## Transfer a photo into a Monet style picture

(This part we got inspiration and learning from <a href="https://www.kaggle.com/basu369victor/style-transfer-deep-learning-algorithm">https://www.kaggle.com/basu369victor/style-transfer-deep-learning-algorithm</a> (<a href="https://www.kaggle.com/basu369victor/style-transfer-deep-learning-algorithm">https://www.kaggle.com/basu369victor/style-transfer-deep-learning-algorithm</a>))

First, we have a original image and a style image. Then, we still use VGG16 but only pick the convolution layers for extracting image's features and delete the layers for classification. Finally, we will get a new picture combine the style of the style image and the objects from original image.

```
In [1]: import os
    import numpy as np
    import tensorflow
    from tensorflow.keras import applications
    from tensorflow.keras.applications import vgg16
    from tensorflow.keras.models import Model
    from scipy.optimize import fmin_l_bfgs_b
    from tensorflow.keras.preprocessing.image import load_img, save_img, img_to_import matplotlib
    import matplotlib.pyplot as plt
%matplotlib inline
```

```
In [2]: import tensorflow.keras.backend as K
    K.clear_session()
    ori_path = './photo.jpg'
    style_path = './Claude_Monet.jpg'
```

Generation image's size

```
In [3]: ori_image = load_img(ori_path)
    nrow, ncol = ori_image.size
    nrow = nrow // 10
    ncol = ncol // 10
    print(str(nrow), str(ncol))
```

403 302

Show 2 images

## Photo



Out[4]: <matplotlib.image.AxesImage at 0x7f028571a358>



Pre-Process the images as the VGG16 input. Using tensor to represent the image, and bulid a new image as ouput

```
In [5]: def preprocess(image):
    img = img_to_array(image)
    img = vgg16.preprocess_input(img[np.newaxis,:])
    img = K.variable(img)
    return img
    ori_img = preprocess(ori_image)
    style_img = preprocess(style_image)
    result_image = K.placeholder((1,ncol, nrow,3)) # 'channels_last' format()
    result_image.shape
```

WARNING:tensorflow:From /usr/local/lib/python3.5/dist-packages/tensorflo w/python/ops/resource\_variable\_ops.py:435: colocate\_with (from tensorflo w.python.framework.ops) is deprecated and will be removed in a future ver sion.

Instructions for updating:

Colocations handled automatically by placer.

Out[5]: TensorShape([Dimension(1), Dimension(302), Dimension(403), Dimension(3)])

Then intergrating original image, style image and result image.

```
In [6]: vgg16_input = K.concatenate([ori_img,style_img,result_image], axis=0)
vgg16_input
```

```
Out[6]: <tf.Tensor 'concat:0' shape=(3, 302, 403, 3) dtype=float32>
```

Import VGG16 model, and make a dictionary

Layer (type)	Output Shape	Param #
input_1 (InputLayer)	(3, 302, 403, 3)	0
block1_conv1 (Conv2D)	(3, 302, 403, 64)	1792
block1_conv2 (Conv2D)	(3, 302, 403, 64)	36928
block1_pool (MaxPooling2D)	(3, 151, 201, 64)	0
block2_conv1 (Conv2D)	(3, 151, 201, 128)	73856
block2_conv2 (Conv2D)	(3, 151, 201, 128)	147584
block2_pool (MaxPooling2D)	(3, 75, 100, 128)	0
block3_conv1 (Conv2D)	(3, 75, 100, 256)	295168
block3_conv2 (Conv2D)	(3, 75, 100, 256)	590080
block3_conv3 (Conv2D)	(3, 75, 100, 256)	590080
block3_pool (MaxPooling2D)	(3, 37, 50, 256)	0
block4_conv1 (Conv2D)	(3, 37, 50, 512)	1180160
block4_conv2 (Conv2D)	(3, 37, 50, 512)	2359808
block4_conv3 (Conv2D)	(3, 37, 50, 512)	2359808
block4_pool (MaxPooling2D)	(3, 18, 25, 512)	0
block5_conv1 (Conv2D)	(3, 18, 25, 512)	2359808
block5_conv2 (Conv2D)	(3, 18, 25, 512)	2359808
block5_conv3 (Conv2D)	(3, 18, 25, 512)	2359808
block5_pool (MaxPooling2D)	(3, 9, 12, 512)	0

