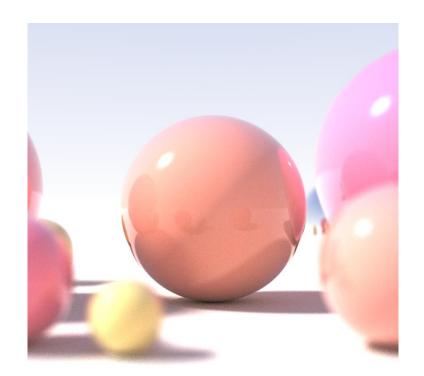
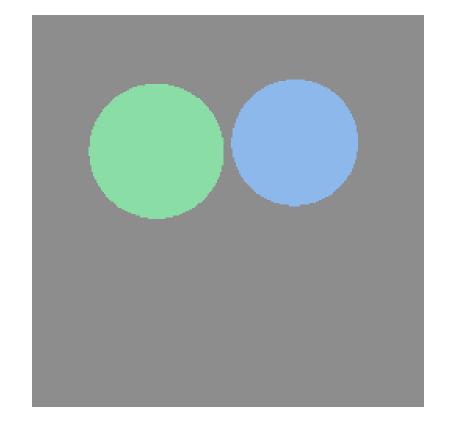
## Ray Tracing





### **Ray Casting**

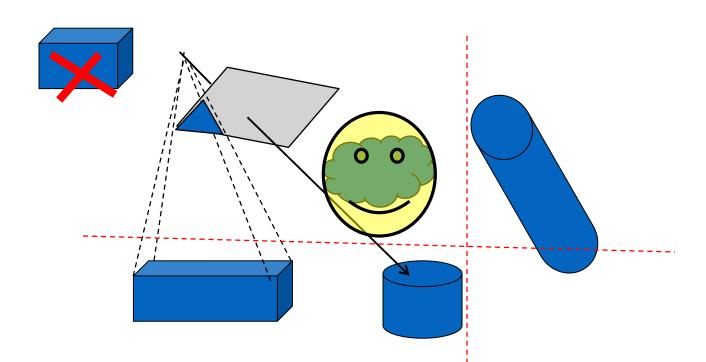
```
for 0 <= iy < ny
  for 0 <= ix < nx
{
    ray = camera.getRay(ix, iy);
    firstSurface = scene.intersect(result,ray);
    if (firstSurface)
        image.set(ix, iy, firstSurface.color);
    else
        image.set(ix, iy, background.color);
}</pre>
```

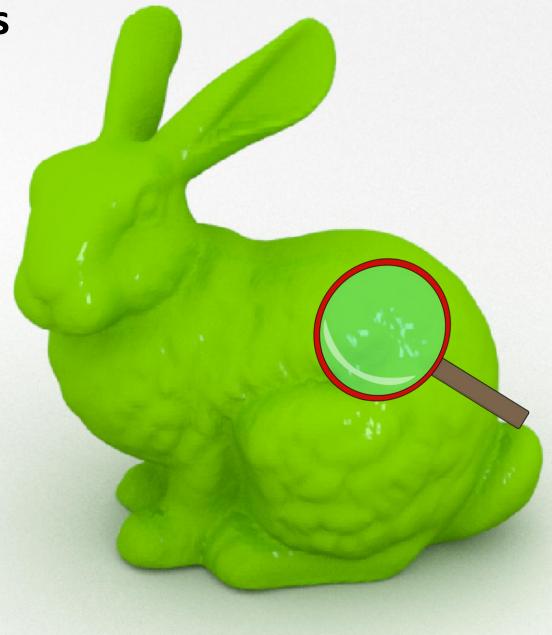


### Ray Intersection: Efficiency Considerations

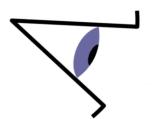
Speed-up the intersection process.

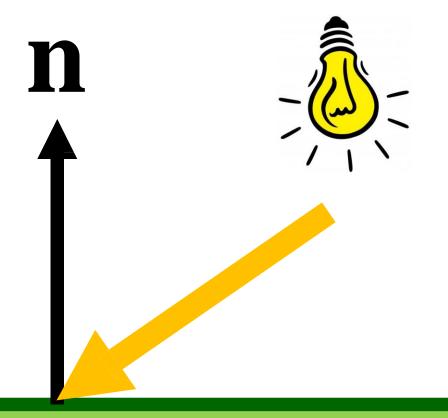
- Ignore object that clearly don't intersect.
- Use proxy geometry.
- Subdivide and structure space hierarchically.
- Project volume onto image to ignore entire sets of rays.

