# A single-source C++20 HLS flow for function evaluation on FPGA

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July 6, 2022

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- C++ provides a few standard integral types:
  - ► Signed or not: unsigned int, signed int
  - Different width: int8\_t, uint16\_t, int32\_t, uint64\_t, ... if supportec
- C23 adds fundamental N-bit type: \_BitInt(22)
- And a small set of floating point types:
  - ► float IEEE binary32 if supported
  - ▶ double IEEE binary64 if supported
  - long double IEEE binary128 if supported, or anything, really
  - ▶ \_Decimal{32,64,128} (C23) for IEEE decimal floating point, if supported



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#### Some of the types that do not have native C++ support:

- All the variation around 16 bits floating point:
  - ▶ IEEE binarv16
  - ► Google bfloat1
  - IBM DLFloat16
- Arbitrary precision floating point format
- Logarithmic Number System with many bases
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  - Posit
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Can we offer C++ types that represent these types?
Can we have these types working with HLS?
Without needing *Frankenstein*-like HLS-RTL integration?
With good QOR?

4 . 2



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Library proposes template type FPNumber<W<sub>E</sub>, W<sub>F</sub>>





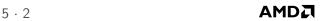


Library proposes template type FPNumber<W<sub>E</sub>, W<sub>F</sub>>

| IEEE binary16 = FP<5, 10> 
$$W_{E} = 5$$
  $W_{F} = 10$  |  $W_{F} = 1$ 

Library proposes template type FPNumber $<W_E$ ,  $W_F>$ 

IEEE binary16 = FP<5, 10> 
$$W_{E} = 5$$
 
$$W_{F} = 10$$
 
$$s \quad e_{4} \quad e_{3} \quad e_{2} \quad e_{1} \quad e_{0} \quad f_{9} \quad f_{8} \quad f_{7} \quad f_{6} \quad f_{5} \quad f_{4} \quad f_{3} \quad f_{2} \quad f_{1} \quad f_{0}$$
 
$$bfloat16 = FP<8,7>$$
 
$$W_{E} = 8$$
 
$$W_{F} = 7$$
 
$$s \quad e_{7} \quad e_{6} \quad e_{5} \quad e_{4} \quad e_{3} \quad e_{2} \quad e_{1} \quad e_{0} \quad f_{6} \quad f_{5} \quad f_{4} \quad f_{3} \quad f_{2} \quad f_{1} \quad f_{0}$$



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bfloat16 = FP<8,7>
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My completely custom float type = FP<7, 9> 
$$W_F = 7$$

$$W_E = 7$$
  $W_F = 9$ 
 $s \quad e_6 \quad e_5 \quad e_4 \quad e_3 \quad e_2 \quad e_1 \quad e_0 \quad f_8 \quad f_7 \quad f_6 \quad f_5 \quad f_4 \quad f_3 \quad f_2 \quad f_1 \quad f_0$ 

### The posit encoding scheme

A posit encoding is parametrized by the word size N and the exponent shift size  $W_{es}$ . For a positive value, the code is made of the following fields:

- The first sign bit s is set to zero
- ullet The range encoded by the length r of a sequence of identical bits b ended by  $ar{b}$
- The exponent shift es on Wes bits
- The remaining  $N (k + 2 + W_{es})$  bits are the significand bits f

The encoded value is

$$v = 1.\mathbf{f} \cdot 2^{\mathbf{k}2^{W_{es}} + \mathbf{es}}$$

$$\mathbf{k} = \begin{cases} -r & \text{if } b = 0\\ r - 1 & \text{if } b = 1 \end{cases}$$

Negative values are encoded as 2's complement of their opposite





- Word size *N*
- Exponent: computed from variable length sequence r of identical bits
- Remaining bits: fraction bits



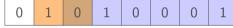
- Word size N
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$$r=1$$

0 1 0 1 0 0 0 1  $1.10001 \times 2^{1-1} = 1.53125$ 

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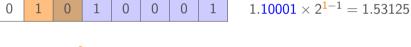


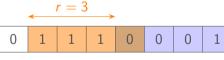
$$1.001 \times 2^{3-1} = 4.5$$

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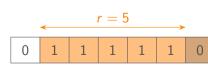
0

