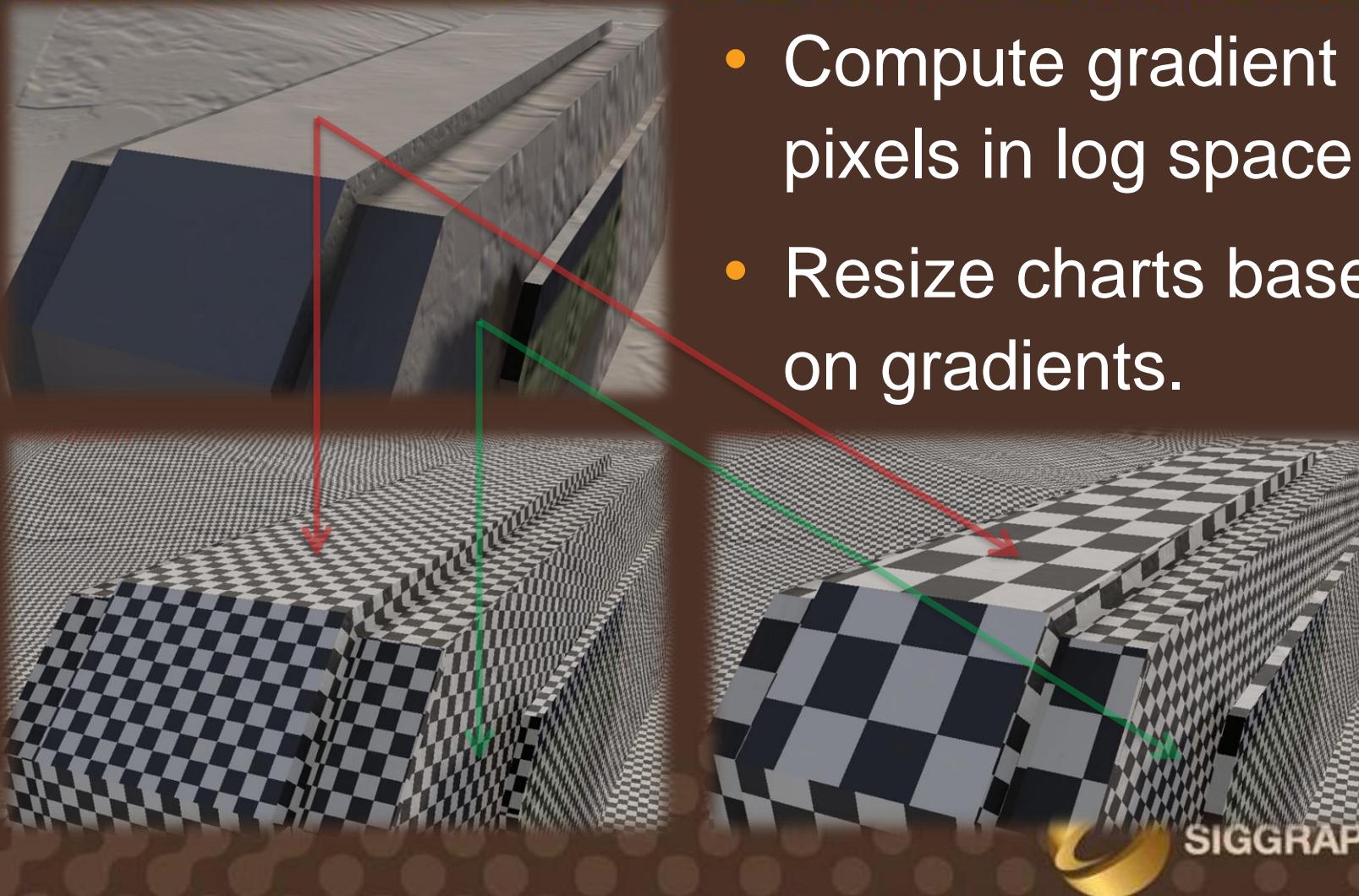


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Compression

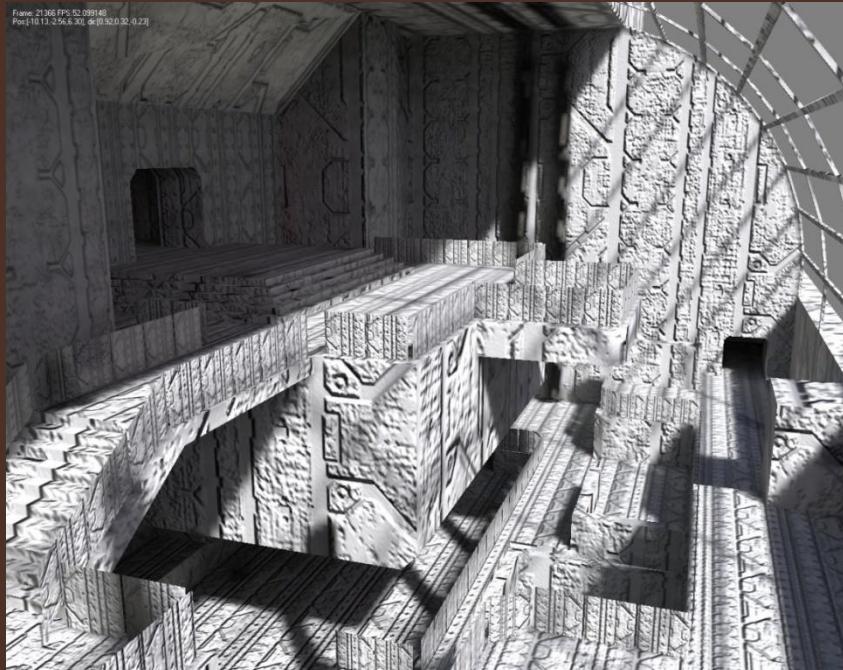
- Two Stage Process.
- Signal Based Optimization.
 - Sub-chart optimization.
