```
LinksPlatform's Platform Collections Methods Class Library
     ./csharp/Platform.Collections.Methods/GenericCollectionMethodsBase.cs
   using System.Collections.Generic;
using System.Runtime.CompilerServices;
   using Platform.Numbers;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods
9
        /// <summary>
        /// <para>Represents a range between minimum and maximum values.</para>
10
        /// <para>Представляет диапазон между минимальным и максимальным значениями.</para>
11
       /// </summary>
12
       /// <remarks>
13
        /// <para>Based on <a href="http://stackoverflow.com/questions/5343006/is-there-a-c-sharp-ty|
        _{\hookrightarrow} pe-for-representing-an-integer-range">the question at
           StackOverflow</a>.</para>
       /// <para>Oсновано на <a href="http://stackoverflow.com/questions/5343006/is-there-a-c-sharp_
15
            -type-for-representing-an-integer-range">вопросе в
           StackOverflow</a>.</para>
        /// </remarks>
       public abstract class GenericCollectionMethodsBase<TElement>
            /// <summary>
19
            /// <para>Presents the Range in readable format.</para>
20
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
            /// </summary>
22
            /// <returns><para>String representation of the Range.</para><para>Строковое
23
               представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected virtual TElement GetZero() => default;
26
            /// <summary>
27
            /// <para>Presents the Range in readable format.</para>
2.8
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
29
            /// </summary>
            /// <returns><para>String representation of the Range.</para><para>Строковое
            → представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
32
           protected virtual bool EqualToZero(TElement value) => EqualityComparer.Equals(value,
33

    Zero);

            /// <summary>
35
            /// <para>Presents the Range in readable format.</para>
36
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
37
            /// </summary>
38
            /// <returns><para>String representation of the Range.</para>Строковое
39
               представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected virtual bool AreEqual(TElement first, TElement second) =>
41

→ EqualityComparer.Equals(first, second);

            /// <summary>
            /// <para>Presents the Range in readable format.</para>
44
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
45
            /// </summary>
46
            /// <returns><para>String representation of the Range.</para><para>Строковое
47
               представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected virtual bool GreaterThanZero(TElement value) => Comparer.Compare(value, Zero)
49
            \rightarrow > 0;
50
            /// <summary>
            /// <para>Presents the Range in readable format.</para>
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
5.3
            /// </summary>
54
            /// <returns><para>String representation of the Range.</para><para>Строковое
               представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected virtual bool GreaterThan(TElement first, TElement second) =>
            → Comparer.Compare(first, second) > 0;
            /// <summary>
            /// <para>Presents the Range in readable format.</para>
60
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
            /// </summary>
```

```
/// <returns><para>String representation of the Range.</para><para>Строковое
63
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool GreaterOrEqualThanZero(TElement value) => Comparer.Compare(value,
             \rightarrow Zero) >= 0;
66
            /// <summary>
            /// <para>Presents the Range in readable format.</para>
68
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
69
            /// </summary>
            /// <returns><para>String representation of the Range.</para><para>Строковое
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
72
            protected virtual bool GreaterOrEqualThan(TElement first, TElement second) =>
73
            74
            /// <summary>
75
            /// <para>Presents the Range in readable format.</para>
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
77
            /// </summary>
78
            /// <returns><para>String representation of the Range.</para><para>Строковое
79
               представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool LessOrEqualThanZero(TElement value) => Comparer.Compare(value,

→ Zero) <= 0;
</p>
82
            /// <summary>
            /// <para>Presents the Range in readable format.</para>
84
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
8.5
            /// </summary>
            /// <returns><para>String representation of the Range.</para><para>Строковое
               представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool LessOrEqualThan(TElement first, TElement second) =>
89
               Comparer.Compare(first, second) <= 0;</pre>
90
            /// <summary>
            /// <para>Presents the Range in readable format.</para>
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
            /// </summary>
94
            /// <returns><para>String representation of the Range.</para><para>Строковое
95
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
96
            protected virtual bool LessThanZero(TElement value) => Comparer.Compare(value, Zero) < 0;</pre>
97
98
            /// <summary>
99
            /// <para>Presents the Range in readable format.</para>
100
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
101
            /// </summary>
102
            /// <returns><para>String representation of the Range.</para><para>Строковое
103
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
104
            protected virtual bool LessThan(TElement first, TElement second) =>
105
               Comparer.Compare(first, second) < 0;</pre>
106
            /// <summary>
107
            /// <para>Presents the Range in readable format.</para>
108
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
109
            /// </summary>
110
            /// <returns><para>String representation of the Range.</para><para>Строковое
111
               представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual TElement Increment(TElement value) =>
            → Arithmetic<TElement>.Increment(value);
114
            /// <summary>
            /// <para>Presents the Range in readable format.</para>
116
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
117
            /// </summary>
            /// <returns><para>String representation of the Range.</para><para>Строковое
119
               представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
120
            protected virtual TElement Decrement(TElement value) =>
121
               Arithmetic<TElement>.Decrement(value);
122
            /// <summary>
123
            /// <para>Presents the Range in readable format.</para>
```

```
/// <para>Представляет диапазон в удобном для чтения формате.</para>
125
             /// </summary>
             /// <returns><para>String representation of the Range.</para><para>Строковое
127
                представление диапазона.</para></returns>
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
128
             protected virtual TElement Add(TElement first, TElement second) =>
129
             → Arithmetic<TElement>.Add(first, second);
130
             /// <summary>
131
             /// <para>Presents the Range in readable format.</para>
             /// <para>Представляет диапазон в удобном для чтения формате.</para>
133
             /// </summary>
134
             /// <returns><para>String representation of the Range.</para><para>Строковое
135
             → представление диапазона.</para></returns>
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected virtual TElement Subtract(TElement first, TElement second) =>
137
             → Arithmetic<TElement>.Subtract(first, second);
138
            protected readonly TElement Zero;
protected readonly TElement One;
139
            protected readonly TElement Two;
protected readonly EqualityComparer<TElement> EqualityComparer;
protected readonly Comparer<TElement> Comparer;
141
142
144
             /// <summary>
145
             /// <para>Presents the Range in readable format.</para>
             /// <para>Представляет диапазон в удобном для чтения формате.</para>
147
             /// </summary>
148
             /// <returns><para>String representation of the Range.</para><para>Строковое
149
                представление диапазона.</para></returns>
             protected GenericCollectionMethodsBase()
151
                 EqualityComparer = EqualityComparer<TElement>.Default;
152
                 Comparer = Comparer<Telement>.Default;
153
                 Zero = GetZero(); //-V3068
                 One = Increment(Zero); //-V3068
155
                 Two = Increment(One); //-V3068
156
             }
        }
158
159
     ./csharp/Platform.Collections.Methods/Lists/AbsoluteCircularDoublyLinkedListMethods.cs
1.2
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
 2
    namespace Platform.Collections.Methods.Lists
 4
        public abstract class AbsoluteCircularDoublyLinkedListMethods<TElement> :
            AbsoluteDoublyLinkedListMethodsBase<TElement>
 6
             public void AttachBefore(TElement baseElement, TElement newElement)
                 var baseElementPrevious = GetPrevious(baseElement);
                 SetPrevious(newElement, baseElementPrevious);
10
11
                 SetNext(newElement, baseElement);
                 if (AreEqual(baseElement, GetFirst()))
12
                 {
13
                     SetFirst(newElement);
                 SetNext(baseElementPrevious, newElement);
16
                 SetPrevious(baseElement, newElement);
17
                 IncrementSize();
18
             }
19
20
             public void AttachAfter(TElement baseElement, TElement newElement)
22
                 var baseElementNext = GetNext(baseElement);
23
