# Kirill Zakharov Pade Approximation

#### Clear[padeApprox]

$$\begin{split} &\text{funD}[\text{fun}\_,\,y_-,\,k_-,\,h_-] := D[\text{fun}[y]\,,\,\{y,\,k\}]\,\,/.\,\,y \to \,h \\ &\text{padeApprox}[\text{fun}\_,\,x0_-,\,m_-] := Module\big[\{t,\,x=x0,\,\text{array}=\{\}\},\,Do\big[t=\frac{-\text{fun}[x]}{\text{funD}[k,\,i,\,x]};\\ &x = \frac{x^2}{x-t};\\ &\text{AppendTo}[\text{array},\,x]\,,\,\{i,\,1,\,m\}\big];\\ &\text{N}\,/\,@\,\text{array}\big] \end{split}$$

## Задаем функцию

fun[y\_] := 
$$y^3 + 6y^2 + 9y - 4$$
  
1st = padeApprox[fun, 3.6, 3];

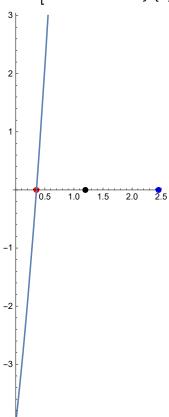
#### Ответ

lst[3]

0.354205

#### Визуальное представление

Show[Graphics[{PointSize[0.04], Blue, Point[{lst[1], 0}],  $\label{eq:black_point} $$ Black, Point[\{lst[3], 0\}], Axes \to True], $$ $$$  $Plot[x^3 + 6x^2 + 9x - 4, \{x, -5, 5\}, PlotRange \rightarrow \{Automatic, \{-4, 3\}\}]]$ 



### Проверка

Solve 
$$\left[ x^3 + 6 x^2 + 9 x - 4 == 0, x \right]$$
  $\left\{ \left\{ x \rightarrow \bigcirc 0.355... \right\}, \left\{ x \rightarrow \bigcirc -3.18... - 1.08... i \right\} \right\}, \left\{ x \rightarrow \bigcirc -3.18... + 1.08... i \right\} \right\}$