Cheatsheet - Trigonometry

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1. Intro

If B=90, then AC is called the **hypotenuse**, the side **opposite** of θ is BC and the remaining side, AB, is **adjacent** to θ . Angle A is written as $\angle BAC$, $\angle A$ or just A.

Each side of a triangle is named based on the lowercase letter of the angle opposite of the side.

$$a = BC$$

$$b = AC$$

$$c = AB$$

The total degree of all angles is always 180°

$$A + B + C = 180^{\circ}$$

2. Convert Degree to Radiant

$$360^{\circ} = 2\pi \text{ rads}$$

To convert x degrees to radians y:

$$x \cdot \frac{\pi}{180} = y$$

For example, $255\degree$:

$$225 \cdot \frac{\pi}{180} \approx 3.93 \text{ rads}$$

And in reverse:

$$3.93 \cdot \frac{180}{\pi} \approx 225^{\circ}$$

3. Trigonometrical Ratios

Sinus, cosine and tangent are trigonometric functions that can be applied to right-angled triangles to determine the degree of an angle. The degree of an angle is independent from the length of each side.

$$\sin \theta = \frac{\text{side opposite to} \ \ \theta}{\text{hypotenuse}} = \frac{\text{BC}}{\text{AC}}$$

$$\cos \theta = rac{ ext{side adjacent to} \ \ heta}{ ext{hypotenuse}} = rac{ ext{AB}}{ ext{AC}}$$

$$\tan \theta = \frac{\text{side opposite to} \ \ \theta}{\text{side adjacent to} \ \ \theta} = \frac{\text{BC}}{\text{AB}}$$

Sinus and cosine are always less than one.

$$\sin x \leq 1$$

$$\cos x \leq 1$$

The ratio of an angle can be reversed.

$$\sin 45^{\circ} = 0.70710678$$

$$\sin^{-1} 0.70710678 = 45^{\circ}$$

4. Pythagoras, Sinus and Cosine Rule

For any right-angled triangle, the following theorem applies:

$$a^2 + b^2 = c^2$$

$$\sqrt{a^2 + b^2} = c$$

 $where \ c \ is the \ hypotenuse. For \ any \ right-angled, \ acute \ and \ obtuse \ (non \ right-angled) \ triangles, \ the \ sinus \ and \ cosine \ rules \ apply:$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

and:

. . .

$$a2 = b2 + c2 - 2bc cos A$$
$$b2 = a2 + c2 - 2ac cos B$$
$$c2 = a2 + b2 - 2ab cos C$$

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