                 SetPrevious(newElement, baseElement);
                 SetNext(newElement, baseElementNext)
25
                 if (AreEqual(baseElement, GetLast()))
26
                 {
                     SetLast(newElement);
29
                 SetPrevious(baseElementNext, newElement);
30
                 SetNext(baseElement, newElement);
                 IncrementSize();
32
33
             public void AttachAsFirst(TElement element)
```

```
36
                var first = GetFirst();
                if (EqualToZero(first))
38
39
                     SetFirst(element);
                     SetLast(element);
41
                     SetPrevious(element, element);
42
                     SetNext(element, element);
43
                     IncrementSize();
                }
45
                else
46
                {
47
                     AttachBefore(first, element);
48
                }
49
            }
51
            public void AttachAsLast(TElement element)
                var last = GetLast();
54
                if (EqualToZero(last))
55
56
                     AttachAsFirst(element);
57
                }
58
                else
59
                {
60
61
                     AttachAfter(last, element);
                }
62
            }
63
            public void Detach(TElement element)
65
66
                var elementPrevious = GetPrevious(element);
67
                var elementNext = GetNext(element);
68
                if (AreEqual(elementNext, element))
69
70
                     SetFirst(Zero);
71
                     SetLast(Zero);
72
                }
73
                else
7.4
7.5
                     SetNext(elementPrevious, elementNext);
76
                     SetPrevious(elementNext, elementPrevious);
77
                     if (AreEqual(element, GetFirst()))
78
79
                         SetFirst(elementNext);
80
81
                     if (AreEqual(element, GetLast()))
82
                     {
                         SetLast(elementPrevious);
85
86
                SetPrevious(element, Zero);
                SetNext(element, Zero);
88
                DecrementSize();
89
            }
90
        }
91
92
     ./csharp/Platform.Collections.Methods/Lists/AbsoluteDoublyLinkedListMethodsBase.cs
1.3
   using System.Runtime.CompilerServices;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
4
   namespace Platform.Collections.Methods.Lists
6
        public abstract class AbsoluteDoublyLinkedListMethodsBase<TElement> :
           DoublyLinkedListMethodsBase<TElement>
8
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetFirst();
10
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetLast();
13
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
15
            protected abstract TElement GetSize();
16
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
            protected abstract void SetFirst(TElement element);
```

```
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract void SetLast(TElement element);
22
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
24
            protected abstract void SetSize(TElement size);
25
26
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
27
            protected void IncrementSize() => SetSize(Increment(GetSize()));
28
29
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
30
            protected void DecrementSize() => SetSize(Decrement(GetSize()));
31
        }
32
   }
33
1.4
     ./csharp/Platform.Collections.Methods/Lists/AbsoluteOpenDoublyLinkedListMethods.cs
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
3
4
       public abstract class AbsoluteOpenDoublyLinkedListMethods<TElement> :
           AbsoluteDoublyLinkedListMethodsBase<TElement>
6
            public void AttachBefore(TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
10
                SetNext(newElement, baseElement);
                if (EqualToZero(baseElementPrevious))
12
13
                    SetFirst(newElement);
14
                }
15
                else
16
                {
17
                    SetNext(baseElementPrevious, newElement);
18
19
                SetPrevious(baseElement, newElement);
20
                IncrementSize();
21
            }
22
23
            public void AttachAfter(TElement baseElement, TElement newElement)
24
25
                var baseElementNext = GetNext(baseElement);
26
                SetPrevious(newElement, baseElement);
27
                SetNext(newElement, baseElementNext);
28
                if (EqualToZero(baseElementNext))
                {
30
                    SetLast(newElement);
31
                }
32
                else
33
                {
34
                    SetPrevious(baseElementNext, newElement);
36
                SetNext(baseElement, newElement);
37
                IncrementSize();
38
            }
39
40
            public void AttachAsFirst(TElement element)
41
42
                var first = GetFirst();
43
                if (EqualToZero(first))
44
45
                    SetFirst(element);
46
                    SetLast(element);
47
                    SetPrevious(element, Zero);
49
                    SetNext(element, Zero);
                    IncrementSize();
50
                }
                else
52
                {
53
                    AttachBefore(first, element);
                }
55
            }
56
57
            public void AttachAsLast(TElement element)
58
                var last = GetLast();
                if (EqualToZero(last))
61
```

```
AttachAsFirst(element);
63
                }
                else
6.5
                {
                    AttachAfter(last, element);
67
                }
68
            }
69
70
            public void Detach(TElement element)
71
                var elementPrevious = GetPrevious(element);
73
                var elementNext = GetNext(element);
74
                if (EqualToZero(elementPrevious))
75
76
                    SetFirst(elementNext);
77
                }
78
                else
79
                {
80
                    SetNext(elementPrevious, elementNext);
81
                }
82
                if (EqualToZero(elementNext))
83
                {
84
                    SetLast(elementPrevious);
                }
86
                else
87
                {
88
                    SetPrevious(elementNext, elementPrevious);
89
90
                SetPrevious(element, Zero);
92
                SetNext(element, Zero);
                DecrementSize();
93
            }
       }
95
   }
96
1.5
     ./csharp/Platform.Collections.Methods/Lists/DoublyLinkedListMethodsBase.cs
   using System.Runtime.CompilerServices;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
5
   {
        /// <remarks>
        /// Based on <a href="https://en.wikipedia.org/wiki/Doubly_linked_list">doubly linked
        → list</a> implementation.
           </remarks>
9
        public abstract class DoublyLinkedListMethodsBase<TElement> :
10
           GenericCollectionMethodsBase<TElement>
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetPrevious(TElement element);
14
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetNext(TElement element);
16
17
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
            protected abstract void SetPrevious(TElement element, TElement previous);
19
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
            protected abstract void SetNext(TElement element, TElement next);
        }
23
   }
^{24}
     ./csharp/Platform.Collections.Methods/Lists/RelativeCircularDoublyLinkedListMethods.cs
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
3
   {
4
       public abstract class RelativeCircularDoublyLinkedListMethods<TElement> :
5
           RelativeDoublyLinkedListMethodsBase<TElement>
6
            public void AttachBefore(TElement headElement, TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
10
                SetNext(newElement, baseElement);
                if (AreEqual(baseElement, GetFirst(headElement)))
```

```
SetFirst(headElement, newElement);
        SetNext(baseElementPrevious, newElement);
        SetPrevious(baseElement, newElement);
        IncrementSize(headElement);
    }
   public void AttachAfter(TElement headElement, TElement baseElement, TElement newElement)
        var baseElementNext = GetNext(baseElement);
        SetPrevious(newElement, baseElement);
        SetNext(newElement, baseElementNext);
        if (AreEqual(baseElement, GetLast(headElement)))
        {
            SetLast(headElement, newElement);
        SetPrevious(baseElementNext, newElement);
        SetNext(baseElement, newElement);
        IncrementSize(headElement);
   public void AttachAsFirst(TElement headElement, TElement element)
        var first = GetFirst(headElement);
        if (EqualToZero(first))
        {
            SetFirst(headElement, element);
            SetLast(headElement, element);
            SetPrevious(element, element);
            SetNext(element, element);
            IncrementSize(headElement);
        }
        else
        {
            AttachBefore(headElement, first, element);
        }
    }
   public void AttachAsLast(TElement headElement, TElement element)
        var last = GetLast(headElement);
        if (EqualToZero(last))
        {
            AttachAsFirst(headElement, element);
        }
        else
        {
            AttachAfter(headElement, last, element);
        }
    }
   public void Detach(TElement headElement, TElement element)
        var elementPrevious = GetPrevious(element);
        var elementNext = GetNext(element);
        if (AreEqual(elementNext, element))
            SetFirst(headElement, Zero);
            SetLast(headElement, Zero);
        }
        else
            SetNext(elementPrevious, elementNext);
            SetPrevious(elementNext, elementPrevious);
            if (AreEqual(element, GetFirst(headElement)))
            {
                SetFirst(headElement, elementNext);
               (AreEqual(element, GetLast(headElement)))
                SetLast(headElement, elementPrevious);
        SetPrevious(element, Zero);
        SetNext(element, Zero);
        DecrementSize(headElement);
    }
}
```