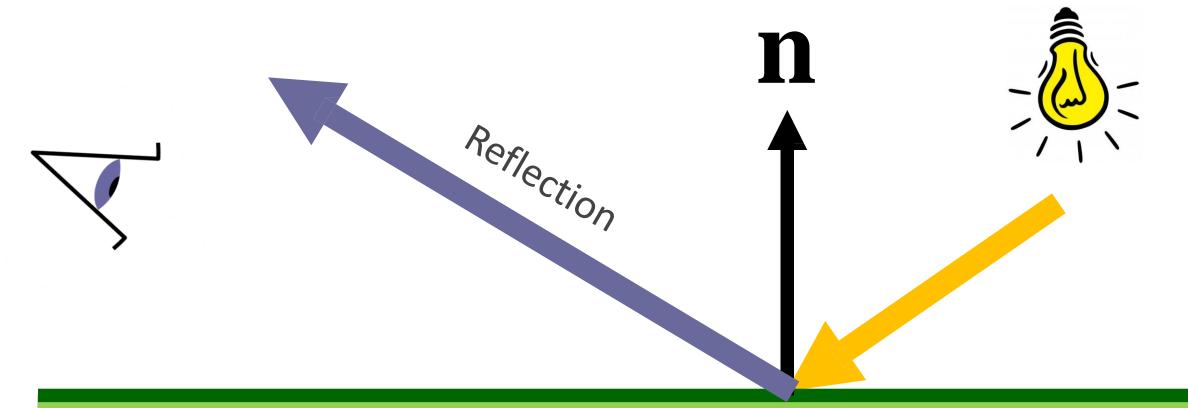




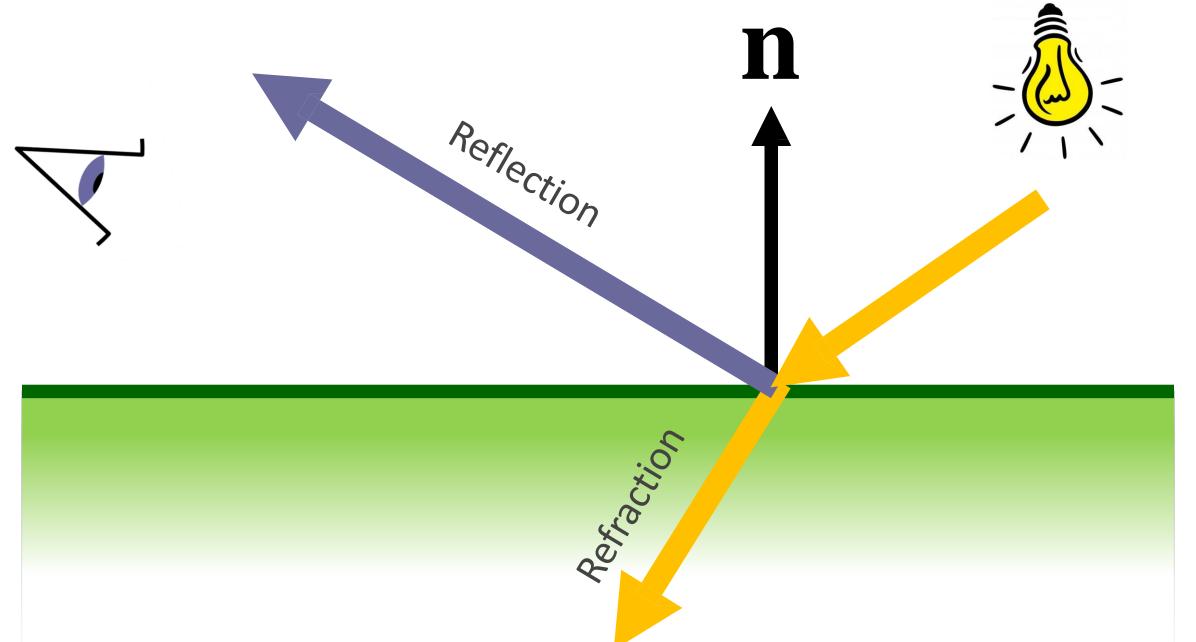










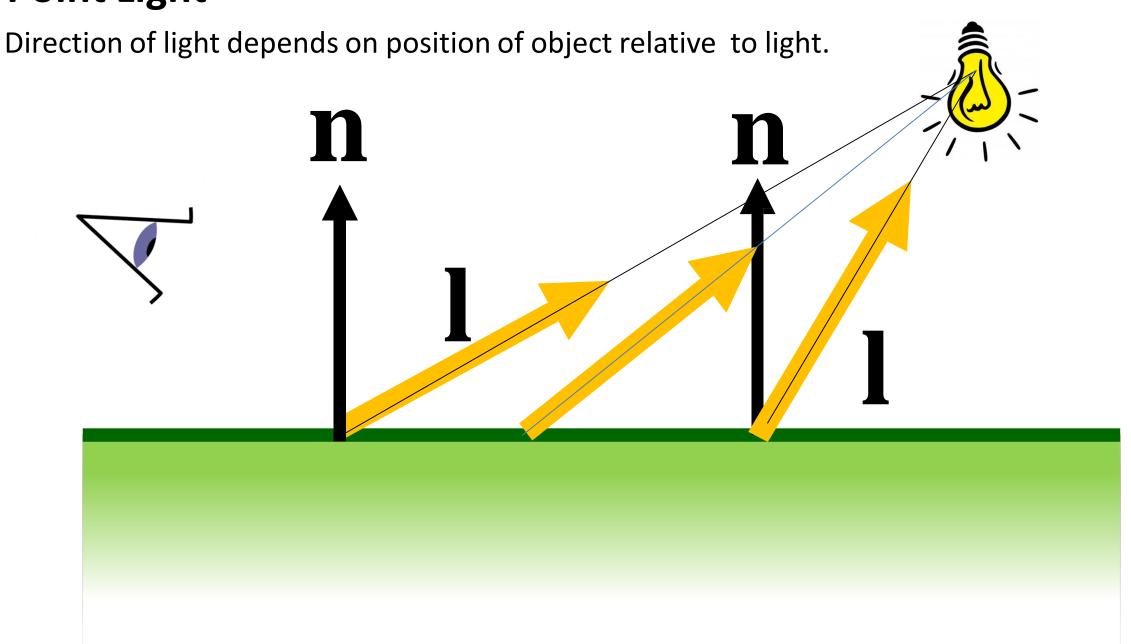




### **Directional Light**

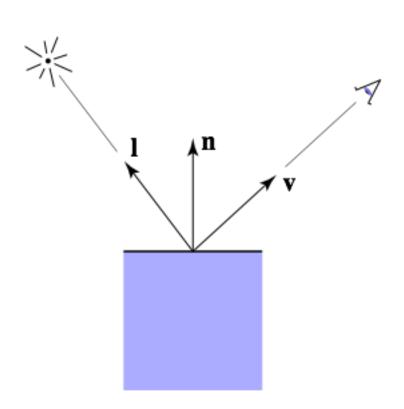
Direction of light is independent of the object. Light is very far away

### **Point Light**



### **Shading**

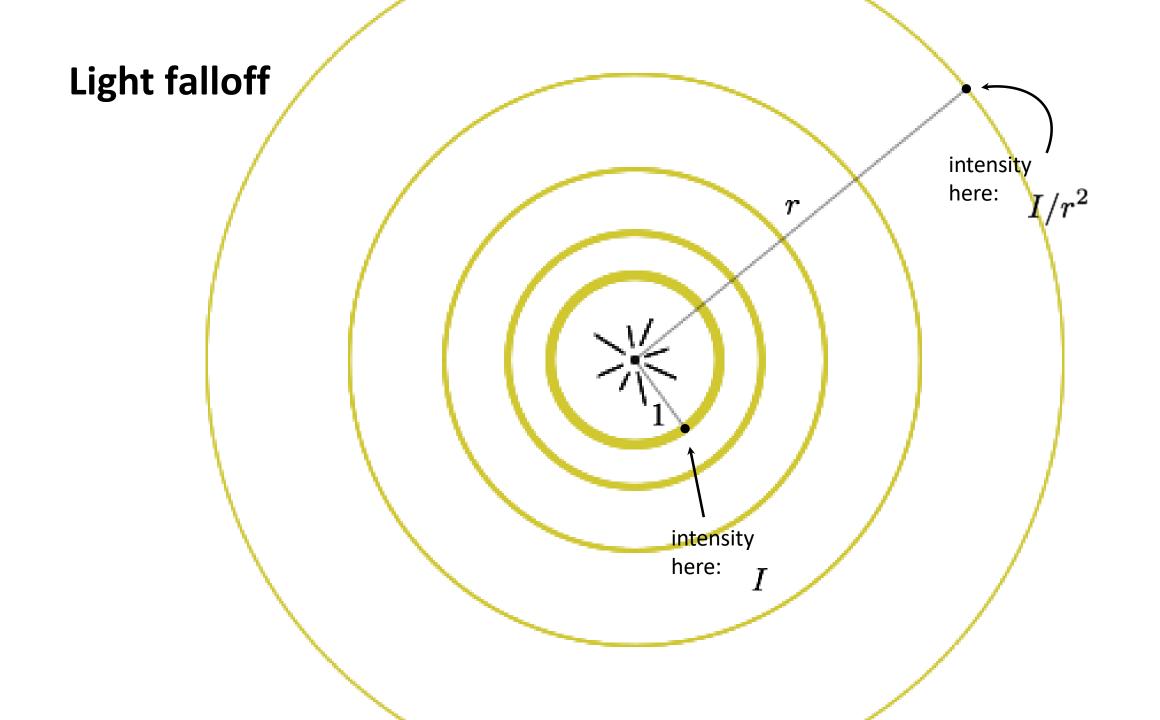
- Compute light reflected toward camera
- Inputs:
  - eye direction
  - light direction(for each of many lights)
  - surface normal
  - surface parameters(color, shininess, ...)



