```
LinksPlatform's Platform Collections Methods Class Library
     ./csharp/Platform.Collections.Methods/GenericCollectionMethodsBase.cs
   using System.Collections.Generic;
using System.Runtime.CompilerServices;
2
   using Platform. Numbers;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
5
   namespace Platform.Collections.Methods
8
        /// <summary>
9
       /// <para>Represents the basic system of methods for a collection of elements of type
10
            TElement.</para>
        /// <para>Представляет базовую реализацию методов коллекции элементов типа TElement.</para>
       /// </summary>
12
       public abstract class GenericCollectionMethodsBase<TElement>
13
14
            /// <summary>
15
            /// <para>Presents the Range in readable format.</para>
16
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
17
            /// </summary>
18
            /// <returns><para>String representation of the Range.</para><para>Строковое
19
            → представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual TElement GetZero() => default;
21
22
            /// <summary>
23
            /// <para>Presents the Range in readable format.</para>
24
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
25
            /// </summary>
            /// <returns><para>String representation of the Range.</para><para>Строковое
27
               представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
28
            protected virtual bool EqualToZero(TElement value) => EqualityComparer.Equals(value,
29

→ Zero);

30
            /// <summary>
31
            /// <para>Presents the Range in readable format.</para>
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
33
            /// </summary>
34
            /// <returns><para>String representation of the Range.</para><para>Строковое
35
               представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
36
            protected virtual bool AreEqual(TElement first, TElement second) =>
37

→ EqualityComparer.Equals(first, second);

            /// <summary>
39
            /// <para>Presents the Range in readable format.</para>
40
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
41
            /// </summary>
            /// <returns><para>String representation of the Range.</para><para>Строковое
43
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
44
            protected virtual bool GreaterThanZero(TElement value) => Comparer.Compare(value, Zero)
45
            \rightarrow > 0;
46
            /// <summary>
            /// <para>Presents the Range in readable format.</para>
48
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
49
            /// </summary>
50
            /// <returns><para>String representation of the Range.</para><para>Строковое
               представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
52
            protected virtual bool GreaterThan(TElement first, TElement second) =>
53
               Comparer.Compare(first, second) > 0;
            /// <summary>
5.5
            /// <para>Presents the Range in readable format.</para>
56
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
            /// </summary>
58
            /// <returns><para>String representation of the Range.</para><para>Строковое
59
               представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool GreaterOrEqualThanZero(TElement value) => Comparer.Compare(value,
               Zero) \geq 0;
62
            /// <summary>
```

```
/// <para>Presents the Range in readable format.</para>
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
            /// </summary>
            /// <returns><para>String representation of the Range.</para><para>Строковое
               представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool GreaterOrEqualThan(TElement first, TElement second) =>
               Comparer.Compare(first, second) >= 0;
70
            /// <summary>
            /// <para>Presents the Range in readable format.</para>
72
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
73
            /// </summary>
            /// <returns><para>String representation of the Range.</para><para>Строковое
            → представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
76
            protected virtual bool LessOrEqualThanZero(TElement value) => Comparer.Compare(value,

    Zero) <= 0;
</pre>
            /// <summary>
79
            /// <para>Presents the Range in readable format.</para>
80
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
            /// </summary>
82
            /// <returns><para>String representation of the Range.</para><para>Строковое
83
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool LessOrEqualThan(TElement first, TElement second) =>

→ Comparer.Compare(first, second) <= 0;
</p>
86
            /// <summary>
            /// <para>Presents the Range in readable format.</para>
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
89
            /// </summary>
90
            /// <returns><para>String representation of the Range.</para>Строковое
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
92
            protected virtual bool LessThanZero(TElement value) => Comparer.Compare(value, Zero) < 0;
93
94
            /// <summarv>
95
            /// <para>Presents the Range in readable format.</para>
96
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
            /// </summary>
            /// <returns><para>String representation of the Range.</para><para>Строковое
99
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
100
            protected virtual bool LessThan(TElement first, TElement second) =>

→ Comparer.Compare(first, second) < 0;
</p>
102
            /// <summary>
103
            /// <para>Presents the Range in readable format.</para>
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
105
            /// </summary>
106
            /// <returns><para>String representation of the Range.</para>Строковое
               представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
108
            protected virtual TElement Increment(TElement value) =>
109
               Arithmetic<TElement>.Increment(value);
110
            /// <summarv>
111
            /// <para>Presents the Range in readable format.</para>
112
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
            /// </summary>
114
            /// <returns><para>String representation of the Range.</para><para>Строковое
115
               представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
116
            protected virtual TElement Decrement(TElement value) =>
             → Arithmetic<TElement>.Decrement(value);
118
            /// <summary>
            /// <para>Presents the Range in readable format.</para>
120
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
121
            /// </summary>
122
            /// <returns><para>String representation of the Range.</para><para>Строковое
                представление диапазона.</para></returns>
124
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual TElement Add(TElement first, TElement second) =>
125
            → Arithmetic<TElement>.Add(first, second);
```

```
126
             /// <summary>
             /// <para>Presents the Range in readable format.</para>
128
             /// <para>Представляет диапазон в удобном для чтения формате.</para>
129
             /// </summary>
             /// <returns><para>String representation of the Range.</para><para>Строковое
             \hookrightarrow представление диапазона.</para></returns>
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
132
            protected virtual TElement Subtract(TElement first, TElement second) =>
133
                Arithmetic<TElement>.Subtract(first, second);
134
             /// <summary>
135
             /// <para>Returns minimum value of the range.</para>
136
             /// <para>Возвращает минимальное значение диапазона.</para>
             /// </summary>
138
139
            protected readonly TElement Zero;
140
             /// <summarv>
141
             /// <para>Returns minimum value of the range.</para>
142
             /// <para>Возвращает минимальное значение диапазона.</para>
143
             /// </summary>
144
            protected readonly TElement One;
145
              /// <summary>
147
             /// <para>Returns minimum value of the range.</para>
148
149
             /// <para>Возвращает минимальное значение диапазона.</para>
             /// </summary>
150
            protected readonly TElement Two;
151
152
             /// <summary>
153
             /// <para>Returns minimum value of the range.</para>
154
             /// <para>Возвращает минимальное значение диапазона.</para>
155
             /// <\bracessummary>
156
            protected readonly EqualityComparer<TElement> EqualityComparer;
158
             /// <summary>
             /// <para>Returns minimum value of the range.</para>
160
             /// <para>Возвращает минимальное значение диапазона.</para>
161
             /// </summary>
162
            protected readonly Comparer<TElement> Comparer;
163
164
             /// <summary>
165
             /// <para>Presents the Range in readable format.</para>
166
             /// <para>Представляет диапазон в удобном для чтения формате.</para>
             /// </summary>
168
             /// <returns><para>String representation of the Range.</para><para>Строковое
169
             → представление диапазона.</para></returns>
            protected GenericCollectionMethodsBase()
170
                 EqualityComparer = EqualityComparer<TElement>.Default;
172
                 Comparer = Comparer<TElement>.Default;
173
                 Zero = GetZero(); //-V3068
174
                 One = Increment(Zero); //-V3068
Two = Increment(One); //-V3068
175
176
             }
177
        }
178
1.2
     ./csharp/Platform. Collections. Methods/Lists/Absolute Circular Doubly Linked List Methods. cs
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
 1
    namespace Platform.Collections.Methods.Lists
 3
    {
        public abstract class AbsoluteCircularDoublyLinkedListMethods<TElement> :
 5
            AbsoluteDoublyLinkedListMethodsBase<TElement>
             public void AttachBefore(TElement baseElement, TElement newElement)
                 var baseElementPrevious = GetPrevious(baseElement);
                 SetPrevious(newElement, baseElementPrevious);
10
                 SetNext(newElement, baseElement);
1.1
                 if (AreEqual(baseElement, GetFirst()))
12
                 {
13
                     SetFirst(newElement);
14
15
                 SetNext(baseElementPrevious, newElement);
16
                 SetPrevious(baseElement, newElement);
                 IncrementSize();
18
```

}

```
20
            public void AttachAfter(TElement baseElement, TElement newElement)
22
                 var baseElementNext = GetNext(baseElement);
23
                 SetPrevious(newElement, baseElement);
                 SetNext(newElement, baseElementNext);
25
                 if (AreEqual(baseElement, GetLast()))
26
27
                 {
                     SetLast(newElement);
29
                 SetPrevious(baseElementNext, newElement);
30
                 SetNext(baseElement, newElement);
                 IncrementSize();
32
            }
33
34
            public void AttachAsFirst(TElement element)
35
36
                 var first = GetFirst();
                 if (EqualToZero(first))
38
39
                     SetFirst(element);
40
                     SetLast(element);
41
                     SetPrevious(element, element);
42
                     SetNext(element, element);
43
                     IncrementSize();
                 }
45
                 else
46
                 {
47
                     AttachBefore(first, element);
48
                 }
49
            }
51
52
            public void AttachAsLast(TElement element)
53
                 var last = GetLast();
54
                 if (EqualToZero(last))
55
                 {
                     AttachAsFirst(element);
57
                 }
58
                 else
5.9
                 {
60
                     AttachAfter(last, element);
61
            }
63
            public void Detach(TElement element)
65
66
                 var elementPrevious = GetPrevious(element);
                 var elementNext = GetNext(element);
                 if (AreEqual(elementNext, element))
69
70
                     SetFirst(Zero);
                     SetLast(Zero);
72
                 }
73
                 else
74
7.5
                     SetNext(elementPrevious, elementNext);
76
                     SetPrevious(elementNext, elementPrevious);
77
                     if (AreEqual(element, GetFirst()))
78
                     {
79
                         SetFirst(elementNext);
                     }
81
                     if (AreEqual(element, GetLast()))
82
83
                         SetLast(elementPrevious);
                     }
85
86
                 SetPrevious(element, Zero);
                 SetNext(element, Zero);
88
                 DecrementSize();
89
            }
90
        }
91
   }
92
```