- DXT HDR compression.
 - Use 2 DXT5 to compress each floating point texture.

Signal Based Optimization

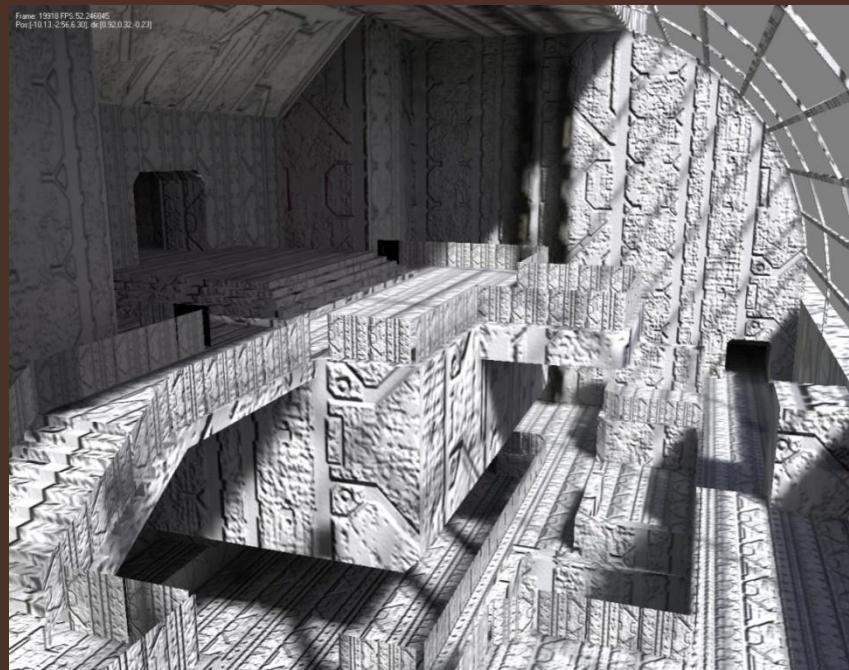


- Compute gradient of pixels in log space.
- Resize charts based on gradients.