### **Computing the Normal at a Hit Point**

- Polygon normal: cross product of two non-collinear edges.
- Implicit surface normal f(p)=0: gradient(f)(p).
- Explicit parametric surface f(a,b):

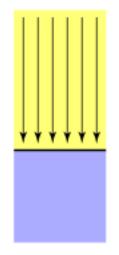
 $\delta f(s,b)/\delta s X \delta f(a,t)/\delta t$ .



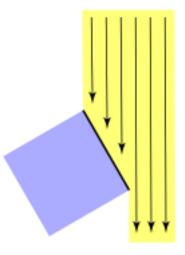


### Diffuse reflection

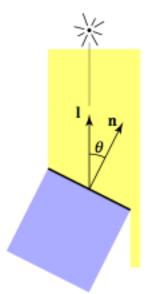
- Light is scattered uniformly in all directions
  - the surface color is the same for all viewing directions
- Lambert's cosine law



Top face of cube receives a certain amount of light



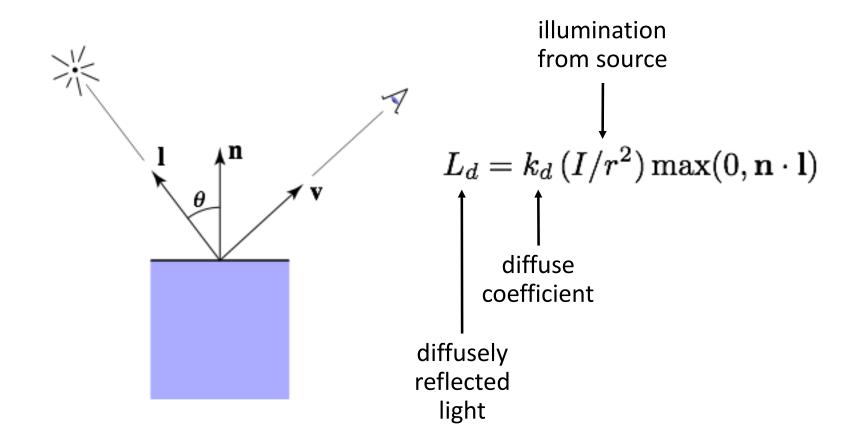
Top face of 60° rotated cube intercepts half the light



In general, light per unit area is proportional to  $\cos \theta = 1 \bullet n$ 

### **Lambertian shading**

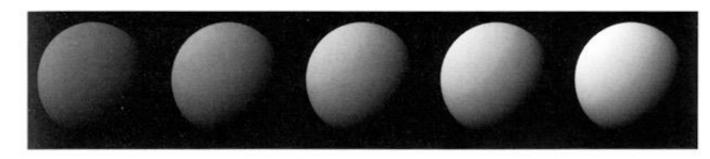
Shading independent of view direction

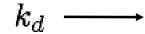


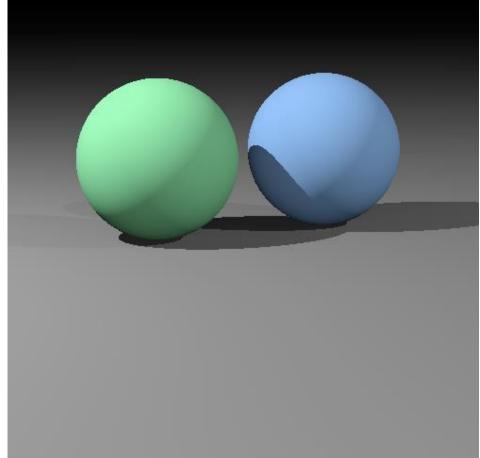


### **Lambertian shading**

### Produces a matte appearance

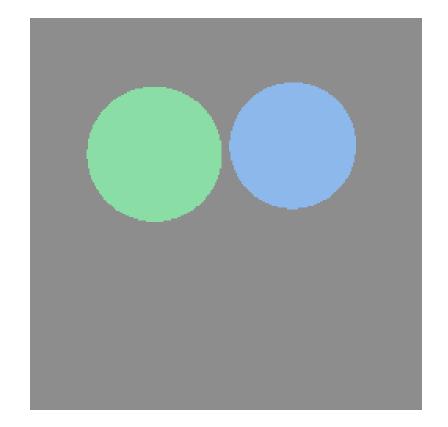






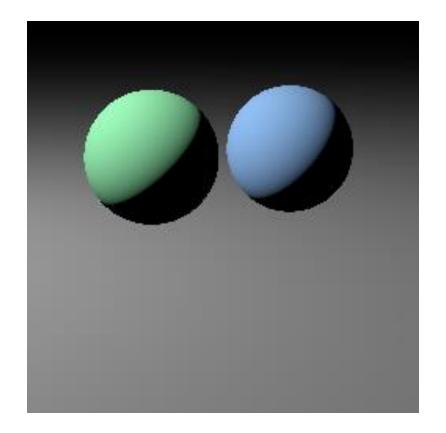
### Image without shading

```
for 0 <= iy < ny
  for 0 <= ix < nx
{
    ray = camera.getRay(ix, iy);
    firstSurface = scene.intersect(result,ray);
    if (firstSurface)
        image.set(ix, iy, firstSurface.color);
    else
        image.set(ix, iy, background.color);
}</pre>
```



### Image with shading

```
for 0 \le iy \le ny
  for 0 \le ix \le nx
    ray = camera.getRay(ix, iy);
    firstSurface = scene.intersect(result,ray);
    image.set(ix, iy,
           firstSurface.shade(ray,light,result.point,
                   result.normal);
     else
       image.set(ix, iy, background.color);
Surface.shade(ray,light,point,normal) {
         I=light.pos-position;
         it= surface.k*light.intensity*max(0,normal.l);
         return surface.color*it;
```

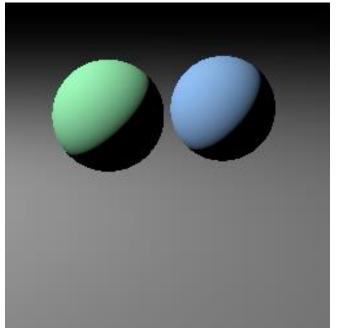


# **Adding Shadows**



### **Shadows**

- Surface is only illuminated if nothing blocks its view of the light.
- With ray tracing it's easy to check if a point in the scene is in shadow.
   just shoot a ray from the point to the light and intersect it with the scene!



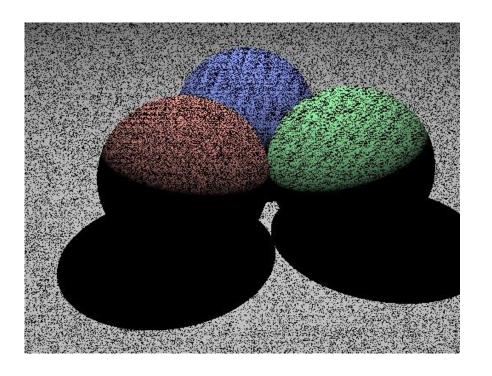
Without shadows

With shadows



### **Classic shadow error**

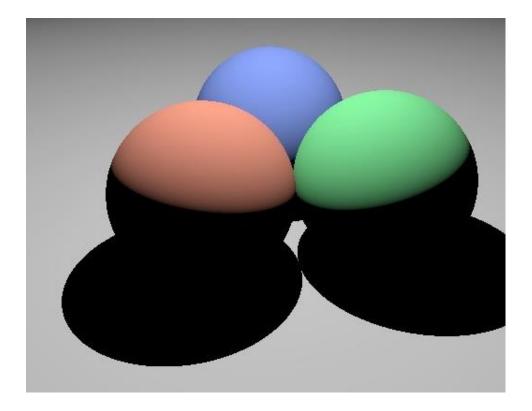
What's going on?





