

# **High Performance Fortran**

Tutorial

at

Europar'99

by Fabien COELHO

## **Fabien Coelho**

- Engineering degree in 1993
- PhD on HPF Compilation in 1996
- researcher at cole des mines de Paris, France
  - algebraic transformations to improve performance
  - focus on scientific applications
  - PhD Student: Julien Zory
- visitor at IMEC, Belgium
  - Francky Catthoor's team
  - program transformations for low power
  - focus on embedded applications

## Sources

- HPF language specifications  
<http://dacnet.rice.edu/Depts/CRPC/HPFF/>
- The HPF Handbook  
by Koelber, Loveman, Schreiber, Steele and Zosel  
MIT Press

## **Tutorial outline**

- What is HPF? MPI? OMP?
- History of HPF
- Presentation of HPF
- Examples of codes
- Conclusion

## **MPI vs HPF vs OMP**

What they have in common:

- 3 letters acronymes
  - Message Passing Interface
  - High Performance Fortran
  - Open Multi Processing
- to express parallelism
- based on standard languages
  - Fortran
  - C

## Why Parallelism?

So as to improve performance of applications

- inside processors:
  - super-scalar/VLIW  
different instructions at the same time
  - pipelines, vector processors  
start next computation before previous is finished
  - replication of functional units
- network of processors (slow network/fast processors, 2 orders!)

## Parallel Hardware: Multiple Data

- Shared Memory vs Distributed Memory
  - SM: communications/addressing by OS/HW
  - DM: YOU take care (user/compiler, OS...) communication and addressing are hard management of data distribution among processors...
- Control flow: Single vs Multiple Instruction
  - SIMD: one processor + many computing elements
  - MIMD: multiple processors

## Examples of parallel machines

general purpose machines: MIMD survived

- SM-MIMD: shared memory multi-processors  
SUN servers, Intel-based mp  
not scalable wrt #procs
- DM-MIMD: IBM SP2, Cray T3E, SGI Origin 2000  
scalable wrt #procs

special purpose machines: often SIMD (DSP, ASICS)

- DM-SIMD: CM2, MMX (in processor)



## Parallel Programming

- Control Parallelism (based on threads/processes...)  
fork/join model, synchronizations...
  - MPI: processes are spawned
  - OMP: multi threading on loops
  - Tera computer...
- Data Parallelism
  - same computation on different elements
  - Fortran 90, HPF
  - simpler codes (one flow, SIMD-like)

## Data Parallelism

- manipulation of arrays as scalars
- operation can be applied in parallel

```
program dataparallel
integer, parameter:: n=1000
real, dimension(n,n):: A, B, C
A = ..., B = ...
C = 0.0
do while (MAXVAL(ABS(C-B))>0.1)
    C = B ! old B is saved
    B = MATMUL(A, B) + B
end do
end
```

## **Control parallelism**

- fork parallel communicating 'processes'
- beware of data sharing!
- join back...
- can be hidden in the language (OMP)  
the memory is shared among processors
- addressing issues handled by OS/HW

## Control parallel example

```
program controlparallelism
  real, dimension(n):: v
  integer:: count
  count = 0
!$omp parallel, do
  do i=1, n
    if (v(i).gt.floor) then
! synchronization needed...
!$omp      atomic
      count = count + 1
    endif
  enddo
!$omp end parallel
```

## **Control parallelism: message passing**

- fork PROCESSES (a la Unix)
- library to send and receive messages
- addressing managed by programmer

## MP example

```
program messagepassing
  real, dimension(n/2):: v ! v(n)
  spawn(2,...)
    if (i am process 1) then
! v holds first half v(1) is v(1)
      senddatato(2)
      ...
    else if (i am process 2) then
! v holds second half, v(1) is V((n/2)+1)
      receivedatafrom(1)
      ...
    endif
```

## **Control vs Data parallelism**

A dual philosophy:

- control parallel
  - distribute iterations
  - data will follow
- data parallel
  - distribute data
  - iterations will follow

## **Parallel programming and architectures**

- Shared Memory, MIMD
  - OMP is the only standard! things are simple!
- Distributed Memory, MIMD
  - MPI: low level, everything by hand!
  - HPF: put the trouble on the compiler!



## What is the trouble?

On a Distributed Memory parallel machine

- find available parallelism
  - program semantics must not be changed!
  - automatic detection of parallelism?
  - hints: language? assertions?
- must distribute data on processors!
  - otherwise no parallelism!
  - how? when? hints?
  - impact on addressing? on performance?
- non local data communication and store?

## High Performance Fortran

- Data Parallel language
- based on Fortran 90/95  
the language of scientific computing
- plus directives (i.e. hints as comments)  
YOU are going to help!  
program still in Fortran
- a de facto standard  
not a ISO or ANSI standard  
however only one available!  
contribution to the standard (FORALL)

## Fortran standard...

- dusty deck Fortran IV/66/77 code legacy
- engineers are used to Fortran
- software engineering improvements with Fortran 90
  - structured programming
  - data structures, allocate
  - better library of functions  
e.g. TRANSPOSE MATMUL
- other option: SISAL (functionnal)
- new Fortran 95: small improvements

## History of HPF: the Forum

- DEC initiative end of 1991
- composition: vendors, researchers, users
- aim: to propose an industry standard
  - offer portability for users
  - as a commercial argument
- meetings

## HPF versions...

- 03/1992-03/1993: HPF 1.0 + subset  
subset: selection of features, Fortran 77 based
- 04/1994-10/1994: HPF 1.1 + subset
- 01/1995-11/1996: HPF 2.0 + approved extensions  
AE: how should extensions should look like  
no more subset
- kernel HPF: efficient part of the language

## Organization

- regular meetings in the USA
- specialized work groups AND mailing lists
  - data distribution, forall
  - Fortran 90, intrinsics, I/O...
- one regularly-participating organisation, one vote
- language defined by the majority...

## Existing base

- Standards
  - Fortran 77
  - Fortran 90 (long awaited Fortran 8x)
  - PC Fortran (for share memory)
- Vendors products
  - CM-Fortran from Thinking Machine
  - MPP-Fortran
- Research prototypes
  - Fortran D (Ken Kennedy, Rice University)
  - Vienna Fortran (Hans Peter Zima, Vienna

University)



## Ideas taken

For this existing base

- compilation directives seen as comments
- sequential program + data mapping
- data parallel array sections (F90)
- concepts of alignment and distribution  
i.e. two level mapping
- two semantics of parallel loops

## Life of the Forum

- great battles: Templates or not Templates
- lost projects: I/O
- forgotten principles  
not only directives  
but extensions included in Fortran 95!
- forgotten dead lines;-)

## **HPF 1.0, May 3 1993**

- a Fortran for parallel computers
- data parallel model
- based on Fortran 90
- data mapping directives
- parallel constructs/instructions
- intrinsic functions (reductions)
- official subset...

## **HPF 2.0, October 19, 1996**

- hopefully the same language!
- specification fixes
- features deleted... since in ISO Fortran!
- features moved as approved extensions
- new approved extensions developed
- new feature included: REDUCTION
- no more subset

## HPF Programming Model

- 2 factors influence parallel performance
  - available parallelism
  - needed communications
- HPF tunes the program:
  - parallel constructs
  - data mapping directives

## Presentation of the language 2.0

- data mapping directives
  - data parallel application are data-driven
  - communications cost is prohibitive
  - emphasize data mapping
- parallelism!
  - implicit parallelism
  - parallel loopS
  - intrinsics
- other issues

## Directives

- considered as Fortran comments
- can be declarative or executable
- can expand on several lines  
with F90 continuations &
- spaces are meaningful!

```
      program directive
!hpf$ here is a directive
      print *, 'hello'
*hpf$ another directive &
chpf$   spawned on 2 lines
      end
```

## Data Mapping Model

- Group lead by Guy L. Steele Jr
  - was Thinking Machine Corp.
  - then at SUN for JAVA
- Aims
  - specify the mapping of arrays
  - onto the processors of a DM machine.
  - understandable intuitive for users
  - optimisable for compilers
  - suitable to applications



## **2/3 level mapping**

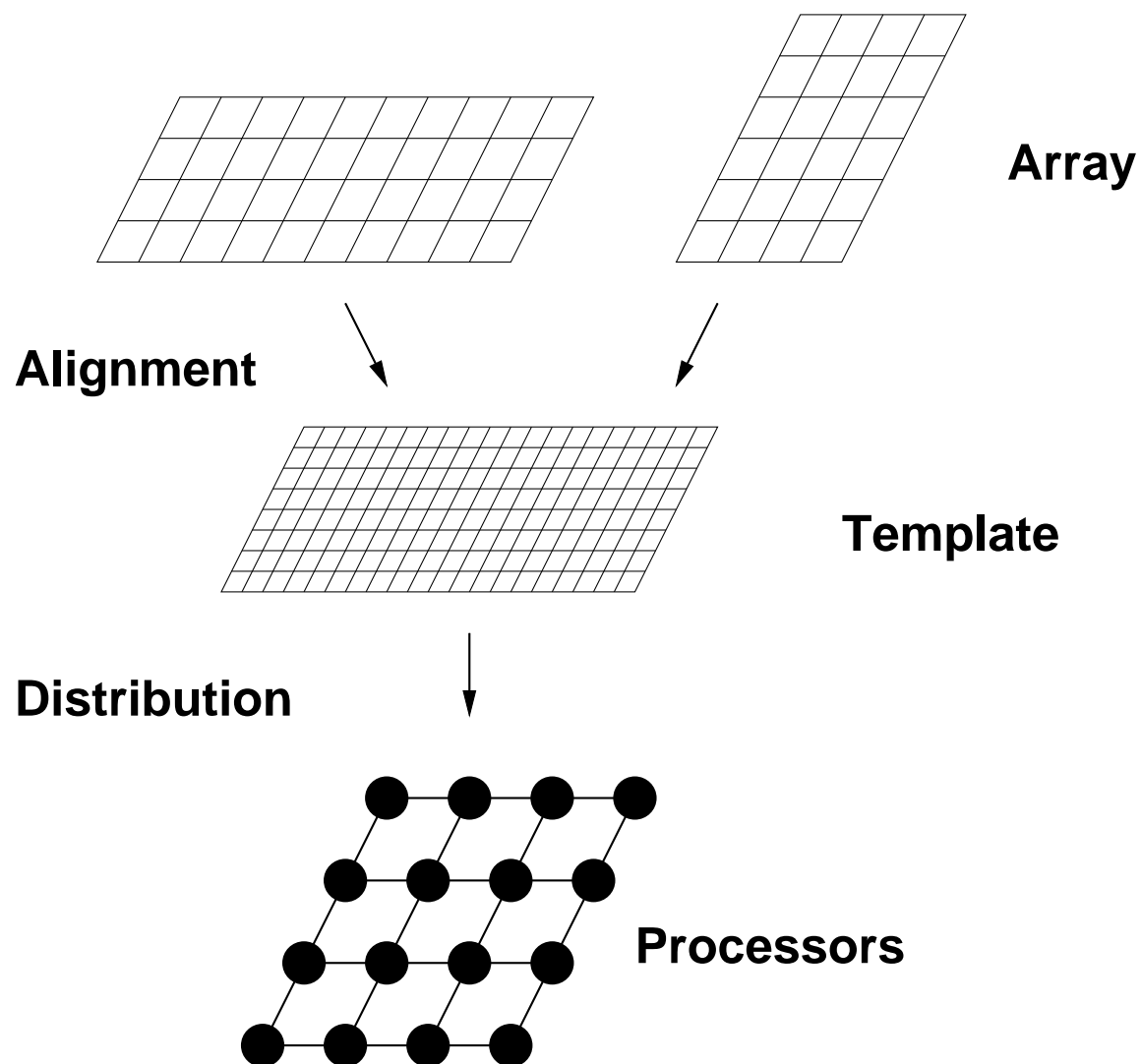
- Arrays are aligned with Templates
- Templates are distributed on Processors
- Processors may be mapped on physical processors

Only the 2 first levels are specified and used

4 directives:

ALIGN TEMPLATE DISTRIBUTE PROCESSORS

## **HPF Mapping Model**



## 2 Level Mapping

load balancing and reduced communications

- Affine Alignment: ALIGN
  - relative data mapping  
'this array must be mapped as this one'
  - close to the application/problem  
decide data locality
- Regular distribution: DISTRIBUTE
  - distribute data on the processors, BLOCK or CYCLIC
  - close to the machine/architecture

## Templates

TEMPLATE is a declaration directive

- array of nothing
- not allocated!
- used as an alignment target
- an array can be used as a template

```
!hpf$ template t(100), t2(n,m)
!hpf$ dimension(n,n), template :: &
!hpf$                      domain
```

## Alignment

ALIGN is a declaration directive

- arrays are aligned with templates
- 2 array elements aligned with the same template element will be on the same processor
- data locality

```
!hpf$ ALIGN A(I,...) WITH T(affine(I),...)
```