Signal Optimization Result



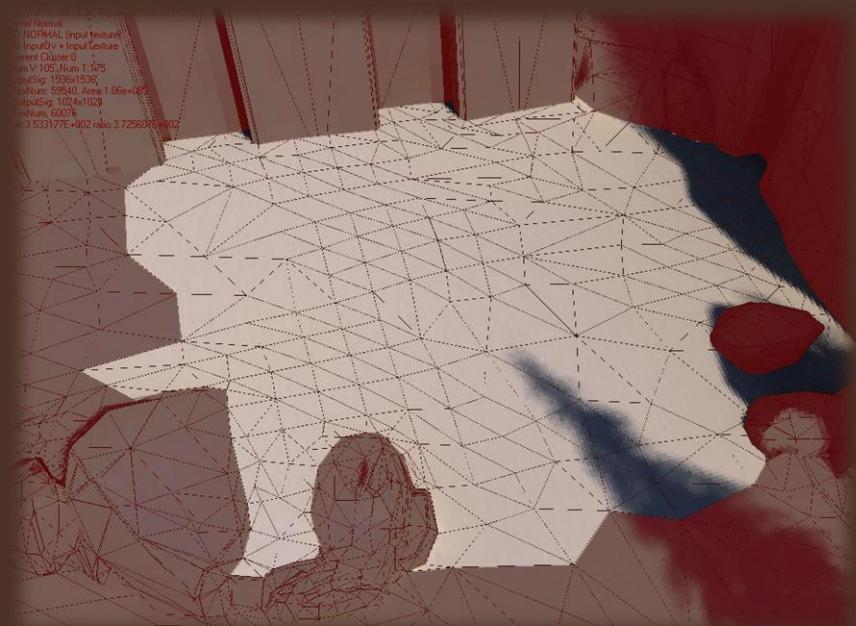
Before: 1024x1024



After: 512x512

Subchart Optimization

- Charts with only a few high freq pixels can still get large area.
- Solution: cut out the high frequency area into a separate chart.



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DXT HDR Compression

- Use two DXT5 textures to compress the SH coefficients (HDR, positive/negative)

4 x 4 block:

| | | |
|---------|--------------------------------|---------------|
| DXT[0]: | Alpha (Luminance) / 64 bits | RGB / 64 bits |
| DXT[1]: | Alpha (Luminance) / 64 bits | RGB / 64 bits |



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“Luvw” Color Space

- Each SH coefficient is a RGB vector and is converted to Luvw color space.
- L: magnitude of the RGB vector.
 - Non negative.
 - Stored in DXT5 x 2's alpha channels for higher precision.
- uvw: normalized vector.
 - Good coherence, we store in the rgb channels of DXT5.



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Luminance

- Store square root of L for higher dynamic range.
- Similar to log space, but cheaper to decode.



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Luminance Compression

- Use 2nd DXT alpha to compensate for the error.

Alpha channel of a 4 x 4 block

DXT[0]: $\text{Block}[0] = \text{DXT_compress}(\sqrt{L_{\text{block}}})$

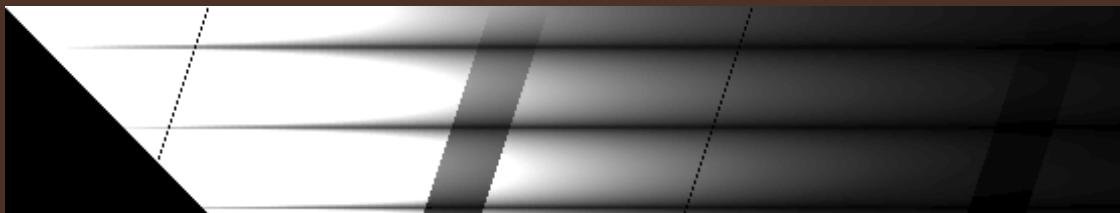
DXT[1]: $\text{Block}[1] = \text{DXT_compress}(L_{\text{block}} / \text{Decompress}(\text{Block}[0]))$



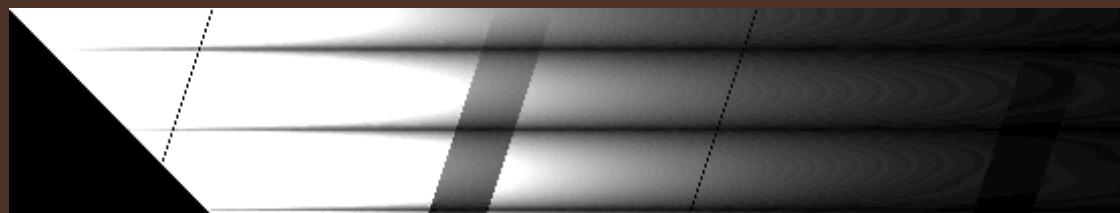
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Luminance Decoding

- $L = \text{Alpha0} * \text{Alpha1} * \text{Max_Luminance}$



2 DXT5 alpha blocks



Just 1 alpha block



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UVW compression

- Similar, use 2nd DXT5 to minimize error.

RGB channel of a 4 x 4 block

DXT[0]: $\text{Block}[0] = \text{DXT_compress}(\text{RGB_block} / 2 + 0.5)$

DXT[1]: $\text{Block}[1] = \text{DXT_compress}((\text{RGB_block} - \text{Decompress}(\text{Block}[0])) / 2 + 0.5)$

- Decode: $\text{UVW} = (\text{rgb0} + \text{rgb1}) * 2 - 2$



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Compression Summary

- Signal compression re-packs charts based on signal frequency. (4: 1 compression ratio).
 - Sub-chart optimization break up charts if desired.
- DXT HDR compression compresses the raw floating point value. (3: 1 compression ratio)
- Overall 12 : 1 compression ratio, quality loss is perceptibly small.