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21 22

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7.3

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82 83

85 86

88

```
92
     ./csharp/Platform. Collections. Methods/Lists/Relative Doubly Linked List Methods Base.cs
1.7
   using System.Runtime.CompilerServices;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
5
6
       public abstract class RelativeDoublyLinkedListMethodsBase<TElement> :
           DoublyLinkedListMethodsBase<TElement>
8
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetFirst(TElement headElement);
10
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
12
            protected abstract TElement GetLast(TElement headElement);
13
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
15
            protected abstract TElement GetSize(TElement headElement);
16
17
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
            protected abstract void SetFirst(TElement headElement, TElement element);
19
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract void SetLast(TElement headElement, TElement element);
23
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract void SetSize(TElement headElement, TElement size);
25
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
27
            protected void IncrementSize(TElement headElement) => SetSize(headElement,
2.8

→ Increment(GetSize(headElement)));
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
30
            protected void DecrementSize(TElement headElement) => SetSize(headElement,
31
               Decrement(GetSize(headElement)));
       }
32
   }
33
     ./csharp/Platform.Collections.Methods/Lists/RelativeOpenDoublyLinkedListMethods.cs
1.8
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
3
   {
4
       public abstract class RelativeOpenDoublyLinkedListMethods<TElement> :
5
           RelativeDoublyLinkedListMethodsBase<TElement>
6
            public void AttachBefore(TElement headElement, TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
                SetNext(newElement, baseElement);
11
                if (EqualToZero(baseElementPrevious))
12
13
                    SetFirst(headElement, newElement);
14
                }
15
                else
                {
17
                    SetNext(baseElementPrevious, newElement);
18
19
                SetPrevious(baseElement, newElement);
20
                IncrementSize(headElement);
21
            }
23
            public void AttachAfter(TElement headElement, TElement baseElement, TElement newElement)
24
25
                var baseElementNext = GetNext(baseElement);
26
                SetPrevious(newElement, baseElement);
27
                SetNext(newElement, baseElementNext);
                if (EqualToZero(baseElementNext))
29
                {
30
                    SetLast(headElement, newElement);
31
                }
32
                else
33
                {
34
                    SetPrevious(baseElementNext, newElement);
36
                SetNext(baseElement, newElement);
```

```
IncrementSize(headElement);
38
            }
40
            public void AttachAsFirst(TElement headElement, TElement element)
42
                var first = GetFirst(headElement);
43
                if (EqualToZero(first))
44
                    SetFirst(headElement, element);
46
                    SetLast(headElement, element);
47
                    SetPrevious(element, Zero);
48
                    SetNext(element, Zero);
                     IncrementSize(headElement);
50
                }
51
                else
52
                {
53
                     AttachBefore(headElement, first, element);
55
            }
56
57
            public void AttachAsLast(TElement headElement, TElement element)
58
59
                var last = GetLast(headElement);
                if (EqualToZero(last))
61
62
                     AttachAsFirst(headElement, element);
63
                }
                else
65
                {
                     AttachAfter(headElement, last, element);
67
68
            }
70
            public void Detach(TElement headElement, TElement element)
72
                var elementPrevious = GetPrevious(element);
7.3
                var elementNext = GetNext(element);
74
                if (EqualToZero(elementPrevious))
76
                    SetFirst(headElement, elementNext);
77
                }
78
                else
79
                {
80
                    SetNext(elementPrevious, elementNext);
82
                if (EqualToZero(elementNext))
83
                    SetLast(headElement, elementPrevious);
85
                }
86
87
                else
                {
88
                    SetPrevious(elementNext, elementPrevious);
89
                SetPrevious(element, Zero);
91
                SetNext(element, Zero);
92
                DecrementSize(headElement);
93
            }
        }
95
96
     ./csharp/Platform. Collections. Methods/Trees/Recursionless Size Balanced Tree Methods.cs\\
1.9
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
2
3
   namespace Platform.Collections.Methods.Trees
   {
4
        public abstract class RecursionlessSizeBalancedTreeMethods<TElement> :
            SizedBinaryTreeMethodsBase<TElement>
6
            protected override void AttachCore(ref TElement root, TElement node)
                while (true)
10
                     ref var left = ref GetLeftReference(root);
                     var leftSize = GetSizeOrZero(left);
12
                    ref var right = ref GetRightReference(root);
13
                     var rightSize = GetSizeOrZero(right);
14
                     if (FirstIsToTheLeftOfSecond(node, root)) // node.Key less than root.Key
16
                         if (EqualToZero(left))
17
```

```
{
        IncrementSize(root);
        SetSize(node, One);
        left = node;
        return;
    if (FirstIsToTheLeftOfSecond(node, left)) // node.Key less than left.Key
        if (GreaterThan(Increment(leftSize), rightSize))
            RightRotate(ref root);
        }
        else
            IncrementSize(root);
            root = ref left;
    else // node.Key greater than left.Key
        var leftRightSize = GetSizeOrZero(GetRight(left));
        if (GreaterThan(Increment(leftRightSize), rightSize))
            if (EqualToZero(leftRightSize) && EqualToZero(rightSize))
                SetLeft(node, left);
                SetRight(node, root);
                SetSize(node, Add(leftSize, Two)); // Two (2) - node the size of
                 \rightarrow root and a node itself
                SetLeft(root, Zero);
                SetSize(root, One);
                root = node;
                return;
            LeftRotate(ref left);
            RightRotate(ref root);
        }
        else
            IncrementSize(root);
            root = ref left;
    }
else // node.Key greater than root.Key
    if (EqualToZero(right))
        IncrementSize(root);
        SetSize(node, One);
        right = node;
        return;
    if (FirstIsToTheRightOfSecond(node, right)) // node.Key greater than
       right.Key
    {
        if (GreaterThan(Increment(rightSize), leftSize))
        {
            LeftRotate(ref root);
        }
        else
            IncrementSize(root);
            root = ref right;
    else // node.Key less than right.Key
        var rightLeftSize = GetSizeOrZero(GetLeft(right));
        if (GreaterThan(Increment(rightLeftSize), leftSize))
            if (EqualToZero(rightLeftSize) && EqualToZero(leftSize))
            {
                SetLeft(node, root);
                SetRight(node, right);
                SetSize(node, Add(rightSize, Two)); // Two (2) - node the size
                 \hookrightarrow of root and a node itself
                SetRight(root, Zero);
                SetSize(root, One);
```

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91

```
root = node;
                        return;
                    RightRotate(ref right);
                    LeftRotate(ref root);
                else
                {
                    IncrementSize(root);
                    root = ref right;
                }
            }
        }
    }
}
protected override void DetachCore(ref TElement root, TElement node)
    while (true)
        ref var left = ref GetLeftReference(root);
        var leftSize = GetSizeOrZero(left);
        ref var right = ref GetRightReference(root);
        var rightSize = GetSizeOrZero(right);
        if (FirstIsToTheLeftOfSecond(node, root)) // node.Key less than root.Key
            var decrementedLeftSize = Decrement(leftSize);
            if (GreaterThan(GetSizeOrZero(GetRightOrDefault(right)),
                decrementedLeftSize))
            {
                LeftRotate(ref root);
            else if (GreaterThan(GetSizeOrZero(GetLeftOrDefault(right)),
                decrementedLeftSize))
                RightRotate(ref right);
                LeftRotate(ref root);
            }
            else
                DecrementSize(root);
                root = ref left;
        else if (FirstIsToTheRightOfSecond(node, root)) // node.Key greater than root.Key
            var decrementedRightSize = Decrement(rightSize);
            if (GreaterThan(GetSizeOrZero(GetLeftOrDefault(left)), decrementedRightSize))
            {
                RightRotate(ref root);
            else if (GreaterThan(GetSizeOrZero(GetRightOrDefault(left)),
               decrementedRightSize))
                LeftRotate(ref left);
                RightRotate(ref root);
            }
            else
                DecrementSize(root);
                root = ref right;
            }
        else // key equals to root.Key
               (GreaterThanZero(leftSize) && GreaterThanZero(rightSize))
            {
                TElement replacement;
                if (GreaterThan(leftSize, rightSize))
                    replacement = GetRightest(left);
                    DetachCore(ref left, replacement);
                }
                else
                {
                    replacement = GetLeftest(right);
                    DetachCore(ref right, replacement);
                }
```

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163

166

```
SetLeft(replacement, left);
169
                              SetRight(replacement, right);
                              SetSize(replacement, Add(leftSize, rightSize));
171
                              root = replacement;
173
                          else if (GreaterThanZero(leftSize))
174
175
                              root = left;
176
                          }
177
                          else if (GreaterThanZero(rightSize))
                          {
179
180
                              root = right;
                          }
                          else
182
                          {
                              root = Zero;
184
                          ClearNode(node);
186
187
                          return;
                     }
                 }
189
            }
190
        }
191
    }
192
1.10
       ./csharp/Platform.Collections.Methods/Trees/SizeBalancedTreeMethods.cs
    using System;
 2
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
    namespace Platform.Collections.Methods.Trees
 6
        public abstract class SizeBalancedTreeMethods<TElement> :
            SizedBinaryTreeMethodsBase<TElement>
 8
             protected override void AttachCore(ref TElement root, TElement node)
10
                 if (EqualToZero(root))
1.1
                 {
12
                     root = node;
13
                     IncrementSize(root);
14
15
                 else
16
                 {
17
                     IncrementSize(root);
                     if (FirstIsToTheLeftOfSecond(node, root))
19
20
21
                          AttachCore(ref GetLeftReference(root), node);
                          LeftMaintain(ref root);
22
23
                     else
25
                          AttachCore(ref GetRightReference(root), node);
26
                          RightMaintain(ref root);
27
                     }
28
                 }
29
             }
30
31
             protected override void DetachCore(ref TElement root, TElement nodeToDetach)
32
                 ref var currentNode = ref root;
34
                 ref var parent = ref root;
35
                 var replacementNode = Zero;
36
                 while (!AreEqual(currentNode, nodeToDetach))
37
38
                     DecrementSize(currentNode);
39
                     if (FirstIsToTheLeftOfSecond(nodeToDetach, currentNode))
41
                          parent = ref currentNode;
42
                          currentNode = ref GetLeftReference(currentNode);
43
44
                     else if (FirstIsToTheRightOfSecond(nodeToDetach, currentNode))
45
                          parent = ref currentNode;
47
                          currentNode = ref GetRightReference(currentNode);
49
                     else
50
51
                          throw new InvalidOperationException("Duplicate link found in the tree.");
52
```

```
}
    }
    var nodeToDetachLeft = GetLeft(nodeToDetach);
    var node = GetRight(nodeToDetach);
    if (!EqualToZero(nodeToDetachLeft) && !EqualToZero(node))
        var leftestNode = GetLeftest(node);
        DetachCore(ref GetRightReference(nodeToDetach), leftestNode);
        SetLeft(leftestNode, nodeToDetachLeft);
        node = GetRight(nodeToDetach);
        if (!EqualToZero(node))
            SetRight(leftestNode, node);
            SetSize(leftestNode, Increment(Add(GetSize(nodeToDetachLeft),

   GetSize(node))));
        }
        else
        {
            SetSize(leftestNode, Increment(GetSize(nodeToDetachLeft)));
        replacementNode = leftestNode;
    else if (!EqualToZero(nodeToDetachLeft))
        replacementNode = nodeToDetachLeft;
    }
    else if (!EqualToZero(node))
        replacementNode = node;
    if (AreEqual(root, nodeToDetach))
    {
        root = replacementNode;
    else if (AreEqual(GetLeft(parent), nodeToDetach))
        SetLeft(parent, replacementNode);
    }
    else if (AreEqual(GetRight(parent), nodeToDetach))
        SetRight(parent, replacementNode);
    ClearNode(nodeToDetach);
private void LeftMaintain(ref TElement root)
    if (!EqualToZero(root))
        var rootLeftNode = GetLeft(root);
        if (!EqualToZero(rootLeftNode))
            var rootRightNode = GetRight(root);
            var rootRightNodeSize = GetSize(rootRightNode);
            var rootLeftNodeLeftNode = GetLeft(rootLeftNode);
            if (!EqualToZero(rootLeftNodeLeftNode) &&
                (EqualToZero(rootRightNode) ||
                    GreaterThan(GetSize(rootLeftNodeLeftNode), rootRightNodeSize)))
            {
                RightRotate(ref root);
            }
            else
            {
                var rootLeftNodeRightNode = GetRight(rootLeftNode);
                if (!EqualToZero(rootLeftNodeRightNode) &&
                    (EqualToZero(rootRightNode)
                        GreaterThan(GetSize(rootLeftNodeRightNode), rootRightNodeSize)))
                {
                    LeftRotate(ref GetLeftReference(root));
                    RightRotate(ref root);
                }
                else
                {
                    return;
                }
            LeftMaintain(ref GetLeftReference(root))
            RightMaintain(ref GetRightReference(root));
```