Total params: 14,714,688
Trainable params: 14,714,688

Non-trainable params: 0

Check the dictionary

```
In [8]: model_dict
Out[8]: {'block1 conv1': <tf.Tensor 'block1 conv1/Relu:0' shape=(3, 302, 403, 64)
        dtype=float32>,
         'block1_conv2': <tf.Tensor 'block1_conv2/Relu:0' shape=(3, 302, 403, 64)
        dtype=float32>,
         'block1 pool': <tf.Tensor 'block1 pool/MaxPool:0' shape=(3, 151, 201, 6
        4) dtype=float32>,
          'block2_conv1': <tf.Tensor 'block2_conv1/Relu:0' shape=(3, 151, 201, 12
        8) dtype=float32>,
         'block2 conv2': <tf.Tensor 'block2_conv2/Relu:0' shape=(3, 151, 201, 12
        8) dtype=float32>,
         'block2 pool': <tf.Tensor 'block2 pool/MaxPool:0' shape=(3, 75, 100, 12
        8) dtype=float32>,
         'block3_conv1': <tf.Tensor 'block3_conv1/Relu:0' shape=(3, 75, 100, 256)
        dtype=float32>,
         'block3 conv2': <tf.Tensor 'block3_conv2/Relu:0' shape=(3, 75, 100, 256)
        dtype=float32>,
         'block3 conv3': <tf.Tensor 'block3 conv3/Relu:0' shape=(3, 75, 100, 256)
        dtype=float32>,
         'block3_pool': <tf.Tensor 'block3_pool/MaxPool:0' shape=(3, 37, 50, 256)
        dtype=float32>,
          'block4_conv1': <tf.Tensor 'block4_conv1/Relu:0' shape=(3, 37, 50, 512)
        dtype=float32>,
         'block4 conv2': <tf.Tensor 'block4 conv2/Relu:0' shape=(3, 37, 50, 512)
        dtype=float32>,
         'block4 conv3': <tf.Tensor 'block4 conv3/Relu:0' shape=(3, 37, 50, 512)
        dtype=float32>,
         'block4 pool': <tf.Tensor 'block4 pool/MaxPool:0' shape=(3, 18, 25, 512)
        dtype=float32>,
         'block5 conv1': <tf.Tensor 'block5 conv1/Relu:0' shape=(3, 18, 25, 512)
        dtype=float32>,
         'block5 conv2': <tf.Tensor 'block5 conv2/Relu:0' shape=(3, 18, 25, 512)
        dtype=float32>,
         'block5_conv3': <tf.Tensor 'block5_conv3/Relu:0' shape=(3, 18, 25, 512)
        dtype=float32>,
          'block5 pool': <tf.Tensor 'block5 pool/MaxPool:0' shape=(3, 9, 12, 512)
        dtype=float32>,
         'input 1': <tf.Tensor 'concat:0' shape=(3, 302, 403, 3) dtype=float32>}
```

Vgg16 is usually used to classificate, however, here we need to delete the classification purpose layyers.

In this case, we decided to use 6 convolution layers to get the image's feature and one layers as output style feature

Using dictionary and layers we choosed late step to gerenate features

```
In [10]: features = model_dict['block5_conv2']
    ori_features = features[0, :, :, :]
    new_features = features[2, :, :, :]
```

We need a optimizer to minimize the loss between style image and new image. After reading the "Optimizers Guide" (<a href="https://qiskit.org/documentation/aqua/optimizers.html">https://qiskit.org/documentation/aqua/optimizers.html</a>), we decided to use the Limited-memory Broyden-Fletcher-Goldfarb-Shanno Bound, because this optimizer has a direct callable function by scipy (<a href="https://docs.scipy.org/doc/scipy/reference/generated/scipy.optimize.fmin | bfgs b.html">https://docs.scipy.org/doc/scipy/reference/generated/scipy.optimize.fmin | bfgs b.html</a>))

```
In [11]: from scipy.optimize import fmin_l_bfgs_b
# x, f, d= fmin_l_bfgs_b(func, x0)

# x : array_like(Estimated position of the minimum.)
# f : float(Value of func at the minimum.)
# d : dict(Information dictionary.)
# func : callable f(x,*args) Function to minimise.
# x0 : ndarray Initial guess.
```

Here we decided to use the error square as loss and gradients descent which we learned in lecture.