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Rendering Diffuse Lighting

- Static Geometry.
 - SH light map is bound as a surface textures.
 - Per pixel: evaluate normal with the SH vector.
 - Exactly like in Spherical Harmonics Irradiance Env Map.
- Dynamic Objects.
 - Sample the SH light maps based on object position.
 - Render object using PRT and the SH vector.

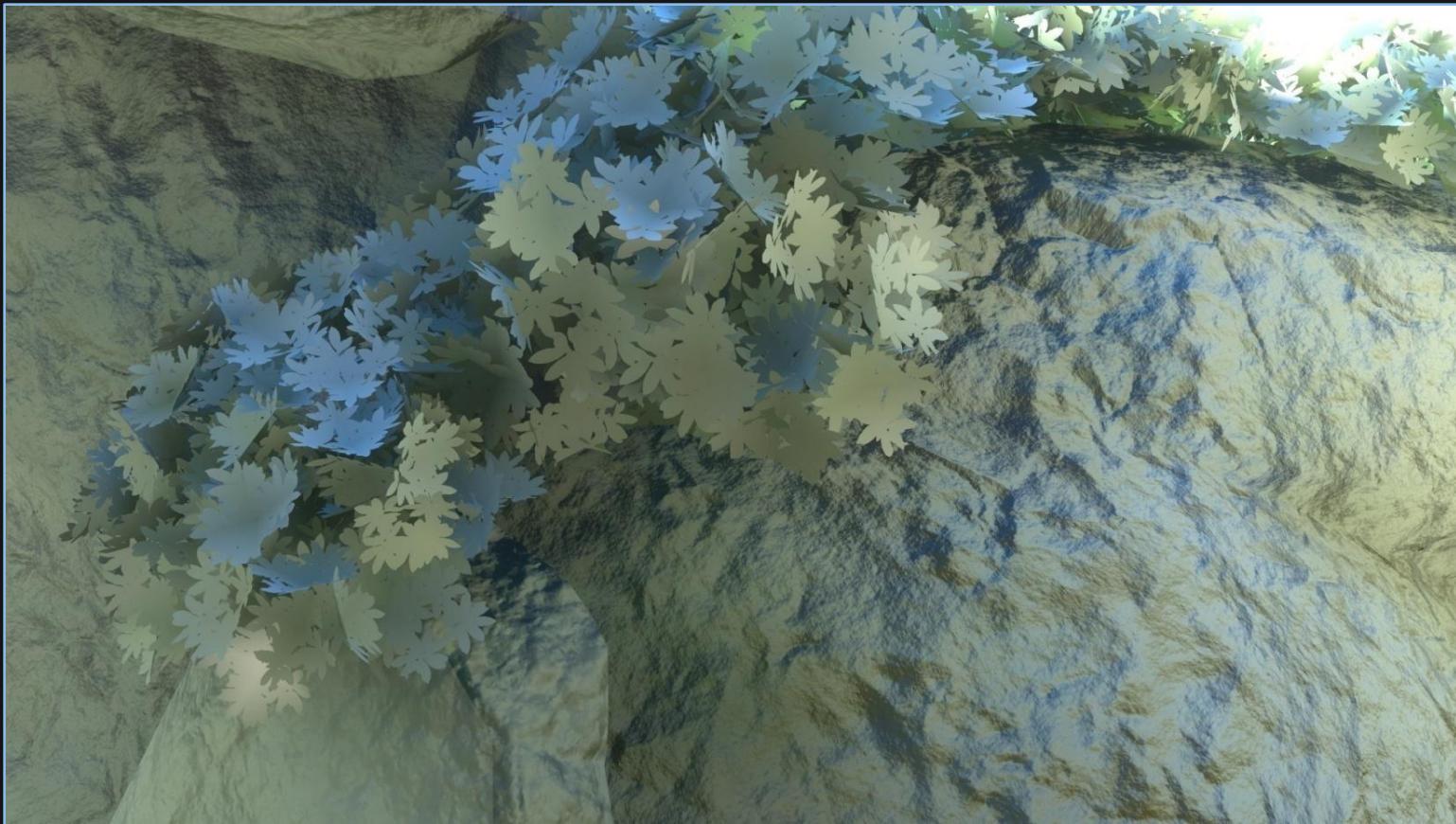
Diffuse Lighting Examples



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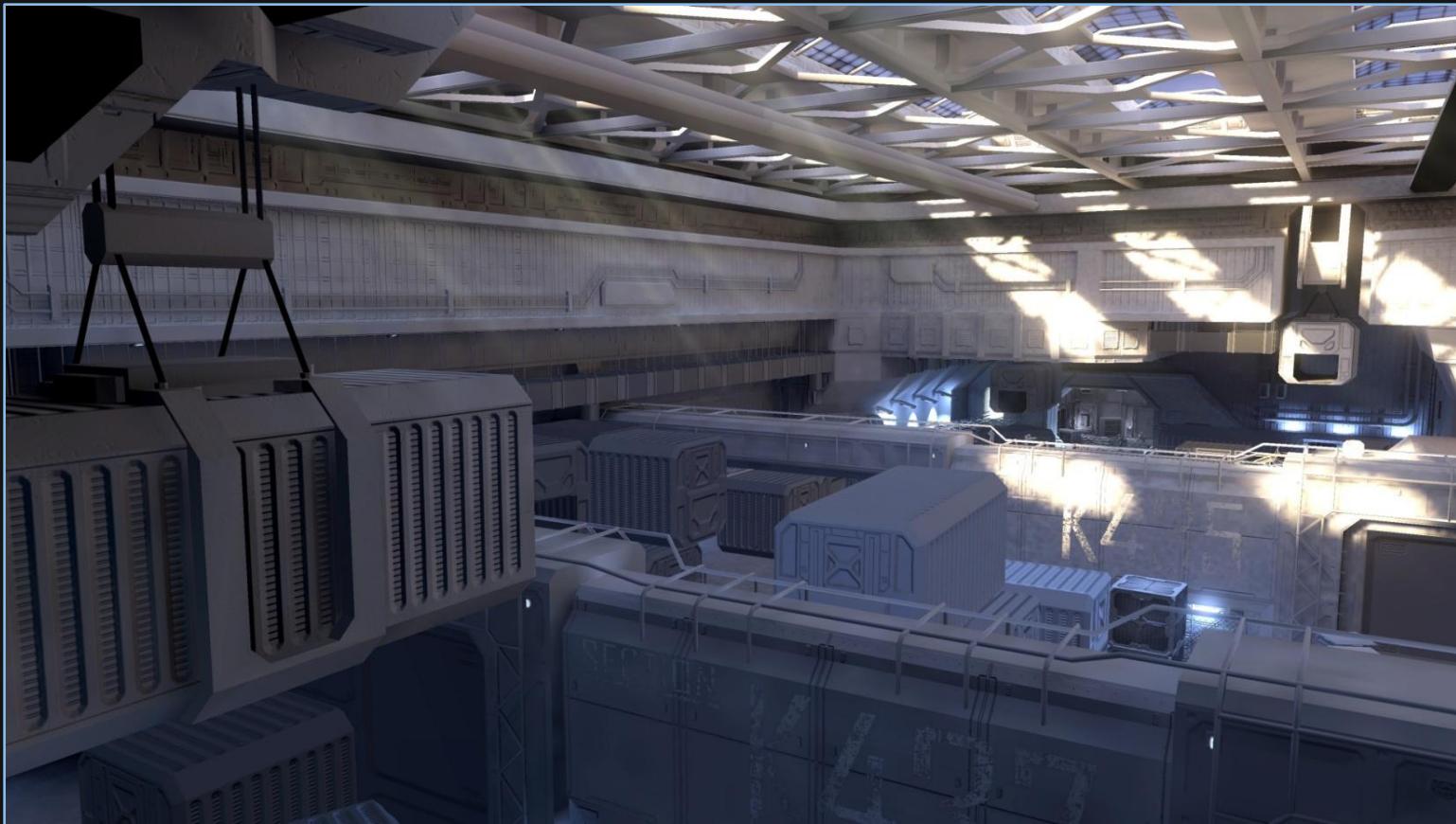
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Optimization

- Reduce storage and ALU count.
- Pull out dominant light, store intensity.

$$E = \sum_{i=0, \dots, 8} (\lambda_i - c Y_i(d))^2, E' = 0$$

$$c = \sum_{i=0, \dots, 8} (\lambda_i Y_i(d)) / \sum_{i=0, \dots, 8} Y_i(d)^2$$

- Store linear SH instead of quadratic.
- In shader, do $(N * L + sh_eval(sh[]) - c * Y(d), N)$.

Comparing “SH 2.5” and SH 3



SH quadratic



N . L + SH linear



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Material Motivation

- BRDF expressiveness.
- Real time performance.
- Compatible with Halo 3 lighting model.
- Requires low storage.



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Halo3 Material Model

- Separate reflectance into separate, low to high frequency parts.

- Diffuse.



- Low frequency glossy (area specular).



- Mid frequency glossy (environment map).



- High frequency glossy (analytical specular).



- Handle each with different techniques.



