```
LinksPlatform's Platform Collections Methods Class Library
     ./csharp/Platform. Collections. Methods/Generic Collection Methods Base.cs\\
   using System.Collections.Generic;
   using System.Runtime.CompilerServices;
2
   using Platform.Numbers;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods
        public abstract class GenericCollectionMethodsBase<TElement>
10
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
11
            protected virtual TElement GetZero() => default;
13
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
14
            protected virtual bool EqualToZero(TElement value) => EqualityComparer.Equals(value,

    Zero);

16
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
17
            protected virtual bool AreEqual(TElement first, TElement second) =>

→ EqualityComparer.Equals(first, second);

19
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool GreaterThanZero(TElement value) => Comparer.Compare(value, Zero)
            \rightarrow > 0;
22
23
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool GreaterThan(TElement first, TElement second) =>
24

→ Comparer.Compare(first, second) > 0;

25
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
26
            protected virtual bool GreaterOrEqualThanZero(TElement value) => Comparer.Compare(value,
            \rightarrow Zero) >= 0;
2.8
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
2.9
            protected virtual bool GreaterOrEqualThan(TElement first, TElement second) =>
                Comparer.Compare(first, second) >= 0;
31
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
32
            protected virtual bool LessOrEqualThanZero(TElement value) => Comparer.Compare(value,
             \rightarrow Zero) <= 0;
34
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool LessOrEqualThan(TElement first, TElement second) =>
36

→ Comparer.Compare(first, second) <= 0;
</p>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool LessThanZero(TElement value) => Comparer.Compare(value, Zero) < 0;</pre>
39
40
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
41
            protected virtual bool LessThan(TElement first, TElement second) =>
42
                Comparer.Compare(first, second) < 0;</pre>
43
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
44
            protected virtual TElement Increment(TElement value) =>
45
                Arithmetic<TElement>.Increment(value);
46
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
47
            protected virtual TElement Decrement(TElement value) =>
            → Arithmetic<TElement>.Decrement(value);
49
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
50
            protected virtual TElement Add(TElement first, TElement second) =>
                Arithmetic<TElement>.Add(first, second);
52
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual TElement Subtract(TElement first, TElement second) =>
               Arithmetic<TElement>.Subtract(first, second);
55
            protected readonly TElement Zero;
protected readonly TElement One;
            protected readonly TElement Two;
protected readonly EqualityComparer<TElement> EqualityComparer;
58
            protected readonly Comparer<TElement> Comparer;
60
61
            protected GenericCollectionMethodsBase()
62
63
                EqualityComparer = EqualityComparer<TElement>.Default;
64
```

```
Comparer = Comparer<TElement>.Default;
65
                Zero = GetZero(); //-V3068
                One = Increment(Zero); //-V3068
67
                Two = Increment(One); //-V3068
68
            }
        }
70
7.1
     ./csharp/Platform.Collections.Methods/Lists/CircularDoublyLinkedListMethods.cs
1.2
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
3
4
        public abstract class CircularDoublyLinkedListMethods<TElement> :
           DoublyLinkedListMethodsBase<TElement>
6
            public void AttachBefore(TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
10
                SetNext(newElement, baseElement);
11
                if (AreEqual(baseElement, GetFirst()))
12
                {
13
                    SetFirst(newElement);
14
15
                SetNext(baseElementPrevious, newElement);
16
                SetPrevious(baseElement, newElement);
17
                IncrementSize();
            }
19
20
            public void AttachAfter(TElement baseElement, TElement newElement)
21
22
                var baseElementNext = GetNext(baseElement);
23
                SetPrevious(newElement, baseElement);
                SetNext(newElement, baseElementNext);
25
                if (AreEqual(baseElement, GetLast()))
26
27
                    SetLast(newElement);
28
29
                SetPrevious(baseElementNext, newElement);
30
                SetNext(baseElement, newElement);
                IncrementSize();
32
            }
33
34
            public void AttachAsFirst(TElement element)
35
36
                var first = GetFirst();
                if (EqualToZero(first))
38
39
                    SetFirst(element);
                    SetLast(element);
41
                    SetPrevious(element, element);
42
                    SetNext(element, element);
43
                    IncrementSize();
                }
45
                else
46
                {
47
                     AttachBefore(first, element);
48
            }
51
            public void AttachAsLast(TElement element)
53
                var last = GetLast();
54