5.3

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119

121

123

125

126

```
LeftMaintain(ref root)
128
                         RightMaintain(ref root);
                     }
130
                 }
131
             }
133
            private void RightMaintain(ref TElement root)
134
135
                 if (!EqualToZero(root))
136
                 {
137
                     var rootRightNode = GetRight(root);
138
                     if (!EqualToZero(rootRightNode))
139
140
                          var rootLeftNode = GetLeft(root);
141
142
                          var rootLeftNodeSize = GetSize(rootLeftNode);
                          var rootRightNodeRightNode = GetRight(rootRightNode);
143
                         if (!EqualToZero(rootRightNodeRightNode) &&
144
                              (EqualToZero(rootLeftNode) |
145
                                 GreaterThan(GetSize(rootRightNodeRightNode), rootLeftNodeSize)))
                          {
146
                              LeftRotate(ref root);
147
148
                         else
149
                          {
150
                              var rootRightNodeLeftNode = GetLeft(rootRightNode);
                              if (!EqualToZero(rootRightNodeLeftNode) &&
152
                                  (EqualToZero(rootLeftNode) ||
153
                                      GreaterThan(GetSize(rootRightNodeLeftNode), rootLeftNodeSize)))
154
                                  RightRotate(ref GetRightReference(root));
                                  LeftRotate(ref root);
156
                              }
157
                              else
                              {
159
                                  return;
                              }
161
162
                         LeftMaintain(ref GetLeftReference(root));
163
                         RightMaintain(ref GetRightReference(root));
164
                         LeftMaintain(ref root);
165
                         RightMaintain(ref root);
166
                     }
167
                 }
168
            }
169
        }
    }
171
      ./csharp/Platform.Collections.Methods/Trees/SizedAndThreadedAVLBalancedTreeMethods.cs
1.11
    using System;
    using System.Runtime.CompilerServices;
    using System. Text;
    #if USEARRAYPOOL
    using Platform.Collections;
 5
    #endif
    using Platform. Reflection;
 7
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
    namespace Platform.Collections.Methods.Trees
11
12
         /// <summary>
13
        /// Combination of Size, Height (AVL), and threads.
14
        /// </summary>
15
        /// <remarks>
16
        /// Based on: <a href="https://github.com/programmatom/TreeLib/blob/master/TreeLib/TreeLib/G<sub>|</sub>
17
            enerated/AVLTreeList.cs">TreeLib.AVLTreeList</a>.
        /// Which itself based on: <a
18
            href="https://github.com/GNOME/glib/blob/master/glib/gtree.c">GNOME/glib/gtree</a>.
        /// </remarks>
19
        public abstract class SizedAndThreadedAVLBalancedTreeMethods<TElement> :
20
            SizedBinaryTreeMethodsBase<TElement>
            private static readonly int _maxPath = 11 * NumericType<TElement>.BytesSize + 4;
22
23
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
24
            protected override TElement GetRightest(TElement current)
                 var currentRight = GetRightOrDefault(current);
27
                 while (!EqualToZero(currentRight))
```

```
current = currentRight;
        currentRight = GetRightOrDefault(current);
    return current;
}
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected override TElement GetLeftest(TElement current)
    var currentLeft = GetLeftOrDefault(current);
    while (!EqualToZero(currentLeft))
        current = currentLeft;
        currentLeft = GetLeftOrDefault(current);
    return current;
}
public override bool Contains(TElement node, TElement root)
    while (!EqualToZero(root))
        if (FirstIsToTheLeftOfSecond(node, root)) // node.Key < root.Key</pre>
        {
            root = GetLeftOrDefault(root);
        else if (FirstIsToTheRightOfSecond(node, root)) // node.Key > root.Key
            root = GetRightOrDefault(root);
        else // node.Key == root.Key
            return true;
    return false;
}
protected override void PrintNode(TElement node, StringBuilder sb, int level)
    base.PrintNode(node, sb, level);
    sb.Append(' ');
    sb.Append(GetLeftIsChild(node) ? 'l' : 'L');
    sb.Append(GetRightIsChild(node) ? 'r' : 'R');
    sb.Append(' ');
    sb.Append(GetBalance(node));
}
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected void IncrementBalance(TElement node) => SetBalance(node,
   (sbyte)(GetBalance(node) + 1));
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected void DecrementBalance(TElement node) => SetBalance(node,
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected override TElement GetLeftOrDefault(TElement node) => GetLeftIsChild(node) ?

    GetLeft(node) : default;

[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected override TElement GetRightOrDefault(TElement node) => GetRightIsChild(node) ?
   GetRight(node) : default;
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected abstract bool GetLeftIsChild(TElement node);
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected abstract void SetLeftIsChild(TElement node, bool value);
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected abstract bool GetRightIsChild(TElement node);
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected abstract void SetRightIsChild(TElement node, bool value);
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected abstract sbyte GetBalance(TElement node);
```