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Cook Torrance BRDF

$$f(V, L) = k_d R_d + k_s \cdot F \cdot R_m$$

view direction
diffuse reflection
specular reflection
specular lobe



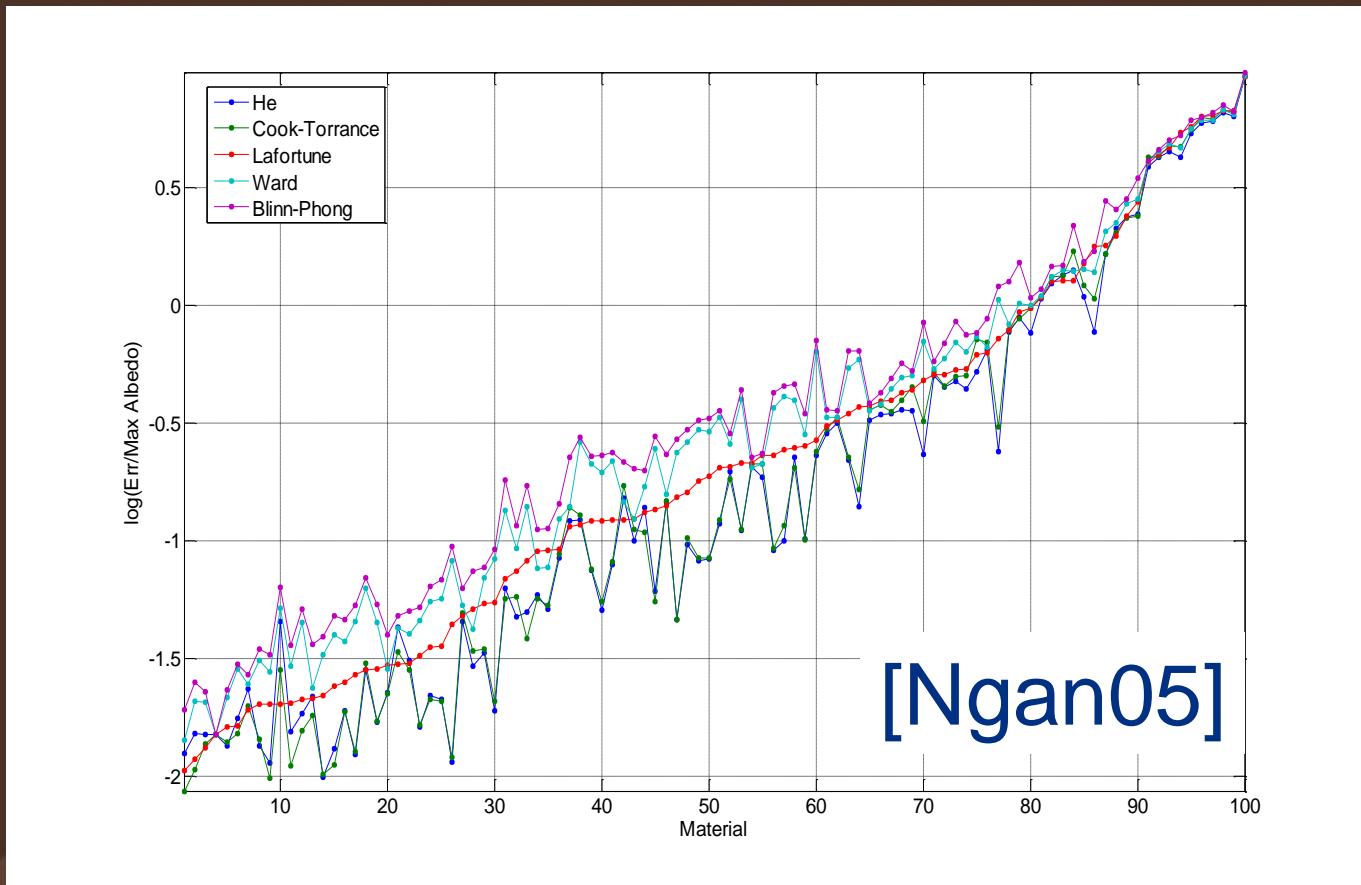
$$R_m(V, L) = \frac{D G}{\pi(N \cdot L)(N \cdot V)}$$

D: microfacet distribution function

G: geometry term

[CookTorrance81]

Cook Torrance BRDF



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Analytical Specular



- Evaluate BRDF directly in pixel shader (point light)
- Use the dominant light direction and intensity.
- HLSL listing in paper.



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Environment Map



- Render cube map at discrete locations.
- Filter out high frequency.
- Pre-divide by area specular.
- Multiply back in shader.



