## 1. Exponential Expressions

An expression of the form  $a^x$  is called an **exponential expression**, where a is the **base** and x is the **exponent, power** or **index**.

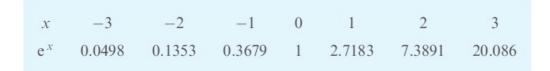
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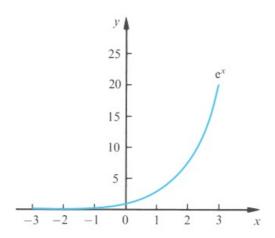
The most common exponential expression is  $e^x$ , where e is the constant 2.71828.... Also known as "Euler's number". This number is found in many natural phenomena.

## 2. Exponential Functions

An exponential function has the form of  $y=e^x$  . This function has important properties:

- y is never negative.
- When x=0, then y=1
- As *x* increases, then *y* increases (**exponential growth**).





## 3. Logarithms

The logarithm is the inverse function to the exponentiation. The following two equations are equivalent.

$$y = a^x \Leftrightarrow \log_a(y) = x$$

For example:

$$5^3 = 125 \Leftrightarrow \log_5(125) = 3$$

Also, conventionally we define  ${f natural\ logarithms}$  as:

$$\log = \log_{10}$$

$$ln = log_e$$

## 3.1. Calculating Logarithms to any Base

$$\log_a X = \frac{\log_{10} X}{\log_{10} a}$$

$$\log_a X = \frac{\ln X}{\ln a}$$

This also means that - for example:

$$\log_5(125) = \frac{\log(125)}{\log(5)}$$

Additionally:

$$\log_a a = 1$$

3.2. Laws

First Law:

 $\log A + \log B = \log AB$ 

Second Law:

$$\log A - \log B = \log \left(\frac{A}{B}\right)$$

Also note that:

$$log 1 = 0$$

Third Law

$$n \log A = \log A^n$$

such as  $3\log 2 = \log 2^3 = \log 8$ . This applies for all  $n\in\mathbb{R}$ .

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