                if (EqualToZero(last))
                {
56
                     AttachAsFirst(element);
57
                }
58
                else
59
                {
60
                     AttachAfter(last, element);
62
            }
63
64
            public void Detach(TElement element)
65
66
                var elementPrevious = GetPrevious(element);
                var elementNext = GetNext(element);
68
```

```
if (AreEqual(elementNext, element))
6.9
                    SetFirst(Zero);
7.1
                    SetLast(Zero);
72
                }
                else
74
75
                    SetNext(elementPrevious, elementNext);
76
                    SetPrevious(elementNext, elementPrevious);
77
                    if (AreEqual(element, GetFirst()))
78
                        SetFirst(elementNext);
80
                    }
81
                    if (AreEqual(element, GetLast()))
82
                        SetLast(elementPrevious);
84
85
                SetPrevious(element, Zero);
87
                SetNext(element, Zero);
88
                DecrementSize();
89
            }
       }
91
92
     ./csharp/Platform.Collections.Methods/Lists/DoublyLinkedListMethodsBase.cs
1.3
   using System.Runtime.CompilerServices;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
        /// <remarks>
       /// Based on <a href="https://en.wikipedia.org/wiki/Doubly_linked_list">doubly linked
           list</a> implementation.
        /// </remarks>
       public abstract class DoublyLinkedListMethodsBase<TElement> :
10
           GenericCollectionMethodsBase<TElement>
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetFirst();
13
14
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
15
            protected abstract TElement GetLast();
16
17
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
            protected abstract TElement GetPrevious(TElement element);
19
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
            protected abstract TElement GetNext(TElement element);
23
24
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetSize();
26
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract void SetFirst(TElement element);
28
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
30
            protected abstract void SetLast(TElement element);
31
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
33
            protected abstract void SetPrevious(TElement element, TElement previous);
34
35
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
36
            protected abstract void SetNext(TElement element, TElement next);
38
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
39
            protected abstract void SetSize(TElement size);
40
41
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected void IncrementSize() => SetSize(Increment(GetSize()));
43
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
45
            protected void DecrementSize() => SetSize(Decrement(GetSize()));
46
       }
47
   }
```

```
./csharp/Platform.Collections.Methods/Lists/OpenDoublyLinkedListMethods.cs
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
4
   {
        public abstract class OpenDoublyLinkedListMethods<TElement> :
           DoublyLinkedListMethodsBase<TElement>
6
            public void AttachBefore(TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
10
                SetNext(newElement, baseElement);
11
12
                if (EqualToZero(baseElementPrevious))
                {
13
                    SetFirst(newElement);
14
                }
                else
16
                {
17
                    SetNext(baseElementPrevious, newElement);
18
19
                SetPrevious(baseElement, newElement);
20
                IncrementSize();
            }
22
23
            public void AttachAfter(TElement baseElement, TElement newElement)
25
                var baseElementNext = GetNext(baseElement);
26
                SetPrevious(newElement, baseElement);
                SetNext(newElement, baseElementNext);
28
                if (EqualToZero(baseElementNext))
29
30
                    SetLast(newElement);
31
                }
32
                else
                {
34
                    SetPrevious(baseElementNext, newElement);
35
36
                SetNext(baseElement, newElement);
37
                IncrementSize();
38
            }
39
40
            public void AttachAsFirst(TElement element)
41
42
                var first = GetFirst();
43
                if (EqualToZero(first))
44
45
                    SetFirst(element);
                    SetLast(element);
47
                    SetPrevious(element, Zero);
48
                    SetNext(element, Zero);
                    IncrementSize();
50
                }
51
                else
53
                     AttachBefore(first, element);
54
                }
            }
56
            public void AttachAsLast(TElement element)
59
                var last = GetLast()
60
                if (EqualToZero(last))
62
                     AttachAsFirst(element);
63
                }
                else
65
66
                     AttachAfter(last, element);
67
68
            }
69
70
            public void Detach(TElement element)
7.1
                var elementPrevious = GetPrevious(element);
73
                var elementNext = GetNext(element);
74
                if (EqualToZero(elementPrevious))
75
```

```
SetFirst(elementNext);
                }
                else
79
                {