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$$1.001 \times 2^{3-1} = 4.5$$



$$1.1 \times 2^{5-1} = 24$$





Word size N

0

- Exponent: computed from variable length sequence *r* of identical bits
- Remaining bits: fraction bits

$$r = 1$$

0 1 0 1 0 0 0 1

1.10001 ×  $2^{1-1} = 1.53125$ 
 $r = 3$ 

0 1 1 1 0 0 0 1

1.001 ×  $2^{3-1} = 4.5$ 
 $r = 5$ 

0 1 1 1 1 1 0 1

 $r = 7$ 



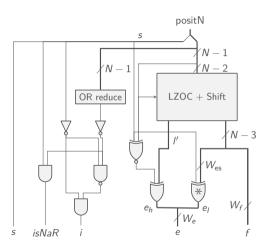
 $1 \times 2^{7-1} - 64$ 

```
using posit_t = PositNumber<8, 2>;
auto adder(posit_t a, posit_t b) {
    return a + b;
}
```



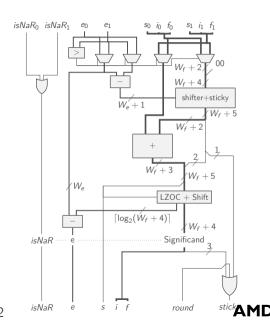
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**Figure:** Posit to internal FP representation decoder