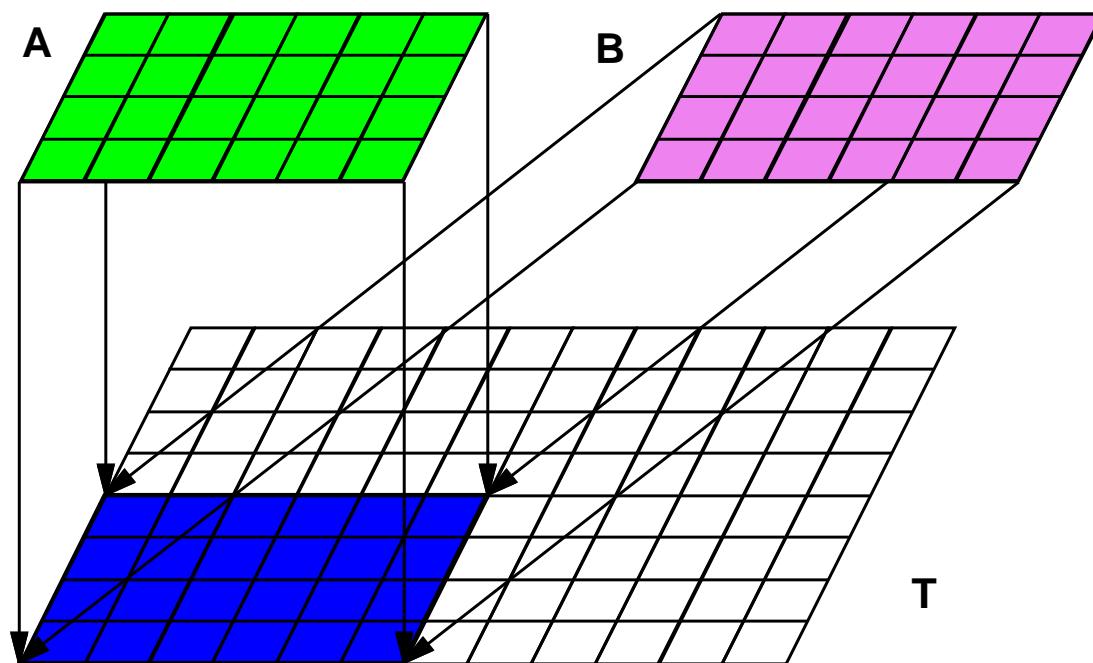
## Constraints

- Affine function
  - one dummy variable  $a*I+b$
  - $a$  and  $b$  are integers
- one use of dummy variables  
NO: `ALIGN A(I) WITH T(I,I)...`

## **Alignment expressivity**

- direct mapping
- transposition
- reversing
- replication
- collapsing
- ...

## Direct mapping

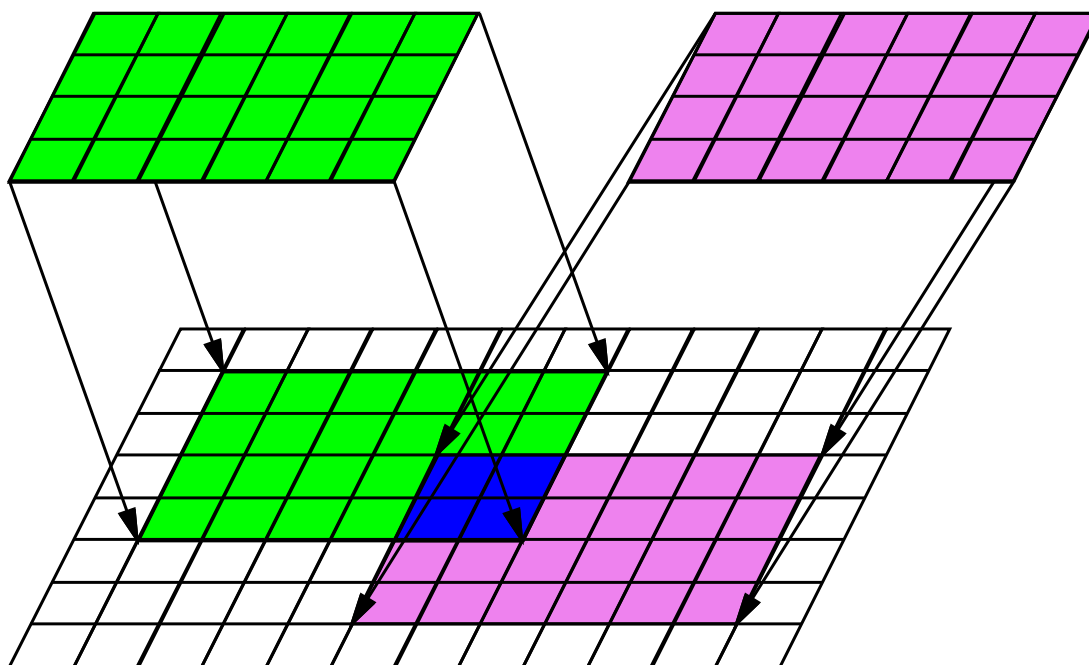


align  $A(i, j)$  with  $T(i, j)$

align B with T



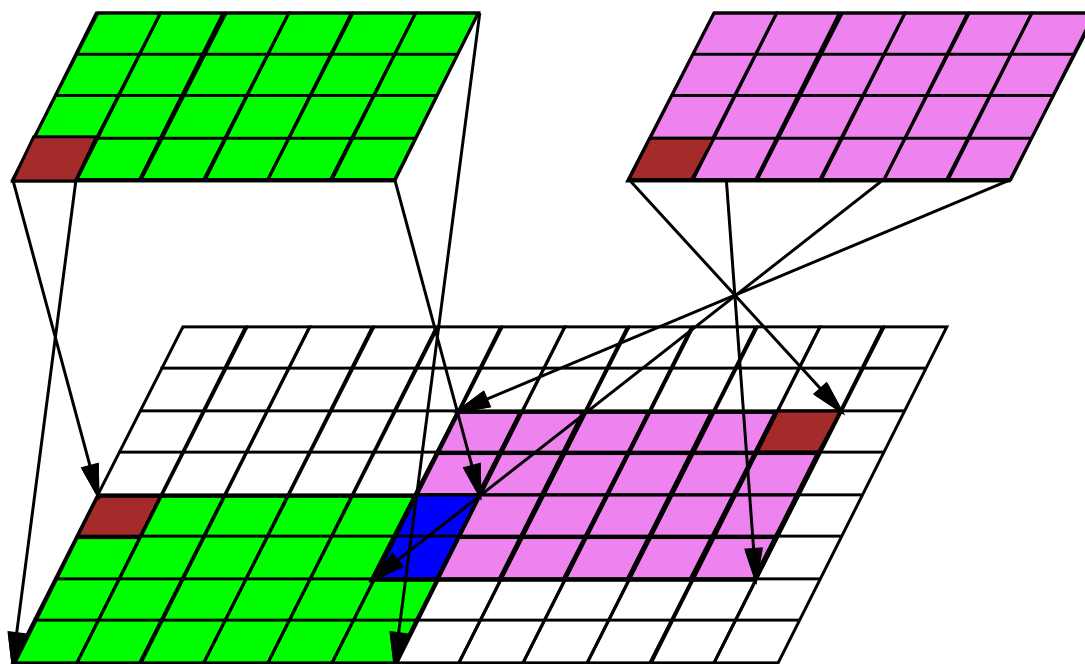
## Shift



align A(**i**,**j**) with T(**i+1**,**j+3**)

align B(:, :) with T(**6:11**,**2:5**)

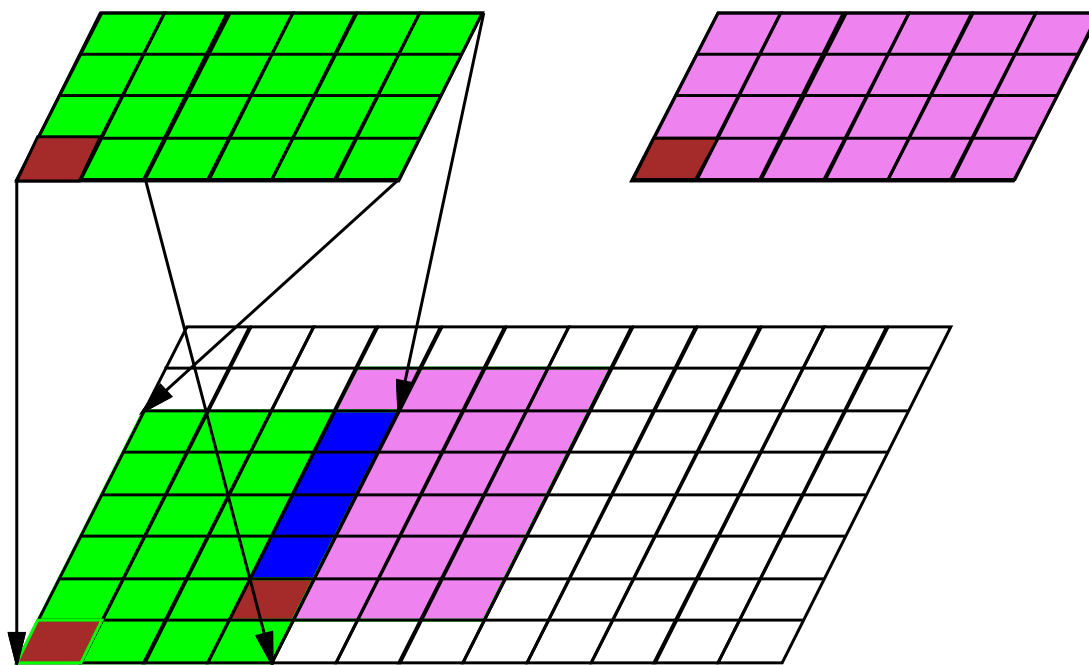
## Reversing



align A(**i**,**j**) with T(**i**,**5-j**)

align B(:, :) with T(**11:6:-1**, **6:3:-1**)

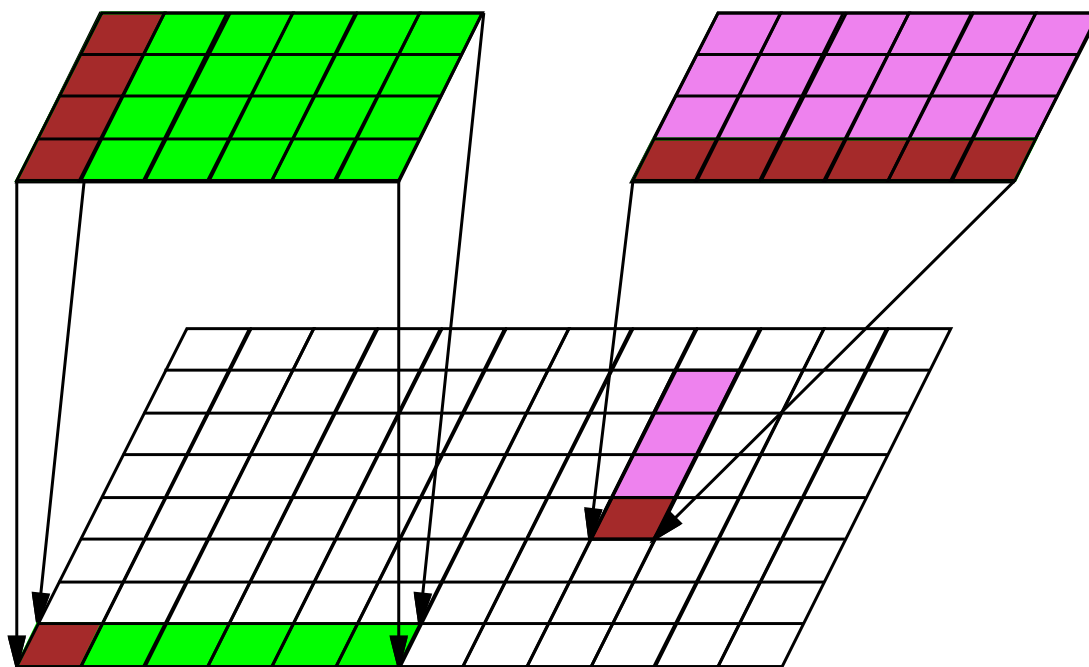
## Transposition



align A(**i**,**j**) with T(**j**,**i**)

align B(**i**,**j**) with T(**j**+3,**i**+1)