                     SetNext(elementPrevious, elementNext);
81
82
                if (EqualToZero(elementNext))
83
                     SetLast(elementPrevious);
85
                }
86
                else
87
                {
88
                     SetPrevious(elementNext, elementPrevious);
89
                SetPrevious(element, Zero);
91
                SetNext(element, Zero);
92
                DecrementSize();
            }
94
        }
95
96
     ./csharp/Platform.Collections.Methods/Trees/RecursionlessSizeBalancedTreeMethods.cs
1.5
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
-1
   namespace Platform.Collections.Methods.Trees
3
        public abstract class RecursionlessSizeBalancedTreeMethods<TElement> :
5
           SizedBinaryTreeMethodsBase<TElement>
6
            protected override void AttachCore(ref TElement root, TElement node)
                while (true)
10
                     ref var left = ref GetLeftReference(root);
11
                     var leftSize = GetSizeOrZero(left);
                     ref var right = ref GetRightReference(root);
                     var rightSize = GetSizeOrZero(right);
14
                     if (FirstIsToTheLeftOfSecond(node, root)) // node.Key less than root.Key
15
16
                         if (EqualToZero(left))
17
                         {
18
                             IncrementSize(root);
19
                             SetSize(node, One);
                             left = node;
21
                             return;
22
23
                         if (FirstIsToTheLeftOfSecond(node, left)) // node.Key less than left.Key
25
                             if (GreaterThan(Increment(leftSize), rightSize))
26
                             {
27
                                  RightRotate(ref root);
28
                             }
29
                             else
31
                                  IncrementSize(root);
32
                                  root = ref left;
33
34
35
                               // node.Key greater than left.Key
                         else
37
                             var leftRightSize = GetSizeOrZero(GetRight(left));
38
                             if (GreaterThan(Increment(leftRightSize), rightSize))
39
40
                                  if (EqualToZero(leftRightSize) && EqualToZero(rightSize))
41
42
                                  {
                                      SetLeft(node, left);
44
                                      SetRight(node, root);
                                      SetSize(node, Add(leftSize, Two)); // Two (2) - node the size of
45
                                       \hookrightarrow root and a node itself
                                      SetLeft(root, Zero);
46
                                      SetSize(root, One);
47
                                      root = node;
                                      return;
49
                                 LeftRotate(ref left);
51
                                  RightRotate(ref root);
52
                             }
53
                             else
54
```

```
IncrementSize(root);
                    root = ref left;
                }
            }
        else // node.Key greater than root.Key
            if (EqualToZero(right))
                IncrementSize(root);
                SetSize(node, One);
                right = node;
                return;
            if (FirstIsToTheRightOfSecond(node, right)) // node.Key greater than
                right.Key
                if (GreaterThan(Increment(rightSize), leftSize))
                    LeftRotate(ref root);
                }
                else
                {
                    IncrementSize(root);
                    root = ref right;
            else // node.Key less than right.Key
                var rightLeftSize = GetSizeOrZero(GetLeft(right));
                   (GreaterThan(Increment(rightLeftSize), leftSize))
                    if (EqualToZero(rightLeftSize) && EqualToZero(leftSize))
                        SetLeft(node, root);
                        SetRight(node, right);
                        SetSize(node, Add(rightSize, Two)); // Two (2) - node the size
                            of root and a node itself
                        SetRight(root, Zero);
                        SetSize(root, One);
                        root = node;
                        return;
                    RightRotate(ref right);
                    LeftRotate(ref root);
                }
                else
                    IncrementSize(root);
                    root = ref right;
                }
            }
        }
    }
}
protected override void DetachCore(ref TElement root, TElement node)
    while (true)
        ref var left = ref GetLeftReference(root);
        var leftSize = GetSizeOrZero(left);
        ref var right = ref GetRightReference(root);
        var rightSize = GetSizeOrZero(right);
        if (FirstIsToTheLeftOfSecond(node, root)) // node.Key less than root.Key
            var decrementedLeftSize = Decrement(leftSize);
            if (GreaterThan(GetSizeOrZero(GetRightOrDefault(right)),
                decrementedLeftSize))
            {
                LeftRotate(ref root);
            }
            else if (GreaterThan(GetSizeOrZero(GetLeftOrDefault(right)),
                decrementedLeftSize))
            {
                RightRotate(ref right);
                LeftRotate(ref root);
            }
```