Define Output Loss Function, using error square (keras.backend.square(x) <a href="https://keras.io/backend/">https://keras.io/backend/</a>)

```
In [12]: # we has total 7 layers, the last ouput layer get smallest weight
    output_weight=0.03
    output_loss = output_weight * K.sum(K.square(new_features - ori_features))
```

Define Style Loss Function, using Gram Matrices

A Gram matrix of vectors a1, ..., an is a matrix G

s.t. G=⟨ai,aj⟩ for all i,j if vectors a1, ... ,an are columns of a matrix A, then G=ATA a Gram matrix is Positive Definite and Symmetric if vectors a1, ... ,an are the rows of A (A would be so-called "Data Matrix"), then G=AAT, and it's called left Gram matrix

Then still using error square to caclutate 2 matrices loss

Define How to Caculate the initial gradients, uising keras.backend.gradients(loss, variables) <a href="https://keras.io/backend/#gradients">https://keras.io/backend/#gradients</a> (<a href="https://keras.io/backend/#gradients">https://keras.io/backend/#gradients</a>)

```
In [14]: for layer_name in feature_layers:
    features = model_dict[layer_name]
    style_features = features[1, :, :, :]
    new_features = features[2, :, :, :]
    style_loss = style_loss_function(style_features, new_features)
    # 1 output layer, 6 convolution layers(features)
    output_loss = output_loss + (1 / nfeature_layer) * style_loss
    gradient = K.gradients(output_loss, result_image)
    loss_list = [output_loss]
    loss_list += gradient #Record gradient
    keras_function = K.function([result_image], loss_list)
```

With loss function and initial gradients, now we define the callable function to minimise using in optimizer.

Using original image as the input

```
In [16]: # run scipy-based optimization (L-BFGS) over the pixels of the generated ima
# so as to minimize the neural style loss
X = load_img(ori_path, target_size=(ncol, nrow))
X = np.expand_dims(img_to_array(X), axis=0)
X = vgg16.preprocess_input(X)
```

Start iterating using Limited-memory Broyden-Fletcher-Goldfarb-Shanno Bound

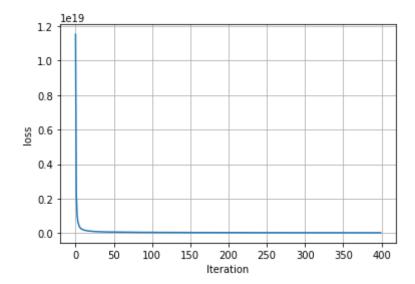
```
In [17]:    nitr = 400
    neval = 20 #Maximum number of function evaluations.
loss = []
for i in range(nitr):
    print('Iteration = {}'.format(i))
    if i == 0:
        opt_loss = float('Inf') #initial min loss
    X, func_min, d= fmin_l_bfgs_b(function.loss, X.flatten(), fprime=function loss.append(func_min)
    print(d['grad'])
    if func_min < opt_loss:
        opt_loss = func_min
        opt_X = X.copy()</pre>
```

```
Iteration = 0
[ 1.12871153e+13 9.67454595e+12 3.44800965e+12 ... 1.10163237e+12
 -4.79169118e+11 -1.46461442e+11]
Iteration = 1
[-1.38585270e+12 -7.72080337e+11 1.25274489e+12 ... 2.99249140e+11
  2.53802136e+11 2.26965545e+101
Iteration = 2
[ 1.42048231e+12 3.60088601e+11 -3.27851016e+11 ... 7.72686807e+10
  2.60116019e+09 9.72613386e+101
Iteration = 3
[2.75204997e+11 6.76066263e+10 2.63078314e+11 ... 6.59419955e+10
 1.10414971e+11 8.19095142e+101
Iteration = 4
[ 2.99091149e+10 -6.28181565e+10 -3.54626109e+10 ... 1.47346883e+10
  8.29418865e+10 7.99861637e+101
Iteration = 5
[-7.14945331e+10 \quad 3.54930065e+11 \quad 4.05361787e+10 \quad \dots \quad 1.99629906e+10
  2.46782198e+10 5.56122235e+101
Iteration = 6
```

Plot the minimum loss each iteration.

```
In [28]: plt.plot(loss)
   plt.grid()
   plt.xlabel('Iteration')
   plt.ylabel('loss')
```

```
Out[28]: Text(0, 0.5, 'loss')
```



Then convert output array to image.

VGG-16 was trained using Caffe, and Caffe uses OpenCV to load images which uses BGR by default, so both VGG models are expecting BGR images.