1.3 ./csharp/Platform.Collections.Methods/Lists/AbsoluteDoublyLinkedListMethodsBase.cs
 using System.Runtime.CompilerServices;
 #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member

```
namespace Platform.Collections.Methods.Lists
5
6
       public abstract class AbsoluteDoublyLinkedListMethodsBase<TElement> :
7
           DoublyLinkedListMethodsBase<TElement>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetFirst();
10
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
12
            protected abstract TElement GetLast();
13
14
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
15
            protected abstract TElement GetSize();
16
17
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
            protected abstract void SetFirst(TElement element);
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract void SetLast(TElement element);
22
23
24
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract void SetSize(TElement size);
25
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
27
            protected void IncrementSize() => SetSize(Increment(GetSize()));
28
29
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
30
            protected void DecrementSize() => SetSize(Decrement(GetSize()));
31
        }
   }
33
1.4
     ./csharp/Platform.Collections.Methods/Lists/AbsoluteOpenDoublyLinkedListMethods.cs
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
-1
2
3
   namespace Platform.Collections.Methods.Lists
4
       public abstract class AbsoluteOpenDoublyLinkedListMethods<TElement> :
5
           AbsoluteDoublyLinkedListMethodsBase<TElement>
6
            public void AttachBefore(TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
10
                SetNext(newElement, baseElement);
                if (EqualToZero(baseElementPrevious))
                {
13
                    SetFirst(newElement);
14
                }
15
                else
16
17
                    SetNext(baseElementPrevious, newElement);
19
                SetPrevious(baseElement, newElement);
20
                IncrementSize();
            }
22
            public void AttachAfter(TElement baseElement, TElement newElement)
24
25
                var baseElementNext = GetNext(baseElement);
26
                SetPrevious(newElement, baseElement);
27
                SetNext(newElement, baseElementNext);
2.8
                if (EqualToZero(baseElementNext))
29
31
                    SetLast(newElement);
                }
32
                else
33
                {
34
                    SetPrevious(baseElementNext, newElement);
35
                SetNext(baseElement, newElement);
37
                IncrementSize();
38
            }
39
40
            public void AttachAsFirst(TElement element)
41
                var first = GetFirst();
43
                if (EqualToZero(first))
44
```

```
SetFirst(element);
46
                     SetLast(element);
                     SetPrevious(element, Zero);
48
                     SetNext(element, Zero);
49
                     IncrementSize();
                }
5.1
                else
52
53
                     AttachBefore(first, element);
54
                }
55
            }
56
57
            public void AttachAsLast(TElement element)
58
59
                var last = GetLast();
60
                if (EqualToZero(last))
61
                     AttachAsFirst(element);
63
                }
64
                else
65
                {
66
                     AttachAfter(last, element);
67
                }
            }
69
70
            public void Detach(TElement element)
7.1
72
                var elementPrevious = GetPrevious(element);
73
                var elementNext = GetNext(element);
                if (EqualToZero(elementPrevious))
7.5
76
                     SetFirst(elementNext);
77
                }
78
                else
79
                {
80
                     SetNext(elementPrevious, elementNext);
81
                }
82
                if (EqualToZero(elementNext))
83
                {
84
                     SetLast(elementPrevious);
85
                }
86
                else
87
                {
88
                     SetPrevious(elementNext, elementPrevious);
89
90
                SetPrevious(element, Zero);
91
                SetNext(element, Zero);
                DecrementSize();
93
            }
94
        }
95
   }
96
     ./csharp/Platform.Collections.Methods/Lists/DoublyLinkedListMethodsBase.cs
1.5
   using System.Runtime.CompilerServices;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
3
   namespace Platform.Collections.Methods.Lists
5
        /// <remarks>
        /// Based on <a href="https://en.wikipedia.org/wiki/Doubly_linked_list">doubly linked
        → list</a> implementation.
/// </remarks>
        public abstract class DoublyLinkedListMethodsBase<TElement> :
10
            GenericCollectionMethodsBase<TElement>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
12
            protected abstract TElement GetPrevious(TElement element);
13
14
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
15
            protected abstract TElement GetNext(TElement element);
16
17
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
            protected abstract void SetPrevious(TElement element, TElement previous);
20
21
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract void SetNext(TElement element, TElement next);
22
        }
23
   }
```

```
./csharp/Platform.Collections.Methods/Lists/RelativeCircularDoublyLinkedListMethods.cs
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
   {
4
       public abstract class RelativeCircularDoublyLinkedListMethods<TElement> :
5
           RelativeDoublyLinkedListMethodsBase<TElement>
6
            public void AttachBefore(TElement headElement, TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
10
                SetNext(newElement, baseElement);
11
12
                if (AreEqual(baseElement, GetFirst(headElement)))
                {
13
                    SetFirst(headElement, newElement);
14
                SetNext(baseElementPrevious, newElement);
                SetPrevious(baseElement, newElement);
17
                IncrementSize(headElement);
18
            }
20
            public void AttachAfter(TElement headElement, TElement baseElement, TElement newElement)
22
                var baseElementNext = GetNext(baseElement);
23
                SetPrevious(newElement, baseElement);
24
                SetNext(newElement, baseElementNext);
25
                if (AreEqual(baseElement, GetLast(headElement)))
26
                {
27
                    SetLast(headElement, newElement);
29
                SetPrevious(baseElementNext, newElement);
30
31
                SetNext(baseElement, newElement);
32
                IncrementSize(headElement);
33
            public void AttachAsFirst(TElement headElement, TElement element)
35
36
                var first = GetFirst(headElement);
                if (EqualToZero(first))
38
39
                    SetFirst(headElement, element);
40
                    SetLast(headElement, element);
42
                    SetPrevious(element, element);
                    SetNext(element, element);
43
                    IncrementSize(headElement);
44
                }
45
                else
46
                {
47
                    AttachBefore(headElement, first, element);
48
                }
49
            }
5.1
            public void AttachAsLast(TElement headElement, TElement element)
                var last = GetLast(headElement);
54
                if (EqualToZero(last))
55
                    AttachAsFirst(headElement, element);
57
                }
58
                else
59
                {
60
                    AttachAfter(headElement, last, element);
61
                }
62
            }
63
            public void Detach(TElement headElement, TElement element)
65
66
                var elementPrevious = GetPrevious(element);
67
                var elementNext = GetNext(element);
                if (AreEqual(elementNext, element))
69
7.0
                    SetFirst(headElement, Zero);
                    SetLast(headElement, Zero);
72
7.3
                else
74
75
                    SetNext(elementPrevious, elementNext);
76
```

```
SetPrevious(elementNext, elementPrevious);
                    if (AreEqual(element, GetFirst(headElement)))
79
                        SetFirst(headElement, elementNext);
80
                    }
                       (AreEqual(element, GetLast(headElement)))
82
83
                        SetLast(headElement, elementPrevious);
84
86
                SetPrevious(element, Zero);
87
                SetNext(element, Zero);
                DecrementSize(headElement);
89
            }
90
       }
91
92
   }
1.7
     ./csharp/Platform. Collections. Methods/Lists/Relative Doubly Linked List Methods Base.cs
   using System.Runtime.CompilerServices;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
3
   namespace Platform.Collections.Methods.Lists
5
6
       public abstract class RelativeDoublyLinkedListMethodsBase<TElement> :
           DoublyLinkedListMethodsBase<TElement>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetFirst(TElement headElement);
10
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
12
            protected abstract TElement GetLast(TElement headElement);
14
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetSize(TElement headElement);
16
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
            protected abstract void SetFirst(TElement headElement, TElement element);
19
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
2.1
            protected abstract void SetLast(TElement headElement, TElement element);
22
23
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
^{24}
            protected abstract void SetSize(TElement headElement, TElement size);
25
26
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected void IncrementSize(TElement headElement) => SetSize(headElement,
            → Increment(GetSize(headElement)));
29
30
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected void DecrementSize(TElement headElement) => SetSize(headElement,
31
            → Decrement(GetSize(headElement)));
       }
32
   }
33
     ./csharp/Platform. Collections. Methods/Lists/Relative Open Doubly Linked List Methods. cs
1.8
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
2
   namespace Platform.Collections.Methods.Lists
3
   {
4
       public abstract class RelativeOpenDoublyLinkedListMethods<TElement> :
5
           RelativeDoublyLinkedListMethodsBase<TElement>
            public void AttachBefore(TElement headElement, TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
10
                SetNext(newElement, baseElement);
11
                if (EqualToZero(baseElementPrevious))
12
                {
13
                    SetFirst(headElement, newElement);
                }
15
16
                else
                {
17
                    SetNext(baseElementPrevious, newElement);
18
19
                SetPrevious(baseElement, newElement);
20
                IncrementSize(headElement);
```

```
22
23
            public void AttachAfter(TElement headElement, TElement baseElement, TElement newElement)
2.4
                 var baseElementNext = GetNext(baseElement);
26
                 SetPrevious(newElement, baseElement);
27
                 SetNext(newElement, baseElementNext);
28
                 if (EqualToZero(baseElementNext))
29
30
                     SetLast(headElement, newElement);
31
                 }
                 else
33
                 {
34
                     SetPrevious(baseElementNext, newElement);
36
                 SetNext(baseElement, newElement);
37
                 IncrementSize(headElement);
             }
39
40
            public void AttachAsFirst(TElement headElement, TElement element)
41
42
                 var first = GetFirst(headElement);
43
                 if (EqualToZero(first))
                 {
45
                     SetFirst(headElement, element);
46
                     SetLast(headElement, element);
SetPrevious(element, Zero);
47
                     SetNext(element, Zero);
49
                     IncrementSize(headElement);
50
                 }
                 else
52
53
                     AttachBefore(headElement, first, element);
54
                 }
55
            }
57
            public void AttachAsLast(TElement headElement, TElement element)
58
                 var last = GetLast(headElement);
60
                 if (EqualToZero(last))
61
62
63
                     AttachAsFirst(headElement, element);
                 }
64
                 else
                 {
66
                     AttachAfter(headElement, last, element);
67
                 }
            }
70
            public void Detach(TElement headElement, TElement element)
71
72
                 var elementPrevious = GetPrevious(element);
73
                 var elementNext = GetNext(element);
                 if (EqualToZero(elementPrevious))
7.5
76
                     SetFirst(headElement, elementNext);
77
                 }
78
                 else
79
                 {
                     SetNext(elementPrevious, elementNext);
81
82
                 if (EqualToZero(elementNext))
83
                 {
84
                     SetLast(headElement, elementPrevious);
85
                 }
86
87
                 else
                 {
88
                     SetPrevious(elementNext, elementPrevious);
89
90
                 SetPrevious(element, Zero);
91
                 SetNext(element, Zero);
92
                 DecrementSize(headElement);
93
            }
94
        }
95
96
```