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126

127

128

```
else
130
                              DecrementSize(root);
132
                              root = ref left;
134
135
                      else if (FirstIsToTheRightOfSecond(node, root)) // node.Key greater than root.Key
136
137
                          var decrementedRightSize = Decrement(rightSize);
138
                          if (GreaterThan(GetSizeOrZero(GetLeftOrDefault(left)), decrementedRightSize))
139
140
                          {
                              RightRotate(ref root);
141
                          }
142
143
                          else if (GreaterThan(GetSizeOrZero(GetRightOrDefault(left)),
                              decrementedRightSize))
                              LeftRotate(ref left);
145
                              RightRotate(ref root);
146
                          else
148
149
                              DecrementSize(root);
                              root = ref right;
151
153
                      else // key equals to root. Key
154
155
                             (GreaterThanZero(leftSize) && GreaterThanZero(rightSize))
156
                          if
                          {
157
                              TElement replacement;
                              if (GreaterThan(leftSize, rightSize))
159
160
                                   replacement = GetRightest(left);
161
                                   DetachCore(ref left, replacement);
162
                              }
163
                              else
165
                                   replacement = GetLeftest(right);
166
167
                                   DetachCore(ref right, replacement);
168
                              SetLeft(replacement, left);
169
                              SetRight(replacement, right);
170
                              SetSize(replacement, Add(leftSize, rightSize));
171
                              root = replacement;
172
173
                          else if (GreaterThanZero(leftSize))
174
                          {
175
                              root = left;
176
                          }
177
                          else if (GreaterThanZero(rightSize))
178
179
                              root = right;
180
                          }
                          else
182
                          {
183
                              root = Zero:
184
185
                          ClearNode(node);
                          return;
187
                     }
188
                 }
189
             }
190
        }
191
     ./csharp/Platform.Collections.Methods/Trees/SizeBalancedTreeMethods.cs
    using System;
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
    namespace Platform.Collections.Methods.Trees
 6
        public abstract class SizeBalancedTreeMethods<TElement> :
            SizedBinaryTreeMethodsBase<TElement>
             protected override void AttachCore(ref TElement root, TElement node)
10
                 if (EqualToZero(root))
11
```

```
root = node;
        IncrementSize(root);
    }
    else
    {
        IncrementSize(root);
        if (FirstIsToTheLeftOfSecond(node, root))
            AttachCore(ref GetLeftReference(root), node);
            LeftMaintain(ref root);
        }
        else
            AttachCore(ref GetRightReference(root), node);
            RightMaintain(ref root);
        }
    }
}
protected override void DetachCore(ref TElement root, TElement nodeToDetach)
    ref var currentNode = ref root;
    ref var parent = ref root;
    var replacementNode = Zero;
    while (!AreEqual(currentNode, nodeToDetach))
        DecrementSize(currentNode);
        if (FirstIsToTheLeftOfSecond(nodeToDetach, currentNode))
            parent = ref currentNode;
            currentNode = ref GetLeftReference(currentNode);
        else if (FirstIsToTheRightOfSecond(nodeToDetach, currentNode))
            parent = ref currentNode;
            currentNode = ref GetRightReference(currentNode);
        else
        {
            throw new InvalidOperationException("Duplicate link found in the tree.");
        }
    }
    var nodeToDetachLeft = GetLeft(nodeToDetach);
    var node = GetRight(nodeToDetach);
    if (!EqualToZero(nodeToDetachLeft) && !EqualToZero(node))
        var leftestNode = GetLeftest(node);
        DetachCore(ref GetRightReference(nodeToDetach), leftestNode);
        SetLeft(leftestNode, nodeToDetachLeft);
        node = GetRight(nodeToDetach);
        if (!EqualToZero(node))
            SetRight(leftestNode, node);
SetSize(leftestNode, Increment(Add(GetSize(nodeToDetachLeft),

   GetSize(node)));
        }
        else
        {
            SetSize(leftestNode, Increment(GetSize(nodeToDetachLeft)));
        replacementNode = leftestNode;
    }
    else if (!EqualToZero(nodeToDetachLeft))
        replacementNode = nodeToDetachLeft;
    }
    else if (!EqualToZero(node))
    {
        replacementNode = node;
    if (AreEqual(root, nodeToDetach))
        root = replacementNode;
    }
    else if (AreEqual(GetLeft(parent), nodeToDetach))
        SetLeft(parent, replacementNode);
    else if (AreEqual(GetRight(parent), nodeToDetach))
```