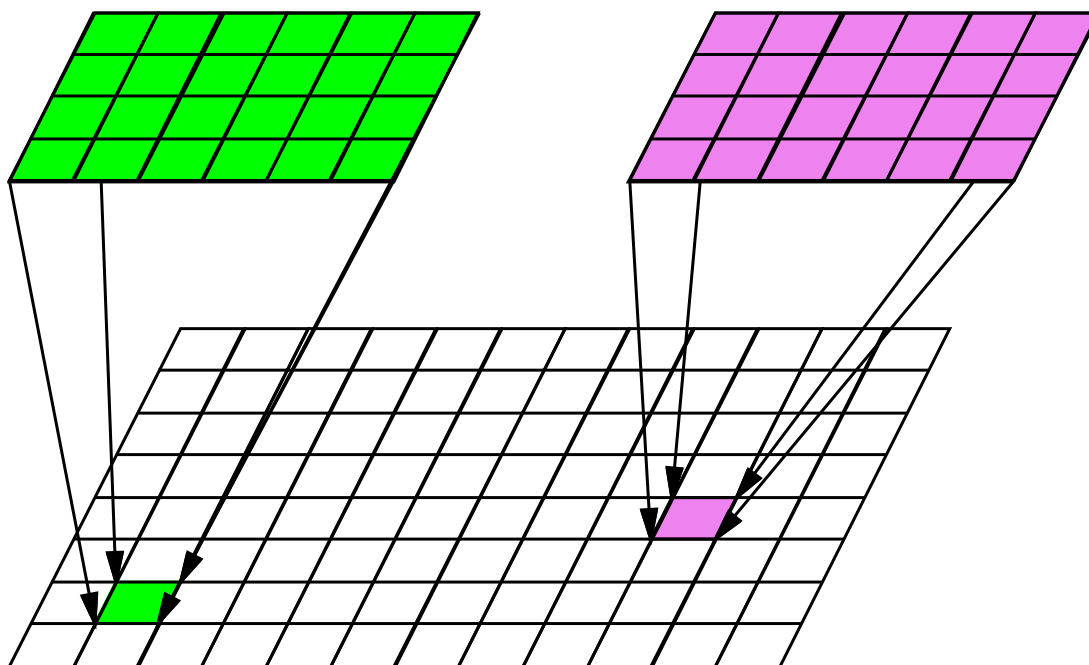
## Collapsing



align A(**i**,\*) with T(**i**,1)

align B(\*,:) with T(**9**,4:7)

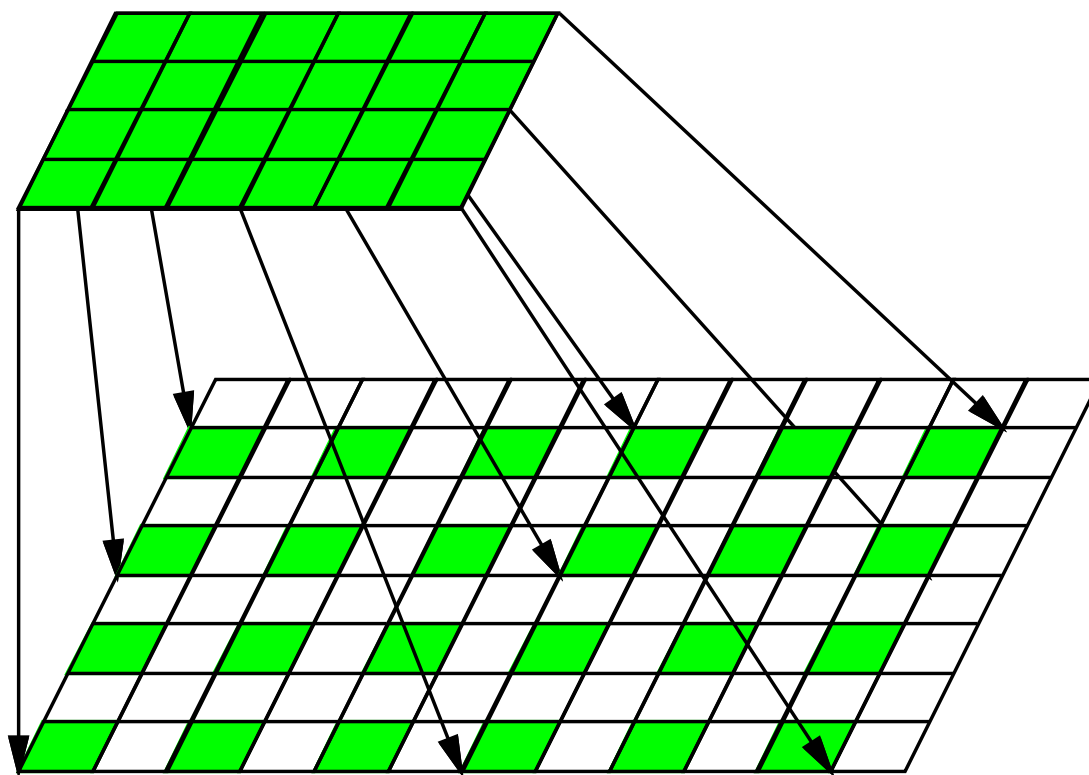
## More collapsing



```
align A(*,*) with T(2,2)
```

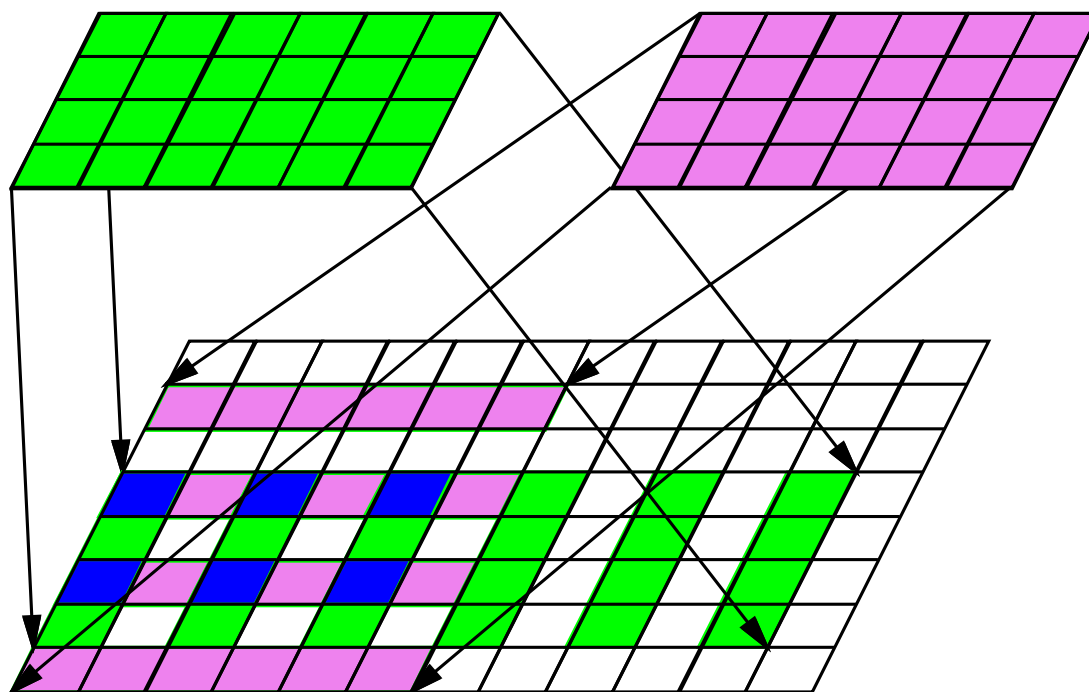
```
align B(*,*) with T(10,4)
```

## Scattering



align  $A(i, j)$  with  $T(2*i-1, 2*j-1)$

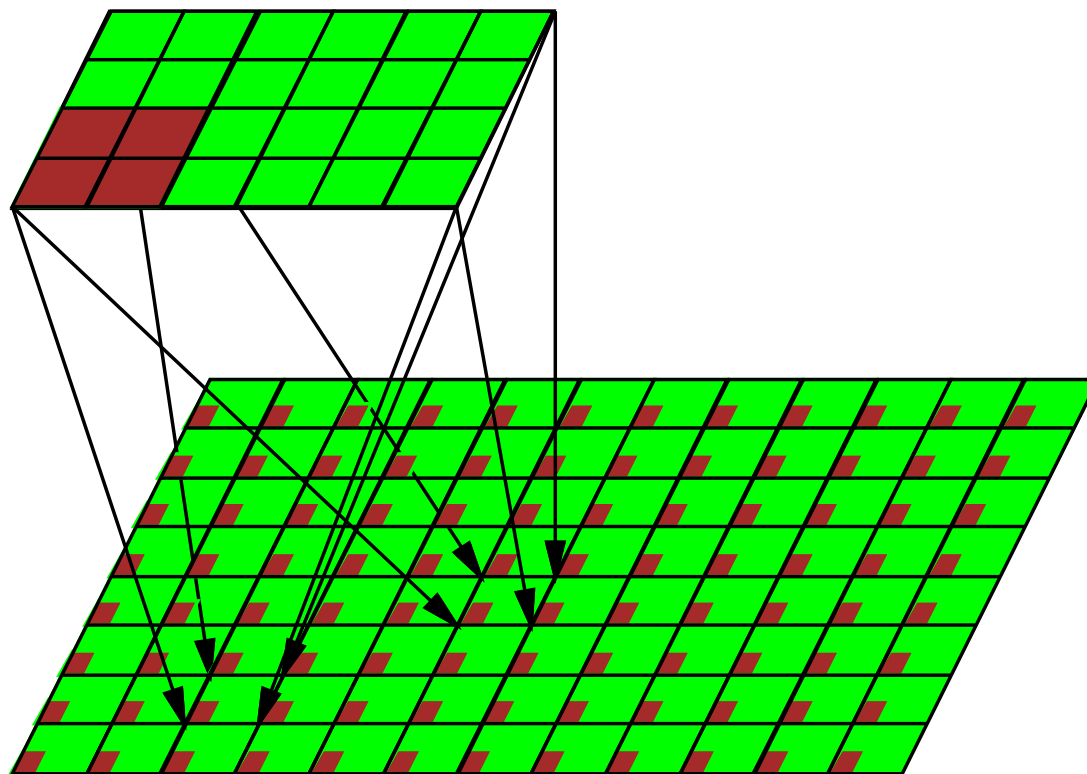
## Scattering



align A(*i*,*j*) with T(2\**i*-1,*j*+1)

align B(*i*,*j*) with T(*i*,2\**j*-1)

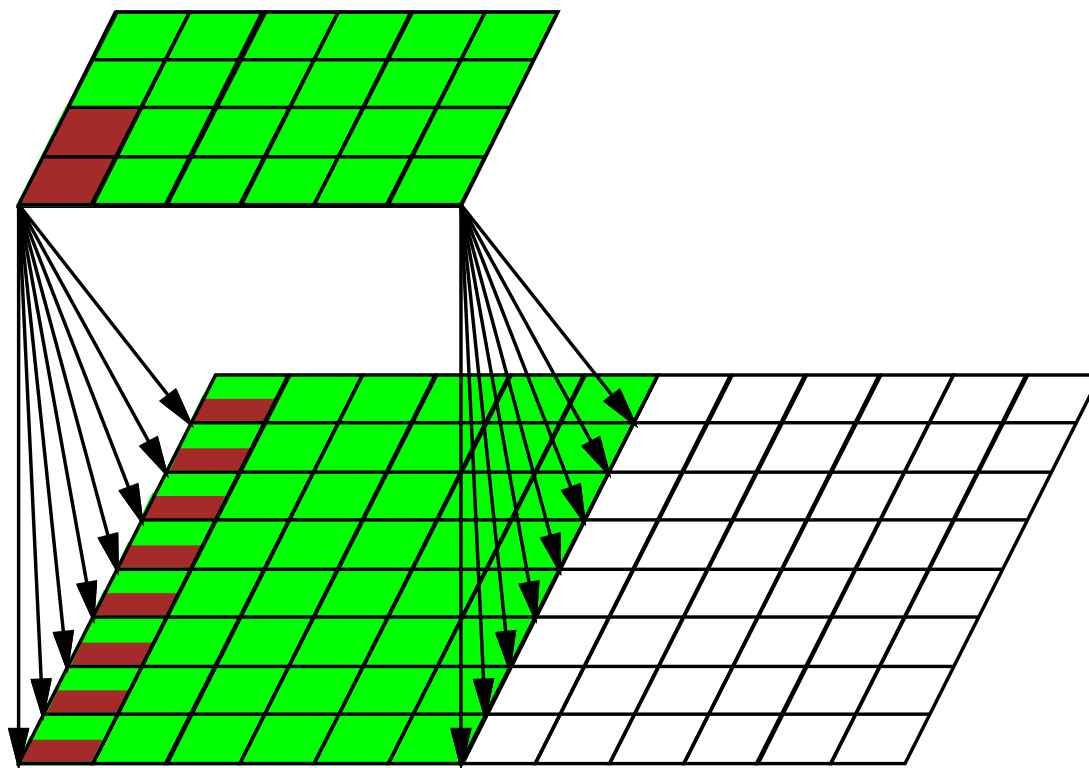
## Replication



```
align A(*,*) with T(*,*)
```