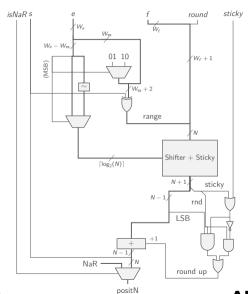
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**Figure:** Perform lossless compressed addition



```
using posit_t = PositNumber<8, 2>;
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```

Figure: Convert the result back to Posit



#### LNS

- Logarithmic Number System (LNS): number represented by its logarithm
  - $\triangleright$  Stored value v in fixed-point represents 2
  - ▶ e.g. stored value of 2.75 represents  $2^{2.75} \approx 6.72717$
- Product simplified (addition of the logarithms)
- Addition require computation of logarithm and power function

In base 2 with X > Y, and  $L_X$  and  $L_Y$  the representation of X and Y respectively:

$$\begin{array}{rcl} L_{X+Y} & = & \log_2(2^{L_X} + 2^{L_Y}) \\ & = & \log_2\left(2^{L_X}(1 + 2^{L_Y - L_X})\right) \\ & = & \log_2(2^{L_X}) + \log_2(1 + 2^{L_Y - L_X}) \\ & = & L_X + f_{\oplus}(L_Y - L_X), & \text{with } f_{\oplus}(r) = \log_2(1 + 2^r) \end{array}$$



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How to compute a value for

$$f_{\oplus}: r \mapsto \log_2(1+2^r)$$

Composition of elementary functions not OK:

- No control on error (or need high precision on intermediates for worst case scenario
- Quite slow (sum of the latencies of individual functions)

We can do something better !



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- An arbitrary fixed-point domain  $\mathcal{D}$ , e.g.  $\{k \cdot 2^{-2} \mid \forall k \in [0...15]\}$
- A unary function  $f: \mathcal{D} \to \mathbb{R}$ , e.g.  $f: x \mapsto \sin(\pi \cdot x/2)$
- An accuracy constraint ε
- ε of the form 2<sup>p</sup>

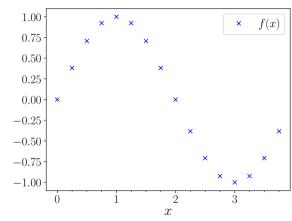
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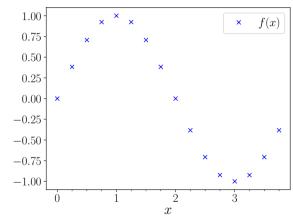
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1.00

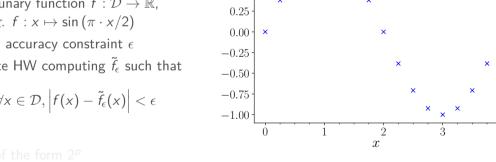
0.75 -

0.50

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Generate HW computing  $\tilde{f}_{\epsilon}$  such that

$$\forall x \in \mathcal{D}, \left| f(x) - \tilde{f}_{\epsilon}(x) \right| < \epsilon$$





×

f(x)

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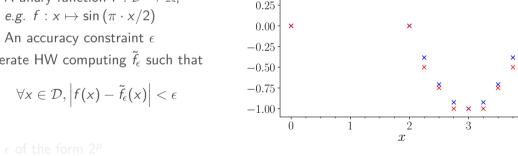
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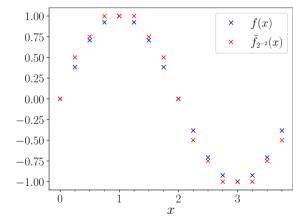
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#### User types related to fixed-point:

- FixedFormat<H, L, signedness> template type to represent fixed-point formats
- FixedNumber<Format> to represent a value of a given format

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using format\_t = FixedFormat<2,-3, unsigned>;
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$$10110_2 \cdot 2^{-3} = 22 \cdot 2^{-3} = 2.75$$

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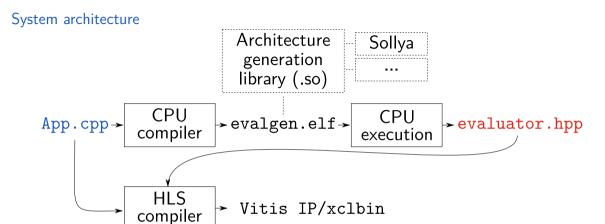
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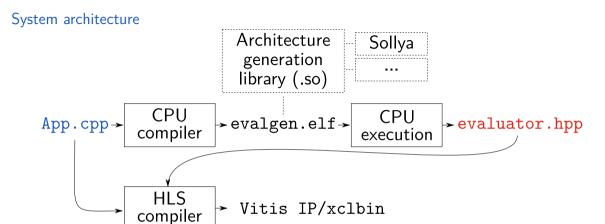
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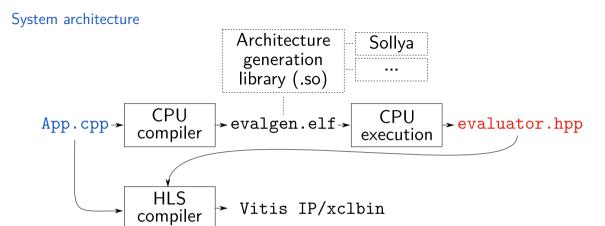
# Evaluation of $x \mapsto \sin(x \cdot \pi + 1.5)$ faithful at $2^{-9}$ using format\_t = FixedFormat<2, -3, unsigned>; auto shifted\_sin\_pi(FixedNumber<format\_t> value) { auto x = FreeVariable{value}; auto f = $\sin(x * cst::pi + 1.5_cst)$ ; return f.evaluate<-9>(); }



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#### System architecture

Runtime library internals – computing  $x \cdot \pi$ 

#### User written code

```
using number_format = FixedFormat<2, -1, unsigned>;
auto mul_by_pi(FixedNumber<number_format> x) {
  return evaluate<-2>(FreeVariable{x} * cst::pi);
}
```

#### System architecture

Runtime library internals – computing  $x \cdot \pi$ 

# Generated specialization header – specialized evaluator type

```
template<>
struct Evaluator<
BinaryOp<
  NullaryOp<OperationType<OperationKind::PI>>,
  FreeVariable<FixedNumber<FixedFormat<2, -1, unsigned>>>,
  OperationType<OperationKind::MUL>
>, -2> {
  auto evaluate(/*...*/) {/*...*/}
}
```



#### System architecture

Runtime library internals – computing  $x \cdot \pi$ 

## Generated specialization header – chunk of the specialization