### **Classic shadow error**

Start shadow rays just outside surface



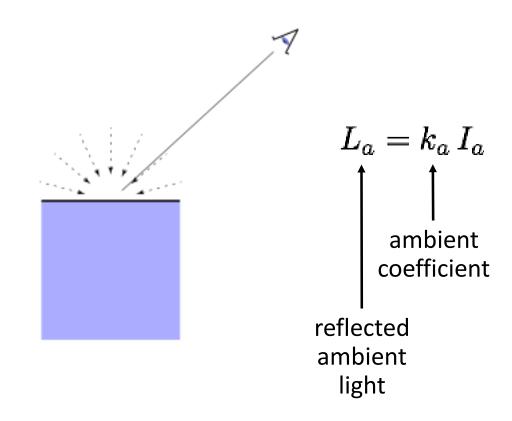
### Multiple lights

- Important to fill in black shadows
- Just loop over lights, add contributions
- Ambient shading
  - black shadows are not really right
  - one solution: dim light at camera
  - alternative: add a constant "ambient" color to the shading...

### **Ambient shading**

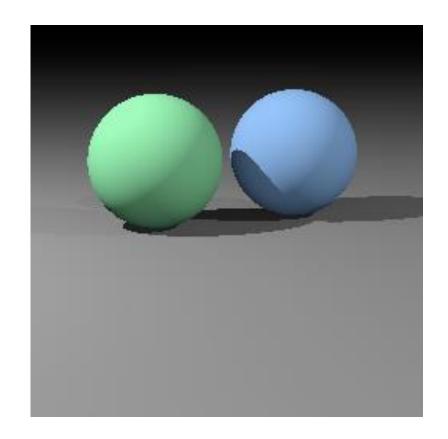
### Shading that does not depend on anything

 add constant color to account for disregarded illumination and fill in black shadows



### Image with multiple lights

```
shade(ray, lights, point, normal) {
  result = ambient;
 for light in lights {
         I=light.pos-position;
         shadowray=(point+\varepsilon*normal,I);
         if !scene.intersect(result,shadowray)
             it= surface.k*light.intensity*max(0,normal.l);
             result+= surface.color*it;
  return result;
```