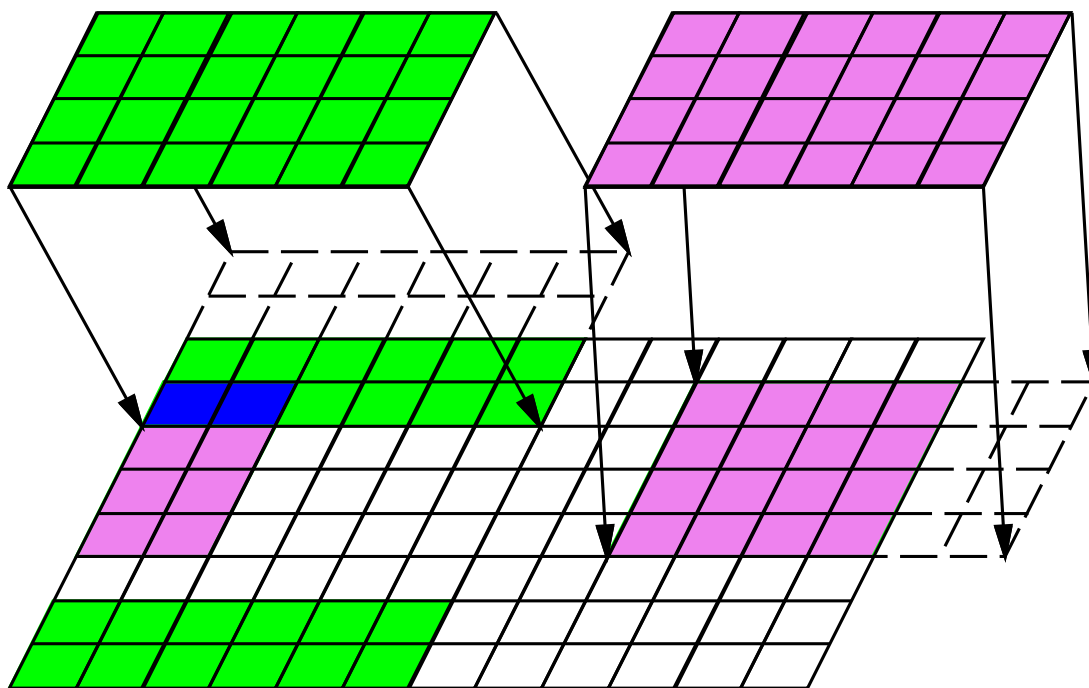


## Partial replication



```
align A(:,*) with T(:,*)
```

## NO overlaps



align A(i,j) with T(i,j+6)    ! non

align B(:, :) with T(9: , 4:7)    ! non

## Processors

PROCESSORS is a declaration directive

- declares abstract processor arrays
- often correspond to actual processors
- can query the number of processors:

`NUMBER_OF_PROCESSORS()`

```
!hpf$ PROCESSORS P(10), Q(4,4)
```

```
!hpf$ PROCESSORS Z(2:3,8)
```

```
!hpf$ PROCESSORS R(NUMBER_OF_PROCESSORS())
```

## Distribution

DISTRIBUTE is a declaration directive

- templates are distributed on processors
- template elements are grouped together on a processor element

```
!hpf$ DISTRIBUTE T(BLOCK,*) ONTO P
```

```
!hpf$ DISTRIBUTE T2(CYCLIC,CYCLIC(10)) ONTO Q
```

## Use of **BLOCK** and **CYCLIC**

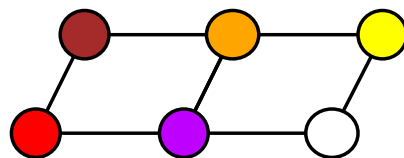
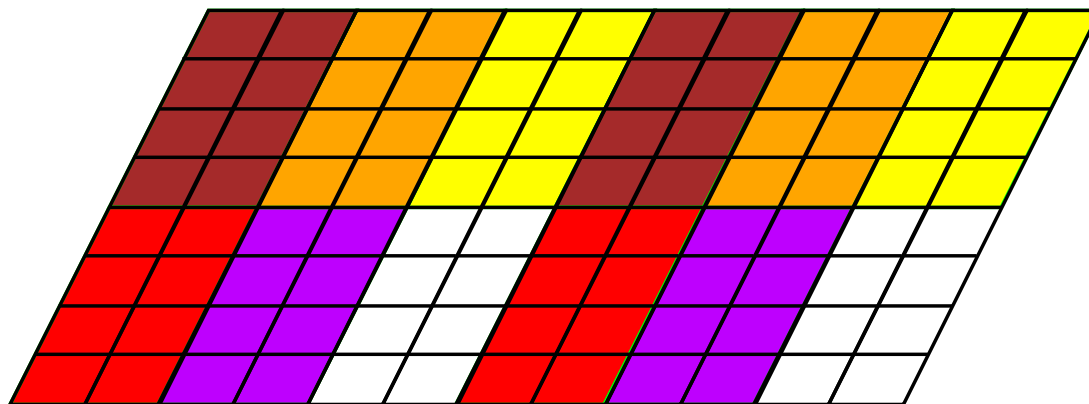
**BLOCK** regular distribution for neighbor comms  
typical of stencil computations

**BLOCK(n)** adjust block size

**CYCLIC** distribute load

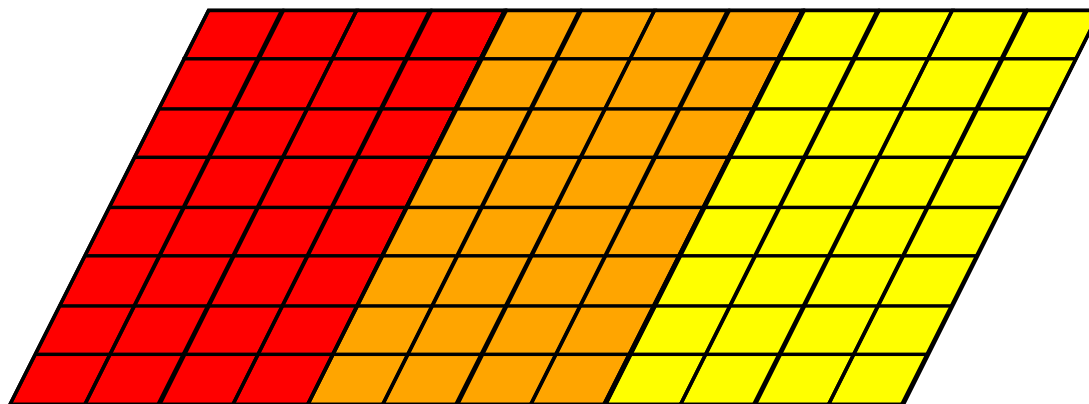
**CYCLIC(n)** both load balance and neighbor comms.

## Distribution



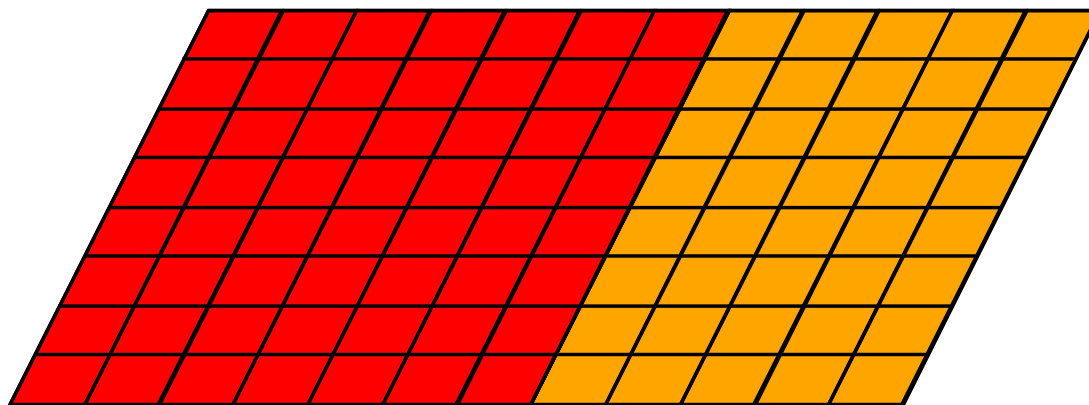
distribute T(...,...) onto P

## Block distribution



distribute T(**block**,\*) onto P

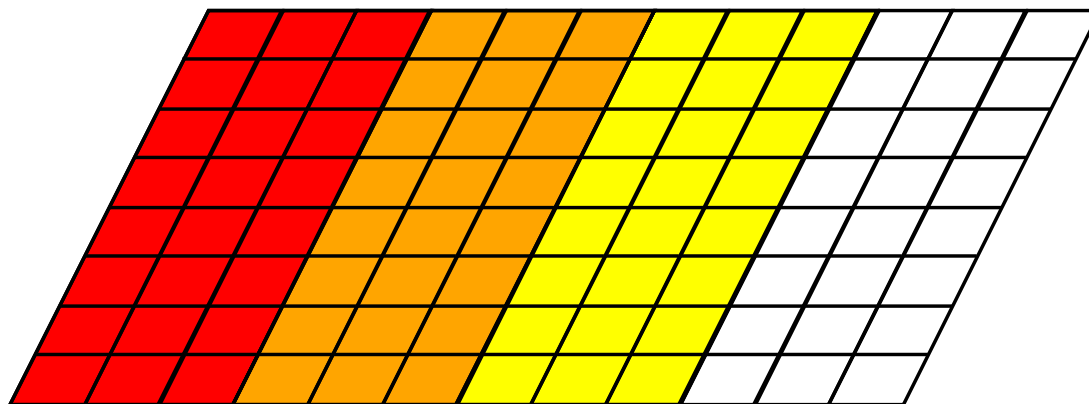
## Block(n) distribution



distribute T(block(7),\*) onto P

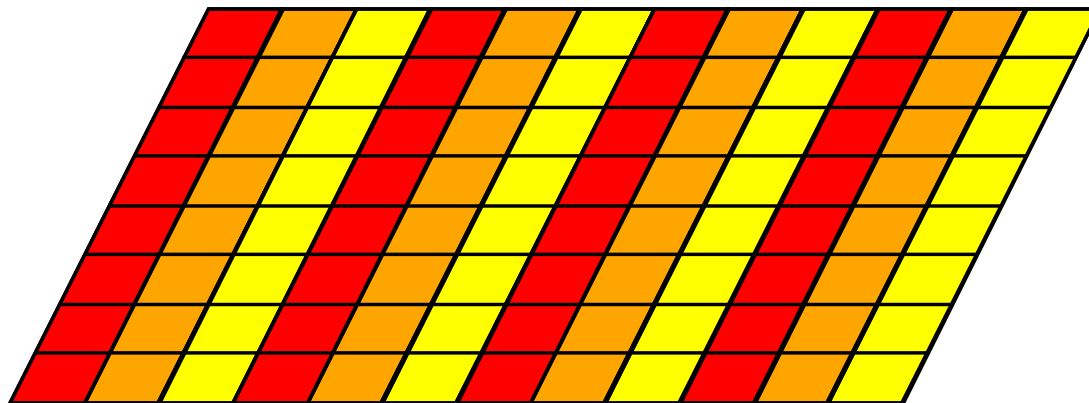


## Block(n) distribution



distributed T(block(3),\*) onto P ! non

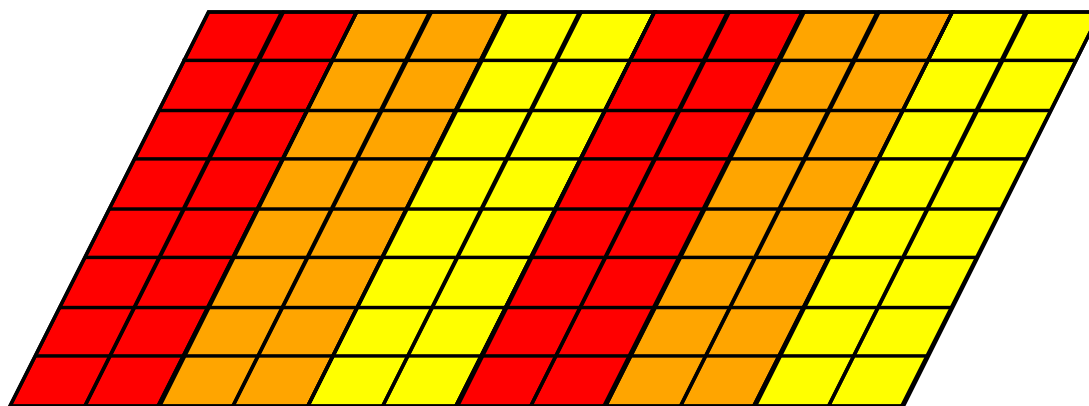
## Cyclic distribution



n

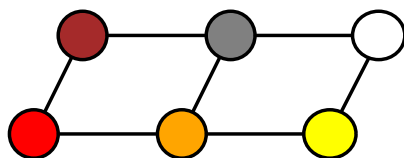
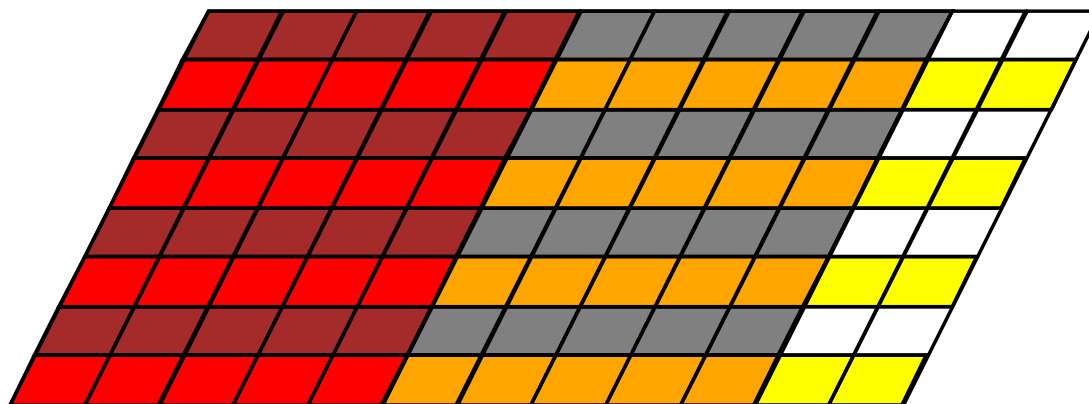
distribute T(**cyclic**,\*) onto P

## Cyclic(n) distribution



distribute T(**cyclic(2)**,\*) onto P

## Multi dimensional distributions



```
distribute T(block(5),cyclic(1)) onto P
```

## The template debate...

Heavy discussions on the mailing list

- Hans Zima, Vienna
  - Vienna Fortran does not include templates
  - templates do not improve expressivity
  - one more non user friendly concept
- Ken Kennedy, Rice
  - Fortran D includes similar decompositions
  - they can be larger than any array
  - easier port, clearer for the user

## Other mapping directives

**REALIGN** executable, dynamic alignment

**REDISTRIBUTE** executable, dynamic distribution

**DYNAMIC** attribute to an object which can be RE...

Moved as approved extensions...