1.9 ./csharp/Platform.Collections.Methods/Trees/RecursionlessSizeBalancedTreeMethods.cs

1 #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member

```
namespace Platform.Collections.Methods.Trees
    public abstract class RecursionlessSizeBalancedTreeMethods<TElement> :
       SizedBinaryTreeMethodsBase<TElement>
        protected override void AttachCore(ref TElement root, TElement node)
            while (true)
            {
                ref var left = ref GetLeftReference(root);
                var leftSize = GetSizeOrZero(left);
                ref var right = ref GetRightReference(root);
                var rightSize = GetSizeOrZero(right);
                if (FirstIsToTheLeftOfSecond(node, root)) // node.Key less than root.Key
                    if (EqualToZero(left))
                    {
                        IncrementSize(root);
                        SetSize(node, One);
                        left = node;
                        return:
                    if (FirstIsToTheLeftOfSecond(node, left)) // node.Key less than left.Key
                        if (GreaterThan(Increment(leftSize), rightSize))
                             RightRotate(ref root);
                        }
                        else
                         {
                             IncrementSize(root);
                             root = ref left;
                          // node.Key greater than left.Key
                    else
                        var leftRightSize = GetSizeOrZero(GetRight(left));
                        if (GreaterThan(Increment(leftRightSize), rightSize))
                             if (EqualToZero(leftRightSize) && EqualToZero(rightSize))
                                 SetLeft(node, left);
                                 SetRight(node, root)
                                 SetSize(node, Add(leftSize, Two)); // Two (2) - node the size of

→ root and a node itself

                                 SetLeft(root, Zero);
                                 SetSize(root, One);
                                 root = node;
                                 return;
                             LeftRotate(ref left);
                             RightRotate(ref root);
                        }
                        else
                             IncrementSize(root);
                             root = ref left;
                        }
                    }
                else // node.Key greater than root.Key
                    if (EqualToZero(right))
                    {
                        IncrementSize(root);
                        SetSize(node, One);
                        right = node;
                        return:
                    if (FirstIsToTheRightOfSecond(node, right)) // node.Key greater than
                        right.Key
                        if (GreaterThan(Increment(rightSize), leftSize))
                        {
                            LeftRotate(ref root);
                        }
                        else
                             IncrementSize(root);
```

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7.1

72

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74

75

```
root = ref right;
                }
            }
            else // node.Key less than right.Key
                var rightLeftSize = GetSizeOrZero(GetLeft(right));
                if (GreaterThan(Increment(rightLeftSize), leftSize))
                     if (EqualToZero(rightLeftSize) && EqualToZero(leftSize))
                         SetLeft(node, root);
                         SetRight(node, right);
                         SetSize(node, Add(rightSize, Two)); // Two (2) - node the size
                         \hookrightarrow of root and a node itself
                         SetRight(root, Zero);
                         SetSize(root, One);
                         root = node;
                         return;
                    RightRotate(ref right);
                    LeftRotate(ref root);
                }
                else
                {
                    IncrementSize(root);
                    root = ref right;
                }
            }
        }
    }
protected override void DetachCore(ref TElement root, TElement node)
    while (true)
        ref var left = ref GetLeftReference(root);
        var leftSize = GetSizeOrZero(left);
        ref var right = ref GetRightReference(root);
        var rightSize = GetSizeOrZero(right);
        if (FirstIsToTheLeftOfSecond(node, root)) // node.Key less than root.Key
            var decrementedLeftSize = Decrement(leftSize);
               (GreaterThan(GetSizeOrZero(GetRightOrDefault(right)),
            if
                decrementedLeftSize))
                LeftRotate(ref root);
            }
            else if (GreaterThan(GetSizeOrZero(GetLeftOrDefault(right)),
                decrementedLeftSize))
            {
                RightRotate(ref right);
                LeftRotate(ref root);
            }
            else
            {
                DecrementSize(root);
                root = ref left;
        else if (FirstIsToTheRightOfSecond(node, root)) // node.Key greater than root.Key
            var decrementedRightSize = Decrement(rightSize);
            if (GreaterThan(GetSizeOrZero(GetLeftOrDefault(left)), decrementedRightSize))
                RightRotate(ref root);
            }
            else if (GreaterThan(GetSizeOrZero(GetRightOrDefault(left)),
                decrementedRightSize))
            {
                LeftRotate(ref left);
                RightRotate(ref root);
            else
            {
                DecrementSize(root);
                root = ref right;
```