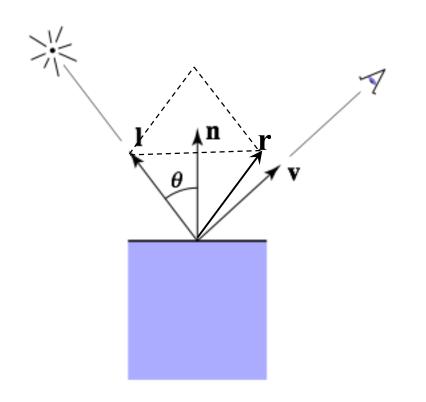




### Mirror reflection

### Intensity depends on view direction

reflects incident light from mirror direction



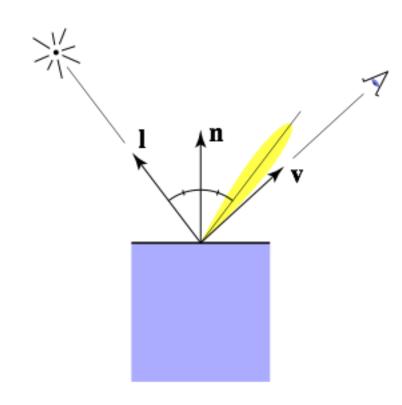
$$r = 2(n.l)n - l$$

### **Specular shading (Phong)**

### Intensity depends on view direction

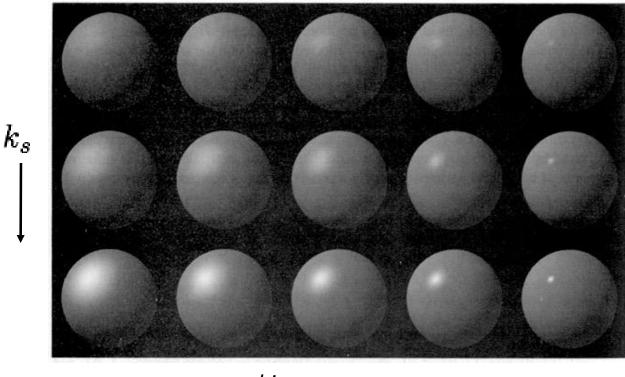
bright near mirror configuration

$$k_s * l_s * (v.r)^{shiny}$$

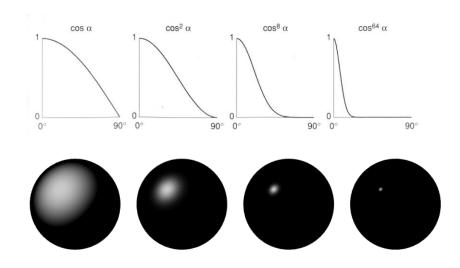


### **Phong model**

### Increasing *shiny* narrows the lobe

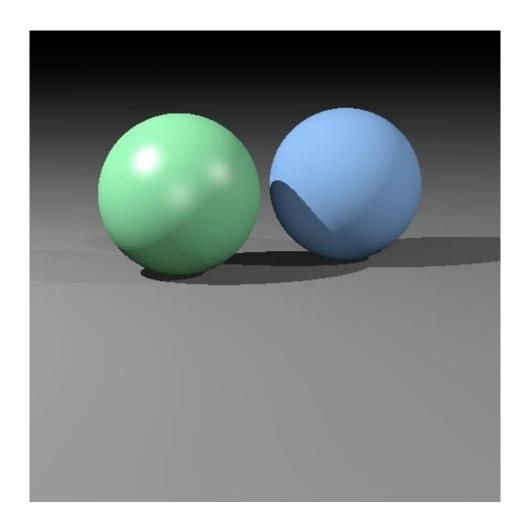






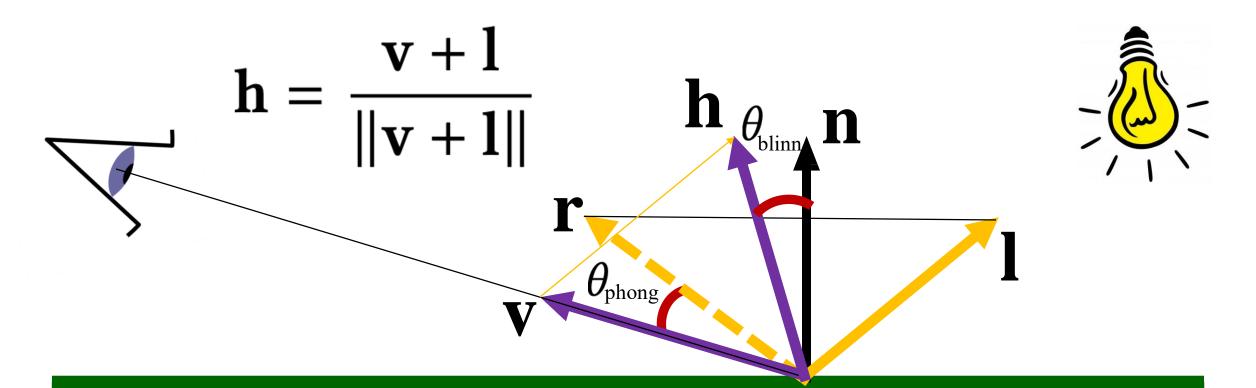


### **Diffuse + Specular (Phong) shading**

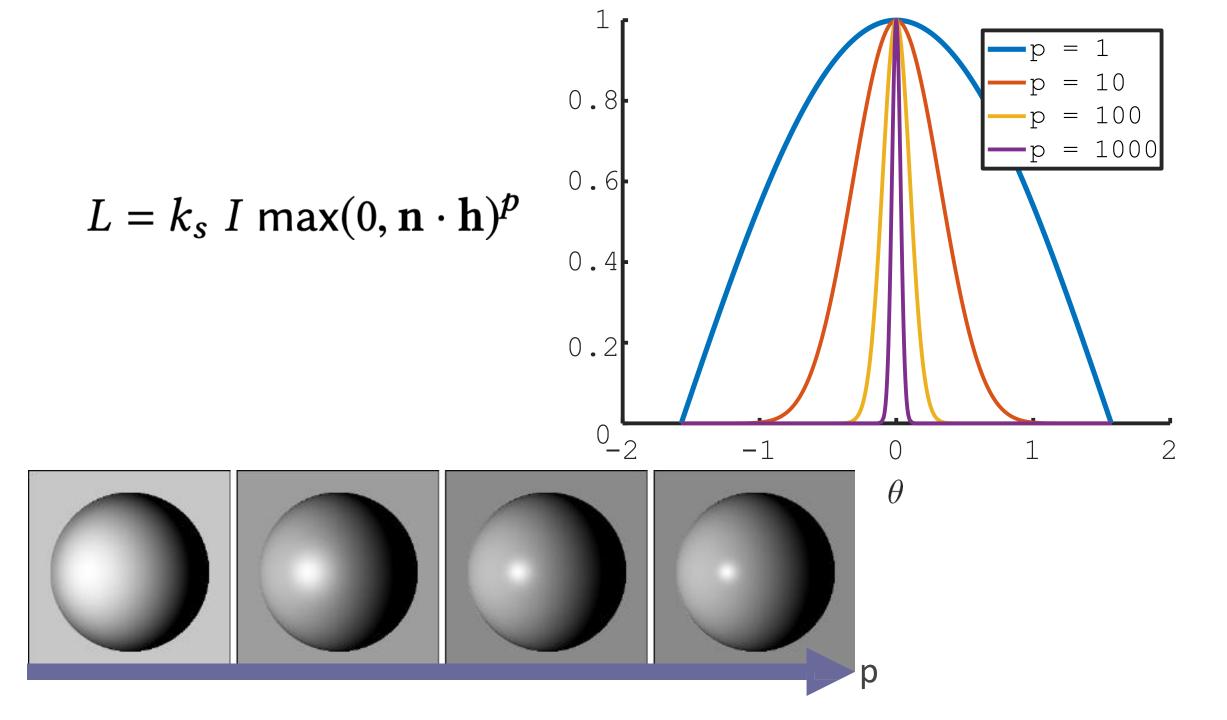




### **Specular Shading (Blinn)**

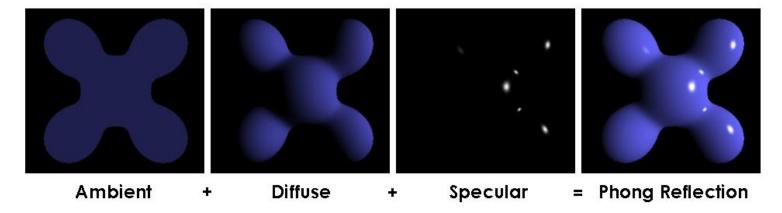








### **Local Illumination**



Usually include ambient, diffuse, Phong in one model

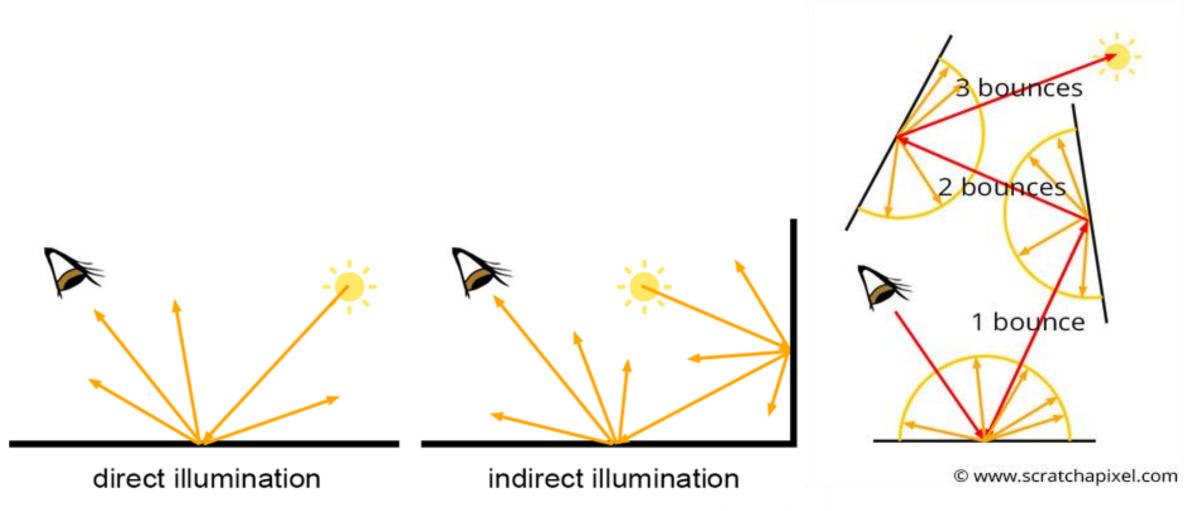
$$L = L_a + L_d + L_s$$
  
=  $k_a I_a + k_d (I/r^2) \max(0, \mathbf{n} \cdot \mathbf{l}) + k_s (I/r^2) \max(0, \mathbf{n} \cdot \mathbf{h})^p$ 

The final result is the sum over many lights

$$egin{aligned} L &= L_a + \sum_{i=1}^N \left[ (L_d)_i + (L_s)_i 
ight] \ L &= k_a \, I_a + \sum_{i=1}^N \left[ k_d \, (I_i/r_i^2) \max(0, \mathbf{n} \cdot \mathbf{l}_i) + 
ight. \ \left. k_s \, (I_i/r_i^2) \max(0, \mathbf{n} \cdot \mathbf{h}_i)^p 
ight] \end{aligned}$$