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Area Specular



- Main idea:
 - Express BRDF model itself in SH.
 - Pre-integrate key terms into 2D textures.
 - Evaluate BRDF in shader with SH light.
 - Low frequency only.

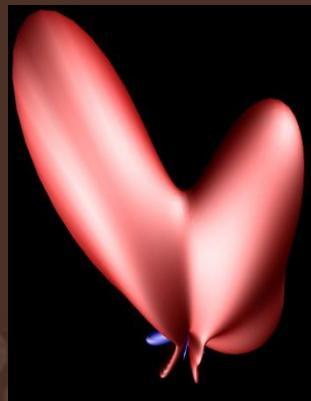


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Light Integration

$$I(V) = \oint [f(V, L) \cos(\theta) L(\omega)] d\omega$$

$$k_d [R_d \oint \cos(\theta) L(\omega) d\omega] + k_s [\oint [FR_m(V, L) \cos(\theta) L(\omega)] d\omega]$$



SH irradiance env. map

??



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Light Integration in SH

$$I_s(V) = k_s \oint [FR_m(V, L)\cos(\theta)L(\omega)]d\omega$$

$$L(\omega) = \sum_{i=0}^8 \lambda_i Y_i(\omega)$$

Project light into SH basis.

Project BRDF and cosine term in SH basis

$$B_{m,i}(V) = \oint \frac{F}{F_0} R_m(V, L) \cos(\theta) Y_i(\omega) d\omega$$

$$I_s(V) = K_s F_0 \sum_{i=0}^8 \lambda_i B_{m,i}(V) \leftarrow \text{Dot product to convolve}$$



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Light Integration in SH Cont.

$$F \approx F_0 + (1 - F_0)(1 - (L \cdot H))^5 \quad [\text{Schilick94}]$$

$$B_{m,i}(V) = \oint \frac{F_0 + (1 - F_0)(1 - (L \cdot H))^5}{F_0} R_m(V, L) \cos(\theta) Y_i(\omega) d\omega$$

$$C_{m,i}(V) = \oint R_m(V, L) \cos(\theta) Y_i(\omega) d\omega$$

$$D_{m,i}(V) = \oint (1 - (L \cdot H)^5) R_m(V, L) \cos(\theta) Y_i(\omega) d\omega$$

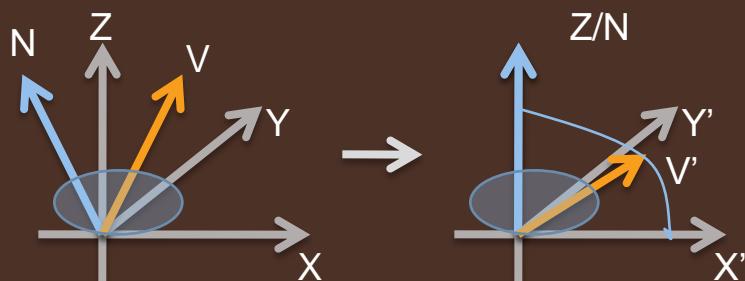
$$B_{m,i}(V) = C_{m,i}(V) + \frac{1 - F_0}{F_0} D_{m,i}(V)$$

← Preintegration



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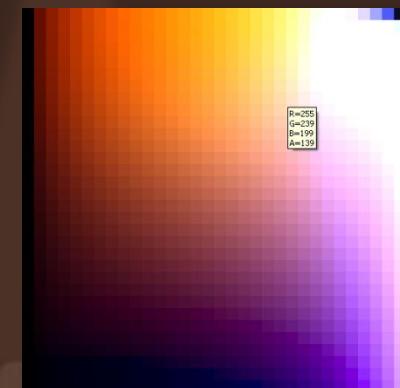
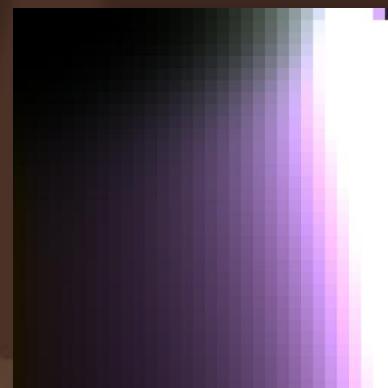
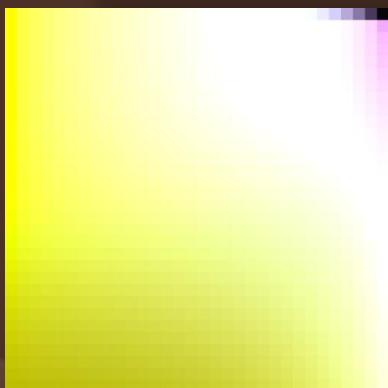
Pre-integration



Reflective symmetry means:

$$C_{m,i}(V) = D_{m,i}(V) = 0, i = 1, 4, 5.$$

Isotropic BRDF = any coordinate frame 16 m values, and 8 V directions is enough.