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146 147 148

149

150

```
153
                      else // key equals to root.Key
155
                          if (GreaterThanZero(leftSize) && GreaterThanZero(rightSize))
156
                              TElement replacement;
158
                              if (GreaterThan(leftSize, rightSize))
159
160
                                   replacement = GetRightest(left);
161
                                   DetachCore(ref left, replacement);
162
                              }
163
                              else
164
165
                              {
166
                                   replacement = GetLeftest(right);
                                   DetachCore(ref right, replacement);
167
168
                              SetLeft(replacement, left);
                              SetRight(replacement, right);
170
                              SetSize(replacement, Add(leftSize, rightSize));
171
172
                              root = replacement;
173
                          else if (GreaterThanZero(leftSize))
174
                              root = left;
176
177
                          else if (GreaterThanZero(rightSize))
178
                          {
179
                              root = right;
                          }
181
                          else
182
                          {
183
                              root = Zero;
                          ClearNode(node);
186
187
                          return;
                     }
188
                 }
189
             }
        }
191
192
      ./csharp/Platform.Collections.Methods/Trees/SizeBalancedTreeMethods.cs
1.10
    using System;
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
    namespace Platform.Collections.Methods.Trees
 5
 6
        public abstract class SizeBalancedTreeMethods<TElement> :
 7
            SizedBinaryTreeMethodsBase<TElement>
             protected override void AttachCore(ref TElement root, TElement node)
 9
10
                 if (EqualToZero(root))
11
12
                     root = node;
13
                      IncrementSize(root);
14
                 }
                 else
16
                      IncrementSize(root);
18
                      if (FirstIsToTheLeftOfSecond(node, root))
19
                          AttachCore(ref GetLeftReference(root), node);
21
                          LeftMaintain(ref root);
22
23
                     else
24
25
                          AttachCore(ref GetRightReference(root), node);
                          RightMaintain(ref root);
27
28
                 }
29
             }
30
31
             protected override void DetachCore(ref TElement root, TElement nodeToDetach)
33
                 ref var currentNode = ref root;
34
                 ref var parent = ref root;
35
                 var replacementNode = Zero;
```

```
while (!AreEqual(currentNode, nodeToDetach))
        DecrementSize(currentNode);
        if (FirstIsToTheLeftOfSecond(nodeToDetach, currentNode))
            parent = ref currentNode;
            currentNode = ref GetLeftReference(currentNode);
        else if (FirstIsToTheRightOfSecond(nodeToDetach, currentNode))
            parent = ref currentNode;
            currentNode = ref GetRightReference(currentNode);
        else
        {
            throw new InvalidOperationException("Duplicate link found in the tree.");
    var nodeToDetachLeft = GetLeft(nodeToDetach);
    var node = GetRight(nodeToDetach);
    if (!EqualToZero(nodeToDetachLeft) && !EqualToZero(node))
    {
        var leftestNode = GetLeftest(node);
        DetachCore(ref GetRightReference(nodeToDetach), leftestNode);
        SetLeft(leftestNode, nodeToDetachLeft);
        node = GetRight(nodeToDetach);
        if (!EqualToZero(node))
            SetRight(leftestNode, node);
            SetSize(leftestNode, Increment(Add(GetSize(nodeToDetachLeft),

   GetSize(node))));
        }
        else
            SetSize(leftestNode, Increment(GetSize(nodeToDetachLeft)));
        replacementNode = leftestNode;
    }
    else if (!EqualToZero(nodeToDetachLeft))
        replacementNode = nodeToDetachLeft;
    else if (!EqualToZero(node))
        replacementNode = node;
    if (AreEqual(root, nodeToDetach))
    {
        root = replacementNode;
    }
    else if (AreEqual(GetLeft(parent), nodeToDetach))
        SetLeft(parent, replacementNode);
    else if (AreEqual(GetRight(parent), nodeToDetach))
        SetRight(parent, replacementNode);
    ClearNode(nodeToDetach);
}
private void LeftMaintain(ref TElement root)
    if (!EqualToZero(root))
        var rootLeftNode = GetLeft(root);
        if (!EqualToZero(rootLeftNode))
            var rootRightNode = GetRight(root);
            var rootRightNodeSize = GetSize(rootRightNode);
            var rootLeftNodeLeftNode = GetLeft(rootLeftNode);
            if (!EqualToZero(rootLeftNodeLeftNode) &&
                (EqualToZero(rootRightNode) ||
                    GreaterThan(GetSize(rootLeftNodeLeftNode), rootRightNodeSize)))
            {
                RightRotate(ref root);
            else
```

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```
113
                               var rootLeftNodeRightNode = GetRight(rootLeftNode);
                              if (!EqualToZero(rootLeftNodeRightNode) &&
115
                                   (EqualToZero(rootRightNode)
116
                                      GreaterThan(GetSize(rootLeftNodeRightNode), rootRightNodeSize)))
                              {
117
                                   LeftRotate(ref GetLeftReference(root));
                                   RightRotate(ref root);
119
120
                              else
121
                              {
122
                                   return;
123
                              }
124
125
126
                          LeftMaintain(ref GetLeftReference(root));
                          RightMaintain(ref GetRightReference(root));
127
                          LeftMaintain(ref root);
128
                          RightMaintain(ref root);
129
                     }
130
                 }
131
             }
132
133
             private void RightMaintain(ref TElement root)
134
                 if (!EqualToZero(root))
136
137
                      var rootRightNode = GetRight(root);
138
139
                     if (!EqualToZero(rootRightNode))
140
                          var rootLeftNode = GetLeft(root);
141
                          var rootLeftNodeSize = GetSize(rootLeftNode);
                          var rootRightNodeRightNode = GetRight(rootRightNode);
143
                          if (!EqualToZero(rootRightNodeRightNode) &&
144
                               (EqualToZero(rootLeftNode) |
145

→ GreaterThan(GetSize(rootRightNodeRightNode), rootLeftNodeSize))))
147
                              LeftRotate(ref root);
                          }
148
                          else
149
                          {
150
                               var rootRightNodeLeftNode = GetLeft(rootRightNode);
151
                              if (!EqualToZero(rootRightNodeLeftNode) &&
152
                                   (EqualToZero(rootLeftNode) ||
153
                                      GreaterThan(GetSize(rootRightNodeLeftNode), rootLeftNodeSize)))
                              {
154
                                   RightRotate(ref GetRightReference(root));
                                  LeftRotate(ref root);
156
157
                              else
158
                              {
159
                                   return;
                              }
161
162
163
                          LeftMaintain(ref GetLeftReference(root))
                          RightMaintain(ref GetRightReference(root));
164
                          LeftMaintain(ref root)
165
                          RightMaintain(ref root);
166
                     }
167
                 }
168
             }
169
        }
170
    }
171
       ./csharp/Platform. Collections. Methods/Trees/SizedAndThreadedAVLBalancedTreeMethods.cs
1.11
    using System;
    using System.Runtime.CompilerServices;
 2
          System. Text;
    #if ŬSEARRAYPOOL
 4
    using Platform.Collections;
 5
    using Platform. Reflection;
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
10
    namespace Platform.Collections.Methods.Trees
11
12
13
         /// <summary>
        /// Combination of Size, Height (AVL), and threads.
14
        /// </summary>
15
```

```
/// <remarks>
/// Based on: <a href="https://github.com/programmatom/TreeLib/blob/master/TreeLib/TreeLib/G|
    enerated/AVLTreeList.cs">TreeLib.AVLTreeList</a>.
/// Which itself based on: <a
   href="https://github.com/GNOME/glib/blob/master/glib/gtree.c">GNOME/glib/gtree</a>.
/// </remarks>
public abstract class SizedAndThreadedAVLBalancedTreeMethods<TElement> :
   SizedBinaryTreeMethodsBase<TElement>
    private static readonly int _maxPath = 11 * NumericType<TElement>.BytesSize + 4;
    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    protected override TElement GetRightest(TElement current)
        var currentRight = GetRightOrDefault(current);
        while (!EqualToZero(currentRight))
            current = currentRight;
            currentRight = GetRightOrDefault(current);
        return current;
    }
    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    protected override TElement GetLeftest(TElement current)
        var currentLeft = GetLeftOrDefault(current);
        while (!EqualToZero(currentLeft))
            current = currentLeft;
            currentLeft = GetLeftOrDefault(current);
        return current;
    }
    public override bool Contains(TElement node, TElement root)
        while (!EqualToZero(root))
            if (FirstIsToTheLeftOfSecond(node, root)) // node.Key < root.Key</pre>
            {
                root = GetLeftOrDefault(root);
            else if (FirstIsToTheRightOfSecond(node, root)) // node.Key > root.Key
            {
                root = GetRightOrDefault(root);
            }
            else // node.Key == root.Key
                return true;
        return false;
    }
    protected override void PrintNode(TElement node, StringBuilder sb, int level)
        base.PrintNode(node, sb, level);
        sb.Append(' ');
        sb.Append(GetLeftIsChild(node) ? 'l' : 'L');
        \verb|sb.Append(GetRightIsChild(node)|? 'r' : 'R');\\
        sb.Append(' ');
        sb.Append(GetBalance(node));
    }
    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    protected void IncrementBalance(TElement node) => SetBalance(node,
       (sbyte)(GetBalance(node) + 1));
    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    protected void DecrementBalance(TElement node) => SetBalance(node,
    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    protected override TElement GetLeftOrDefault(TElement node) => GetLeftIsChild(node) ?

   GetLeft(node) : default;

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
```

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```
protected override TElement GetRightOrDefault(TElement node) => GetRightIsChild(node) ?

→ GetRight(node) : default;
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected abstract bool GetLeftIsChild(TElement node);
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected abstract void SetLeftIsChild(TElement node, bool value);
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected abstract bool GetRightIsChild(TElement node);
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected abstract void SetRightIsChild(TElement node, bool value);
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected abstract sbyte GetBalance(TElement node);
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected abstract void SetBalance(TElement node, sbyte value);
        protected override void AttachCore(ref TElement root, TElement node)
            unchecked
            {
                // TODO: Check what is faster to use simple array or array from array pool
                // TODO: Try to use stackalloc as an optimization (requires code generation,
                  because of generics)
#if USEARRAYPOOL
                var path = ArrayPool.Allocate<TElement>(MaxPath);
                var pathPosition = 0;
                path[pathPosition++] = default;
#else
                var path = new TElement[_maxPath];
                var pathPosition = 1;
#endif
                var currentNode = root;
                while (true)
                    if (FirstIsToTheLeftOfSecond(node, currentNode))
                    {
                           (GetLeftIsChild(currentNode))
                            IncrementSize(currentNode);
                            path[pathPosition++] = currentNode;
                            currentNode = GetLeft(currentNode);
                        else
                             // Threads
                            SetLeft(node, GetLeft(currentNode));
                            SetRight(node, currentNode);
                            SetLeft(currentNode, node);
                            SetLeftIsChild(currentNode, true);
                            DecrementBalance(currentNode);
                            SetSize(node, One);
                            FixSize(currentNode); // Should be incremented already
                            break:
                    else if (FirstIsToTheRightOfSecond(node, currentNode))
                        if (GetRightIsChild(currentNode))
                            IncrementSize(currentNode);
                            path[pathPosition++] = currentNode;
                            currentNode = GetRight(currentNode);
                        }
                        else
                            // Threads
                            SetRight(node, GetRight(currentNode));
                            SetLeft(node, currentNode);
                            SetRight(currentNode, node);
                            SetRightIsChild(currentNode, true);
                            IncrementBalance(currentNode);
                            SetSize(node, One);
                            FixSize(currentNode); // Should be incremented already
                            break;
```