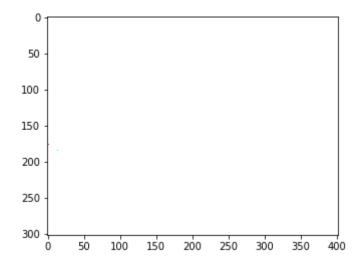
The official mean that gets used in the vgg16.py file is [123.68, 116.779, 103.939] (https://forums.fast.ai/t/how-is-vgg16-mean-calculated/4577/9 (https://forums.fast.ai/t/how-is-vgg16-mean-calculated/4577/9))

So we need to covert BGR to RGB before imshow

```
In [19]: opt_X = opt_X.reshape((ncol, nrow, 3))
    vgg_mean = [103.939,116.779,123.68]
    for i in range(3):
        opt_X[:, :, i] = opt_X[:, :, i] + vgg_mean[i]
    plt.imshow(opt_X)
```

Clipping input data to the valid range for imshow with RGB data ([0..1] f or floats or [0..255] for integers).

Out[19]: <matplotlib.image.AxesImage at 0x7f022aa3c0b8>

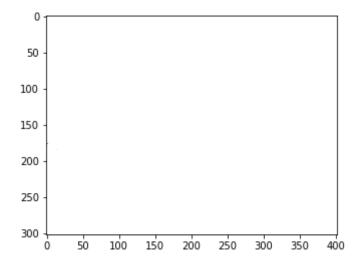


Clipping input data to the valid range for imshow with RGB data ([0..1] for floats or [0..255] for integers).

```
In [20]: opt_X = opt_X[:, :, ::-1]
    opt_X = np.clip(opt_X, 0, 255)
    plt.imshow(opt_X)
```

Clipping input data to the valid range for imshow with RGB data ([0..1] f or floats or [0..255] for integers).

Out[20]: <matplotlib.image.AxesImage at 0x7f022aafc518>



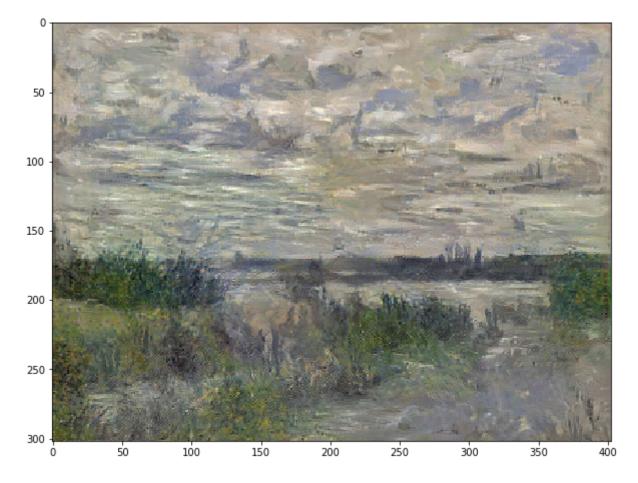
Convert the numpy arrays to uint8 before passing them to Image.fromarray

np array should have data type as uint8

(https://stackoverflow.com/questions/10443295/combine-3-separate-numpy-arrays-to-an-rgb-image-in-python (https://stackoverflow.com/questions/10443295/combine-3-separate-numpy-arrays-to-an-rgb-image-in-python))

```
In [24]: opt_X = opt_X.astype('uint8')
    plt.figure(figsize=(10,10))
    plt.imshow(opt_X)
```

Out[24]: <matplotlib.image.AxesImage at 0x7f022ab5b5c0>



```
In [22]:
         # Ori
         plt.figure(figsize=(20,20))
         plt.subplot(1,3,1)
         plt.title("ori image", fontsize=20)
         plt.axis('off')
         plt.imshow(ori_image)
         # style
         plt.subplot(1,3,2)
         plt.title("style", fontsize=20)
         img_style = load_img(style_path)
         plt.axis('off')
         plt.imshow(style_image)
         # new painting
         plt.subplot(1,3,3)
         plt.title("new painting", fontsize=20)
         plt.axis('off')
         plt.imshow(opt_X)
```

Out[22]: <matplotlib.image.AxesImage at 0x7f022ac37b70>







In [ ]:

## image-style-change (another example)

(This part we got inspiration and learning from <a href="https://www.kaggle.com/basu369victor/style-transfer-deep-learning-algorithm">https://www.kaggle.com/basu369victor/style-transfer-deep-learning-algorithm</a> (<a href="https://www.kaggle.com/basu369victor/style-transfer-deep-learning-algorithm">https://www.kaggle.com/basu369victor/style-transfer-deep-learning-algorithm</a>)

First, we have a original image and a style image. Then, we still use VGG16 but only pick the convolution layers for extracting image's features and delete the layers for classification. Finally, we will get a new picture combine the style of the style image and the objects from original image.

