GEOPHYSICAL TUTORIAL

EULER DECONVOLUTION OF POTENTIAL-FIELD DATA

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In this tutorial, we will talk about a widely used method of interpretation for potential-field data called Euler deconvolution. Our goal is to demonstrate its usefulness and, most important, to call attention to some pitfalls encountered in interpretation of the results. The code and synthetic data required to reproduce our results and figures can be found in the accompanying IPython notebooks (ipython.org/notebook) at dx.doi.org/10.6084/m9.figshare.923450 or github.com/pinga-lab/paper-tle-euler-tutorial. The notebooks also expand the analysis presented here. We encourage you to download the data and try them on your software of choice. For this tutorial, we will use the implementation in the open-source Python package Fatiando a Terra (fatiando.org).

Brief overview

Euler deconvolution was developed first by Thompson (1982) and later extended by Reid et al. (1990). Since then, it has been adapted and improved by Keating (1998), Mushayandebvu et al. (2004), and many others. The popularity of Euler deconvolution is largely because of its great simplicity of implementation and use, making it the tool of choice for a quick initial interpretation.

In many cases, maps of gravity and magnetic data (and transformations thereof) provide good constraints on the horizontal location of an anomaly source. Euler deconvolution adds an extra dimension to the interpretation. It estimates a set of (x, y, z) points that ideally fall inside the source of the anomaly. Euler deconvolution requires the x-, y-, and z-derivatives of the data and a parameter called the *structural index* (SI).

The SI, which is an integer number related to the homogeneity of the potential field, varies for different fields and source types (Stavrev and Reid, 2007). For example, in the case of total-field magnetic-anomaly data, a sphere is represented by an SI of 3, whereas a dike is represented by an SI of 1. There are methods that can estimate the SI, and we refer the reader to Barbosa et al. (1999) and to Melo et al. (2013) for more information.

An example with synthetic data

The best way to fully grasp the usefulness and limitations of any geophysical method is to apply it in a controlled setting using synthetic data. To make things more interesting, we will apply the Euler deconvolution to data generated by a model that differs slightly from ideal sources (Figure 1).

First we need to calculate the three directional derivatives of the data. For gridded data, this can be done with the fourier transform using module fourier from Fatiando a Terra. Assuming that the data have been loaded into NumPy arrays x, y, z with the respective x-, y-, z-coordinates of each data point and the array data with our magnetic data (see the accompanying notebook):

```
from fatiando.gravmag import fourier
from fatiando import utils
# Need data in SI units
data_si = utils.nt2si(data)
# shape = (ny, nx) number of points in y and x
dx = fourier.derivx(x, y, data_si, shape)
dy = fourier.derivy(x, y, data_si, shape)
dz = fourier.derivz(x, y, data_si, shape)
```

Now that we have calculated the derivatives, we have to create a solver to run the deconvolution. Fatiando provides the Classic solver, which uses the whole data set to estimate a single point (source location). The usual strategy for multiple sources, introduced by Reid et al. (1990), is to use a *moving window* over the data. A point is estimated for each window using the data that fall inside it, producing a large number of solutions. The challenge then becomes separating the good solutions from the spurious ones.

FitzGerald et al. (2004) provide an overview of different selection criteria. Fatiando provides the MovingWindow solver, which can run a given Euler solver on a moving window (see the accompanying notebook for more details on the selection criterion used):

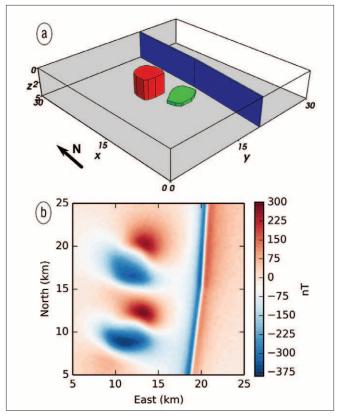


Figure 1. (a) Our model. The model simulates a dike (blue), a sill (green), and an intrusive body (red). (b) Synthetic total-field anomaly data. Data are corrupted with 5-nT pseudo-random Gaussian noise.

from fatiando.gravmag.euler\ import Classic, MovingWindow classic = Classic(x, y, z,data si, dx, dy, dz, struct index) solver = MovingWindow(classic, windows = (50, 50), size = (1000, 50)1000)); solver.fit()

Calling solver. fit () runs the deconvolution using the specified 50-x-50 windows of 1-km size. The estimated points are stored in the solver. estimate_variable.

For comparison, we ran the deconvolution using various combinations of structural index and window size. Figure 2 shows scatter plots of the solutions (the typical way Euler solutions are presented). Notice how changing the window size influences the spread of the solutions and can affect interpretation. For example, for a 1-km window and structural index of 3, we cannot tell apart the two

model bodies in the left. Furthermore, increasing the structural index will increase the depths of the solutions.

We can view these solutions in three dimensions using the Fatiando module myv, a wrapper for the Mayavi visualization software (code.enthought.com/projects/mayavi):

```
from fatiando.vis import myv
myv.figure(); myv.points(solver.estimate )
myv.axes(myv.outline(model bounds)); myv.show()
```

This will create something similar to the image in Figure 3. Notice that the Euler solutions do fall approximately inside the sources. However, it is curious how the solutions make archlike structures that have no relation to the actual forms of the sources. In fact, Silva et al. (2001) show that Euler solutions are biased and that the bias depends on the movingwindow scheme and selection criterion used.

Last few words of caution

We repeat this here for emphasis: Euler deconvolution solutions do not represent the 3D outline of the sources. At most, they indicate an approximate source location. It is crucial to remember that Euler solutions are subject to nonuniqueness and bias just like any other geophysical inverse problem. Tests using synthetic data are indispensable to assert the plausibility of our interpretations. **TLE**

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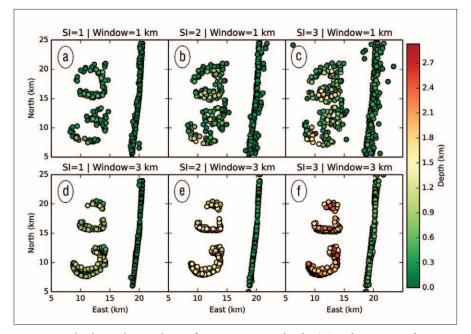


Figure 2. Euler deconvolution solutions for varying structural index (SI) and moving-window size.

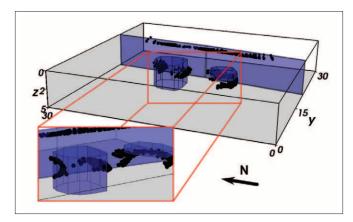


Figure 3. 3D view of Euler deconvolution solutions (black dots) for a moving window of 3 km and structural index of 3.

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