```
auto initial value = [](FixedNumber<FixedFormat<2, 0, unsigned>> p) {
  constexpr auto values = Table<3, FixedFormat<4, -4, unsigned>>{{
    Ob000001101 ubi, // Values specific to the function to evaluate
    Ob000111111 ubi, // Need external tools to compute them with an
   Ob001110001 ubi, // accuracy warranty.
    0b010100011 ubi,
    0b011010110 ubi,
    0b100001000 ubi,
    0b100111010 ubi,
    Ob101101100 ubi}};
 auto to_num_key = p.value();
 return values[to num kev];
 };
```

- Requires a reference function of high precision (provided by sollya)
- Sub-sampling to produce table of initial values (TIV)
- Differences between TIV and values stored in Offset Table (TO)
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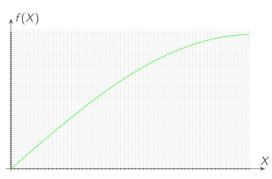


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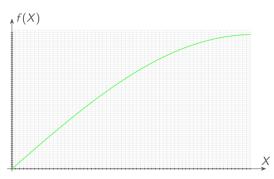


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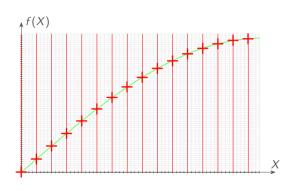


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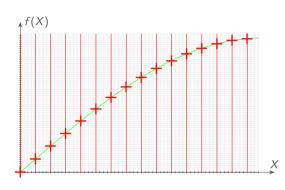


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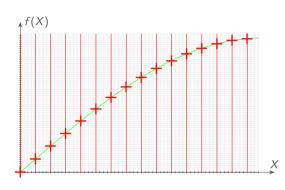


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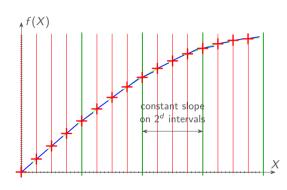


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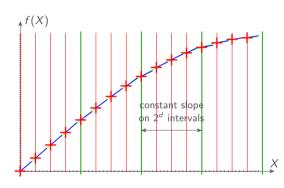
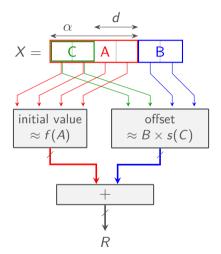


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#### Bipartite approximation



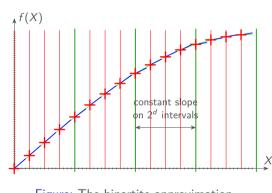


Figure: The bipartite approximation

Figure: Bipartite architecture





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### Simplified LNS adder code