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```
{
        SetRight(parent, replacementNode);
    ClearNode(nodeToDetach);
}
private void LeftMaintain(ref TElement root)
    if (!EqualToZero(root))
    {
        var rootLeftNode = GetLeft(root);
        if (!EqualToZero(rootLeftNode))
            var rootRightNode = GetRight(root);
            var rootRightNodeSize = GetSize(rootRightNode);
            var rootLeftNodeLeftNode = GetLeft(rootLeftNode);
            if (!EqualToZero(rootLeftNodeLeftNode) &&
                (EqualToZero(rootRightNode) ||
                    GreaterThan(GetSize(rootLeftNodeLeftNode), rootRightNodeSize)))
            {
                RightRotate(ref root);
            else
            {
                var rootLeftNodeRightNode = GetRight(rootLeftNode);
                if (!EqualToZero(rootLeftNodeRightNode) &&
                     (EqualToZero(rootRightNode) ||
                        GreaterThan(GetSize(rootLeftNodeRightNode), rootRightNodeSize)))
                {
                    LeftRotate(ref GetLeftReference(root));
                    RightRotate(ref root);
                }
                else
                {
                    return;
                }
            LeftMaintain(ref GetLeftReference(root));
            RightMaintain(ref GetRightReference(root));
            LeftMaintain(ref root);
            RightMaintain(ref root);
        }
    }
}
private void RightMaintain(ref TElement root)
    if (!EqualToZero(root))
    {
        var rootRightNode = GetRight(root);
        if (!EqualToZero(rootRightNode))
            var rootLeftNode = GetLeft(root);
            var rootLeftNodeSize = GetSize(rootLeftNode);
            var rootRightNodeRightNode = GetRight(rootRightNode);
            if (!EqualToZero(rootRightNodeRightNode) &&
                (EqualToZero(rootLeftNode) |
                    GreaterThan(GetSize(rootRightNodeRightNode), rootLeftNodeSize)))
                LeftRotate(ref root);
            else
            {
                var rootRightNodeLeftNode = GetLeft(rootRightNode);
                if (!EqualToZero(rootRightNodeLeftNode) &&
                     (EqualToZero(rootLeftNode) ||
                        GreaterThan(GetSize(rootRightNodeLeftNode), rootLeftNodeSize)))
                {
                    RightRotate(ref GetRightReference(root));
                    LeftRotate(ref root);
                }
                else
                {
                    return;
                }
            LeftMaintain(ref GetLeftReference(root));
            RightMaintain(ref GetRightReference(root));
```

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159

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161 162

```
LeftMaintain(ref root)
165
                         RightMaintain(ref root);
                     }
167
                }
168
            }
169
        }
170
171
     ./csharp/Platform.Collections.Methods/Trees/SizedAndThreadedAVLBalancedTreeMethods.cs
1.7
    using System;
          System.Runtime.CompilerServices;
    using
    using System. Text;
 3
    #if USEARRAYPOOL
    using Platform.Collections;
 5
    #endif
    using Platform.Reflection;
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
 9
10
    namespace Platform.Collections.Methods.Trees
11
12
         /// <summary>
13
         /// Combination of Size, Height (AVL), and threads.
14
        /// </summary>
15
        /// <remarks>
16
        /// Based on: <a href="https://github.com/programmatom/TreeLib/blob/master/TreeLib/TreeLib/G<sub>|</sub>
17
            enerated/AVLTreeList.cs">TreeLib.AVLTreeList</a>.
        /// Which itself based on: <a
18
            href="https://github.com/GNOME/glib/blob/master/glib/gtree.c">GNOME/glib/gtree</a>.
        /// </remarks>
19
        public abstract class SizedAndThreadedAVLBalancedTreeMethods<TElement> :
20
            SizedBinaryTreeMethodsBase<TElement>
            private static readonly int _maxPath = 11 * NumericType<TElement>.BytesSize + 4;
23
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
24
             protected override TElement GetRightest(TElement current)
26
                 var currentRight = GetRightOrDefault(current);
27
                 while (!EqualToZero(currentRight))
                 {
29
                     current = currentRight;
30
                     currentRight = GetRightOrDefault(current);
31
32
                 return current;
             }
34
35
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
36
            protected override TElement GetLeftest(TElement current)
37
38
                 var currentLeft = GetLeftOrDefault(current);
                 while (!EqualToZero(currentLeft))
40
41
                     current = currentLeft;
42
                     currentLeft = GetLeftOrDefault(current);
43
44
                 return current;
45
             }
46
47
            public override bool Contains(TElement node, TElement root)
48
                 while (!EqualToZero(root))
50
51
                     if (FirstIsToTheLeftOfSecond(node, root)) // node.Key < root.Key</pre>
52
53
                         root = GetLeftOrDefault(root);
54
5.5
                     else if (FirstIsToTheRightOfSecond(node, root)) // node.Key > root.Key
                     {
57
                         root = GetRightOrDefault(root);
58
                     }
5.9
                     else // node.Key == root.Key
60
61
                         return true;
63
64
                 return false;
65
             }
66
```