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102

```
104
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
106
             protected abstract void SetBalance(TElement node, sbyte value);
             protected override void AttachCore(ref TElement root, TElement node)
108
109
                 unchecked
110
                 {
111
                      // TODO: Check what is faster to use simple array or array from array pool
112
                     // TODO: Try to use stackalloc as an optimization (requires code generation,
113
                        because of generics)
    #if USEARRAYPOOL
114
                      var path = ArrayPool.Allocate<TElement>(MaxPath);
115
                     var pathPosition = 0;
116
                     path[pathPosition++] = default;
117
    #else
118
                     var path = new TElement[_maxPath];
119
                     var pathPosition = 1;
120
    #endif
121
                     var currentNode = root;
122
                     while (true)
123
124
                          if (FirstIsToTheLeftOfSecond(node, currentNode))
125
                          {
126
                              if (GetLeftIsChild(currentNode))
                              {
128
129
                                  IncrementSize(currentNode);
                                  path[pathPosition++] = currentNode;
130
                                   currentNode = GetLeft(currentNode);
131
132
                              else
133
                              {
134
                                   // Threads
135
                                   SetLeft(node, GetLeft(currentNode));
136
137
                                  SetRight(node, currentNode);
                                  SetLeft(currentNode, node);
138
                                  SetLeftIsChild(currentNode, true);
139
                                  DecrementBalance(currentNode);
141
                                  SetSize(node, One);
                                  FixSize(currentNode); // Should be incremented already
142
                                  break;
143
144
145
                          else if (FirstIsToTheRightOfSecond(node, currentNode))
146
147
                              if (GetRightIsChild(currentNode))
148
149
                                   IncrementSize(currentNode);
150
                                  path[pathPosition++] = currentNode;
151
                                  currentNode = GetRight(currentNode);
152
                              }
                              else
154
                                   // Threads
156
                                  SetRight(node, GetRight(currentNode));
157
                                  SetLeft(node, currentNode);
158
                                  SetRight(currentNode, node);
                                  SetRightIsChild(currentNode, true);
160
                                   IncrementBalance(currentNode);
161
162
                                   SetSize(node, One);
                                  FixSize(currentNode); // Should be incremented already
163
                                  break;
164
                              }
                          }
166
                          else
167
168
                              throw new InvalidOperationException("Node with the same key already
169
                               → attached to a tree.");
                          }
170
                      // Restore balance. This is the goodness of a non-recursive
172
                     // implementation, when we are done with balancing we 'break'
173
                     // the loop and we are done.
                     while (true)
175
176
177
                          var parent = path[--pathPosition];
                          var isLeftNode = !AreEqual(parent, default) && AreEqual(currentNode,
178

→ GetLeft(parent));
```

```
var currentNodeBalance = GetBalance(currentNode);
179
                           if (currentNodeBalance < -1 || currentNodeBalance > 1)
181
                                currentNode = Balance(currentNode);
182
                                if (AreEqual(parent, default))
                                {
184
                                    root = currentNode;
185
                                else if (isLeftNode)
187
188
                                    SetLeft(parent, currentNode);
189
190
                                    FixSize(parent);
                                }
191
192
                                else
                                {
193
                                    SetRight(parent, currentNode);
194
                                    FixSize(parent);
196
197
                           currentNodeBalance = GetBalance(currentNode);
198
                              (currentNodeBalance == 0 || AreEqual(parent, default))
199
                           {
200
                                break;
                           }
202
                              (isLeftNode)
203
204
                           {
                                DecrementBalance(parent);
205
                           }
206
                           else
                           {
208
                                IncrementBalance(parent);
209
210
                           currentNode = parent;
211
212
    #if USEARRAYPOOL
213
                      ArrayPool.Free(path);
214
    #endif
215
216
             }
217
218
             private TElement Balance(TElement node)
219
220
                  unchecked
221
222
                       var rootBalance = GetBalance(node);
223
                       if (rootBalance < -1)</pre>
224
                           var left = GetLeft(node);
226
                           if (GetBalance(left) > 0)
227
228
                                SetLeft(node, LeftRotateWithBalance(left));
230
                                FixSize(node);
231
                           node = RightRotateWithBalance(node);
232
233
                      else if (rootBalance > 1)
234
235
                           var right = GetRight(node);
                           if (GetBalance(right) < 0)</pre>
237
                           {
238
                                SetRight(node, RightRotateWithBalance(right));
239
240
                                FixSize(node);
241
242
                           node = LeftRotateWithBalance(node);
243
                      return node;
244
                  }
246
             protected TElement LeftRotateWithBalance(TElement node)
248
249
                  unchecked
250
251
                       var right = GetRight(node);
252
253
                       if (GetLeftIsChild(right))
254
                           SetRight(node, GetLeft(right));
255
256
                       else
257
```

```
SetRightIsChild(node, false);
            SetLeftIsChild(right, true);
        SetLeft(right, node);
        // Fix size
        SetSize(right, GetSize(node));
        FixSize(node);
        // Fix balance
        var rootBalance = GetBalance(node);
        var rightBalance = GetBalance(right);
        if (rightBalance <= 0)</pre>
            if (rootBalance >= 1)
                SetBalance(right, (sbyte)(rightBalance - 1));
            }
            else
            {
                SetBalance(right, (sbyte)(rootBalance + rightBalance - 2));
            SetBalance(node, (sbyte)(rootBalance - 1));
        else
        {
            if
               (rootBalance <= rightBalance)</pre>
                SetBalance(right, (sbyte)(rootBalance - 2));
            }
            else
            {
                SetBalance(right, (sbyte)(rightBalance - 1));
            SetBalance(node, (sbyte)(rootBalance - rightBalance - 1));
        return right;
    }
}
protected TElement RightRotateWithBalance(TElement node)
    unchecked
    {
        var left = GetLeft(node);
        if (GetRightIsChild(left))
            SetLeft(node, GetRight(left));
        }
        else
            SetLeftIsChild(node, false);
            SetRightIsChild(left, true);
        SetRight(left, node);
        // Fix size
        SetSize(left, GetSize(node));
        FixSize(node);
        // Fix balance
        var rootBalance = GetBalance(node);
        var leftBalance = GetBalance(left);
        if (leftBalance <= 0)</pre>
        {
            if (leftBalance > rootBalance)
            {
                SetBalance(left, (sbyte)(leftBalance + 1));
            }
            else
                SetBalance(left, (sbyte)(rootBalance + 2));
            SetBalance(node, (sbyte)(rootBalance - leftBalance + 1));
        else
            i f
                (rootBalance <= -1)
            {
                SetBalance(left, (sbyte)(leftBalance + 1));
            }
```

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 $\frac{326}{327}$

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330 331

332

333

334

```
else
                    {
                        SetBalance(left, (sbyte)(rootBalance + leftBalance + 2));
                    SetBalance(node, (sbyte)(rootBalance + 1));
                return left;
            }
        }
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected override TElement GetNext(TElement node)
            var current = GetRight(node);
            if (GetRightIsChild(node))
                return GetLeftest(current);
            return current;
        }
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected override TElement GetPrevious(TElement node)
            var current = GetLeft(node);
            if (GetLeftIsChild(node))
            {
                return GetRightest(current);
            return current;
        protected override void DetachCore(ref TElement root, TElement node)
            unchecked
#if USEARRAYPOOL
                var path = ArrayPool.Allocate<TElement>(MaxPath);
                var pathPosition = 0;
                path[pathPosition++] = default;
#else
                var path = new TElement[_maxPath];
                var pathPosition = 1;
#endif
                var currentNode = root;
                while (true)
                    if (FirstIsToTheLeftOfSecond(node, currentNode))
                        if (!GetLeftIsChild(currentNode))
                        {
                            throw new InvalidOperationException("Cannot find a node.");
                        DecrementSize(currentNode);
                        path[pathPosition++] = currentNode;
                        currentNode = GetLeft(currentNode);
                    else if (FirstIsToTheRightOfSecond(node, currentNode))
                        if (!GetRightIsChild(currentNode))
                        {
                            throw new InvalidOperationException("Cannot find a node.");
                        DecrementSize(currentNode);
                        path[pathPosition++] = currentNode;
                        currentNode = GetRight(currentNode);
                    }
                    else
                    {
                        break;
                    }
                var parent = path[--pathPosition];
                var balanceNode = parent;
                var isLeftNode = !AreEqual(parent, default) && AreEqual(currentNode,
                    GetLeft(parent));
                   (!GetLeftIsChild(currentNode))
                if
                    if (!GetRightIsChild(currentNode)) // node has no children
```

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```
if (AreEqual(parent, default))
            root = Zero;
        }
        else if (isLeftNode)
            SetLeftIsChild(parent, false);
            SetLeft(parent, GetLeft(currentNode));
            IncrementBalance(parent);
        else
        {
            SetRightIsChild(parent, false);
            SetRight(parent, GetRight(currentNode));
            DecrementBalance(parent);
    else // node has a right child
        var successor = GetNext(currentNode);
        SetLeft(successor, GetLeft(currentNode));
        var right = GetRight(currentNode);
        if (AreEqual(parent, default))
            root = right;
        }
        else if (isLeftNode)
            SetLeft(parent, right);
            IncrementBalance(parent);
        else
        {
            SetRight(parent, right);
            DecrementBalance(parent);
    }
else // node has a left child
      (!GetRightIsChild(currentNode))
    {
        var predecessor = GetPrevious(currentNode);
        SetRight(predecessor, GetRight(currentNode));
        var leftValue = GetLeft(currentNode);
        if (AreEqual(parent, default))
        {
            root = leftValue;
        }
        else if (isLeftNode)
            SetLeft(parent, leftValue);
            IncrementBalance(parent);
        }
        else
            SetRight(parent, leftValue);
            DecrementBalance(parent);
    else // node has a both children (left and right)
        var predecessor = GetLeft(currentNode);
        var successor = GetRight(currentNode);
        var successorParent = currentNode;
        int previousPathPosition = ++pathPosition;
        // find the immediately next node (and its parent)
        while (GetLeftIsChild(successor))
            path[++pathPosition] = successorParent = successor;
            successor = GetLeft(successor);
            if (!AreEqual(successorParent, currentNode))
            {
                DecrementSize(successorParent);
        path[previousPathPosition] = successor;
```

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```
balanceNode = path[pathPosition];
        // remove 'successor' from the tree
        if (!AreEqual(successorParent, currentNode))
            if (!GetRightIsChild(successor))
            {
                 SetLeftIsChild(successorParent, false);
            else
            {
                 SetLeft(successorParent, GetRight(successor));
            IncrementBalance(successorParent);
            SetRightIsChild(successor, true);
            SetRight(successor, GetRight(currentNode));
        }
        else
        {
            DecrementBalance(currentNode);
        // set the predecessor's successor link to point to the right place
        while (GetRightIsChild(predecessor))
            predecessor = GetRight(predecessor);
        SetRight(predecessor, successor);
// prepare 'successor' to replace 'node'
        var left = GetLeft(currentNode);
        SetLeftIsChild(successor, true);
        SetLeft(successor, left);
        SetBalance(successor, GetBalance(currentNode));
        FixSize(successor);
        if (AreEqual(parent, default))
            root = successor;
        }
        else if (isLeftNode)
            SetLeft(parent, successor);
        }
        else
        {
            SetRight(parent, successor);
        }
    }
// restore balance
if (!AreEqual(balanceNode, default))
    while (true)
        var balanceParent = path[--pathPosition];
        isLeftNode = !AreEqual(balanceParent, default) && AreEqual(balanceNode,

→ GetLeft(balanceParent));

        var currentNodeBalance = GetBalance(balanceNode);
        if (currentNodeBalance < -1 || currentNodeBalance > 1)
            balanceNode = Balance(balanceNode);
            if (AreEqual(balanceParent, default))
             {
                root = balanceNode;
            else if (isLeftNode)
                 SetLeft(balanceParent, balanceNode);
            }
            else
            {
                 SetRight(balanceParent, balanceNode);
        currentNodeBalance = GetBalance(balanceNode);
        if (currentNodeBalance != 0 || AreEqual(balanceParent, default))
        {
            break;
        }
           (isLeftNode)
```