(This part we got inspiration and learning from <a href="https://www.kaggle.com/basu369victor/style-transfer-deep-learning-algorithm">https://www.kaggle.com/basu369victor/style-transfer-deep-learning-algorithm</a> (<a href="https://www.kaggle.com/basu369victor/style-transfer-deep-learning-algorithm">https://www.kaggle.com/basu369victor/style-transfer-deep-learning-algorithm</a>)

```
In [1]: import os
    import numpy as np
    import tensorflow
    from tensorflow.keras import applications
    from tensorflow.keras.applications import vgg16
    from tensorflow.keras.models import Model
    from scipy.optimize import fmin_l_bfgs_b
    from tensorflow.keras.preprocessing.image import load_img, save_img, img_to_import matplotlib
    import matplotlib.pyplot as plt
%matplotlib inline
```

/anaconda3/lib/python3.6/site-packages/h5py/\_\_init\_\_.py:36: FutureWarnin g: Conversion of the second argument of issubdtype from `float` to `np.fl oating` is deprecated. In future, it will be treated as `np.float64 == n p.dtype(float).type`.

from .\_conv import register\_converters as \_register\_converters

```
In [2]: import tensorflow.keras.backend as K
K.clear_session()
    ori_path = './Edouard_Manet_49.jpg'
    style_path = './Joan_Miro_38.jpg'
```

Generation image's size

```
In [3]: ori_image = load_img(ori_path)
    nrow, ncol = ori_image.size
    nrow = nrow // 2
    ncol = ncol // 2
    print(str(nrow), str(ncol))
```

486 590

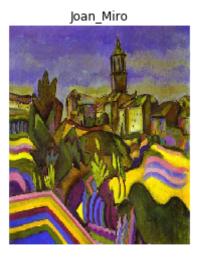
Show 2 images

```
In [4]: ori_image = load_img(ori_path,target_size=(ncol, nrow))
    print(ori_image.size)
    style_image = load_img(style_path, target_size=(ncol, nrow))
    plt.axis('off')
    plt.title('Edouard_Manet')
    plt.imshow(ori_image)
    plt.show()
    plt.axis('off')
    plt.title('Joan_Miro')
    plt.imshow(style_image)
(486, 590)
```

Edouard Manet



Out[4]: <matplotlib.image.AxesImage at 0x132812f550>



Pre-Process the images as the VGG16 input. Using tensor to represent the image, and bulid a new image as outut

```
In [5]: def preprocess(image):
    img = img_to_array(image)
    img = vgg16.preprocess_input(img[np.newaxis,:])
    img = K.variable(img)
    return img
    ori_img = preprocess(ori_image)
    style_img = preprocess(style_image)
    result_image = K.placeholder((1,ncol, nrow,3)) # 'channels_last' format()
    result_image.shape
```

WARNING:tensorflow:From /usr/local/lib/python3.5/dist-packages/tensorflo w/python/ops/resource\_variable\_ops.py:435: colocate\_with (from tensorflo w.python.framework.ops) is deprecated and will be removed in a future ver sion.

Instructions for updating:

Colocations handled automatically by placer.

Out[5]: TensorShape([Dimension(1), Dimension(590), Dimension(486), Dimension(3)])

Then intergrating original image, style image and result image.

```
In [6]: vgg16_input = K.concatenate([ori_img,style_img,result_image], axis=0)
vgg16_input
```

```
Out[6]: <tf.Tensor 'concat:0' shape=(3, 590, 486, 3) dtype=float32>
```

Import VGG16 model, and make a dictionary

Layer (type)	Output Shape	Param #
input_1 (InputLayer)	(3, 590, 486, 3)	0
block1_conv1 (Conv2D)	(3, 590, 486, 64)	1792
block1_conv2 (Conv2D)	(3, 590, 486, 64)	36928
block1_pool (MaxPooling2D)	(3, 295, 243, 64)	0
block2_conv1 (Conv2D)	(3, 295, 243, 128)	73856
block2_conv2 (Conv2D)	(3, 295, 243, 128)	147584
block2_pool (MaxPooling2D)	(3, 147, 121, 128)	0
block3_conv1 (Conv2D)	(3, 147, 121, 256)	295168
block3_conv2 (Conv2D)	(3, 147, 121, 256)	590080
block3_conv3 (Conv2D)	(3, 147, 121, 256)	590080
block3_pool (MaxPooling2D)	(3, 73, 60, 256)	0
block4_conv1 (Conv2D)	(3, 73, 60, 512)	1180160
block4_conv2 (Conv2D)	(3, 73, 60, 512)	2359808
block4_conv3 (Conv2D)	(3, 73, 60, 512)	2359808
block4_pool (MaxPooling2D)	(3, 36, 30, 512)	0
block5_conv1 (Conv2D)	(3, 36, 30, 512)	2359808
block5_conv2 (Conv2D)	(3, 36, 30, 512)	2359808
block5_conv3 (Conv2D)	(3, 36, 30, 512)	2359808
	(3, 18, 15, 512)	