```
protected override void PrintNode(TElement node, StringBuilder sb, int level)
                 base.PrintNode(node, sb, level);
70
                 sb.Append(' '):
71
                 sb.Append(GetLeftIsChild(node) ? 'l' : 'L');
                 sb.Append(GetRightIsChild(node) ? 'r' : 'R');
7.3
                 sb.Append(' ')
74
                 sb.Append(GetBalance(node));
75
77
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
78
            protected void IncrementBalance(TElement node) => SetBalance(node,
79
                (sbyte)(GetBalance(node) + 1));
80
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected void DecrementBalance(TElement node) => SetBalance(node,
82
                (sbyte)(GetBalance(node) - 1));
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected override TElement GetLeftOrDefault(TElement node) => GetLeftIsChild(node) ?
85

   GetLeft(node) : default;

             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected override TElement GetRightOrDefault(TElement node) => GetRightIsChild(node) ?

   GetRight(node) : default;

89
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
90
            protected abstract bool GetLeftIsChild(TElement node);
91
92
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
93
            protected abstract void SetLeftIsChild(TElement node, bool value);
95
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
96
            protected abstract bool GetRightIsChild(TElement node);
98
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract void SetRightIsChild(TElement node, bool value);
100
101
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
102
            protected abstract sbyte GetBalance(TElement node);
103
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
105
            protected abstract void SetBalance(TElement node, sbyte value);
106
107
            protected override void AttachCore(ref TElement root, TElement node)
108
109
                 unchecked
110
111
                     // <code>TODO:</code> Check what is faster to use simple array or array from array pool
112
                     // TODO: Try to use stackalloc as an optimization (requires code generation,
113
                         because of generics)
    #if USEARRAYPOOL
114
                     var path = ArrayPool.Allocate<TElement>(MaxPath);
115
                     var pathPosition = 0;
116
                     path[pathPosition++] = default;
117
    #else
118
                     var path = new TElement[_maxPath];
                     var pathPosition = 1;
120
    #endif
121
                     var currentNode = root;
122
                     while (true)
123
124
                            (FirstIsToTheLeftOfSecond(node, currentNode))
125
126
                              if (GetLeftIsChild(currentNode))
127
128
                                  IncrementSize(currentNode);
129
                                  path[pathPosition++] = currentNode;
130
                                  currentNode = GetLeft(currentNode);
131
132
                              else
133
134
                                  // Threads
135
                                  SetLeft(node, GetLeft(currentNode));
                                  SetRight(node, currentNode);
137
                                  SetLeft(currentNode, node);
138
                                  SetLeftIsChild(currentNode, true);
139
140
                                  DecrementBalance(currentNode);
                                  SetSize(node, One);
141
```

```
FixSize(currentNode); // Should be incremented already
142
143
                                   break;
144
                          }
                          else if (FirstIsToTheRightOfSecond(node, currentNode))
146
147
                               if (GetRightIsChild(currentNode))
148
149
                                   IncrementSize(currentNode);
150
                                   path[pathPosition++] = currentNode;
151
                                   currentNode = GetRight(currentNode);
152
                               }
153
                               else
154
                               {
155
                                    // Threads
156
                                   SetRight(node, GetRight(currentNode));
157
                                   SetLeft(node, currentNode);
159
                                   SetRight(currentNode, node);
                                   SetRightIsChild(currentNode, true);
160
                                    IncrementBalance(currentNode);
161
                                   SetSize(node, One);
162
                                   FixSize(currentNode); // Should be incremented already
163
                               }
165
                          }
166
                          else
167
                           {
168
                               throw new InvalidOperationException("Node with the same key already
169
                               → attached to a tree.");
                          }
170
171
                      // Restore balance. This is the goodness of a non-recursive
172
173
                         implementation, when we are done with balancing we 'break'
                      // the loop and we are done.
174
                      while (true)
175
176
                          var parent = path[--pathPosition];
                          var isLeftNode = !AreEqual(parent, default) && AreEqual(currentNode,
178