## **More about HPF mapping directives**

- Fortran 90 syntactic sugar
- use of intrinsics in directives
- default mapping
- some strange mappings
- HPF mapping limits

## Syntactic sugar

```
!hpf$ processors, dimension(10) :: PROC
!hpf$ template, &
!hpf$    distribute(block) onto PROC, &
!hpf$    dimension(100), &
!hpf$    dynamic :: T1,T2
!hpf$ dynamic, align (:) with T1(:) :: A, B
```



## Use of intrinsics

- `NUMBER_OF_PROCESSORS()`  
number of physical processors available
- `PROCESSORS_SHAPE()`  
processor number of dimension

```
!hpf$ PROCESSORS P(NUMBER_OF_PROCESSORS()), &  
!hpf$    AP(NUMBER_OF_PROCESSORS()/10,10)
```

## Default mappings

- direct alignment
- 1D vector of physical processors
- block distribution

```
!hpf$ align A with B
```

```
!hpf$ distribute B
```

## HPF mapping limits

No arbitrary irregular mapping

! From Vienna Fortran

```
ALIGN A(I) WITH B(f(I))
```

- $f$  is an arbitrary function
- compiler optimizations?

## Mapping at subprogram interfaces

**prescriptive** mapping to enforce (with a remapping)

**descriptive** specify an expected mapping

**transcriptive** unspecified mapping

## Prescriptive mapping

- just like a static mapping

```
subroutine CALCUL(A)
  real A(100,100)
  !hpf$ distribute A(block,block)
  ...
```

- remapping on entry and exit (?)
- runtime cost

## Descriptive mapping

- similar to prescriptive
- assertion to the compiler
- favor optimisations
- all callers must conform, otherwise errors!

```
!hpf$ align A with * T
```

```
!hpf$ distribute * T(block)
```

## Transcriptive mapping

- no information for optimisations?
- template inheritance concept
- syntaxes

```
subroutine CALCUL(A)
  real A(100,100)
  !hpf$ distribute A *
  !hpf$ inherit A
```

## Conclusion to HPF mapping

- close to Fortran D
- replication
- suits arrays
- should favor optimizations
- directives = advice!



## So what?

- array distributed on processors
- the data are shared between them...
- we have now to share the computation
- without changing the semantics
- let's look for parallelism!
  - array expressions
  - parallel loops
  - dataparallel loops
  - and sequential loops...

## **3 loops in HPF**

- Group of Charles Koelbel, Rice University
- sequential do loop: DO
- parallel loop: DO + INDEPENDENT  
iterations to not dependent of the other
- dataparallel loop: FORALL

## 3 loops in HPF

```
do i=1, 10
  a(i) = a(i-1) + a(i) + a(i+1)
enddo
```

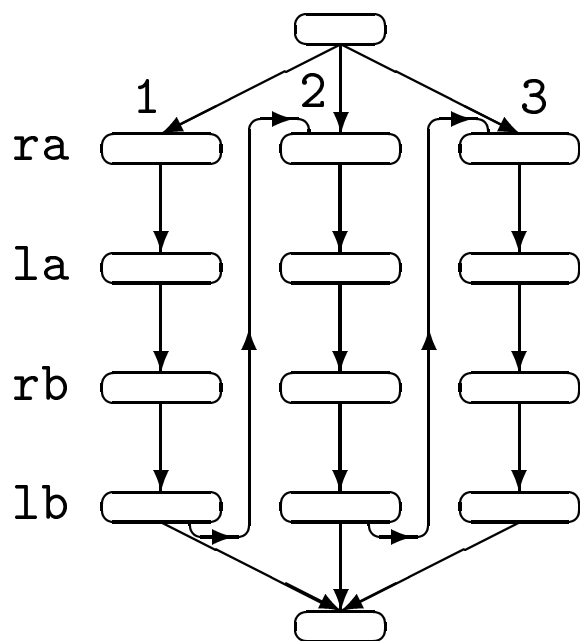
```
!hpf$ independent
```

```
do i=1, 10
  a(i) = 1.0
enddo
```

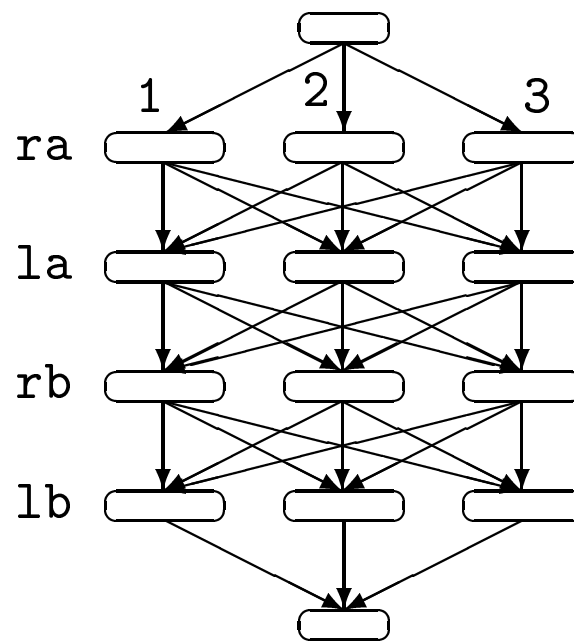
```
forall (i=1:10)
  a(i) = a(i-1) + a(i) + a(i+1)
end forall
```

## DO et FORALL

```
DO i = 1, 3  
  lhsa(i) = rhsa(i)  
  lhsb(i) = rhsb(i)  
END DO
```



```
FORALL ( i = 1:3 )  
  lhsa(i) = rhsa(i)  
  lhsb(i) = rhsb(i)  
END FORALL
```



# INDEPENDENT

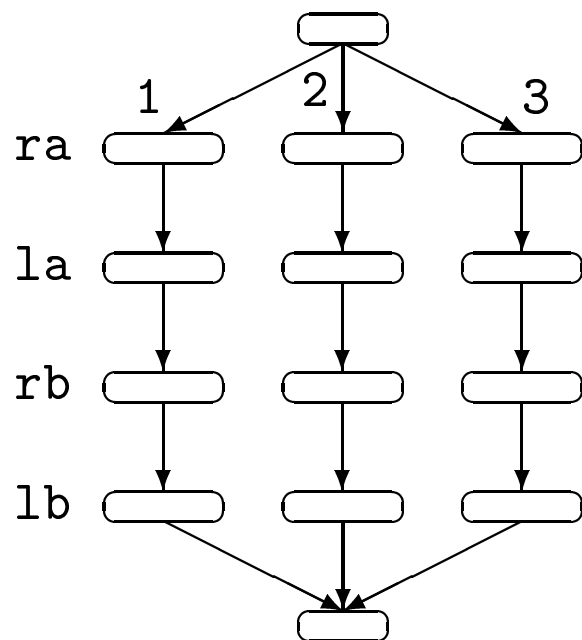
```
!HPF$ INDEPENDENT
```

```
D0 i = 1, 3
```

```
  lhsa(i) = rhsa(i)
```

```
  lhsb(i) = rhsb(i)
```

```
END D0
```



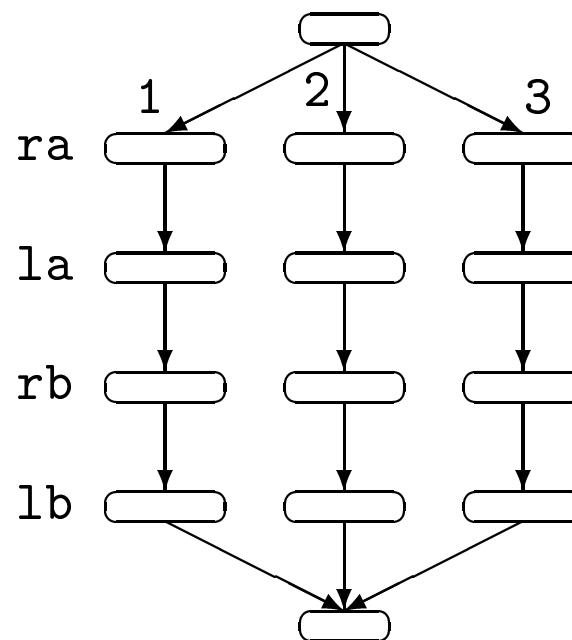
```
!HPF$ INDEPENDENT
```

```
FORALL( i = 1:3 )
```

```
  lhsa(i) = rhsa(i)
```

```
  lhsb(i) = rhsb(i)
```

```
END D0
```



## FORALL: 3 dataparallel loops

- implicit with array sections/expressions

```
A = B + C           ! matrices
```

```
D(1:20) = D(2:21) ! shift
```

- generalization: FORALL statement  
index explicitly named

```
FORALL (i=10:n, j=10:m) a(i,j) = 0.0
```

- extension: FORALL construct

## FORALL statement

- generalize array sections
- dataparallel semantics (SIMD)
- only one assignment
- optional mask
- can call PURE functions

```
FORALL(i=1:n, ..., mask) &  
    assignment
```

```
! transpose
forall(i=1:n, j=1:n) x(i,j) = y(j,i)

forall(i=1:n, y(i).ne.0.0) &
  x(i) = 1.0 / y(i)

! relaxation
forall(i=2:n-1) &
  x(i) = 0.5 * x(i) + 0.25 *(x(i-1)+x(i+1))

forall(i=1:n, y(i).ge.0.0) &
  x(i) = SQRT(y(i))
```



## **FORALL construct**

- extension of FORALL
- includes
  - assignments
  - WHEREs or FORALLs

```
FORALL(i=1:n,...,mask)
```

```
  WHERE or FORALL or assigns...
```

```
ENDFORALL
```

```
FORALL(i=1:n)
  A(i,i) = SQRT(A(i,i))
  B(i) = LOG(B(i,i)) + i
ENDFORALL
```

```
FORALL(i=1:n,j=1:n)
  WHERE (b(i,j)>0.0)
    a(i,j) = 1.0
  ELSEWHERE
    a(i,j) = -1.0
  ENDWHERE
ENDFORALL
```

## PURE attribute to functions

- user functions which behaves like intrinsics
  - no I/Os, no STOP, no PAUSE...
  - no access to commons or save data...
- must be declared as such
  - in the function interface
  - in the function itself

```
pure function f(x)
  real :: f
  real, intent(in):: x
  f = (4.3*x+2.1)*x+1.7
end function
```

## INDEPENDENT directive

- a parallel loop!
- iterations can be executed in any order
- can specify private variables  
variables private to iterations
- HPF 2.0: can specify reductions
- can apply to DO and FORALL

```
!hpf$ INDEPENDENT, NEW(var-list), REDUCTION(...)  
      DO i=1,n ... / FORALL(i=1:n)
```

## Examples of INDEPENDENT

```
!hpf$ INDEPENDENT
```

```
DO i=1, n
```

```
    A(P(i)) = B(i) ! P is a permutation
```

```
ENDDO
```

```
!hpf$ INDEPENDENT, NEW(x)
```

```
DO i=1, n
```

```
    x = A(i)**3
```

```
    B(i) = x*x + x
```

```
ENDDO
```

```
! square matrix multiplication
!hpf$ INDEPENDENT, NEW(j)
      DO i=1, n
!hpf$   INDEPENDENT, NEW(k,t)
        DO j=1, n
          t = 0.0
!hpf$   INDEPENDENT, REDUCTION(t)
          DO k=1, n
            t = t + A(i,k)*B(k,j)
          ENDDO
          C(i,j) = t
        ENDDO
      ENDDO
```

## **Efficient parallel loop?**

- assertion about parallel semantics
- compiler may not know how to exploit it!
- additional constraints helps:
  - block distributions
  - all data accessed in an iteration are aligned
  - access to neighbor processors
  - remote data stored in overlap areas

## Parallel library functions

- reductions applied on arrays
  - Fortran 90: SUM PROD ALL MAXVAL...
  - HPF/F95: ALL PARITY IALL MAXLOC...
  - include options (DIM, MASK...)
- scans...
  - \_SCATTER
  - \_PREFIX
  - \_SUFFIX
- others: SORT\_UP SORT\_DOWN GRADE\_DOWN GRADE\_UP



## Reductions

associative/commutative operations

parallelism induce numerical issues...

