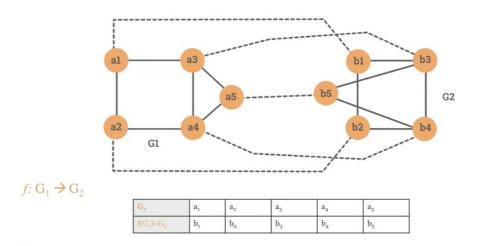
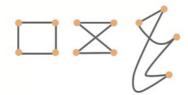
1. Definition

Two graphs G_1 and G_2 are isomorphic if there is a bijection (invertible function) $f:G_1\to G_2$ that preserves adjacency and non-adjacency. Given two vertices u and v, if $u\times v$ is in $E(G_1)$ then $f(u)\times f(v)$ is in $E(G_2)$.



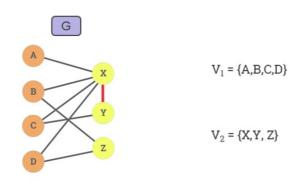
Two graphs with different degree sequences cannot be isomorphic. Two graphs with the same degree sequence are not necessarily isomorphic.



Isomorphic graphs

2. Bipartite Graph

A graph G(V, E) is called a bi-partite graph if the set of vertices V can be partitioned in two non-empty disjoint sets V_1 and V_2 in such a way that each edge e in G has one endpoint in V_1 and another endpoint in V_2 .



The graph is 2-colourable

No odd-length cycles

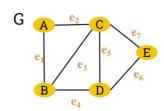
2.1. Matching

A matching is a set of pairwise non-adjacent edges, none of which are loops. That is, no two edges share a common endpoint. A vertex is matched (or saturated) if it is an endpoint of one of the edges in the matching. Otherwise the vertex is unmatched.

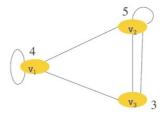
A **maximum** matching is a matching of maximum size such that if any edge is added, it is no longer a matching. The **Hopcroft-Karp algorithm** is commonly used for solving the maximum matching problem in a bipartite graph (*the algorithm is not specified in this cheatsheet*).

3. Adjacency Matrix of Graph

The adjacency list of a graph G is a list of all the vertices in G and their corresponding individual adjacent vertices.



A graph can also be represented by its **adjacency matrix**. The number of edges in an **undirected** graph is equal to half the sum of all the elements (m_{ij}) of it's corresponding adjacency matrix.



$$M(G) = \begin{bmatrix} v_1 & v_1 & v_2 & v_3 \\ v_1 & 2 & 1 & 1 \\ 1 & 2 & 2 \\ v_3 & 1 & 2 & 0 \end{bmatrix}$$

$$\sum m_{ii} = 1+1+1+1+2+2+2+2=5+4+3=12$$

Number of edges in G =
$$(\sum m_{ij})/2 = 12/2 = 6$$

TODO: Adjacency matrix of a digraph

TODO: Dijkstra's algorithm

Last updated 2023-01-12 14:11:06 UTC