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143 144 145

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149

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156

158

159

160 161

162

```
}
165
                           }
                           else
167
                           {
                               throw new InvalidOperationException("Node with the same key already
169
                                → attached to a tree.");
170
171
                      // Restore balance. This is the goodness of a non-recursive
172
                      // implementation, when we are done with balancing we 'break'
173
                      // the loop and we are done.
174
                      while (true)
176
                           var parent = path[--pathPosition];
177
                           var isLeftNode = !AreEqual(parent, default) && AreEqual(currentNode,
178

   GetLeft(parent));
                           var currentNodeBalance = GetBalance(currentNode);
                           if (currentNodeBalance < -1 || currentNodeBalance > 1)
180
181
                               currentNode = Balance(currentNode);
182
                               if (AreEqual(parent, default))
183
184
                                    root = currentNode;
                               }
186
                               else if (isLeftNode)
187
188
                                    SetLeft(parent, currentNode);
189
                                    FixSize(parent);
190
                               }
191
                               else
192
                               {
193
                                    SetRight(parent, currentNode);
194
                                    FixSize(parent);
195
                               }
196
197
                           currentNodeBalance = GetBalance(currentNode);
198
                           if (currentNodeBalance == 0 || AreEqual(parent, default))
199
                           {
200
                               break;
201
                           }
202
                           if (isLeftNode)
203
204
                               DecrementBalance(parent);
205
                           }
206
207
                           else
                           {
208
                               IncrementBalance(parent);
209
                           }
210
                           currentNode = parent;
211
212
    #if USEARRAYPOOL
213
214
                      ArrayPool.Free(path);
    #endif
215
                  }
216
             }
217
218
             private TElement Balance(TElement node)
219
220
                  unchecked
                  {
222
                      var rootBalance = GetBalance(node);
223
                      if (rootBalance < -1)</pre>
224
225
                           var left = GetLeft(node);
226
                           if (GetBalance(left) > 0)
227
229
                               SetLeft(node, LeftRotateWithBalance(left));
                               FixSize(node);
230
231
                          node = RightRotateWithBalance(node);
232
233
                      else if (rootBalance > 1)
234
                           var right = GetRight(node);
236
                           if (GetBalance(right) < 0)</pre>
237
238
                               SetRight(node, RightRotateWithBalance(right));
239
                               FixSize(node);
240
```

```
node = LeftRotateWithBalance(node);
        return node;
    }
}
protected TElement LeftRotateWithBalance(TElement node)
    unchecked
    {
        var right = GetRight(node);
        if (GetLeftIsChild(right))
            SetRight(node, GetLeft(right));
        else
            SetRightIsChild(node, false);
            SetLeftIsChild(right, true);
        SetLeft(right, node);
        // Fix size
        SetSize(right, GetSize(node));
        FixSize(node);
        // Fix balance
        var rootBalance = GetBalance(node);
        var rightBalance = GetBalance(right);
        if (rightBalance <= 0)</pre>
            if (rootBalance >= 1)
                SetBalance(right, (sbyte)(rightBalance - 1));
            }
            else
            {
                SetBalance(right, (sbyte)(rootBalance + rightBalance - 2));
            SetBalance(node, (sbyte)(rootBalance - 1));
        else
            if (rootBalance <= rightBalance)</pre>
                SetBalance(right, (sbyte)(rootBalance - 2));
            }
            else
            {
                SetBalance(right, (sbyte)(rightBalance - 1));
            }
            SetBalance(node, (sbyte)(rootBalance - rightBalance - 1));
        return right;
    }
}
protected TElement RightRotateWithBalance(TElement node)
    unchecked
        var left = GetLeft(node);
        if (GetRightIsChild(left))
            SetLeft(node, GetRight(left));
        }
        else
            SetLeftIsChild(node, false);
            SetRightIsChild(left, true);
        SetRight(left, node);
        // Fix size
        SetSize(left, GetSize(node));
        FixSize(node);
        // Fix balance
        var rootBalance = GetBalance(node);
        var leftBalance = GetBalance(left);
        if (leftBalance <= 0)</pre>
```

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```
319
                          if (leftBalance > rootBalance)
321
                               SetBalance(left, (sbyte)(leftBalance + 1));
322
                          }
                          else
324
                          {
325
                               SetBalance(left, (sbyte)(rootBalance + 2));
326
327
                          SetBalance(node, (sbyte)(rootBalance - leftBalance + 1));
328
                      else
330
331
332
                             (rootBalance <= -1)
                          {
333
                               SetBalance(left, (sbyte)(leftBalance + 1));
334
                          else
336
                               SetBalance(left, (sbyte)(rootBalance + leftBalance + 2));
338
339
                          SetBalance(node, (sbyte)(rootBalance + 1));
340
                      return left;
342
                 }
343
             }
344
345
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
347
             protected override TElement GetNext(TElement node)
348
                 var current = GetRight(node);
349
                 if (GetRightIsChild(node))
350
351
                      return GetLeftest(current);
353
                 return current;
354
             }
356
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected override TElement GetPrevious(TElement node)
358
359
                 var current = GetLeft(node);
360
                 if (GetLeftIsChild(node))
361
362
                      return GetRightest(current);
363
364
                 return current;
365
             }
366
367
             protected override void DetachCore(ref TElement root, TElement node)
368
                 unchecked
370
371
    #if USEARRAYPOOL
372
                      var path = ArrayPool.Allocate<TElement>(MaxPath);
373
                      var pathPosition = 0;
374
                      path[pathPosition++] = default;
375
376
    #else
                      var path = new TElement[_maxPath];
377
                      var pathPosition = 1;
378
    #endif
379
                      var currentNode = root;
380
                      while (true)
381
382
                          if (FirstIsToTheLeftOfSecond(node, currentNode))
383
384
                               if (!GetLeftIsChild(currentNode))
385
                               {
386
                                   throw new InvalidOperationException("Cannot find a node.");
387
388
389
                               DecrementSize(currentNode);
                               path[pathPosition++] = currentNode;
390
                               currentNode = GetLeft(currentNode);
391
                          else if (FirstIsToTheRightOfSecond(node, currentNode))
393
394
                               if (!GetRightIsChild(currentNode))
395
                               {
396
                                   throw new InvalidOperationException("Cannot find a node.");
397
```

```
DecrementSize(currentNode);
        path[pathPosition++] = currentNode;
        currentNode = GetRight(currentNode);
    }
    else
    {
        break;
    }
var parent = path[--pathPosition];
var balanceNode = parent;
var isLeftNode = !AreEqual(parent, default) && AreEqual(currentNode,
   GetLeft(parent));
if (!GetLeftIsChild(currentNode))
{
      (!GetRightIsChild(currentNode)) // node has no children
        if (AreEqual(parent, default))
            root = Zero;
        else if (isLeftNode)
            SetLeftIsChild(parent, false);
            SetLeft(parent, GetLeft(currentNode));
            IncrementBalance(parent);
        }
        else
        {
            SetRightIsChild(parent, false);
            SetRight(parent, GetRight(currentNode));
            DecrementBalance(parent);
    else // node has a right child
        var successor = GetNext(currentNode);
        SetLeft(successor, GetLeft(currentNode));
        var right = GetRight(currentNode);
        if (AreEqual(parent, default))
            root = right;
        else if (isLeftNode)
            SetLeft(parent, right);
            IncrementBalance(parent);
        }
        else
            SetRight(parent, right);
            DecrementBalance(parent);
    }
else // node has a left child
    if (!GetRightIsChild(currentNode))
    {
        var predecessor = GetPrevious(currentNode);
        SetRight(predecessor, GetRight(currentNode));
        var leftValue = GetLeft(currentNode);
        if (AreEqual(parent, default))
            root = leftValue;
        }
        else if (isLeftNode)
            SetLeft(parent, leftValue);
            IncrementBalance(parent);
        else
            SetRight(parent, leftValue);
            DecrementBalance(parent);
        }
    }
```

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```
else // node has a both children (left and right)
        var predecessor = GetLeft(currentNode);
        var successor = GetRight(currentNode);
        var successorParent = currentNode
        int previousPathPosition = ++pathPosition;
        // find the immediately next node (and its parent)
        while (GetLeftIsChild(successor))
            path[++pathPosition] = successorParent = successor;
            successor = GetLeft(successor);
            if (!AreEqual(successorParent, currentNode))
                DecrementSize(successorParent);
            }
        path[previousPathPosition] = successor;
        balanceNode = path[pathPosition];
        // remove 'successor' from the tree
        if (!AreEqual(successorParent, currentNode))
            if (!GetRightIsChild(successor))
            {
                SetLeftIsChild(successorParent, false);
            }
            else
            {
                SetLeft(successorParent, GetRight(successor));
            IncrementBalance(successorParent);
            SetRightIsChild(successor, true);
            SetRight(successor, GetRight(currentNode));
        else
        {
            DecrementBalance(currentNode);
        // set the predecessor's successor link to point to the right place
        while (GetRightIsChild(predecessor))
            predecessor = GetRight(predecessor);
        SetRight(predecessor, successor);
        // prepare 'successor' to replace 'node'
        var left = GetLeft(currentNode);
        SetLeftIsChild(successor, true);
        SetLeft(successor, left);
        SetBalance(successor, GetBalance(currentNode));
        FixSize(successor);
        if (AreEqual(parent, default))
        {
            root = successor;
        }
        else if (isLeftNode)
            SetLeft(parent, successor);
        else
        {
            SetRight(parent, successor);
        }
   }
// restore balance
  (!AreEqual(balanceNode, default))
   while (true)
        var balanceParent = path[--pathPosition];
        isLeftNode = !AreEqual(balanceParent, default) && AreEqual(balanceNode,

→ GetLeft(balanceParent));
        var currentNodeBalance = GetBalance(balanceNode);
           (currentNodeBalance < -1 || currentNodeBalance > 1)
            balanceNode = Balance(balanceNode);
            if (AreEqual(balanceParent, default))
            {
                root = balanceNode;
```