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566

```
IncrementBalance(balanceParent);
569
                              }
                              else
571
                              {
                                  DecrementBalance(balanceParent);
573
574
                              balanceNode = balanceParent;
575
                          }
576
577
                     ClearNode(node);
578
    #if USEARRAYPOOL
579
                     ArrayPool.Free(path);
580
    #endif
581
582
             }
583
584
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
585
             protected override void ClearNode(TElement node)
586
587
                 SetLeft(node, Zero);
588
                 SetRight(node, Zero);
589
                 SetSize(node, Zero);
590
                 SetLeftIsChild(node, false);
591
592
                 SetRightIsChild(node, false);
593
                 SetBalance(node, 0);
             }
594
        }
595
    }
596
      ./csharp/Platform.Collections.Methods/Trees/SizedBinaryTreeMethodsBase.cs
    //#define ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
    using System;
 3
    using System. Diagnostics;
    using System.Runtime.CompilerServices;
using System.Text;
    using Platform. Numbers;
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
 9
10
    namespace Platform.Collections.Methods.Trees
11
12
13
        public abstract class SizedBinaryTreeMethodsBase<TElement> :
            GenericCollectionMethodsBase<TElement>
14
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
15
            protected abstract ref TElement GetLeftReference(TElement node);
17
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
            protected abstract ref TElement GetRightReference(TElement node);
20
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetLeft(TElement node);
22
23
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
24
            protected abstract TElement GetRight(TElement node);
25
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
27
            protected abstract TElement GetSize(TElement node);
28
29
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
30
            protected abstract void SetLeft(TElement node, TElement left);
32
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
33
            protected abstract void SetRight(TElement node, TElement right);
35
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
37
            protected abstract void SetSize(TElement node, TElement size);
38
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
39
            protected abstract bool FirstIsToTheLeftOfSecond(TElement first, TElement second);
40
41
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
42
            protected abstract bool FirstIsToTheRightOfSecond(TElement first, TElement second);
43
44
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
45
            protected virtual TElement GetLeftOrDefault(TElement node) => AreEqual(node, default) ?
46
                default : GetLeft(node);
47
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
```

```
protected virtual TElement GetRightOrDefault(TElement node) => AreEqual(node, default) ?
49
             → default : GetRight(node);
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected void IncrementSize(TElement node) => SetSize(node, Increment(GetSize(node)));
52
53
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
54
            protected void DecrementSize(TElement node) => SetSize(node, Decrement(GetSize(node)));
56
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected TElement GetLeftSize(TElement node) => GetSizeOrZero(GetLeftOrDefault(node));
58
59
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected TElement GetRightSize(TElement node) => GetSizeOrZero(GetRightOrDefault(node));
61
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
63
            protected TElement GetSizeOrZero(TElement node) => EqualToZero(node) ? Zero :
64

   GetSize(node);
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
66
            protected void FixSize(TElement node) => SetSize(node, Increment(Add(GetLeftSize(node),
67

   GetRightSize(node))));
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
69
            protected void LeftRotate(ref TElement root) => root = LeftRotate(root);
70
71
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
72
            protected TElement LeftRotate(TElement root)
74
    var right = GetRight(root);
#if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
75
76
                 if (EqualToZero(right))
77
78
                     throw new InvalidOperationException("Right is null.");
79
                 }
80
81
    #endif
                 SetRight(root, GetLeft(right));
82
                 SetLeft(right, root);
83
                 SetSize(right, GetSize(root));
84
                 FixSize(root);
85
                 return right;
86
             }
88
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected void RightRotate(ref TElement root) => root = RightRotate(root);
90
91
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
92
            protected TElement RightRotate(TElement root)
93
94
    var left = GetLeft(root);
#if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
96
                 if (EqualToZero(left))
97
                 {
98
                     throw new InvalidOperationException("Left is null.");
99
                 }
100
    #endif
101
                 SetLeft(root, GetRight(left));
102
                 SetRight(left, root);
                 SetSize(left, GetSize(root));
104
                 FixSize(root);
105
                 return left;
106
107
108
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
109
            protected virtual TElement GetRightest(TElement current)
110
                 var currentRight = GetRight(current);
112
                 while (!EqualToZero(currentRight))
113
114
                     current = currentRight;
115
                     currentRight = GetRight(current);
116
                 return current;
118
119
120
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected virtual TElement GetLeftest(TElement current)
122
123
                 var currentLeft = GetLeft(current);
124
```

```
while (!EqualToZero(currentLeft))
125
                      current = currentLeft;
127
                      currentLeft = GetLeft(current);
129
                 return current;
130
             }
131
132
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected virtual TElement GetNext(TElement node) => GetLeftest(GetRight(node));
134
135
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
136
             protected virtual TElement GetPrevious(TElement node) => GetRightest(GetLeft(node));
137
138
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
139
             public virtual bool Contains(TElement node, TElement root)
140
141
                 while (!EqualToZero(root))
142
143
                      if (FirstIsToTheLeftOfSecond(node, root)) // node.Key < root.Key</pre>
144
                      {
                          root = GetLeft(root);
146
147
                      else if (FirstIsToTheRightOfSecond(node, root)) // node.Key > root.Key
149
                          root = GetRight(root);
150
151
                      else // node.Key == root.Key
152
153
                          return true;
154
155
156
                 return false;
157
158
159
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
160
             protected virtual void ClearNode(TElement node)
161
                 SetLeft(node, Zero)
163
                 SetRight(node, Zero);
164
                 SetSize(node, Zero);
165
             }
167
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             public void Attach(ref TElement root, TElement node)
169
170
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
17\,1
                 ValidateSizes(root);
172
                 Debug.WriteLine("--BeforeAttach--");
173
                 Debug.WriteLine(PrintNodes(root));
174
                 Debug.WriteLine("----"):
175
                 var sizeBefore = GetSize(root);
176
    #endif
177
                 if (EqualToZero(root))
178
179
                      SetSize(node, One);
180
181
                      root = node;
182
                      return;
183
    AttachCore(ref root, node);
#if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
184
185
                 Debug.WriteLine("--AfterAttach--");
186
                 Debug.WriteLine(PrintNodes(root));
187
                 Debug.WriteLine("----");
188
                 ValidateSizes(root)
189
                 var sizeAfter = GetSize(root);
                 if (!AreEqual(Arithmetic.Increment(sizeBefore), sizeAfter))
191
                 {
192
                      throw new InvalidOperationException("Tree was broken after attach.");
193
                 }
    #endif
195
197
198
             protected abstract void AttachCore(ref TElement root, TElement node);
199
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
200
             public void Detach(ref TElement root, TElement node)
201
202
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
203
```

```
ValidateSizes(root);
204
                 Debug.WriteLine("--BeforeDetach--");
                 Debug.WriteLine(PrintNodes(root));
206
                 Debug.WriteLine("----"):
207
                 var sizeBefore = GetSize(root);
                 if (EqualToZero(root))
209
210
                     throw new InvalidOperationException($"Элемент с {node} не содержится в
211
                      → дереве.");
212
    #endif
213
                 DetachCore(ref root, node);
214
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
215
                 Debug.WriteLine("--AfterDetach--");
216
217
                 Debug.WriteLine(PrintNodes(root));
                 Debug.WriteLine("----");
218
                 ValidateSizes(root);
219
                 var sizeAfter = GetSize(root);
220
                 if (!AreEqual(Arithmetic.Decrement(sizeBefore), sizeAfter))
222
                     throw new InvalidOperationException("Tree was broken after detach.");