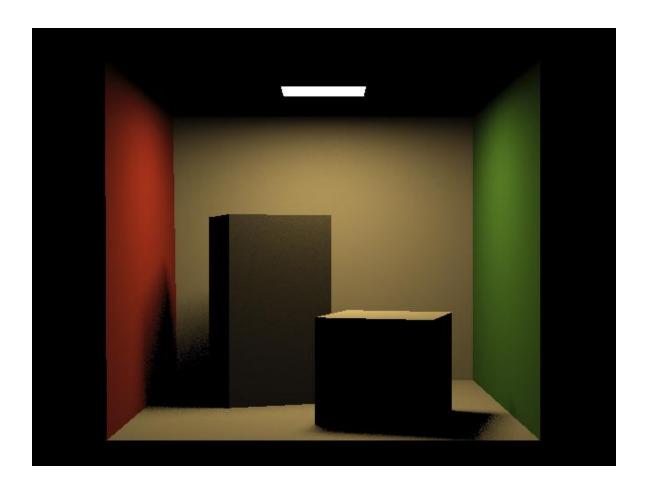


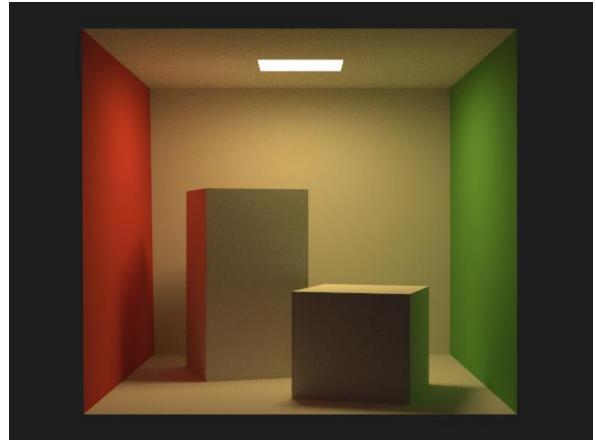
# Direct Illumination ...no Global Effects so far





### **Direct vs. Indirect Illumination**





http://www.deluxerender.com/2017/01/the-cornell-box-a-renderers-rite-of-pathage/https://en.wikipedia.org/wiki/Cornell\_box



### Local vs. Global Illumination

### **Local Illumination Models**

- e.g. Phong, Blinn.
- Model source from a light reflected once off a surface towards the eye.
- Indirect light is included with an ad hoc "ambient" term which is normally constant across the scene.

### Global Illumination Models

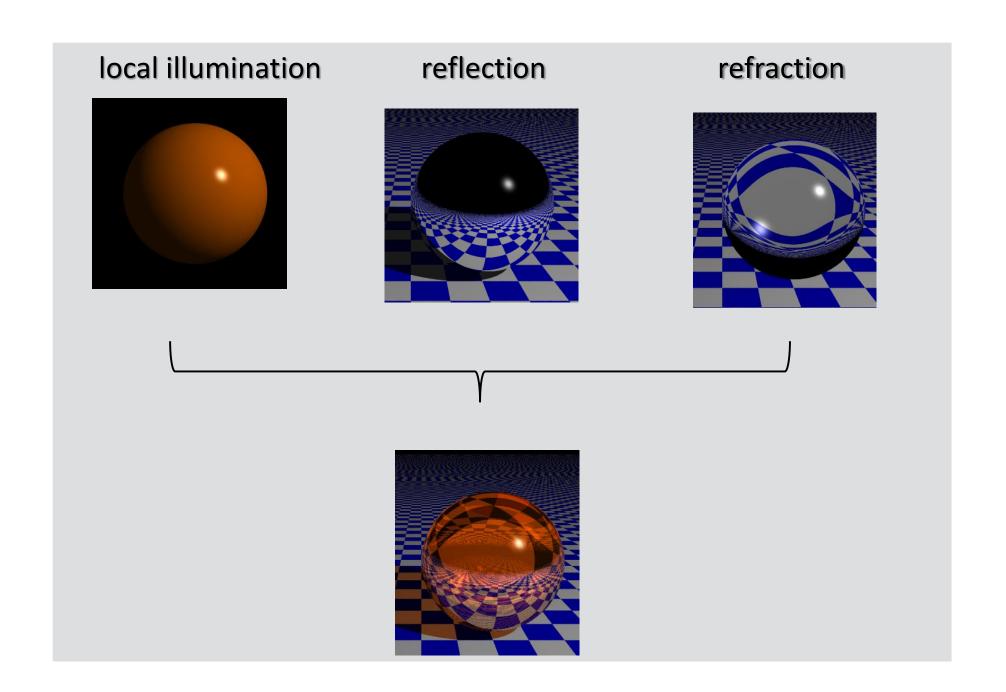
- e.g. recursive ray tracing (incomplete model).
- Try to measure light propagation in the scene.
- Model interaction between objects, other objects, and their environment

### **Path Tracing**

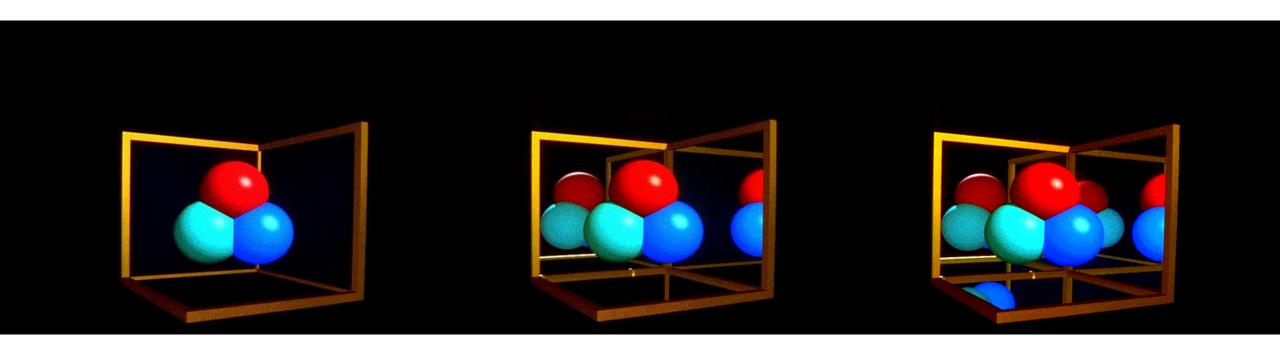
 A ray from a light L can bounce of any number of specular S and diffuse objects D before entering the eye E. The paths from E to L for eg. can be

- Rays are infinitely thin
- Don't disperse

Ray Tracing model shiny objects exhibiting multiple reflections, i.e. paths of the form
 E - S\* - D+ – L.



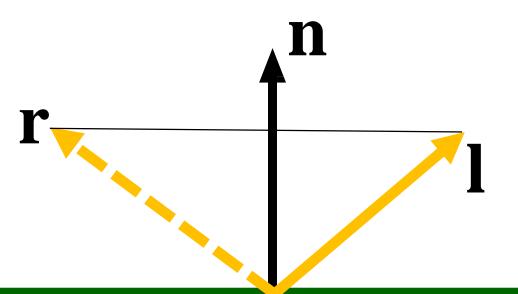
# **Ray Tracing recursion**





# Reminder: reflected ray

$$r = 2(n.l)n - l$$



#### **Ray Tracing**

```
for each pixel in the image {
    pixel colour = rayTrace(viewRay, 0)
}
```

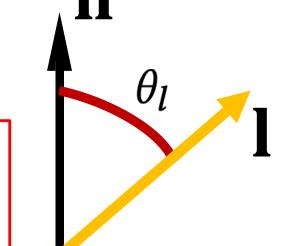
```
colour rayTrace(Ray, depth) {
    for each object in the scene {
        if(Intersect ray with object) {
            colour = shading model
            if(depth < maxDepth)
            colour +=rayTrace(reflectedRay, depth+1)
        }
    }
    return colour
}</pre>
```