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547

548

549

550

```
552
                                   else if (isLeftNode)
554
                                       SetLeft(balanceParent, balanceNode);
555
                                   }
                                  else
557
                                   {
558
                                       SetRight(balanceParent, balanceNode);
559
                                   }
560
561
                              currentNodeBalance = GetBalance(balanceNode);
562
                                 (currentNodeBalance != 0 || AreEqual(balanceParent, default))
563
564
565
                                  break;
                              }
566
                                 (isLeftNode)
567
568
                                   IncrementBalance(balanceParent);
569
570
                              else
571
                              {
572
                                  DecrementBalance(balanceParent);
573
                              balanceNode = balanceParent;
575
                          }
576
577
                     ClearNode(node);
578
    #if USEARRAYPOOL
579
                     ArrayPool.Free(path);
580
    #endif
581
                 }
582
             }
583
584
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
585
             protected override void ClearNode(TElement node)
586
587
                 SetLeft(node, Zero);
588
                 SetRight(node, Zero);
589
                 SetSize(node, Zero);
591
                 SetLeftIsChild(node, false);
                 SetRightIsChild(node, false);
592
                 SetBalance(node, 0);
593
             }
        }
595
596
       ./csharp/Platform.Collections.Methods/Trees/SizedBinaryTreeMethodsBase.cs
1.12
    //#define ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
 1
    using System;
 3
    using System Diagnostics;
    using System.Runtime.CompilerServices;
 5
    using System. Text;
 6
    using Platform. Numbers;
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
10
    namespace Platform.Collections.Methods.Trees
12
        public abstract class SizedBinaryTreeMethodsBase<TElement> :
13
            GenericCollectionMethodsBase<TElement>
14
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected abstract ref TElement GetLeftReference(TElement node);
17
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected abstract ref TElement GetRightReference(TElement node);
19
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
             protected abstract TElement GetLeft(TElement node);
22
23
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
24
             protected abstract TElement GetRight(TElement node);
25
26
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
27
             protected abstract TElement GetSize(TElement node);
29
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
30
             protected abstract void SetLeft(TElement node, TElement left);
```

```
[MethodImpl(MethodImplOptions.AggressiveInlining)]
33
             protected abstract void SetRight(TElement node, TElement right);
3.5
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected abstract void SetSize(TElement node, TElement size);
37
38
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
39
            protected abstract bool FirstIsToTheLeftOfSecond(TElement first, TElement second);
40
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
42
            protected abstract bool FirstIsToTheRightOfSecond(TElement first, TElement second);
43
44
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
45
            protected virtual TElement GetLeftOrDefault(TElement node) => AreEqual(node, default) ?
46

→ default : GetLeft(node);
47
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
48
            protected virtual TElement GetRightOrDefault(TElement node) => AreEqual(node, default) ?

→ default : GetRight(node);

50
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected void IncrementSize(TElement node) => SetSize(node, Increment(GetSize(node)));
53
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected void DecrementSize(TElement node) => SetSize(node, Decrement(GetSize(node)));
55
56
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
57
            protected TElement GetLeftSize(TElement node) => GetSizeOrZero(GetLeftOrDefault(node));
58
59
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
60
            protected TElement GetRightSize(TElement node) => GetSizeOrZero(GetRightOrDefault(node));
61
62
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
63
            protected TElement GetSizeOrZero(TElement node) => EqualToZero(node) ? Zero :
64

   GetSize(node);
65
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
66
            protected void FixSize(TElement node) => SetSize(node, Increment(Add(GetLeftSize(node),

→ GetRightSize(node))));
68
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
69
            protected void LeftRotate(ref TElement root) => root = LeftRotate(root);
71
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected TElement LeftRotate(TElement root)
7.3
74
    var right = GetRight(root);
#if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
75
76
                 if (EqualToZero(right))
77
                 {
78
                     throw new InvalidOperationException("Right is null.");
79
                 }
80
    #endif
81
                 SetRight(root, GetLeft(right));
82
                 SetLeft(right, root);
83
                 SetSize(right, GetSize(root));
                 FixSize(root);
85
                 return right;
             }
87
88
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
89
            protected void RightRotate(ref TElement root) => root = RightRotate(root);
90
91
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
92
            protected TElement RightRotate(TElement root)
93
    var left = GetLeft(root);
#if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
95
96
                 if (EqualToZero(left))
97
                 {
98
                     throw new InvalidOperationException("Left is null.");
99
                 }
    #endif
101
102
                 SetLeft(root, GetRight(left));
103
                 SetRight(left, root);
                 SetSize(left, GetSize(root));
104
                 FixSize(root);
105
                 return left;
106
             }
107
```

```
[MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected virtual TElement GetRightest(TElement current)
            var currentRight = GetRight(current);
            while (!EqualToZero(currentRight))
                current = currentRight;
                currentRight = GetRight(current);
            return current;
        }
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected virtual TElement GetLeftest(TElement current)
            var currentLeft = GetLeft(current);
            while (!EqualToZero(currentLeft))
                current = currentLeft;
                currentLeft = GetLeft(current);
            return current;
        }
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected virtual TElement GetNext(TElement node) => GetLeftest(GetRight(node));
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected virtual TElement GetPrevious(TElement node) => GetRightest(GetLeft(node));
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public virtual bool Contains(TElement node, TElement root)
            while (!EqualToZero(root))
                   (FirstIsToTheLeftOfSecond(node, root)) // node.Key < root.Key
                    root = GetLeft(root);
                else if (FirstIsToTheRightOfSecond(node, root)) // node.Key > root.Key
                    root = GetRight(root);
                else // node.Key == root.Key
                {
                    return true;
            return false;
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected virtual void ClearNode(TElement node)
            SetLeft(node, Zero)
            SetRight(node, Zero);
            SetSize(node, Zero);
        }
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public void Attach(ref TElement root, TElement node)
#if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
            ValidateSizes(root);
            Debug.WriteLine("--BeforeAttach--");
            Debug.WriteLine(PrintNodes(root));
            Debug.WriteLine("----");
            var sizeBefore = GetSize(root);
#endif
            if (EqualToZero(root))
            {
                SetSize(node, One);
                root = node;
                return;
AttachCore(ref root, node); #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
            Debug.WriteLine("--AfterAttach--");
```