- Fortran 90
  - arithmetic: SUM (+) PROD (\*)
  - logical: ALL (.and.) ANY (.or.) COUNT (.true.)
  - order: MAXVAL (max) MINVAL (min)
  - location: MAXLOC MINLOC
- HPF
  - logical: PARITY (.xor.)
  - bitwise: IALL IANY IPARITY

## SCATTER functions

- reordering in Fortran 90
- based on permutations
- extended with `_SCATTER`
- how to combine indexed elements...

```
! A    = [ 10 20 30 ]
```

```
! V    = [ 1 2 3 4 ]
```

```
! IDX = [ 3 2 1 ] ! IDX is a permutation
```

```
      V[IDX] = A
```

```
! V    = [ 30 20 10 4 ]
```

## SCATTER functions...

- base array to be modified
- contributing array
- integer index arrays
  - as many as DIM(base)
  - conformant to contributing array
- optionnal mask (logical array)

```
! A      = [ 10. 20. 30. 40. ]
```

```
! IDX    = [ 1 2 1 2 ]
```

```
! BASE   = [ 1. 2. 3. ]
```

```
      X = SUM_SCATTER(A, BASE, IDX)
```

```
! X      = [ 41. 62. 3. ]
```

## **PREFIX and SUFFIX functions**

- accumulation of elements
- forward or backward
- optional MASK, SEGMENT, DIM, EXCLUSIVE

```
! A = [ 1. 2. 3. 4. ]
```

```
      S = SUM_PREFIX(A)
```

```
! S = [ 1. 3. 6. 10. ]
```

```
      P = PROD_SUFFIX(A)
```

```
! P = [ 24. 24. 12. 4. ]
```

## PREFIX and DIM option

- DIM: operation performed on it
- else array is linearized...

```
! A = [ 1 2 3 ]
```

```
!      [ 4 5 6 ]
```

```
S = SUM_PREFIX(A, DIM=2) ! S = [ 1 3 6 ]
```

```
!      [ 4 9 15 ]
```

```
P = PROD_SUFFIX(A, DIM=1) ! P = [ 1 10 18 ]
```

```
!      [ 4 5 6 ]
```

```
T = SUM_PREFIX(A) ! T = [ 1 7 15 ]
```

```
!      [ 5 12 21 ]
```

## PREFIX options

- MASK: element contributes if true
- EXCLUSIVE: current element does not contribute
- SEGMENT: grouping on linearized array

```
! S = [ T T F F F T T F ]
```

```
! A = [ 1 2 3 4 5 6 7 8 ]
```

```
      B = SUM_PREFIX(A,SEGMENT=S)
```

```
! B = [ 1 3 3 7 12 6 13 8 ]
```

```
      C = SUM_PREFIX(A,MASK=S)
```

```
! C = [ 1 3 3 3 3 9 16 16 ]
```

```
      D = SUM_PREFIX(A,MASK=S,EXCLUSIVE=.true.)
```

```
! D = [ 0 1 0 3 7 0 6 0 ]
```

## options and array expressions

- MASK, SEGMENT, indexes  
can be the result of array op.

```
! A = [ 0 1 8 4 7 9 ]  
!      [ 2 5 6 3 1 7 ]  
      S = SUM_PREFIX(A, MASK=A.gt.4)  
! AM = [ 0 0 8 0 7 9 ]  
!      [ 0 5 6 0 0 7 ]  
! S   = [ 0 0 13 19 26 35 ]  
!      [ 0 5 19 19 26 42 ]
```

## **Rationale for scans**

- SCATTER, PREFIX, SUFFIX
- quite specialized operations
- usefull to some applications
- parallel version can be developped
- but not in HPF!
- thus made available in the library



## Sort functions

efficient parallel implementations

- compute permutations
  - GRADE\_UP
  - GRADE\_DOWN
- performs the sort
  - SORT\_UP
  - SORT\_DOWN

## GRADE example

```
! A = [ -1  5 -3  4 ]  
!      [  2  1  0  9 ]  
! GRADE_UP(A) = [ 1  3 ]  
!                [ 1  1 ]  
!                [ 2  3 ]  
!                [ 2  2 ]  
!                [ 2  1 ]  
!                [ 1  4 ]  
!                ...
```

## Miscellaneous scalar functions

- ILEN: number of bits needed
- LEADZ: number leading zero bits
- POPCNT: number of bits to 1
- POPPAR: 1 if POPCNT is even, 0 if odd

## **HPF inquiry functions**

- a set of functions to query about array mappings
- non portable wrt Fortran 90
- examples :
  - HPF\_ALIGNMENT
  - HPF\_DISTRIBUTION
  - HPF\_TEMPLATE

## **Conclusion about the library**

- not portable wrt Fortran 90
- performance depends on implementation
- use them if appropriate!

## Extrinsic procedures

- ability to call routine in
  - another language (C, F77, Fortran, HPF-lite)
  - another parallel paradigm (MPI, ...)
- routine called with different conventions:
  - on one pe with all data (serial)
  - on pes... (global, standard HPF!)
  - on every pe with local data (local)
  - ....

## Syntax for extrinsics

- explicit interface in caller
- special declaration in the callee
- with fortran 90 keyword: EXTRINSIC

```
INTERFACE
```

```
    EXTRINSIC(HPF_LOCAL) SUBROUTINE FOO(A)
```

```
        REAL, DIMENSION(:), INTENT(INOUT):: A
```

```
    END SUBROUTINE
```

```
END INTERFACE
```

```
!hpf$ distribute X(BLOCK)
```

```
CALL FOO(X)
```

## function definition

```
EXTRINSIC(HPF_LOCAL) SUBROUTINE FOO(A)
  REAL, DIMENSION(:):: A
  INTEGER I
! query about A LOCAL declaration...
  DO I=LBOUND(A), UBOUND(A)
    ...
  ENDDO
END SUBROUTINE
```



## **F77 serial model**

- call a serial routine in Fortran 77
- for instance, a special I/O routine for X display
- available in ADAPTOR

## **HPF serial model**

- call a serial routine in restricted HPF
- needed data collected before the call
- use Fortran 90 intent declarations!

## HPF local model

- routine coded in restricted HPF!
- no data distribution!
- can use message passing such as MPI
- standard inquiry about local data
- inquiry about data mapping (HPF 2.0 Ap. Ext.)

`MY_PROCESSOR()`

`GLOBAL_TO_LOCAL()`

## **HPF 2.0 approved extensions**

Many proposal which are not incorporated

- data mapping
- data and task parallelism
- asynchronous I/Os
- library extensions
- more extrinsics...

## Approved extensions for data mapping

- REALIGN, REDISTRIBUTE, DYNAMIC...
- mappings on processor subsets  
`DISTRIBUTE T(BLOCK) ONTO P(2:4)`
- RANGE: list of mappings a subroutine might accept...
- SHADOW: overlap with declaration  
`DISTRIBUTE(BLOCK) SHADOW(1:2):: A,`
- ...

## Approved extensions for parallelism

- ON directive to locate computations

```
!hpf$ on home(a(1)), new(x) begin
```

```
    x = ...
```

```
    a(1) = x*x
```

```
!hpf$ end on
```

- TASK\_REGION + ON directive
- active processors
- ...

## **Port of ONDE24 to HPF**

- 2D acoustic wave propagation
  - from IFP: French Oil Institute
  - 1000 lines of Fortran 77
  - target: IBM SP2
  - stencil-based application!
  - direct resolution over time
  - order 2 in time, order 4 in space
- Should be a dream!

## ONDE24 initial performance

- HPF = High Performance!
- code profile: gprof/tprof...
- can use RS6000 performance counters
- result: 40 Mflop/s
- processor peak performance is 250 Mflop/s
- what is the trouble?

## Improving the kernel loop

- cache behavior is ok.
- expression structure:
  - processor needs 4 independent fma:  $a*b+c$
  - more fma can be extracted
  - balanced tree  $\Rightarrow$  more parallelism
- result: 80 Mflop/s!
- with unrolling and scheduling: 110 Mflop/s  
but will not suit HPF...



## ONDE24 declaration cleaning

- larger declaration than used...
- impact on distribution and load balance:
  - few processors used if BLOCK
  - or more communications if CYCLIC(n)
- U and V are the big arrays
- dynamic allocation? not F77...

## Initial declarations

```
INTEGER      NPMAX, NTMAX, NBTRAC
PARAMETER (NPMAX      = 809)
PARAMETER (NTMAX      = 4000)
PARAMETER (NBTRAC     = 50)
REAL*8      U        (NPMAX+1,NPMAX,2)
REAL*8      V        (NPMAX+1,NPMAX)
REAL*8      B        (NPMAX+1,3,3)
REAL*8      UB       (NPMAX+1,3)
REAL*8      UINT     (NPMAX)
REAL*8      SISMO    (NBTRAC,NTMAX)
INTEGER      NP, NT
```

## **Array declarations**

- static allocation
- bounds moved as parameters
- runtime check to match problem
- actual bounds needed in directives
- hence **MUST** be compile-time constants

## Simplified declarations

```
INTEGER NP, NT, NBTRAC  
PARAMETER (NP = 800)  
PARAMETER (NT = 1000)  
PARAMETER (NBTRAC = 50)  
REAL*8      U(NP,NP,2)  
REAL*8      V(NP,NP)  
REAL*8      B(NP,3,3)  
REAL*8      UB(NP,3)  
REAL*8      UINT(NP)  
REAL*8      SISMO(NBTRAC,NT)
```

## ONDE24 Data Mapping

- 1D, 2D and 3D arrays are used
- align data used together...
- must examine actual uses!
- then only ONE distribution

```
!hpf$ TEMPLATE DOMAIN(NP,NP)
```

## U and V arrays

- scan all uses
- $U(I,J,*)$  and neighbors used with  $V(I,J)$
- suggest direct alignment!

```
!hpf$ ALIGN U(I,J,*) WITH DOMAIN(I,J)
```

```
!hpf$ ALIGN V(I,J) WITH DOMAIN(I,J)
```

```
!
```

```
! or
```

```
!
```

```
!hpf$ ALIGN U, V WITH DOMAIN
```

## UINT vector first use

```
DO 92 I = 3, NP-2
    UINT(I) = B(I, 1, 1) * (U(I, NP, KP) + U(I, NP-1, KP))
    [...]
&    + B(I, 1, 3) * (U(I+1, NP-1, KP) + U(I+1, NP, KP) +
&    U(I-1, NP-1, KP) + U(I-1, NP, KP))
92    CONTINUE
DO 93 I = 3, NP-2
    U(I, NP, KP) = UINT(I)
93    CONTINUE

!hpf$ ALIGN UINT(I) WITH DOMAIN(I, NP)
```

## Second use

```
DO 94 I = 3, NP-2
    UINT(I) = B(I, 2, 1) * (U(NP, I, KP) + U(NP-1, I, KP))
    [...]
&      + B(I, 2, 3) * (U(NP-1, I+1, KP) + U(NP, I+1, KP) +
&      U(NP-1, I-1, KP) + U(NP, I-1, KP))
94    CONTINUE
DO 95 I = 3, NP-2
    U(NP, I, KP) = UINT(I)
95    CONTINUE

!hpf$ ALIGN UINT(I) WITH DOMAIN(NP, I)
```



## Third use

```
DO 96 I = 3, NP-2
    UINT(I) = B(I,3,1)*(U(I,1,KP)+U(I,2,KP))
    [...]
&    + B(I,3,3)*(U(I+1,2,KP)+U(I+1,1,KP)+
&    U(I-1,2,KP)+U(I-1,1,KP))
96    CONTINUE
DO 97 I = 3, NP-2
    U(I,1,KP) = UINT(I)
97    CONTINUE

!hpf$ ALIGN UINT(I) WITH DOMAIN(I,1)
```

## UINT Mapping?

- not used elsewhere
- 3 different alignements?
- values directly reused!
- REALIGN?
  - usually not implemented
  - no need to move the data!
- this suggest 3 different arrays!  
UINTW UINTS UINTE (West, South, East)