223
                 }
224
    #endif
225
226
227
             protected abstract void DetachCore(ref TElement root, TElement node);
228
229
             public void FixSizes(TElement node)
230
231
                 if (AreEqual(node, default))
                 {
233
                     return;
234
235
                 FixSizes(GetLeft(node));
236
                 FixSizes(GetRight(node));
                 FixSize(node);
238
239
240
             public void ValidateSizes(TElement node)
241
242
                 if (AreEqual(node, default))
243
                 {
244
                     return;
245
                 }
246
                 var size = GetSize(node);
247
                 var leftSize = GetLeftSize(node);
248
                 var rightSize = GetRightSize(node);
249
                 var expectedSize = Arithmetic.Increment(Arithmetic.Add(leftSize, rightSize));
250
                 if (!AreEqual(size, expectedSize))
251
252
                     throw new InvalidOperationException($ "Size of {node} is not valid. Expected
253

    size: {expectedSize}, actual size: {size}.");
                 ValidateSizes(GetLeft(node));
255
                 ValidateSizes(GetRight(node));
256
             }
258
             public void ValidateSize(TElement node)
259
                 var size = GetSize(node);
261
                 var leftSize = GetLeftSize(node);
262
                 var rightSize = GetRightSize(node);
                 var expectedSize = Arithmetic.Increment(Arithmetic.Add(leftSize, rightSize));
264
                 if (!AreEqual(size, expectedSize))
265
266
                     throw new InvalidOperationException($\B\"Size of \{node\} is not valid. Expected

    size: {expectedSize}, actual size: {size}.");
                 }
             }
269
270
             public string PrintNodes(TElement node)
271
272
273
                 var sb = new StringBuilder();
274
                 PrintNodes(node, sb);
                 return sb.ToString();
275
276
277
278
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
```

```
public void PrintNodes(TElement node, StringBuilder sb) => PrintNodes(node, sb, 0);
279
280
             public void PrintNodes(TElement node, StringBuilder sb, int level)
281
                 if (AreEqual(node, default))
283
                 {
284
                     return;
285
286
                 PrintNodes(GetLeft(node), sb, level + 1);
287
                 PrintNode(node, sb, level);
                 sb.AppendLine();
289
                 PrintNodes(GetRight(node), sb, level + 1);
290
             }
291
292
             public string PrintNode(TElement node)
293
                 var sb = new StringBuilder();
295
                 PrintNode(node, sb)
296
                 return sb.ToString();
298
299
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected void PrintNode(TElement node, StringBuilder sb) => PrintNode(node, sb, 0);
301
302
             protected virtual void PrintNode(TElement node, StringBuilder sb, int level)
303
304
                 sb.Append('\t', level);
305
                 sb.Append(node);
306
                 PrintNodeValue(node, sb);
307
                 sb.Append(' ');
308
                 sb.Append('s');
309
                 sb.Append(GetSize(node));
310
311
             protected abstract void PrintNodeValue(TElement node, StringBuilder sb);
313
        }
314
315
1.13
       ./csharp/Platform.Collections.Methods.Tests/RecursionlessSizeBalancedTree.cs
    using System;
    using System. Collections. Generic;
    using System.Text;
    using Platform.Numbers;
using Platform.Collections.Methods.Trees;
 4
    using Platform.Converters;
    namespace Platform.Collections.Methods.Tests
 9
        public class RecursionlessSizeBalancedTree<TElement> :
10
            RecursionlessSizeBalancedTreeMethods<TElement>
11
             private struct TreeElement
12
13
                 public TElement Size;
                 public
                        TElement Left;
15
                 public TElement Right;
16
17
             private readonly TreeElement[] _elements;
19
             private TElement _allocated;
2.1
             public TElement Root;
22
23
             public TElement Count => GetSizeOrZero(Root);
             public RecursionlessSizeBalancedTree(int capacity) => (_elements, _allocated) = (new
             → TreeElement[capacity], One);
27
             public TElement Allocate()
28
29
                 var newNode = _allocated;
                 if (IsEmpty(newNode))
31
32
                      _allocated = Arithmetic.Increment(_allocated);
33
34
                     return newNode;
                 }
35
36
                 else
37
                     throw new InvalidOperationException("Allocated tree element is not empty.");
38
                 }
```

```
40
41
           public void Free(TElement node)
42
                while (!EqualityComparer.Equals(_allocated, One) && IsEmpty(node))
44
45
                    var lastNode = Arithmetic.Decrement(_allocated);
46
                    if (EqualityComparer.Equals(lastNode, node))
47
48
                        _allocated = lastNode;
49
                        node = Arithmetic.Decrement(node);
50
                    }
51
52
                    else
                    {
53
                        return;
55
                }
56
            }
58
           public bool IsEmpty(TElement node) =>
59
            60
           protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
61

→ Comparer.Compare(first, second) < 0;
</p>
62
           protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>
63
               Comparer.Compare(first, second) > 0;
           protected override ref TElement GetLeftReference(TElement node) => ref
65

   GetElement(node).Left;
66
           protected override TElement GetLeft(TElement node) => GetElement(node).Left;
67
68
           protected override ref TElement GetRightReference(TElement node) => ref
69

   GetElement(node).Right;
70
           protected override TElement GetRight(TElement node) => GetElement(node).Right;
72
           protected override TElement GetSize(TElement node) => GetElement(node).Size;
73
74
           protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
75

⇒ sb.Append(node);

76
           protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
77
            → left;
78
           protected override void SetRight(TElement node, TElement right) =>
79

   GetElement(node).Right = right;

80
           protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =
81

→ size;

82
           private ref TreeElement GetElement(TElement node) => ref
83
               _elements[UncheckedConverter<TElement, long>.Default.Convert(node)];
       }
84
   }
85
     ./csharp/Platform.Collections.Methods.Tests/SizeBalancedTree.cs
1.14
   using System;
   using System.Collections.Generic;
   using System. Text;
3
   using Platform. Numbers;
4
   using Platform.Collections.Methods.Trees;
   using Platform.Converters;
   namespace Platform.Collections.Methods.Tests
8
9
       public class SizeBalancedTree<TElement> : SizeBalancedTreeMethods<TElement>
10
           private struct TreeElement
12
13
                public TElement Size;
public TElement Left;
14
                public TElement Right;
16
            }
17
18
           private readonly TreeElement[] _elements;
private TElement _allocated;
20
21
           public TElement Root;
```

```
23
           public TElement Count => GetSizeOrZero(Root);
2.5
           public SizeBalancedTree(int capacity) => (_elements, _allocated) = (new

→ TreeElement[capacity], One);
27
           public TElement Allocate()
28
                var newNode = _allocated;
30
                if (IsEmpty(newNode))
32
                    _allocated = Arithmetic.Increment(_allocated);
33
                    return newNode;
                }
35
                else
                {
37
                    throw new InvalidOperationException("Allocated tree element is not empty.");
38
39
           }
40
41
           public void Free(TElement node)
43
                while (!EqualityComparer.Equals(_allocated, One) && IsEmpty(node))
44
                    var lastNode = Arithmetic.Decrement(_allocated);
46
                    if (EqualityComparer.Equals(lastNode, node))
47
48
                        _allocated = lastNode;
49
                        node = Arithmetic.Decrement(node);
50
                    else
52
                    {
                        return;
54
                    }
55
                }
           }
57
           public bool IsEmpty(TElement node) =>
59
            Gefault.Equals(GetElement(node), default);
60
           protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>

→ Comparer.Compare(first, second) < 0;
</p>
62
           protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>
63

→ Comparer.Compare(first, second) > 0;
64
           protected override ref TElement GetLeftReference(TElement node) => ref
65

   GetElement(node).Left;
66
           protected override TElement GetLeft(TElement node) => GetElement(node).Left;
67
68
           protected override ref TElement GetRightReference(TElement node) => ref
69

   GetElement(node).Right;
           protected override TElement GetRight(TElement node) => GetElement(node).Right;
7.1
           protected override TElement GetSize(TElement node) => GetElement(node).Size;
73
           protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
75

⇒ sb.Append(node);

76
           protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
            → left;
           protected override void SetRight(TElement node, TElement right) =>
79

   GetElement(node).Right = right;
80
           protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =

→ size;

           private ref TreeElement GetElement(TElement node) => ref
83
            - _ elements[UncheckedConverter<TElement, long>.Default.Convert(node)];
       }
84
   }
85
      ./csharp/Platform.Collections.Methods.Tests/SizedAndThreadedAVLBalancedTree.cs
1.15
   using System;
1
   using System.Collections.Generic;
```