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178

179

181 182

183

184 185

```
Debug.WriteLine(PrintNodes(root));
187
                 Debug.WriteLine("----"):
                 ValidateSizes(root);
189
                 var sizeAfter = GetSize(root);
190
                 if (!AreEqual(Arithmetic.Increment(sizeBefore), sizeAfter))
                 {
192
                      throw new InvalidOperationException("Tree was broken after attach.");
193
                 }
194
    #endif
195
196
197
             protected abstract void AttachCore(ref TElement root, TElement node);
198
199
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
200
             public void Detach(ref TElement root, TElement node)
201
202
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
203
                 ValidateSizes(root);
204
                 Debug.WriteLine("--BeforeDetach--");
205
                 Debug.WriteLine(PrintNodes(root));
206
                 Debug.WriteLine("-----');
207
                 var sizeBefore = GetSize(root);
                 if (EqualToZero(root))
209
                 {
210
                      throw new InvalidOperationException($"Элемент с {node} не содержится в
211
                      → дереве.");
212
    #endif
213
    DetachCore(ref root, node); #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
214
215
                 Debug.WriteLine("--AfterDetach--");
216
                 Debug.WriteLine(PrintNodes(root));
217
                 Debug.WriteLine("----"):
218
                 ValidateSizes(root);
219
                 var sizeAfter = GetSize(root);
220
                 if (!AreEqual(Arithmetic.Decrement(sizeBefore), sizeAfter))
221
222
                      throw new InvalidOperationException("Tree was broken after detach.");
223
                 }
224
    #endif
225
226
227
             protected abstract void DetachCore(ref TElement root, TElement node);
228
229
             public void FixSizes(TElement node)
230
232
                 if (AreEqual(node, default))
                 {
233
234
                     return;
235
                 FixSizes(GetLeft(node));
236
                 FixSizes(GetRight(node));
238
                 FixSize(node);
239
240
             public void ValidateSizes(TElement node)
241
242
                 if (AreEqual(node, default))
^{243}
                 {
244
                     return;
245
                 }
246
                 var size = GetSize(node);
247
                 var leftSize = GetLeftSize(node);
248
249
                 var rightSize = GetRightSize(node);
                 var expectedSize = Arithmetic.Increment(Arithmetic.Add(leftSize, rightSize));
250
                 if (!AreEqual(size, expectedSize))
251
252
                      throw new InvalidOperationException($\sigma"Size of \{node\} is not valid. Expected
253

    size: {expectedSize}, actual size: {size}.");
254
                 ValidateSizes(GetLeft(node));
255
                 ValidateSizes(GetRight(node));
256
             }
257
258
             public void ValidateSize(TElement node)
260
                 var size = GetSize(node);
261
                 var leftSize = GetLeftSize(node);
262
```

```
var rightSize = GetRightSize(node);
263
                  var expectedSize = Arithmetic.Increment(Arithmetic.Add(leftSize, rightSize));
265
                  if (!AreEqual(size, expectedSize))
266
                      throw new InvalidOperationException($ "Size of {node} is not valid. Expected
267

    size: {expectedSize}, actual size: {size}.");
                  }
268
             }
270
             public string PrintNodes(TElement node)
272
                  var sb = new StringBuilder();
273
                  PrintNodes(node, sb);
                  return sb.ToString();
275
276
277
             [{\tt MethodImpl}({\tt MethodImpl}{\tt Options}. {\tt AggressiveInlining}) \, \rfloor
278
             public void PrintNodes(TElement node, StringBuilder sb) => PrintNodes(node, sb, 0);
279
280
             public void PrintNodes(TElement node, StringBuilder sb, int level)
281
282
                  if (AreEqual(node, default))
283
                  {
284
                      return;
286
                  PrintNodes(GetLeft(node), sb, level + 1);
287
                  PrintNode(node, sb, level);
288
289
                  sb.AppendLine()
                 PrintNodes(GetRight(node), sb, level + 1);
290
             }
291
292
             public string PrintNode(TElement node)
293
294
                  var sb = new StringBuilder();
295
                 PrintNode(node, sb)
296
                  return sb.ToString();
298
299
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected void PrintNode(TElement node, StringBuilder sb) => PrintNode(node, sb, 0);
301
303
             protected virtual void PrintNode(TElement node, StringBuilder sb, int level)
304
                  sb.Append('\t', level);
305
                  sb.Append(node);
                  PrintNodeValue(node, sb);
307
                  sb.Append(' ');
308
                  sb.Append('s');
309
                  sb.Append(GetSize(node));
310
311
312
             protected abstract void PrintNodeValue(TElement node, StringBuilder sb);
313
         }
314
    }
       ./csharp/Platform. Collections. Methods. Tests/Recursionless Size Balanced Tree.cs\\
1.13
    using System;
    using System.Collections.Generic;
    using System. Text;
    using Platform. Numbers;
    using Platform.Collections.Methods.Trees;
    using Platform.Converters;
    namespace Platform.Collections.Methods.Tests
 8
 q
         public class RecursionlessSizeBalancedTree<TElement> :
10
             RecursionlessSizeBalancedTreeMethods<TElement>
1.1
             private struct TreeElement
13
                  public TElement Size;
14
                 public TElement Left;
public TElement Right;
15
16
17
18
             private readonly TreeElement[] _elements;
19
             private TElement _allocated;
21
             public TElement Root;
```

```
public TElement Count => GetSizeOrZero(Root);
24
25
            public RecursionlessSizeBalancedTree(int capacity) => (_elements, _allocated) = (new
26

→ TreeElement[capacity], One);
27
            public TElement Allocate()
28
29
                var newNode = _allocated;
30
                if (IsEmpty(newNode))
31
                    _allocated = Arithmetic.Increment(_allocated);
33
                    return newNode;
34
                }
                else
36
                    throw new InvalidOperationException("Allocated tree element is not empty.");
38
                }
39
            }
40
41
            public void Free(TElement node)
42
                while (!EqualityComparer.Equals(_allocated, One) && IsEmpty(node))
44
45
                    var lastNode = Arithmetic.Decrement(_allocated);
                    if (EqualityComparer.Equals(lastNode, node))
47
48
                        _allocated = lastNode;
                        node = Arithmetic.Decrement(node);
50
51
                    else
52
                    {
5.3
                        return;
54
                    }
55
                }
56
            }
58
            public bool IsEmpty(TElement node) =>
            FqualityComparer<TreeElement>.Default.Equals(GetElement(node), default);
60
            protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
61

→ Comparer.Compare(first, second) < 0;</pre>
62
            protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>
63

→ Comparer.Compare(first, second) > 0;

            protected override ref TElement GetLeftReference(TElement node) => ref
65

   GetElement(node).Left;
            protected override TElement GetLeft(TElement node) => GetElement(node).Left;
            protected override ref TElement GetRightReference(TElement node) => ref
69

   GetElement(node).Right;
70
            protected override TElement GetRight(TElement node) => GetElement(node).Right;
            protected override TElement GetSize(TElement node) => GetElement(node).Size;
74
            protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
75

    sb.Append(node);
76
            protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
77
            → left;
            protected override void SetRight(TElement node, TElement right) =>
79

   GetElement(node).Right = right;
80
            protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =
81

→ size;

82
            private ref TreeElement GetElement(TElement node) => ref
            _ _ elements[UncheckedConverter<TElement, long>.Default.Convert(node)];
       }
84
   }
85
      ./csharp/Platform.Collections.Methods.Tests/SizeBalancedTree.cs
1.14
   using System;
   using System.Collections.Generic;
   using System. Text;
3
```

using Platform. Numbers;

```
using Platform.Collections.Methods.Trees;
using Platform.Converters;
namespace Platform.Collections.Methods.Tests
    public class SizeBalancedTree<TElement> : SizeBalancedTreeMethods<TElement>
        private struct TreeElement
            public TElement Size;
            public TElement Left;
            public TElement Right;
        private readonly TreeElement[] _elements;
        private TElement _allocated;
        public TElement Root;
        public TElement Count => GetSizeOrZero(Root);
        public SizeBalancedTree(int capacity) => (_elements, _allocated) = (new
        → TreeElement[capacity], One);
        public TElement Allocate()
            var newNode = _allocated;
            if (IsEmpty(newNode))
                _allocated = Arithmetic.Increment(_allocated);
                return newNode;
            }
            else
            {
                throw new InvalidOperationException("Allocated tree element is not empty.");
            }
        }
        public void Free(TElement node)
            while (!EqualityComparer.Equals(_allocated, One) && IsEmpty(node))
                var lastNode = Arithmetic.Decrement(_allocated);
                if (EqualityComparer.Equals(lastNode, node))
                    _allocated = lastNode;
                   node = Arithmetic.Decrement(node);
                }
                else
                {
                   return;
                }
            }
        }
        public bool IsEmpty(TElement node) =>
        protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>

→ Comparer.Compare(first, second) < 0;</pre>
        protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>

→ Comparer.Compare(first, second) > 0;

        protected override ref TElement GetLeftReference(TElement node) => ref

   GetElement(node).Left;

        protected override TElement GetLeft(TElement node) => GetElement(node).Left;
        protected override ref TElement GetRightReference(TElement node) => ref

   GetElement(node).Right;

        protected override TElement GetRight(TElement node) => GetElement(node).Right;
        protected override TElement GetSize(TElement node) => GetElement(node).Size;
        protected override void PrintNodeValue(TElement node, StringBuilder sb) =>

    sb.Append(node);
```