```
// lns t is a specialization of FixedNumber
lns t LNSAdder(lns t op1, lns t op2) {
  auto min op = min(op1, op2);
  auto max op = max(op1, op2);
  lns_t diff_op = min_op - max_op;
  auto diff fv = FreeVariable { diff_op };
  auto f = log2(1._cst + pow(2._cst, diff_fv));
  auto rounded_f = f + lns t::rounding constant;
  auto result op diff = evaluate<lns t::add prec>(rounded f);
  return max op + result op diff;
```

# Toy applications Additive audio synthesis

#### Additive audio synthesis

$$y(t) = \sum_{k=1}^{K} r_k(t) \sin(2\pi f_k t + \phi_k)$$

- $\phi_k = 0$  and K = 256,  $f_k = 1000 \cdot k/256$
- Reference experiment with all computations in float
- Fixed-point experiments:
  - $r_k$  on 8 bits
  - ightharpoonup evaluation of the sinus faithful at  $2^{-6}$ ,  $2^{-8}$ ,  $2^{-16}$  and  $2^{-22}$



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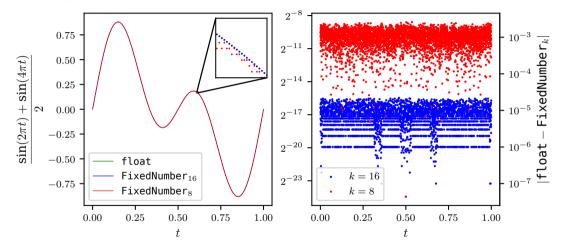
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#### Additive audio synthesis



#### Additive audio synthesis

Experiment		Area				Timing		
Pipeline	Format	LUT	Flip-flop	DSP	BRAM	Latency	Critical path (ns)	Ш
Unpipelined	float	12389	15222	175	0	653	2.787	-
	$FixedNumber_6$	7932	6985	256	129	279	2.907	-
	FixedNumber8	8882	7284	256	257	297	2.901	-
	$FixedNumber_{16}$	5777	6917	256	513	284	2.995	-
	$FixedNumber_{22}$	6551	7304	256	769	270	2.945	-
Pipelined	float	141491	166723	1304	0	226	2.995	128
	$FixedNumber_6$	7442	4977	256	128	5	2.803	1
	$FixedNumber_8$	7568	6500	256	256	5	2.701	1
	$FixedNumber_{16}$	4513	8806	256	512	8	2.806	1
	FixedNumber <sub>22</sub>	5627	9385	256	768	8	3.074	1

Table: Area and timing metrics comparison between float and various FixedNumber for an additive synthesizer of 256 oscillators (target xcvu13p-fhga2104-3-e, clock period 3 ns)





- Relatively simple flow for arbitrary function evaluation in HLS
- Many more custom arithmetic blocks could be integrated
  - ► Tiled/truncated multipliers
  - Bitheaps
  - Better function evaluator strategies
  - Filters...
- Possible usability improvement by hiding the tool interaction inside the compiler itself
- Might be interesting to use MLIR to go from high level function representation to implementation



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#### The terrible library's secret

The library uses many modern C/C++ constructs!

- Concepts
- extended constexpr possibilities
- \_BitInt()
- . . .

How to compile it with our HLS tools?



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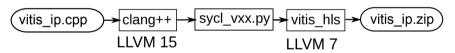
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### Compiler overview

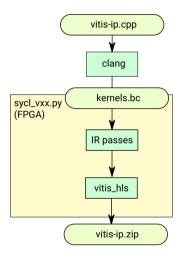
- The library uses C++20
- C++20 compiler for Vitis IPs integrable in Vivado block design
- One command line:

clang++ -target=vitis\_ip-xilinx vitis\_ip.cpp -vitis-ip-part=part-id -o vitis\_ip.zip



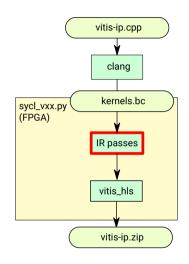
- clang++ is a fork based on the latest upstream
- clang++ 15 has \_BitInt for free!

## Compiler for Vitis IP





## LLVM IR passes used in sycl\_vxx.py



- Basic optimization
- Promote memory to register
  - ▶ LLVM 15 version is better than HLS LLVM 7 one!
- Lower memcpy to load & store
- Extension lowering
- Decoration property generation: pipes, interface...
- Downgrading LLVM IR 15→7



### Downgrading LLVM IR

- LLVM IR is kept upward-compatible but not downward-compatible ©
- So any version of LLVM can consume previous versions easily

#### How is downgrading done:

- Run a pass to remove or rewrite constructs that don't exist in the LLVM IR 7
  - remove or rewrite Attributes, Intrinsics and Instructions
- Run modified version of the IR printer
- Assemble with Vitis's llvm-as

#### Limitation:

- Not all semantic in LLVM 15 can be expressed in LLVM 7
- Some transformations that might cause miscompiles
- The gap keeps growing

Downgrading IR is not sustainable ③



## Unexpected users of sycl\_vxx.py

- Many advanced users seem to try feeding latest LLVM IR (15) to HLS
- We have users of sycl\_vxx.py at PNNL

And SYCL...



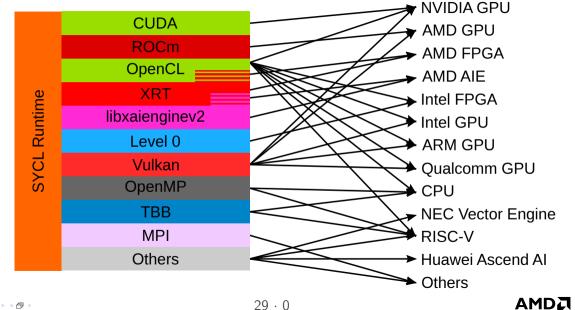


#### **SYCL**

- Khronos Group standard using modern C++ for heterogeneous programming
  - ► Single-source for simplicity and safety
  - ► CPU emulation & debug for free since it is pure C++
  - ▶ Support any back-end of any vendor at the same time: CUDA, OpenCL, HIP, Level0...
  - ▶ Bidirectional interoperability mode: CUDA or OpenCL can use SYCL, SYCL can use OpenMP, HIP or XRT code...
- A dozen of implementations, with 3 more serious ones
  - ► Codeplay ComputeCpp, mainly targeting embedded systems nowadays
  - ▶ hipSYCL (open-source github.com/illuhad/hipSYCL) for any GPU/CPU
  - ▶ Intel oneAPI DPC++ (open-source github.com/intel/llvm) for almost anything



# Typical SYCL stack



## SYCL for FPGA

- Intel oneAPI SYCL DPC++ for Intel FPGA (open-source product)
- Codeplay ComputeCpp for AMD FPGA (not announced yet)
- AMD SYCL for Vitis for AMD FPGA & AIE (open-source research prototype github.com/triSYCL/sycl)

# Specificities of a SYCL compiler

- Our SYCL Compiler for AMD/Xilinx FPGAs
- Fork of DPC++ from Intel
- Single-source and single-binary
  - ► Feels like normal CPU programming
  - Simpler to use
  - Safer
  - ► Single source of truth
- Direct programming
  - Fine grain control
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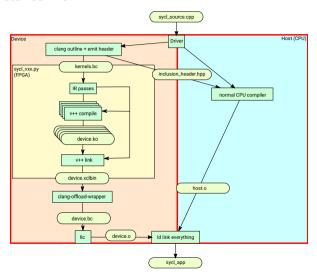
## Overview



Same tools as for the Vitis IP compiler

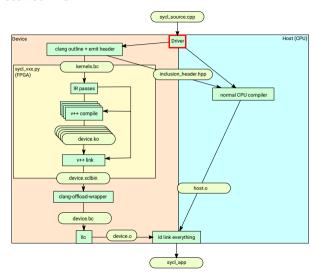
• The device path is shared with the Vitis IP compiler





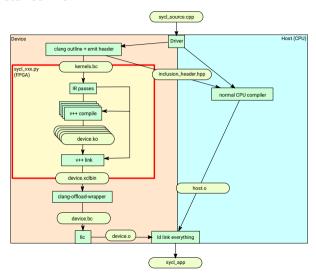
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- Driver hides the complexity
- Still uses sycl\_vxx.py
- Still uses the same IR passes
- But uses v++





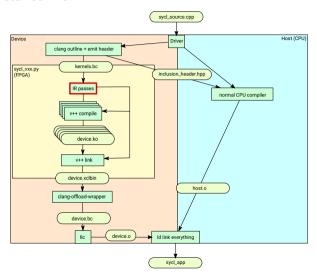
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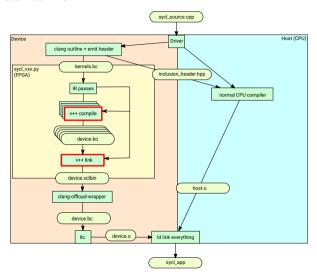
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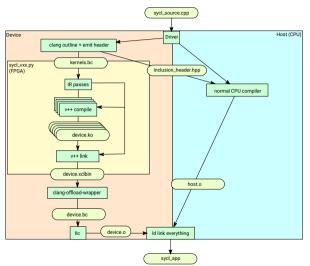




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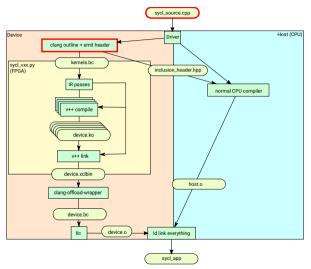
# Single-source & single-binary