using System. Text;

```
using Platform. Numbers;
4
   using Platform.Collections.Methods.Trees;
5
   using Platform.Converters;
   namespace Platform.Collections.Methods.Tests
9
       public class SizedAndThreadedAVLBalancedTree<TElement> :
10
           SizedAndThreadedAVLBalancedTreeMethods<TElement>
11
            private struct TreeElement
12
13
                public TElement Size;
                public
                       TElement Left;
15
                public TElement Right;
16
                public sbyte Balance;
                public bool LeftIsChild;
public bool RightIsChild;
18
19
20
           private readonly TreeElement[] _elements;
22
           private TElement _allocated;
23
24
           public TElement Root;
25
26
           public TElement Count => GetSizeOrZero(Root);
27
           public SizedAndThreadedAVLBalancedTree(int capacity) => (_elements, _allocated) = (new
            → TreeElement[capacity], One);
30
           public TElement Allocate()
31
32
                var newNode = _allocated;
33
                if (IsEmpty(newNode))
35
                    _allocated = Arithmetic.Increment(_allocated);
36
37
                    return newNode;
                }
38
                else
39
                {
40
                    throw new InvalidOperationException("Allocated tree element is not empty.");
41
                }
42
            }
43
44
           public void Free(TElement node)
45
46
                while (!EqualityComparer.Equals(_allocated, One) && IsEmpty(node))
47
48
                    var lastNode = Arithmetic.Decrement(_allocated);
49
                    if (EqualityComparer.Equals(lastNode, node))
50
                        _allocated = lastNode;
52
                        node = Arithmetic.Decrement(node);
53
                    }
                    else
55
                    {
                        return;
57
                    }
58
                }
59
            }
60
           public bool IsEmpty(TElement node) =>
62
            protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
64

→ Comparer.Compare(first, second) < 0;
</p>
65
           protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>

→ Comparer.Compare(first, second) > 0;

67
           protected override sbyte GetBalance(TElement node) => GetElement(node).Balance;
69
           protected override bool GetLeftIsChild(TElement node) => GetElement(node).LeftIsChild;
7.1
           protected override ref TElement GetLeftReference(TElement node) => ref
72

   GetElement(node).Left;
7.3
           protected override TElement GetLeft(TElement node) => GetElement(node).Left;
74
75
           protected override bool GetRightIsChild(TElement node) => GetElement(node).RightIsChild;
76
77
```

```
protected override ref TElement GetRightReference(TElement node) => ref
7.8
               GetElement(node).Right;
79
            protected override TElement GetRight(TElement node) => GetElement(node).Right;
80
81
            protected override TElement GetSize(TElement node) => GetElement(node).Size;
82
83
            protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
84

⇒ sb.Append(node);

            protected override void SetBalance(TElement node, sbyte value) =>
               GetElement(node) . Balance = value;
            protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
             → left;
            protected override void SetLeftIsChild(TElement node, bool value) =>
90

    GetElement(node).LeftIsChild = value;

            protected override void SetRight(TElement node, TElement right) =>

   GetElement(node).Right = right;

93
            protected override void SetRightIsChild(TElement node, bool value) =>

    GetElement(node).RightIsChild = value;

95
            protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =
96

→ size;

            private ref TreeElement GetElement(TElement node) => ref
               _elements[UncheckedConverter<TElement, long>.Default.Convert(node)];
        }
99
    }
100
1.16
      ./csharp/Platform.Collections.Methods.Tests/TestExtensions.cs
   using System;
   using System.Collections.Generic;
         Xŭnit;
    using
   using Platform.Collections.Methods.Trees;
 4
   using Platform.Converters;
   namespace Platform.Collections.Methods.Tests
7
 8
        public static class TestExtensions
 9
10
            public static void TestMultipleCreationsAndDeletions<TElement>(this
11
                SizedBinaryTreeMethodsBase<TElement> tree, Func<TElement> allocate, Action<TElement>
                free, ref TElement root, Func<TElement> treeCount, int maximumOperationsPerCycle)
12
                for (var N = 1; N < maximumOperationsPerCycle; N++)</pre>
1.3
                     var currentCount = 0;
15
                    for (var i = 0; i < N; i++)</pre>
16
17
                         var node = allocate();
18
                         tree.Attach(ref root, node);
19
                         currentCount++;
20
                         Assert.Equal(currentCount, (int)UncheckedConverter<TElement,
21
                            int>.Default.Convert(treeCount()));
                    }
22
                    for (var i = 1; i <= N; i++)</pre>
23
24
                         TElement node = UncheckedConverter<int, TElement>.Default.Convert(i);
                         if (tree.Contains(node, root))
27
                             tree.Detach(ref root, node);
28
                             free(node);
                             currentCount--:
30
                             Assert.Equal(currentCount, (int)UncheckedConverter<TElement,
31
                                int>.Default.Convert(treeCount()));
                        }
                    }
33
                }
34
            }
36
            public static void TestMultipleRandomCreationsAndDeletions<TElement>(this
37
                SizedBinaryTreeMethodsBase<TElement> tree, ref TElement root, Func<TElement>
                treeCount, int maximumOperationsPerCycle)
38
                var random = new System.Random(0);
39
```

```
var added = new HashSet<TElement>();
40
                var currentCount = 0;
41
                for (var N = 1; N < maximumOperationsPerCycle; N++)</pre>
42
                    for (var i = 0; i < N; i++)</pre>
44
45
                         var node = UncheckedConverter<int, TElement>.Default.Convert(random.Next(1,
46
                            N)):
                         if (added.Add(node))
                         {
48
                             tree.Attach(ref root, node);
49
                             currentCount++;
                             {\tt Assert.Equal(currentCount,\ (int)UncheckedConverter{<}TElement,}\\
51
                                int>.Default.Convert(treeCount()));
                         }
52
53
                    for (var i = 1; i <= N; i++)</pre>
54
55
                         TElement node = UncheckedConverter<int,
                             TElement>.Default.Convert(random.Next(1, N));
                         if (tree.Contains(node, root))
57
58
                             tree.Detach(ref root, node);
                             currentCount--;
60
                             Assert.Equal(currentCount, (int)UncheckedConverter<TElement,
61
                              → int>.Default.Convert(treeCount()));
                             added.Remove(node);
                         }
63
                    }
64
                }
            }
66
        }
67
   }
68
1.17
      ./csharp/Platform.Collections.Methods.Tests/TreesTests.cs
   using Xunit;
   namespace Platform.Collections.Methods.Tests
3
4
        public static class TreesTests
5
6
            private const int _n = 500;
            [Fact]
            public static void RecursionlessSizeBalancedTreeMultipleAttachAndDetachTest()
10
11
                var recursionlessSizeBalancedTree = new RecursionlessSizeBalancedTree<uint>(10000);
                recursionlessSizeBalancedTree.TestMultipleCreationsAndDeletions(recursionlessSizeBal
13
                    ancedTree.Allocate, recursionlessSizeBalancedTree.Free, ref
                    recursionlessSizeBalancedTree.Root, () => recursionlessSizeBalancedTree.Count,
                    _n);
            }
1.5
            [Fact]
            public static void SizeBalancedTreeMultipleAttachAndDetachTest()
17
18
                var sizeBalancedTree = new SizeBalancedTree<uint>(10000);
19
                sizeBalancedTree.TestMultipleCreationsAndDeletions(sizeBalancedTree.Allocate,

→ sizeBalancedTree.Free, ref sizeBalancedTree.Root, () => sizeBalancedTree.Count,

                    _n);
            }
22
            [Fact]
24
            public static void SizedAndThreadedAVLBalancedTreeMultipleAttachAndDetachTest()
25
                var avlTree = new SizedAndThreadedAVLBalancedTree<uint>(10000);
26
                avlTree.TestMultipleCreationsAndDeletions(avlTree.Allocate, avlTree.Free, ref
                 → avlTree.Root, () => avlTree.Count, _n);
            }
            [Fact]
30
            public static void RecursionlessSizeBalancedTreeMultipleRandomAttachAndDetachTest()
31
32
                var recursionlessSizeBalancedTree = new RecursionlessSizeBalancedTree<uint>(10000);
33
                {\tt recursionlessSizeBalancedTree.TestMultipleRandomCreationsAndDeletions (reflections)} \\
34
                 recursionlessSizeBalancedTree.Root, () => recursionlessSizeBalancedTree.Count,
                    _n);
            }
```

```
[Fact]
37
           public static void SizeBalancedTreeMultipleRandomAttachAndDetachTest()
39
               var sizeBalancedTree = new SizeBalancedTree<uint>(10000);
40
              sizeBalancedTree.TestMultipleRandomCreationsAndDeletions(ref sizeBalancedTree.Root,
               }
42
43
           [Fact]
          public static void SizedAndThreadedAVLBalancedTreeMultipleRandomAttachAndDetachTest()
45
46
              var avlTree = new SizedAndThreadedAVLBalancedTree<uint>(10000);
47
              avlTree.TestMultipleRandomCreationsAndDeletions(ref avlTree.Root, () =>
               → avlTree.Count, _n);
           }
49
       }
50
51
```

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