Total params: 14,714,688
Trainable params: 14,714,688

Non-trainable params: 0

Check the dictionary

```
In [8]: model_dict
Out[8]: {'block1 conv1': <tf.Tensor 'block1 conv1/Relu:0' shape=(3, 590, 486, 64)
        dtype=float32>,
         'block1_conv2': <tf.Tensor 'block1_conv2/Relu:0' shape=(3, 590, 486, 64)
        dtype=float32>,
         'block1 pool': <tf.Tensor 'block1 pool/MaxPool:0' shape=(3, 295, 243, 6
        4) dtype=float32>,
          'block2_conv1': <tf.Tensor 'block2_conv1/Relu:0' shape=(3, 295, 243, 12
        8) dtype=float32>,
         'block2_conv2': <tf.Tensor 'block2_conv2/Relu:0' shape=(3, 295, 243, 12
        8) dtype=float32>,
         'block2 pool': <tf.Tensor 'block2 pool/MaxPool:0' shape=(3, 147, 121, 12
        8) dtype=float32>,
         'block3_conv1': <tf.Tensor 'block3_conv1/Relu:0' shape=(3, 147, 121, 25
        6) dtype=float32>,
         'block3 conv2': <tf.Tensor 'block3_conv2/Relu:0' shape=(3, 147, 121, 25
        6) dtype=float32>,
         'block3 conv3': <tf.Tensor 'block3 conv3/Relu:0' shape=(3, 147, 121, 25
        6) dtype=float32>,
         'block3_pool': <tf.Tensor 'block3_pool/MaxPool:0' shape=(3, 73, 60, 256)
        dtype=float32>,
          'block4 conv1': <tf.Tensor 'block4_conv1/Relu:0' shape=(3, 73, 60, 512)
        dtype=float32>,
         'block4 conv2': <tf.Tensor 'block4 conv2/Relu:0' shape=(3, 73, 60, 512)
        dtype=float32>,
         'block4 conv3': <tf.Tensor 'block4 conv3/Relu:0' shape=(3, 73, 60, 512)
        dtype=float32>,
         'block4 pool': <tf.Tensor 'block4 pool/MaxPool:0' shape=(3, 36, 30, 512)
        dtype=float32>,
         'block5 conv1': <tf.Tensor 'block5 conv1/Relu:0' shape=(3, 36, 30, 512)
        dtype=float32>,
         'block5 conv2': <tf.Tensor 'block5 conv2/Relu:0' shape=(3, 36, 30, 512)
        dtype=float32>,
         'block5_conv3': <tf.Tensor 'block5_conv3/Relu:0' shape=(3, 36, 30, 512)
        dtype=float32>,
          'block5 pool': <tf.Tensor 'block5 pool/MaxPool:0' shape=(3, 18, 15, 512)
        dtype=float32>,
         'input 1': <tf.Tensor 'concat:0' shape=(3, 590, 486, 3) dtype=float32>}
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Using dictionary and layers we choosed late step to gerenate features

```
In [10]: features = model_dict['block5_conv2']
    ori_features = features[0, :, :, :]
    new_features = features[2, :, :, :]
```

We need a optimizer to minimize the loss between stype image and new image. After reading the "Optimizers Guide" (<a href="https://qiskit.org/documentation/aqua/optimizers.html">https://qiskit.org/documentation/aqua/optimizers.html</a>), we decided to use the Limited-memory Broyden-Fletcher-Goldfarb-Shanno Bound, because this optimizer has a direct callable function by scipy (<a href="https://docs.scipy.org/doc/scipy/reference/generated/scipy.optimize.fmin | bfgs b.html">https://docs.scipy.org/doc/scipy/reference/generated/scipy.optimize.fmin | bfgs b.html</a>))

```
In [11]: from scipy.optimize import fmin_l_bfgs_b
# x, f, d= fmin_l_bfgs_b(func, x0)

# x : array_like(Estimated position of the minimum.)
# f : float(Value of func at the minimum.)
# d : dict(Information dictionary.)
# func : callable f(x,*args) Function to minimise.
# x0 : ndarray Initial guess.
```

Here we decided to use the error square as loss and gradients descent which we learned in lecture.

Define Output Loss Function, using error square (keras.backend.square(x) <a href="https://keras.io/backend/">https://keras.io/backend/</a> (<a href="https://keras.io/backend/">https://keras.io/backend/</a>)