```
// Some host code here
cgh.single_task([=] {
    // Some device code here
});
// Back to host code
```

- Single source
  - Internal attribute
  - Device frontend
  - Host frontend
- Single binary
  - ► clang-offload-wrapper
  - Inclusion header

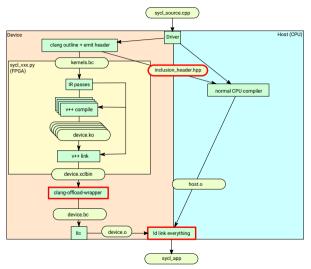
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## Pipeline and dataflow

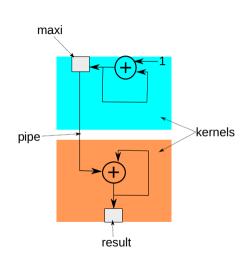
```
h.single task(pipeline kernel([=]{/*Device code*/}));
/// like HLS's "#pragma HLS pipeline" in a kernel
h.single task(pipeline kernel<constrained ii<4>>([=]{/*Device code*/}));
/// like HLS's "#pragma HLS pipeline II=4" in a kernel
h.single task(dataflow kernel([=]{/*Device code*/}));
/// like HLS's "#pragma HLS dataflow" in a kernel
for (...)
 pipeline<auto_ii, rewind_pipeline, flushable>([&]{/*loop body*/});
/// like HLS's "#pragma HLS pipeline enable flush rewind" on a loop
for (...)
  dataflow([&] {/* Loop body executed in dataflow mode */});
/// like HLS's "#pragma HLS dataflow" on a loop
```

• Can express everything #pragma HLS pipeline or #pragma HLS dataflow can

# **Pipes**

