

commitment

LECTURE 10 MON 3/11

Commitment Scheme

two phases:

- $\text{commit}(x)$ produces x with a "commitment"
- $\text{reveal}(x)$ "opens" the commitment and reveals x

properties:

- hiding
- binding
- non-malleability*
given $\text{commit}(x)$ can't generate a commitment to a related value.
i.e. $\text{commit}(x+1)$

* sometimes desired

Pedersen commitment

implementation setup:

- choose p, q large primes s.t. $p-1$ divides q
- choose g as a generator of order q subgroup of \mathbb{Z}_p^*
 $g \in \mathbb{Z}_p^*$ s.t. $\langle g \rangle = \mathbb{Z}_p^*$
- choose at random $a \leftarrow \{1, 2, \dots, q-1\}$ and let $h = g^a$

Note that h also generates $\langle g \rangle$

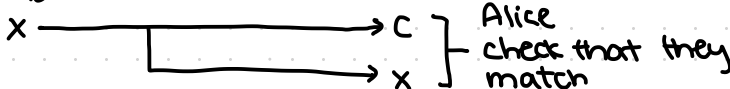
$\text{commit}_{g,h}(x)$:

for $x \in \mathbb{Z}_q$ ($x \in \{0, 1, \dots, q-1\}$), choose at random $r \leftarrow \mathbb{Z}_q$. output commitment $c = g^x h^r \bmod p$

$\text{reveal}(com)$: reveals x and r

receiver verifies that $c = g^x h^r \bmod p$

Bob



Note

x is not necessarily plaintext

has **unconditional hiding** since $\forall c \in \langle g \rangle \quad \forall x \in \mathbb{Z}_q, \exists$ unique
 $r \in \mathbb{Z}_q$ s.t. $g^x h^r = g^{x+ar} = g^z$ for some $z \in \mathbb{Z}_q = \mathbb{C}$
 $\Rightarrow x + ar = z$
 $\Rightarrow r = a^{-1}(z - x) \bmod q$

is **computationally binding** (meaning an all-powerful
adversary could open but not a computationally bounded
one)