```
In [12]: # we has total 7 layers, the last ouput layer get smallest weight
    output_weight=0.03
    output_loss = output_weight * K.sum(K.square(new_features - ori_features))
```

Define Style Loss Function, using Gram Matrices

A Gram matrix of vectors a1, ..., an is a matrix G

s.t. G=⟨ai,aj⟩ for all i,j if vectors a1, ... ,an are columns of a matrix A, then G=ATA a Gram matrix is Positive Definite and Symmetric if vectors a1, ... ,an are the rows of A (A would be so-called "Data Matrix"), then G=AAT, and it's called left Gram matrix

Then still using error square to caclutate 2 matrices loss

Define How to Caculate the initial gradients, uising keras.backend.gradients(loss, variables) <a href="https://keras.io/backend/#gradients">https://keras.io/backend/#gradients</a> (https://keras.io/backend/#gradients)

```
In [14]: for layer_name in feature_layers:
    features = model_dict[layer_name]
    style_features = features[1, :, :, :]
    new_features = features[2, :, :, :]
    style_loss = style_loss_function(style_features, new_features)
    # 1 output layer, 6 convolution layers(features)
    output_loss = output_loss + (1 / nfeature_layer) * style_loss
    gradient = K.gradients(output_loss, result_image)
    loss_list = [output_loss]
    loss_list += gradient #Record gradient
    keras_function = K.function([result_image], loss_list)
```

With loss function and initial gradients, now we define the callable function to minimise using in optimizer.

```
In [15]: class func(object):
    def __init__(self):
        self.loss_value = None

def loss(self, x):
    x = x.reshape((1, ncol, nrow, 3))
    result = keras_function([x])
    self.loss_value = result[0]
    self.grad_values = np.array(result[1:]).flatten().astype('float64')
    return self.loss_value

def grad(self, x):
    grad_values = np.copy(self.grad_values)
    self.loss_value = None
    self.grad_values = None
    return grad_values
function = func()
```

Using original image as the input

```
In [16]: # run scipy-based optimization (L-BFGS) over the pixels of the generated ima
# so as to minimize the neural style loss
X = load_img(ori_path, target_size=(ncol, nrow))
X = np.expand_dims(img_to_array(X), axis=0)
X = vgg16.preprocess_input(X)
```

Start iterating using Limited-memory Broyden-Fletcher-Goldfarb-Shanno Bound

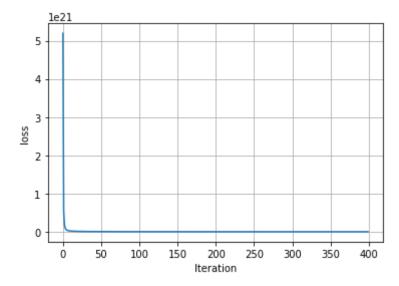
```
In [17]:    nitr = 400
    neval = 20 #Maximum number of function evaluations.
loss = []
for i in range(nitr):
    print('Iteration = {}'.format(i))
    if i == 0:
        opt_loss = float('Inf') #initial min loss
    X, func_min, d= fmin_l_bfgs_b(function.loss, X.flatten(), fprime=function loss.append(func_min)
    print(d['grad'])
    if func_min < opt_loss:
        opt_loss = func_min
        opt_X = X.copy()</pre>
```

```
Iteration = 0
[-1.13819259e+14 \ 2.11088499e+13 \ 7.24103636e+13 \dots 5.96972038e+12
  1.85995991e+13 1.44182818e+12]
Iteration = 1
[ 9.70059153e+12 1.30129005e+13 1.63229123e+10 ... 4.57716374e+12
-6.35074773e+12 -1.16962584e+121
Iteration = 2
[-7.88490564e+13 -6.56955681e+13 -6.55839828e+13 ... 1.81990851e+12
-6.15783072e+12 -9.84203788e+11]
Iteration = 3
[-5.32359309e+12 2.57250443e+13 1.50716348e+13 ... 1.94227130e+12
  4.34667520e+09 -1.62685688e+121
Iteration = 4
[-7.81255893e+13 -6.35482690e+13 -9.43444428e+13 ... 3.86211303e+12
-1.52068869e+12 -1.64111424e+121
Iteration = 5
[-1.63219086e+13 -1.65134074e+11 -9.60866497e+12 ... 2.12884980e+12
-9.67161414e+11 -6.63994434e+11]
Iteration = 6
```

Plot the minimum loss each iteration.