```
using MyHLSstream = pipe<class MyID, int>;
// declare a pipe of ints
cgh.single_task([=] {
  for (int i = 0; i < size; i++)</pre>
    MyHLSstream::write(acc_a[i]);
});
//...
cgh.single_task([=] {
  for (int i = 0; i < size; i++)
    result += MyHLSstream::read();
});
```

- Same API as Intel's SYCL static pipe extension
- No extra configuration, just C++



## Partition Array

```
/// equivalent to int array1[6]
                                                                N-2
partition array<int, 6, block<2>> array1;
                                                                       N-2
/// equivalent to float array2[10]
partition_array<float, 10, cyclic<2>> array2;
                                                                N-3
/// equivalent to long array3[4]
partition array<long, 4, complete<>> array3;
                                                                      N-1

    Multi-dimensional
```

## Memory banks

```
sycl::buffer<int, 1> a;
sycl::buffer<int, 1> b;
q.submit([&](sycl::handler &cgh) {
  sycl::accessor acc_a(a, cgh, accessor_property_list{ddr_bank<1>});
  sycl::accessor acc b(b, cgh, accessor property list{hbm bank<1>});
  cgh.single task([=]{
    for (int i = 0; i < size; i++)</pre>
      acc b += acc a:
 });
});
```

- Support HBM and DDR banks
- No extra configuration, just C++

## How are extensions implemented

## How are extensions processed:

- C++ wrapper with syntax
- Internal generic attribute
- For memory banks only: the frontend generate the generic attribute
- Emit generic information in IR
- IR passes create the correct IR for HLS and configuration for v++
- Reuses Vitis and HLS

## Why:

- The frontend is rarely involved
- The syntax is handled is the SYCL C++ library
- Minimal conflicts with upstream



# **Tooling**

- Users only write C++ (no compiler extensions)
- Internally compiler features are used but with fallbacks
- Users can use all their usual source tools
  - ► IDE & editors (auto-completion on FPGA properties!)
  - Static analysis
  - Refactoring tools
  - any other...
- Single-command to build an application:
   clang++ -fsycl -fsycl-target=fpga64\_hls\_hw src.cpp -o app
- Users can use all the usual build systems on top of it





#### Conclusion

- Successful PoC on using modern Clang/LLVM as HLS front-end
- Pis aller for fulfilling "strong" demand for HLS with modern LLVM IR (PNNL, ...)
- Enable "HLS IP library" using modern C++, help bridging the gap between RTL and HLS
- Building on Intel oneAPI DPC++ to bring SYCL for AMD FPGA (+other devices)
  - Single-source
  - Standard programming model
  - Allow the same flexibility as HLS #pragma

One shared goal: make the programming of FPGAs easier!

## Future work:

- Advance on SYCL for AIE, for full SYCL programmability on ACAP
- Investigate possible usage of MLIR
- Think about SYCL extensions to handle FPGAs I/O in embedded settings (Zynq MPSoC)
- Many possibilities of "HLS IP" libraries