## UINT\* Mapping

```
REAL*8 UINTW(NP), UINTS(NP), UINTE(NP)
```

```
!hpf$ ALIGN UINTE(I) WITH DOMAIN(I,NP)
```

```
!hpf$ ALIGN UINTS(I) WITH DOMAIN(NP,I)
```

```
!hpf$ ALIGN UINTW(I) WITH DOMAIN(I,1)
```

## UB use

```
DO 71 I = 2, NP-1
```

```
    UB(I,1) = U(I, NP-1, KP)
```

```
    UB(I,2) = U(NP-1, I, KP)
```

```
71  UB(I,3) = U(I, 2, KP)
```

```
DO 92 I = 3, NP-2
```

```
    UNTE(I) = U(I, NP, KP) .. U(I, NP-1, KP) .. UB(I,1)
```

```
!hpf$ ALIGN UB(I,1) WITH DOMAIN(I, NP-1) ???
```

```
!hpf$ ALIGN UB(I,2) WITH DOMAIN(NP-1, I) ???
```

```
!hpf$ ALIGN UB(I,3) WITH DOMAIN(I, 2) ???
```

## UB Mapping

- dimension (NP,3)
- temporary store for borders in time loop
- cannot map dimensions separately in HPF
- split UB: UBW, UBS, UBE

## UB\* Mapping

```
REAL*8 UBE(NP), UBS(NP), UBW(NP)
```

```
!hpf$ ALIGN UBE(I) WITH DOMAIN(I,NP-1)
```

```
!hpf$ ALIGN UBS(I) WITH DOMAIN(NP-1,I)
```

```
!hpf$ ALIGN UBW(I) WITH DOMAIN(I,2)
```

```
DO I = 2,NP-1
```

```
    UBE(I) = U(I,NP-1,KP)
```

```
    UBS(I) = U(NP-1,I,KP)
```

```
    UBW(I) = U(I,2,KP)
```

```
ENDDO
```

## B Mapping? first use

```
REAL*8 B(NP,3,3)
```

```
DO 41 I = 2, NP-2
```

```
    V(I,NP) = 2/((1/V(I,NP))+(1/V(I,NP-1)))
```

```
    W = V(I,NP)*DELTAT
```

```
    B(I,1,1) = 1 - (1/(W+H)) * ( 2*H + W*W/H)
```

```
    B(I,1,2) = 2*H/(W+H)
```

```
41    B(I,1,3) = W*W/(2*H*(W+H))
```

```
!hpf$ ALIGN B(I,1,*) WITH DOMAIN(I,NP)
```

## 2nd and 3rd uses

```
DO 42 I = 3, NP-2
```

```
    V(NP, I) = 2 / ((1 / V(NP, I)) + (1 / V(NP-1, I)))
```

```
    W = V(NP, I) * DELTAT
```

```
    B(I, 2, 1) = 1 - (1 / (W + H)) * (2 * H + W * W / H)
```

```
    B(I, 2, 2) = 2 * H / (W + H)
```

```
42    B(I, 2, 3) = W * W / (2 * H * (W + H))
```

```
DO 43 I = 2, NP-2
```

```
    V(I, 1) = 2 / ((1 / V(I, 1)) + (1 / V(I, 2)))
```

```
    W = V(I, 1) * DELTAT
```

```
    B(I, 3, 1) = 1 - (1 / (W + H)) * (2 * H + W * W / H)
```

```
    B(I, 3, 2) = 2 * H / (W + H)
```

```
43    B(I, 3, 3) = W * W / (2 * H * (W + H))
```



## B Mapping

- similar to UB!
- split in UBW, UBS, UBW!

```
REAL*8 BE(NP,3), BS(NP,3), BW(NP,3)
```

```
!hpf$ ALIGN BE(I,*) WITH DOMAIN(I,NP)
```

```
!hpf$ ALIGN BS(I,*) WITH DOMAIN(NP,I)
```

```
!hpf$ ALIGN BW(I,*) WITH DOMAIN(I,1)
```

## SISMO Mapping

- stores received signal
- sismograph placed on the field

```
REAL*8 SISMO(NBTRAC,NT)
```

```
DO 84 I = 1,NBTRAC
```

```
84      SISMO(I,1) = 0.0
```

```
DO 81 I = 1,NBTRAC
```

```
81      SISMO(I,N) = U(IS, NP - NBTRAC + I, KP)
```

```
!hpf$ ALIGN SISMO(I,*) WITH DOMAIN(IS,(NP-NBTRAC)+I) ???
```

## SISMO Mapping

- array shift is legal!
- but IS is a runtime constant...
- depth of source of in field

```
!hpf$ ALIGN SISMO(I,*) WITH DOMAIN(1,(NP-NBTRAC)+I)
```

## 1D or 2D distribution on 4 processors?

### **(BLOCK,\*)**

- shorter inner loop
- $4 \times 3 \times n$  communications per iteration

### **(\*,BLOCK)**

- longer inner loop
- $4 \times 3 \times n$  communications per iteration

### **(BLOCK,BLOCK)**

- smaller local array
- $4 \times 2 \times n$  communications per iteration
- 50% less communications!

## ONDE24 HPF Mapping

- alignment and distribution done!
- now let's find some parallelism!
- must scan all computations and loops...
- parallel if independent of execution order
- Bernstein's conditions:
  - no data conflicts (R/W, W/R, W/W)
  - between DISTINCTS iterations
- requires dependence analyses

## ONDE24 Kernel computation

Potential conflicts

- Write of  $U(I, J, KP)$
- Reads of  $U$  array elements:
  - $U(I, J, KP)$ : no, same iteration
  - $U(I, J, KM)$ : idem
  - $U(I[+-][12], J, KM)$ : no if  $KM$  and  $KP$  differs
  - $U(I, J[+-][12], KM)$ : no if  $KM$  and  $KP$  differs

## KM and KP flip-flop

```
INTEGER    KM,KP
KM = 1
KP = 2
DO 70 N = 2,NT
    ...
    KM = KP
    KP = 3 - KP
70  CONTINUE
```

## Parallel kernel

```
!hpf$ INDEPENDENT, NEW(I)
      DO J = 3, NP-2
!hpf$  INDEPENDENT
      DO I = 3, NP-2
        U(I,J,KP) =
$      (2.*U(I,J,KM)-U(I,J,KP))-V(I,J)*
$      (60.*U(I,J,KM)+(((U(I+2,J,KM) + U(I-2,J,KM))
$                        + (U(I,J-2,KM) + U(I,J+2,KM))))
$      - 16. * ((U(I+1,J,KM) + U(I-1,J,KM))
$      + (U(I,J-1,KM) + U(I,J+1,KM))))))
        ENDDO
      ENDDO
```



## Parallel loops in ONDE24

- 2 parallel loops found!
- time loop is not parallel (obvious)
- still 33 other loops to consider! really!
- initializations...
- other computations...
- I/O and statistics...

## Obviously parallel loops

```
      DO 10 K = 1,2
        DO 10 J = 1,NP
          DO 10 I = 1,NP
10          U(I,J,K) = 0.0
```

```
      DO 84 I = 1,NBTRAC
84      SISMO(I,1) = 0.0
```

```
      DO 51 I = 3,NP-1
51      V(I,2) = (V(I,2)*DELTAT/H)**2
```

## Other loops (1)

many such loop nests:

```
DO 140 I = 3, NP-1
    U(I,2,KP) = 2*U(I,2,KM)-U(I,2,KP)-V(I,2) *
&    (4*U(I,2,KM) - (U(I+1,2,KM)+U(I-1,2,KM)
&    + U(I,1,KM)+U(I,3,KM)))
140 CONTINUE
```

## Parallel version

- border stencils similar to kernel stencil

```
!hpf$ INDEPENDENT
```

```
DO 140 I = 3, NP-1
```

```
      U(I,2,KP) = 2*U(I,2,KM)-U(I,2,KP)-V(I,2) *  
&      (4*U(I,2,KM) - (U(I+1,2,KM)+U(I-1,2,KM)  
&      + U(I,1,KM)+U(I,3,KM)))
```

```
140 CONTINUE
```

## Other loops (2)

3 such loops:

```
DO 41 I = 2, NP-2
  V(I, NP) = 2 / ((1/V(I, NP)) + (1/V(I, NP-1)))
  W        = V(I, NP) * DELTAT
  BE(I, 1) = 1 - (1/(W+H)) * (2*H + W*W/H)
  BE(I, 2) = 2*H/(W+H)
  BE(I, 3) = W*W/(2*H*(W+H))
41 CONTINUE
```

## Parallel version

- arrays are aligned
- $W$  is private (defined and not used AFTER)

```
!hpf$ INDEPENDENT, NEW(W)
DO 41 I = 2, NP-2
    V(I, NP) = 2 / ((1/V(I, NP)) + (1/V(I, NP-1)))
    W        = V(I, NP) * DELTAT
    BE(I, 1) = 1 - (1/(W+H)) * ( 2*H + W*W/H)
    BE(I, 2) = 2*H/(W+H)
    BE(I, 3) = W*W/(2*H*(W+H))
41    CONTINUE
```

## Other loops (3)

- fully parallel... but data not aligned!
- hence it is serialized!
- can be distributed

```
!hpf$ INDEPENDENT
      DO 71 I = 2, NP-1
          UBE(I) = U(I, NP-1, KP)
          UBS(I) = U(NP-1, I, KP)
          UBW(I) = U(I, 2, KP)
71      CONTINUE
```

## Efficient parallel version

```
!hpf$ INDEPENDENT
```

```
DO 71 I = 2, NP-1
```

```
71      UBE(I) = U(I, NP-1, KP)
```

```
!hpf$ INDEPENDENT
```

```
DO 72 I = 2, NP-1
```

```
72      UBS(I) = U(NP-1, I, KP)
```

```
!hpf$ INDEPENDENT
```

```
DO 73 I = 2, NP-1
```

```
73      UBW(I) = U(I, 2, KP)
```



## I/O Loops

- not parallel

```
      DO 21 I = 1, NP
        DO 22 J = 1, NP
          READ (3,*) V(I,J)
22      CONTINUE
21      CONTINUE
```

## Reduction loops

```
VMAX = V(1,1)
VMIN = V(1,1)
DO 112 I = 1, NP
    DO 122 J = 1, NP
        IF (V(I,J).LT.VMIN) THEN
            VMIN = V(I,J)
        ENDIF
        IF (V(I,J).GT.VMAX) THEN
            VMAX = V(I,J)
        ENDIF
122    CONTINUE
112 CONTINUE
```

## Reduction loops

- REDUCTION directive?
  - operation must appear: MAX/MIN
  - not always available in compilers (HPF 2.0)
- Fortran 90 array intrinsics! MAXVAL/MINVAL

```
      VMIN = V(1,1)
!hpf$ INDEPENDENT, REDUCTION(VMIN)
      DO 112 J=1, NP
!hpf$    INDEPENDENT
          DO 112 I=1, NP ! fixed loop order
112      VMIN = MIN(VMIN, V(I,J))

      VMIN = MINVAL(V)
```

## Any other array accesses?

- many individual array accesses
  - signal source
  - initializations and computations in corners
- may lead to many small communications!
- may imply private scalars...
- hints:
  - ON HOME HPF 2.0 directive
  - 1 iteration parallel loop?

## Signal source

```
W = F * (N * DELTAT - 1.0/F)
IF (W**2.LT.TMAX) THEN
  W = (W*PI)**2
  GO = (1.0 - 2.0*W) * EXP (-W)
  U(IS,JS,KM) = U(IS,JS,KM) + GO * 12*V(IS,JS) * H**2
ENDIF
```

## Efficient version with HPF 2.0

```
!hpf$ ON HOME(V(IS,JS)), NEW(W, GO), BEGIN
  W = F * (N * DELTAT - 1.0/F)
  IF (W**2.LT.TMAX) THEN
    W = (W*PI)**2
    GO = (1.0 - 2.0*W) * EXP (-W)
    U(IS,JS,KM) = U(IS,JS,KM) + GO * 12*V(IS,JS) * H**2
  ENDIF
!hpf$ END ON
```

## Efficient version with HPF 1.1?

```
!hpf$ INDEPENDENT, NEW(W,GO)
DO I=1,1
  W = F * (N * DELTAT - 1.0/F)
  IF (W**2.LT.TMAX) THEN
    W = (W*PI)**2
    GO = (1.0 - 2.0*W) * EXP (-W)
    U(IS,JS,KM) = U(IS,JS,KM) + GO * 12*V(IS,JS) * H**2
  ENDIF
ENDDO
```

## Corner computation

```
!hpf$ ON HOME(V(NP-1,NP)), NEW(C1,W), BEGIN
      C1 = 4/((1/V(NP-1,NP))+(1/V(NP-1,NP-1)) +
&          (1/V(NP-2,NP))+(1/V(NP-2,NP-1)) )
      W  = C1*DELTAT
      BE(NP-1,1) = 2*W/(4*W+3*H)
      BE(NP-1,2) = 3*H/(4*W+3*H)
      V(NP-1,NP) = C1
!hpf$ END ON
```



## Summary

- all arrays are mapped
- all parallel loops are marked as such
- is that sufficient?
- no, I/O: sequentialized with elementary messages...

```
DO 21 I = 1,NP
  DO 21 J = 1,NP
    READ (3,*) V(I,J)
```

```
21  CONTINUE
```

## Efficient I/O Loops

```
! implied DO
```

```
    READ (3,*) ((V(I,J), J=1, NP), I=1, NP)
```

```
! array I/O
```

```
    READ (3,*) V(1:NP,1:NP)
```

```
    V = TRANSPOSE(V)
```

## Performance

- with 3 compilers:
  - HPFC (my prototype!)
  - ADAPTOR (Thomas Brandes, GMD)
  - xlhpf (IBM)
- with three different versions...
- 250 Mflop/s on 4 processors

## ONDE24 Conclusion

- alignment suits the parallelisation process
  - focus on relative accesses
  - some data need splitting
- HPF parallelism ok for stencils
  - cannot apply on unrolled version
  - limited to 80 Mflop/s/node
- details:
  - array scalar accesses...
  - I/O...