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75

```
protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
            → left;
            protected override void SetRight(TElement node, TElement right) =>
               GetElement(node).Right = right;
80
            protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =
81

    size;

82
            private ref TreeElement GetElement(TElement node) => ref
83
              _elements[UncheckedConverter<TElement, long>.Default.Convert(node)];
        }
   }
85
1.15
      ./csharp/Platform.Collections.Methods.Tests/SizedAndThreadedAVLBalancedTree.cs
   using System;
   using System.Collections.Generic;
   using System. Text;
3
   using Platform. Numbers;
   using Platform.Collections.Methods.Trees;
5
   using Platform.Converters;
   namespace Platform.Collections.Methods.Tests
9
        public class SizedAndThreadedAVLBalancedTree<TElement> :
10
           SizedAndThreadedAVLBalancedTreeMethods<TElement>
11
            private struct TreeElement
12
13
                public TElement Size;
14
                public TElement Left;
                public TElement Right;
16
                public sbyte Balance;
17
                public bool LeftIsChild
18
                public bool RightIsChild;
19
20
21
            private readonly TreeElement[] _elements;
22
            private TElement _allocated;
23
24
            public TElement Root;
25
            public TElement Count => GetSizeOrZero(Root);
27
28
            public SizedAndThreadedAVLBalancedTree(int capacity) => (_elements, _allocated) = (new
29
            → TreeElement[capacity], One);
30
            public TElement Allocate()
32
33
                var newNode = _allocated;
                if (IsEmpty(newNode))
34
35
                     _allocated = Arithmetic.Increment(_allocated);
                    return newNode;
37
                }
38
                else
39
                {
40
                    throw new InvalidOperationException("Allocated tree element is not empty.");
                }
42
            }
43
44
            public void Free(TElement node)
45
46
                while (!EqualityComparer.Equals(_allocated, One) && IsEmpty(node))
47
48
                    var lastNode = Arithmetic.Decrement(_allocated);
49
                    if (EqualityComparer.Equals(lastNode, node))
50
                         _allocated = lastNode;
52
                        node = Arithmetic.Decrement(node);
                    }
54
                    else
                    {
56
                        return;
                }
5.9
            }
60
61
            public bool IsEmpty(TElement node) =>
62
            EqualityComparer<TreeElement>.Default.Equals(GetElement(node), default);
```

```
63
            protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
               Comparer.Compare(first, second) < 0;</pre>
65
            protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>
66

→ Comparer.Compare(first, second) > 0;

67
            protected override sbyte GetBalance(TElement node) => GetElement(node).Balance;
68
69
            protected override bool GetLeftIsChild(TElement node) => GetElement(node).LeftIsChild;
70
            protected override ref TElement GetLeftReference(TElement node) => ref
72

   GetElement(node).Left;
            protected override TElement GetLeft(TElement node) => GetElement(node).Left;
74
75
            protected override bool GetRightIsChild(TElement node) => GetElement(node).RightIsChild;
76
77
            protected override ref TElement GetRightReference(TElement node) => ref
78

   GetElement(node).Right;

79
            protected override TElement GetRight(TElement node) => GetElement(node).Right;
81
            protected override TElement GetSize(TElement node) => GetElement(node).Size;
82
83
            protected override void PrintNodeValue(TElement node, StringBuilder sb) =>

⇒ sb.Append(node);

85
            protected override void SetBalance(TElement node, sbyte value) =>
86

   GetElement(node).Balance = value;

            protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
            → left;
89
            protected override void SetLeftIsChild(TElement node, bool value) =>
90

→ GetElement(node).LeftIsChild = value;
            protected override void SetRight(TElement node, TElement right) =>
92

   GetElement(node).Right = right;
            protected override void SetRightIsChild(TElement node, bool value) =>
94

→ GetElement(node).RightIsChild = value;
            protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =

    size;

            private ref TreeElement GetElement(TElement node) => ref
98
            - _ elements[UncheckedConverter<TElement, long>.Default.Convert(node)];
        }
99
100
    }
      ./csharp/Platform.Collections.Methods.Tests/TestExtensions.cs
1.16
   using System;
   using System.Collections.Generic;
   using Xunit;
          Platform.Collections.Methods.Trees;
   using
   using Platform.Converters;
   namespace Platform.Collections.Methods.Tests
        public static class TestExtensions
 9
10
            public static void TestMultipleCreationsAndDeletions<TElement>(this
                SizedBinaryTreeMethodsBase<TElement> tree, Func<TElement> allocate, Action<TElement>
                free, ref TElement root, Func<TElement> treeCount, int maximumOperationsPerCycle)
12
                for (var N = 1; N < maximumOperationsPerCycle; N++)</pre>
13
                    var currentCount = 0;
                    for (var i = 0; i < N; i++)</pre>
17
                         var node = allocate();
18
                        tree.Attach(ref root, node);
19
                        currentCount++;
20
                        Assert.Equal(currentCount, (int)UncheckedConverter<TElement,
                           int>.Default.Convert(treeCount()));
22
                    for (var i = 1; i <= N; i++)</pre>
23
```

```
TElement node = UncheckedConverter<int, TElement>.Default.Convert(i);
                         if (tree.Contains(node, root))
27
                             tree.Detach(ref root, node);
28
                             free(node);
                             currentCount--;
30
                             Assert.Equal(currentCount, (int)UncheckedConverter<TElement,
31
                                int>.Default.Convert(treeCount()));
                         }
                    }
33
                }
34
            }
35
36
            public static void TestMultipleRandomCreationsAndDeletions<TElement>(this
37
                SizedBinaryTreeMethodsBase<TElement> tree, ref TElement root, Func<TElement>
                treeCount, int maximumOperationsPerCycle)
            {
38
                var random = new System.Random(0);
39
                var added = new HashSet<TElement>();
40
                var currentCount = 0;
41
                for (var N = 1; N < maximumOperationsPerCycle; N++)</pre>
43
                    for (var i = 0; i < N; i++)</pre>
44
45
                         var node = UncheckedConverter<int, TElement>.Default.Convert(random.Next(1,
                         \rightarrow N));
                         if (added.Add(node))
47
                         {
48
                             tree.Attach(ref root, node);
49
                             currentCount++;
50
                             Assert.Equal(currentCount, (int)UncheckedConverter<TElement,
51
                                 int>.Default.Convert(treeCount()));
53
                    for (var i = 1; i <= N; i++)</pre>
54
55
                         TElement node = UncheckedConverter<int,
56
                             TElement>.Default.Convert(random.Next(1, N));
                         if (tree.Contains(node, root))
57
                             tree.Detach(ref root, node);
59
                             currentCount--;
60
                             Assert.Equal(currentCount, (int)UncheckedConverter<TElement,
61
                                 int>.Default.Convert(treeCount()));
                             added.Remove(node);
62
                         }
63
                    }
                }
65
            }
66
        }
67
   }
      ./csharp/Platform.Collections.Methods.Tests/TreesTests.cs
1.17
   using Xunit;
   namespace Platform.Collections.Methods.Tests
   {
4
        public static class TreesTests
5
6
            private const int _n = 500;
            [Fact]
            public static void RecursionlessSizeBalancedTreeMultipleAttachAndDetachTest()
11
                var recursionlessSizeBalancedTree = new RecursionlessSizeBalancedTree<uint>(10000);
12
                recursionlessSizeBalancedTree.TestMultipleCreationsAndDeletions(recursionlessSizeBal
13
                    ancedTree.Allocate, recursionlessSizeBalancedTree.Free, ref
                    recursionlessSizeBalancedTree.Root, () => recursionlessSizeBalancedTree.Count,
                    _n);
            }
14
15
            [Fact]
16
            public static void SizeBalancedTreeMultipleAttachAndDetachTest()
17
                var sizeBalancedTree = new SizeBalancedTree<uint>(10000);
19
                sizeBalancedTree.TestMultipleCreationsAndDeletions(sizeBalancedTree.Allocate,
20

→ sizeBalancedTree.Free, ref sizeBalancedTree.Root, () => sizeBalancedTree.Count,

                    _n);
```

```
}
21
22
                                   [Fact]
23
                                  public static void SizedAndThreadedAVLBalancedTreeMultipleAttachAndDetachTest()
25
                                               var avlTree = new SizedAndThreadedAVLBalancedTree<uint>(10000);
26
                                               avlTree.TestMultipleCreationsAndDeletions(avlTree.Allocate, avlTree.Free, ref
27
                                                          avlTree.Root, () => avlTree.Count, _n);
29
                                   [Fact]
                                  public static void RecursionlessSizeBalancedTreeMultipleRandomAttachAndDetachTest()
31
32
33
                                               var recursionlessSizeBalancedTree = new RecursionlessSizeBalancedTree<uint>(10000);
34
                                              {\tt recursionlessSizeBalancedTree.TestMultipleRandomCreationsAndDeletions} ({\tt refine} {\tt refine} 
                                                recursionlessSizeBalancedTree.Root, () => recursionlessSizeBalancedTree.Count,
                                                          _n);
                                   }
36
                                   [Fact]
37
                                  public static void SizeBalancedTreeMultipleRandomAttachAndDetachTest()
38
39
                                               var sizeBalancedTree = new SizeBalancedTree<uint>(10000);
40
                                              sizeBalancedTree.TestMultipleRandomCreationsAndDeletions(ref sizeBalancedTree.Root,
                                               }
42
43
                                   [Fact]
44
                                  public static void SizedAndThreadedAVLBalancedTreeMultipleRandomAttachAndDetachTest()
45
46
                                               var avlTree = new SizedAndThreadedAVLBalancedTree<uint>(10000);
47
                                               avlTree.TestMultipleRandomCreationsAndDeletions(ref avlTree.Root, () =>
48
                                               → avlTree.Count, _n);
                                   }
49
                      }
50
          }
51
```

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