# **Refraction (Snell's Law)**

$$c_l \sin(\theta_l) = c_t \sin(\theta_t)$$

$$\mathbf{t} = -\frac{c_l}{c_t} \mathbf{1} + \frac{c_l}{c_t} \cos(\theta_l) \mathbf{n} - \cos\theta_t \mathbf{n}$$





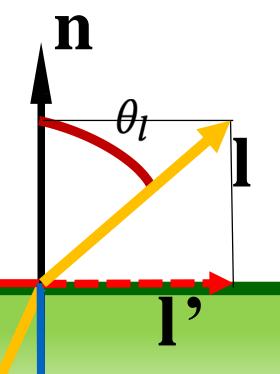


# **Refraction (Snell's Law)**

$$\mathbf{t} = -\frac{c_l}{c_t} \mathbf{1} + \frac{c_l}{c_t} \cos(\theta_l) \mathbf{n} - \cos\theta_t \mathbf{n}$$

$$\theta_t = \sin^{-1}(c_1/c_t \sin(\theta_1))$$

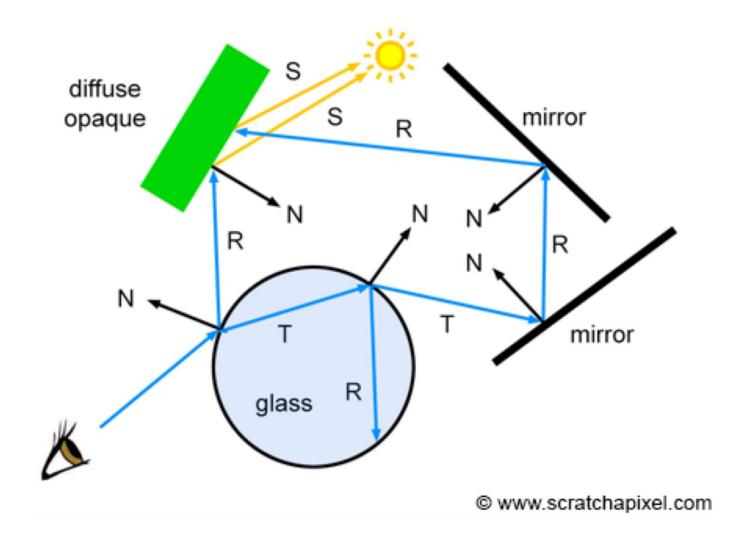
$$l = l' + cos\theta_1 n$$





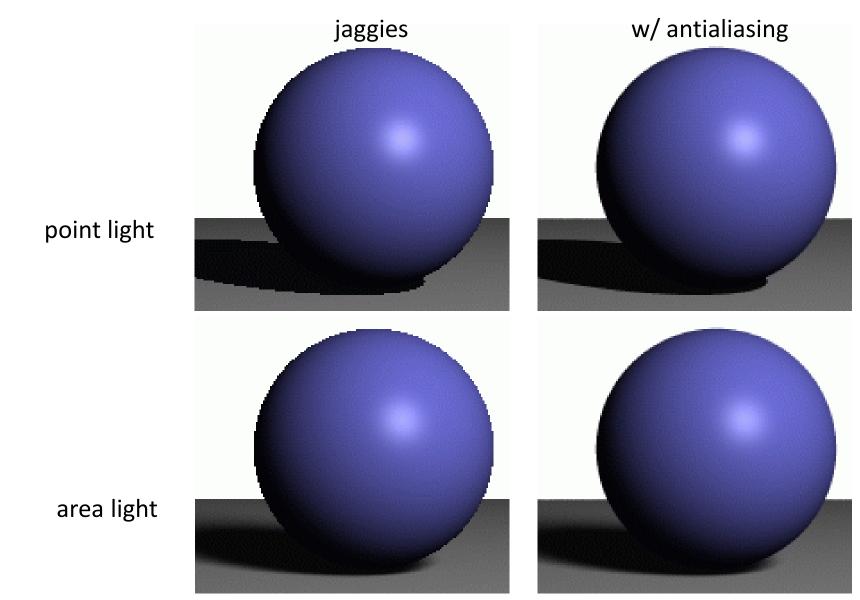
```
colour rayTrace(Ray, depth) {
    for each object in the scene {
         if (Intersect ray with object) {
              colour = shading model
              if (depth < maxDepth) {</pre>
                   colour +=
                        rayTrace(reflectedRay, depth+1)
                   colour +=
                        rayTrace(refractedRay, depth+1)
    return colour
```

## **Ray Spawning**





# **Ray Tracing supersampling**





#### **Ray Tracing**

- Unifies in one framework
  - Hidden surface removal
  - Shadow computation
  - Reflection of light
  - Refraction of light
  - Global **specular** interaction

#### **Ray Tracing Deficiencies**

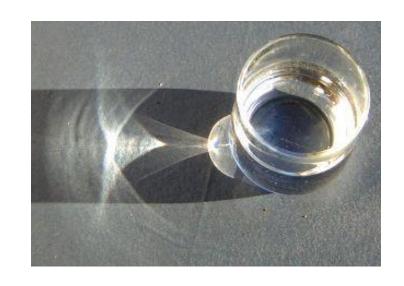
- Intersection computation time can be long (solution: **bounding volumes**).
- Recursive algorithm can lead to exponential complexity (solution: stochastic sampling).
- Ignores light transport mechanisms involving diffuse surfaces.

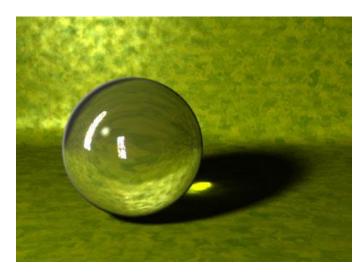




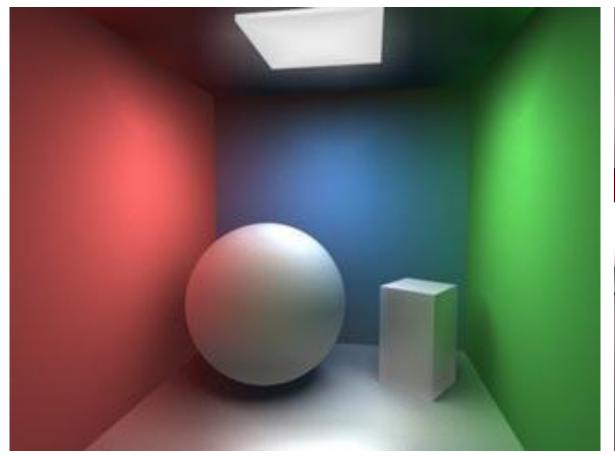
#### **Ray Tracing Improvements: Caustics**

- Transport E-S-S-S-D-S-S-L
- Trace from the light to the surfaces and then from the eye to the surfaces
- "shower" scene with light and then collect it
- "Where does light go?" vs "Where does light come from?"
- Good for caustics





# Radiosity: E – D – D – D - L







## The Rendering Equation



$$L_o(x,ec{w}) = L_e(x,ec{w}) + \int_\Omega f_r(x,ec{w}',ec{w}) L_i(x,ec{w}') (ec{w}'\cdotec{n}) \mathrm{d}ec{w}'$$