C (i=0,2,3,6)

D (i=0,2,3,6)

Rendering Area Specular

- Build a local frame.
- Look up C and D texture.
- Rotate SH light vector into local frame.
- Do SH Dot product.
- HLSL Listing in course note.

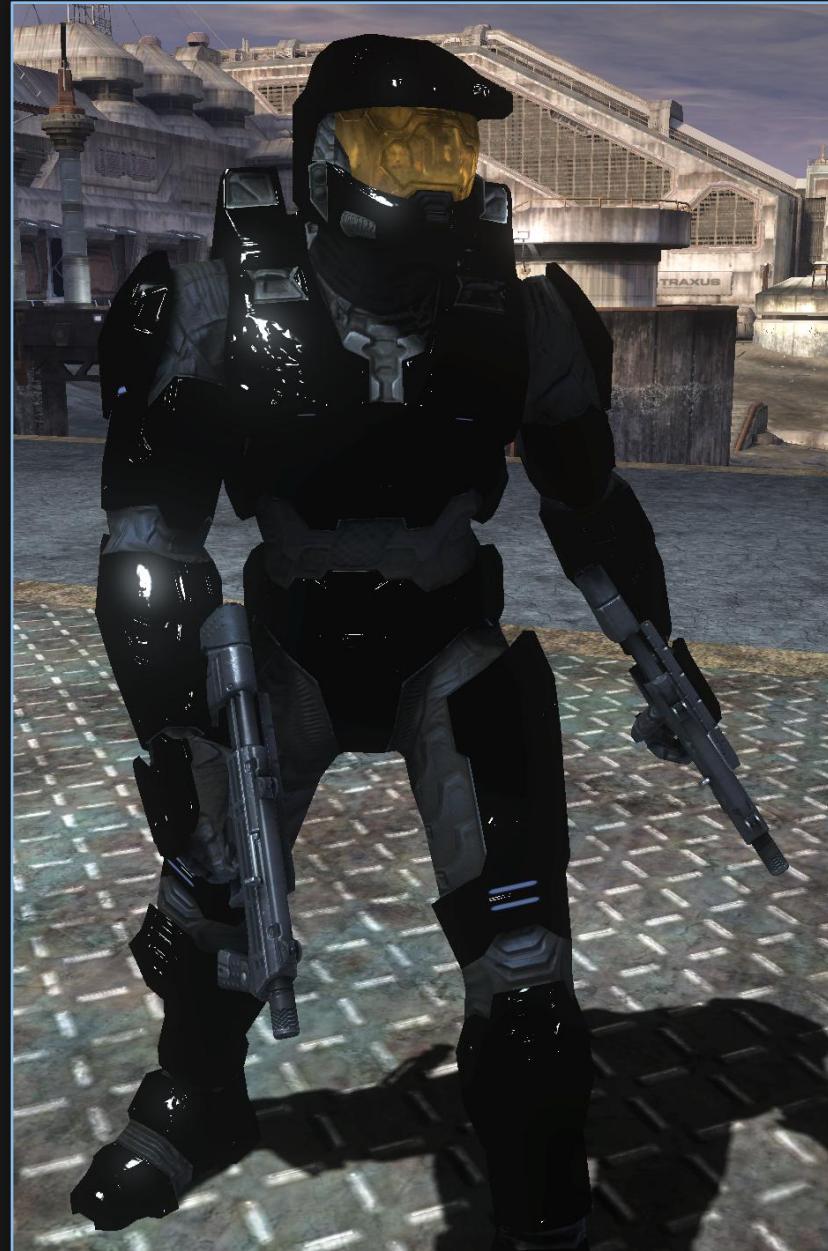


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Results



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Conclusions

- SH light map is a natural extension to the traditional light-mapping pipeline.
- Separating material into layers is a good approximation for all frequency reflectance.
- Area specular is critical for achieving seamless lighting and material integration.
- ALU is cheap, and will get cheaper, take maximum advantage of it.



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Future Work

- Global Illumination with local, moving lights.
- GI for dynamic and semi-dynamic scenes.
- Better lighting basis (less ringing, higher frequency).
- Area specular model with complex transport.
- Measured BRDF.
- Non photo-realistic rendering.



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 - Peter Pike Sloan, Baining Guo, Harry Shum
 - Kutta Srinivasan, Matt Lee, Mikey Wetzel.

Want to team up with the Master Chief?



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