```
In [18]: plt.plot(loss)
    plt.grid()
    plt.xlabel('Iteration')
    plt.ylabel('loss')
```

```
Out[18]: Text(0, 0.5, 'loss')
```



Then convert output array to image.

VGG-16 was trained using Caffe, and Caffe uses OpenCV to load images which uses BGR by default, so both VGG models are expecting BGR images.

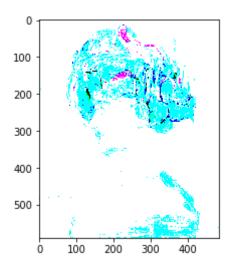
The official mean that gets used in the vgg16.py file is [123.68, 116.779, 103.939] (https://forums.fast.ai/t/how-is-vgg16-mean-calculated/4577/9 (https://forums.fast.ai/t/how-is-vgg16-mean-calculated/4577/9))

So we need to covert BGR to RGB before imshow

```
In [19]: opt_X = opt_X.reshape((ncol, nrow, 3))
    vgg_mean = [103.939,116.779,123.68]
    for i in range(3):
        opt_X[:, :, i] = opt_X[:, :, i] + vgg_mean[i]
    plt.imshow(opt_X)
```

Clipping input data to the valid range for imshow with RGB data ([0..1] f or floats or [0..255] for integers).

Out[19]: <matplotlib.image.AxesImage at 0x7f3dd4526198>

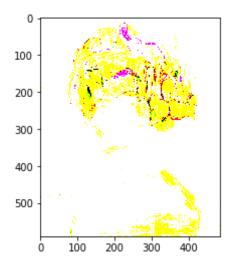


Clipping input data to the valid range for imshow with RGB data ([0..1] for floats or [0..255] for integers).

```
In [20]: opt_X = opt_X[:, :, ::-1]
    opt_X = np.clip(opt_X, 0, 255)
    plt.imshow(opt_X)
```

Clipping input data to the valid range for imshow with RGB data ([0..1] f or floats or [0..255] for integers).

Out[20]: <matplotlib.image.AxesImage at 0x7f3dd435b390>



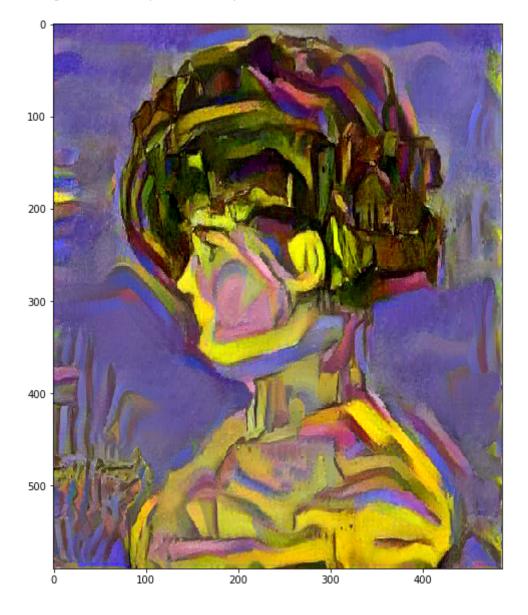
Convert the numpy arrays to uint8 before passing them to Image.fromarray

## np array should have data type as uint8

(https://stackoverflow.com/questions/10443295/combine-3-separate-numpy-arrays-to-an-rgb-image-in-python (https://stackoverflow.com/questions/10443295/combine-3-separate-numpy-arrays-to-an-rgb-image-in-python))

```
In [21]: opt_X = opt_X.astype('uint8')
    plt.figure(figsize=(10,10))
    plt.imshow(opt_X)
```

Out[21]: <matplotlib.image.AxesImage at 0x7f3dd4310a58>



```
In [22]: # Ori
         plt.figure(figsize=(20,20))
         plt.subplot(1,3,1)
         plt.title("ori image", fontsize=20)
         plt.axis('off')
         plt.imshow(ori_image)
         # style
         plt.subplot(1,3,2)
         plt.title("style", fontsize=20)
         img_style = load_img(style_path)
         plt.axis('off')
         plt.imshow(style_image)
         # new painting
         plt.subplot(1,3,3)
         plt.title("new painting", fontsize=20)
         plt.axis('off')
         plt.imshow(opt_X)
```

Out[22]: <matplotlib.image.AxesImage at 0x7f3dd42b91d0>







```
In [ ]:
```