## **The Rendering Equation**

$$L_o(x,ec{w}) = L_e(x,ec{w}) + \int_\Omega f_r(x,ec{w}',ec{w}) L_i(x,ec{w}')(ec{w}'\cdotec{n})\mathrm{d}ec{w}'$$

outgoing light at position **x** and direction **w** 

emitted light at position **x** and direction **w** 

and

reflected light at position **x** and direction **w**'



## **The Rendering Equation**

$$L_o(x,ec{w}) = L_e(x,ec{w}) + \int_\Omega f_r(x,ec{w}',ec{w}) L_i(x,ec{w}') (ec{w}'\cdotec{n}) \mathrm{d}ec{w}'$$

the reflected light at position **x** and direction **w'** 

is the integral over all possible directions **w**'

the incoming light from all directions

times

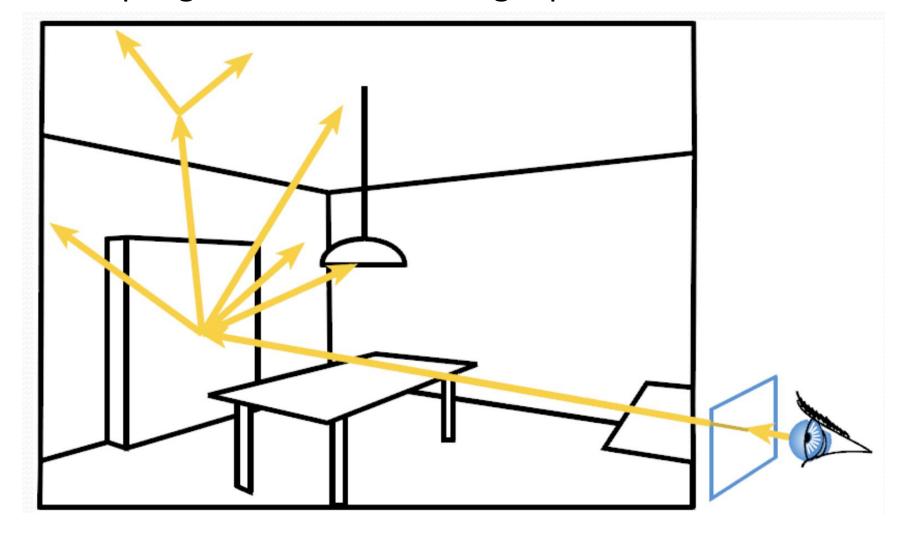
#### **BRDF**:

a function describing how light is reflected at an opaque surface



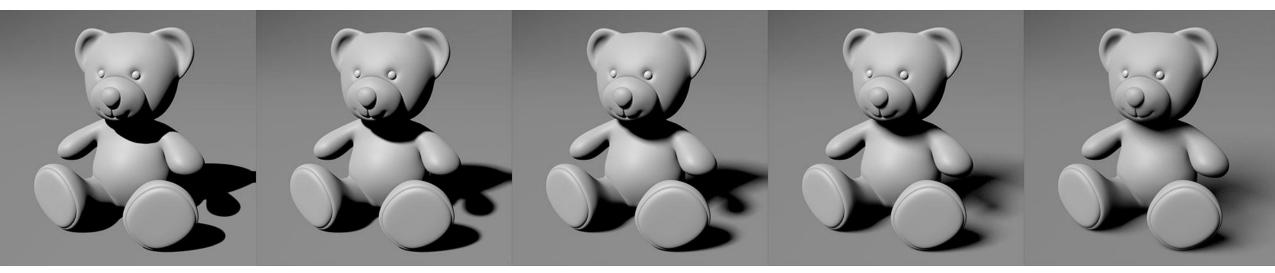
#### **Monte Carlo Methods**

Rely on random sampling to "solve" rendering equation



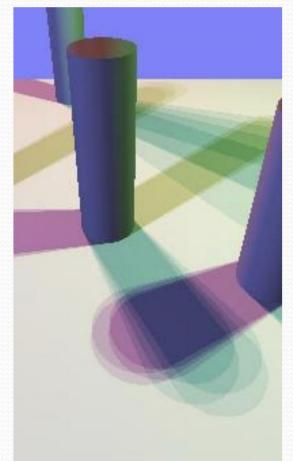


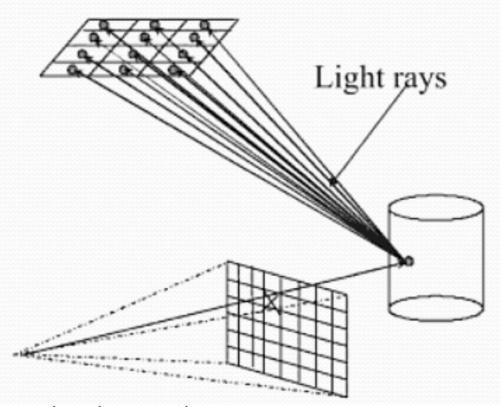
#### Hard v soft shadows



Hard shadow More realistic soft shadows

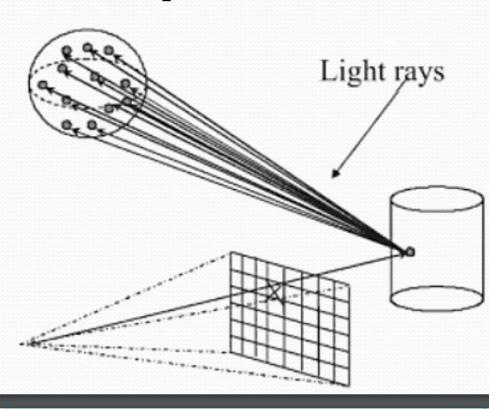
- Disadvantages of the simple uniform method:
  - Very time consuming
  - If the grid resolution is low, artifacts appear in the shadows.

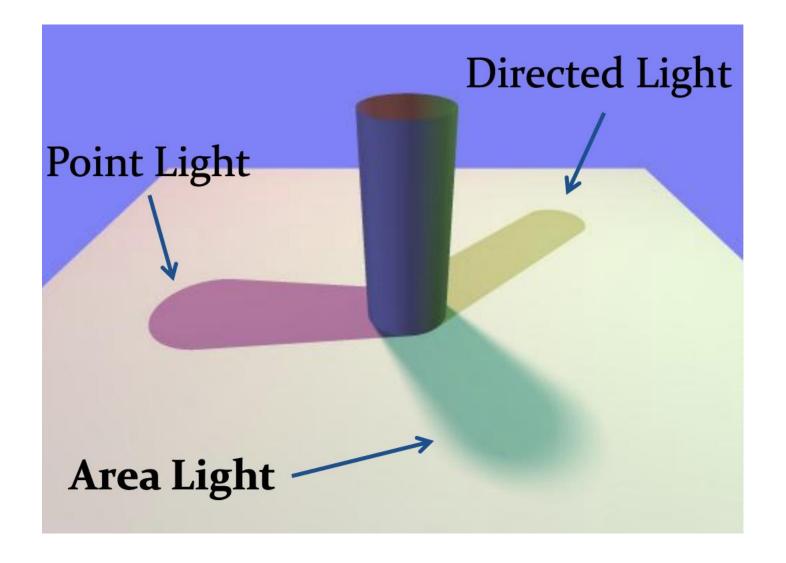




#### Monte-Carlo Area light

- Light is modeled as a sphere
- Highest intensity in the middle. Gradually fade out.
- Shoot n rays to random points in the sphere
- Average their value.







# **Faster Intersections for Ray Tracing**