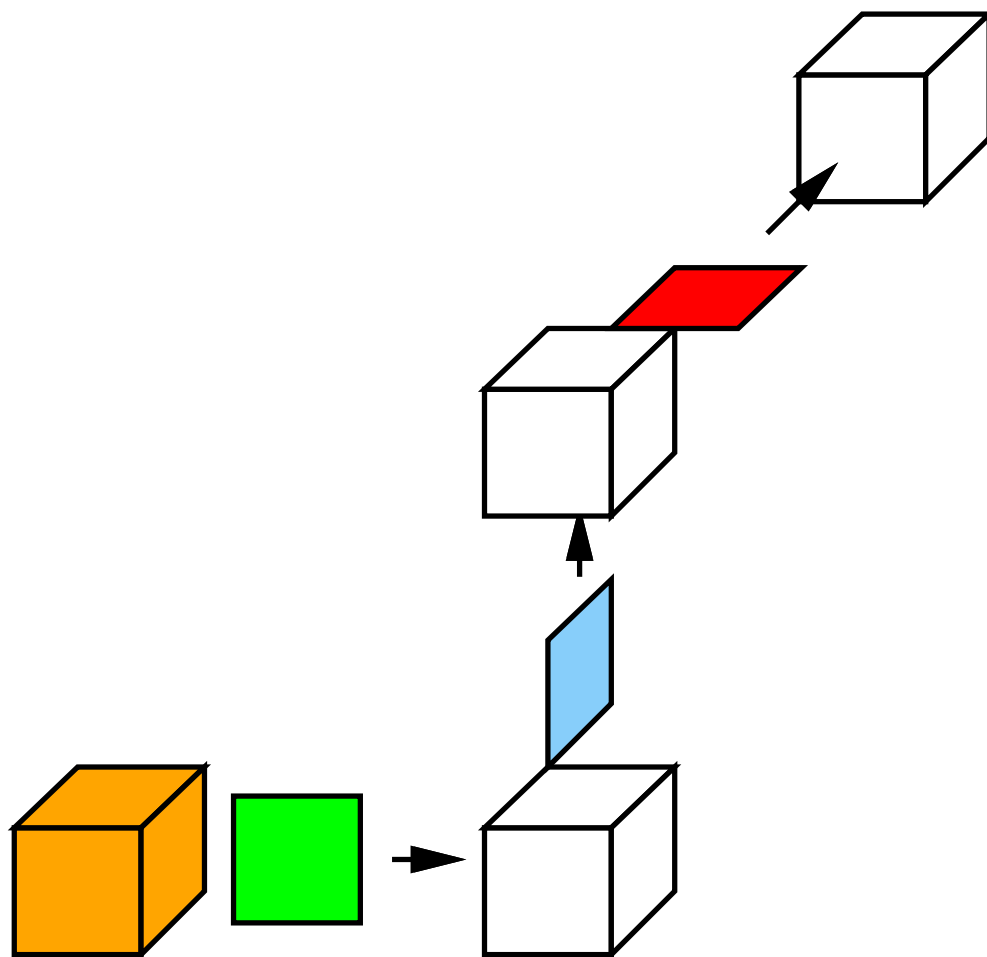
## Tensrus

- solver for elliptic differential equations
- for Poisson, Helmholtz equations
- code features:
  - 3D domain, non uniform cart. grid
  - B-spline collocation method of odd order
  - Multipole expansion for boundary conditions
  - cost:  $N^4$  (FFT is  $N^3 \ln N$ )
- Authors: Jean-Yves Berthou and Laurent Plagne
- CEA: French Nuclear Research Institute

## Computation kernel

- basically matrix products!
- large 3D arrays
  - double float type
  - $N*N*N$ ,  $N=64, 128... 512$
  - up to 1GB per matrix!

## Tensrus: 3D tensor products at CEA



## Initial code

```
SUBROUTINE tensrus(N, MX, MY, MZ, V, T)
```

```
REAL, DIMENSION(N,N) :: MX, MY, MZ
```

```
REAL, DIMENSION(N,N,N):: T, V
```

```
REAL, DIMENSION(N,N,N):: G, F
```

```
DO i = 1, N
```

```
  DO j = 1, N
```

```
    DO k = 1, N
```

```
      F(i,j,k) = V(i,k,j)
```

```
    ENDDO
```

```
  ENDDO
```

```
ENDDO
```



```
DO i = 1, N
  DO j = 1, N
    DO c = 1, N
      G(i, j, c) = 0.0
      DO k = 1, N
        G(i, j, c) = G(i, j, c) + MZ(k, c) * F(i, j, k)
      ENDDO
    ENDDO
  ENDDO
ENDDO
```

```
! and 2 other products with MY and MZ
! final result stored in T
```

## **Improved sequential code**

- reorder all matrix dimensions before product
- loop order take care of cache
- otherwise basically the same

## Better sequential code

```
SUBROUTINE tensrus(N, MX, MY, MZ, V, T)
```

```
REAL, DIMENSION(N,N) :: MX, MY, MZ
```

```
REAL, DIMENSION(N,N,N):: T, V
```

```
REAL, DIMENSION(N,N,N):: G, F
```

```
DO i = 1, N
```

```
  DO j = 1, N
```

```
    DO k = 1, N
```

```
      F(k,j,i) = V(i,j,k)
```

```
    ENDDO
```

```
  ENDDO
```

```
ENDDO
```

```
DO i = 1, N
  DO j = 1, N
    DO k = 1, N
      G(k,j,i) = 0.0
      DO c = 1, N
        G(k,j,i) = G(k,j,i) + MZ(c,k)*F(c,j,i)
      ENDDO
    ENDDO
  ENDDO
ENDDO
```

```
! and 2 other products with MY and MZ
! final result stored in T
```

## **HPF version with remappings (hpfc)**

- descriptive mappings + interface in caller
- (BLOCK,BLOCK,BLOCK) distribution (better comms)
- redistributions AND reorderings...  
no commercial HPF compiler implements RE\*...
- partial replication!
- no reductions: in local memory only

## Parallel code

```
SUBROUTINE tensrus(MX, MY, MZ, V, T)
```

```
REAL, DIMENSION(N,N)  :: MX, MY, MZ
```

```
REAL, DIMENSION(N,N,N):: T, V
```

```
! prescriptive/descriptive mappings:
```

```
!hpf$ TEMPLATE D(N,N,N)
```

```
!hpf$ PROCESSORS P(4,4,4)
```

```
!hpf$ DISTRIBUTE D(BLOCK,BLOCK,BLOCK) ONTO P
```

```
!hpf$ ALIGN MX(*,I) WITH D(I,*,*)
```

```
!hpf$ ALIGN MY(*,J) WITH D(*,J,*)
```

```
!hpf$ ALIGN MZ(*,K) WITH D(*,*,K)
```

```
!hpf$ ALIGN WITH D:: V, T
```

```
      REAL, DIMENSION(N,N,N):: G, F
!hpf$ ALIGN F(k,j,i), G(k,j,i) WITH D(i,j,k)
!hpf$ DYNAMIC F, G
! reordering
!hpf$ INDEPENDENT
      DO i = 1, N
!hpf$      INDEPENDENT
          DO j = 1, N
!hpf$      INDEPENDENT
              DO k = 1, N
                  F(k,j,i) = V(i,j,k)
              ENDDO
          ENDDO
      ENDDO
```

```
! redistribute with partial replication
!hpf$ REALIGN F(*,j,i) WITH D(i,j,*)
!hpf$ INDEPENDENT
      DO i = 1, N
!hpf$      INDEPENDENT
            DO j = 1, N
!hpf$            INDEPENDENT
                  DO k = 1, N
                        G(k,j,i) = 0.0
                        DO c = 1, N
                              G(k,j,i) = G(k,j,i) + MZ(c,k)*F(c,j,i)
                        ENDDO
                  ENDDO
            ENDDO
      ENDDO
ENDDO
```



## **CGS**

- Conjugate Gradient with Neuman Preconditionning
- generated by some applications
- large sparse matrices involved...
- does it suits HPF?
- Catherine Gaudart and Jean-Yves Berthou, CEA

## Computation kernel

! Y = D \* X

```
SUBROUTINE matvect(n, ndiag, irf, d, x, y)
```

```
INTEGER n, ndiag, irf(n, ndiag)
```

```
REAL*8 d(n, ndiag), x(n), y(n)
```

```
DO 10 i = 1, n
```

```
10   y(i) = 0.0
```

```
20   DO 20 i = 1, n
```

```
      DO 20 j = 1, ndiag
```

```
20      y(i) = y(i)+d(i,j)*x(irf(i,j))
```

```
END
```

## Comments about matvect

- $n = 216,000$ ,  $ndiag = 7$
- optimization:
  - $n$  and  $ndiag$  compile time constants!
  - loop unrolling?
  - array transposition?
- parallel on the first large dimension

## Improved matvect

```
SUBROUTINE matvect(irf, d, x, y)
parameter (n=216000)
INTEGER irf(7,n)
REAL*8 d(7,n), x(n), y(n)
DO i = 1, n
    y(i) = d(1,i)*x(irf(1,i))
$      + d(2,i)*x(irf(2,i))
$      + d(3,i)*x(irf(3,i))
$      + d(4,i)*x(irf(4,i))
$      + d(5,i)*x(irf(5,i))
$      + d(6,i)*x(irf(6,i))
$      + d(7,i)*x(irf(7,i))
ENDDO
```

## HPF version

- from call site and loops
  - Y and X BLOCK distributed
  - pointer passed, switch to F90 array sections?
- in matvect: prescriptive mappings
- indirect access to X: full replication

## HPF version

```
SUBROUTINE matvect(irf, d, x, y)
```

```
parameter (n=216000)
```

```
INTEGER irf(7,n)
```

```
REAL*8 d(7,n), x(n), y(n)
```

```
!hpf$ TEMPLATE T(n)
```

```
!hpf$ DISTRIBUTE T(BLOCK)
```

```
!hpf$ ALIGN WITH T(i):: IRF(*,i), D(*,i), Y(i)
```

```
!hpf$ ALIGN WITH T(*):: X(*)
```

```
!hpf$ INDEPENDENT
```

```
DO 10 i = 1, n
```

```
10      y(i) = d(1,i)*x(irf(1,i)) + ...
```

## Communication analyses

Let us assume  $p$  processors

- $216000/p$  elements per processor from  $X$  and  $Y$
- $13 \cdot 216000/p$  ops per processor in matvect
- thus at most  $13 \cdot 216000/p$  elements of  $X$  used
- remapping:  $((p-1)/p) \cdot 216000$  data transfered!
- $p$  grows: constant communications, reduced ops!!
- useless elements transfered!!!
- $p=4$ : 702 Kops/ $p$ , 162 Ktransfers/ $p$
- $p=32$ : 87 Kops/ $p$ , 209 Ktransfers/ $p$

## **How to improve the situation?**

- IRF does not change over matvect calls...
- inspect once to know which data to transfer
- execute the communications many times!
- a lot of reuse: really reduced communications!
- smaller X can be allocated
- implemented by hand in MPI, called from HPF



## Conclusion about HPF

- efficiency?
  - for some applications
  - fine tuning useful
- portability?
  - if same compiler used, yes!
  - otherwise, different versions often needed...
- simplicity?
  - mappings require geometric training;-)
  - YES if compared to MPI!

## HPF vs MPI

- Jean-Yves Berthou:
  - high degree of technicity in both
  - few hours vs few days
  - few weeks vs few months
- HPF always make sense as a first try
  - very good performance on some codes
  - helps understanding the application

## HPF Future ?

- processor performance increases a lot
- shared memory architecture bottleneck: 8 processors
- some applications/institution requires large machines
- vendor support? only PGI?

## Pointers on the web

- HPF: <http://dacnet.rice.edu/Depts/CRPC/HPFF/>
- ADAPTOR:  
<http://www.gmd.de/SCAI/lab/adaptor/>
- PGI: <http://www.pgroup.com/>
- HPFC: <http://www.cri.ensmp.fr/~coelho/hpfc>
- a tutorial: <http://qqq.npac.syr.edu/hpfa/>