   GetLeft(parent));
                          var currentNodeBalance = GetBalance(currentNode);
179
                           if (currentNodeBalance < -1 || currentNodeBalance > 1)
180
181
                               currentNode = Balance(currentNode);
182
                               if (AreEqual(parent, default))
183
                                   root = currentNode;
185
                               }
186
                               else if (isLeftNode)
187
188
                                   SetLeft(parent, currentNode);
189
                                   FixSize(parent);
                               }
191
                               else
                               {
193
                                   SetRight(parent, currentNode);
194
                                   FixSize(parent);
195
                          }
197
                          currentNodeBalance = GetBalance(currentNode);
198
                          if (currentNodeBalance == 0 || AreEqual(parent, default))
199
                           {
200
                               break;
201
                          }
202
                             (isLeftNode)
203
                           {
204
                               DecrementBalance(parent);
                          }
206
207
                          else
                           {
208
                               IncrementBalance(parent);
209
210
                          currentNode = parent;
211
212
    #if USEARRAYPOOL
213
                      ArrayPool.Free(path);
214
    #endif
215
                  }
216
             }
217
```

```
private TElement Balance(TElement node)
    unchecked
    {
        var rootBalance = GetBalance(node);
        if (rootBalance < -1)</pre>
            var left = GetLeft(node);
            if (GetBalance(left) > 0)
                 SetLeft(node, LeftRotateWithBalance(left));
                 FixSize(node);
            node = RightRotateWithBalance(node);
        else if (rootBalance > 1)
            var right = GetRight(node);
            if (GetBalance(right) < 0)</pre>
                 SetRight(node, RightRotateWithBalance(right));
                 FixSize(node);
            node = LeftRotateWithBalance(node);
        return node;
    }
}
protected TElement LeftRotateWithBalance(TElement node)
    unchecked
    {
        var right = GetRight(node);
        if (GetLeftIsChild(right))
            SetRight(node, GetLeft(right));
        }
        else
            SetRightIsChild(node, false);
            SetLeftIsChild(right, true);
        SetLeft(right, node);
        // Fix size
        SetSize(right, GetSize(node));
        FixSize(node);
        // Fix balance
        var rootBalance = GetBalance(node);
        var rightBalance = GetBalance(right);
        if (rightBalance <= 0)</pre>
            if (rootBalance >= 1)
            {
                 SetBalance(right, (sbyte)(rightBalance - 1));
            else
            {
                 SetBalance(right, (sbyte)(rootBalance + rightBalance - 2));
            SetBalance(node, (sbyte)(rootBalance - 1));
        else
               (rootBalance <= rightBalance)</pre>
            {
                 SetBalance(right, (sbyte)(rootBalance - 2));
            }
            else
            {
                 SetBalance(right, (sbyte)(rightBalance - 1));
            SetBalance(node, (sbyte)(rootBalance - rightBalance - 1));
        return right;
    }
}
```

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 $\frac{224}{225}$

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 $\frac{227}{228}$

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 $\frac{240}{241}$

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293

294

```
protected TElement RightRotateWithBalance(TElement node)
            unchecked
            {
                var left = GetLeft(node);
                if (GetRightIsChild(left))
                    SetLeft(node, GetRight(left));
                }
                else
                {
                    SetLeftIsChild(node, false);
                    SetRightIsChild(left, true);
                SetRight(left, node);
                // Fix size
                SetSize(left, GetSize(node));
                FixSize(node);
                // Fix balance
                var rootBalance = GetBalance(node);
                var leftBalance = GetBalance(left);
                if (leftBalance <= 0)</pre>
                    if (leftBalance > rootBalance)
                         SetBalance(left, (sbyte)(leftBalance + 1));
                    }
                    else
                     {
                         SetBalance(left, (sbyte)(rootBalance + 2));
                    SetBalance(node, (sbyte)(rootBalance - leftBalance + 1));
                else
                    if (rootBalance <= -1)</pre>
                     {
                         SetBalance(left, (sbyte)(leftBalance + 1));
                    }
                    else
                     {
                         SetBalance(left, (sbyte)(rootBalance + leftBalance + 2));
                    SetBalance(node, (sbyte)(rootBalance + 1));
                return left;
            }
        }
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected override TElement GetNext(TElement node)
            var current = GetRight(node);
            if (GetRightIsChild(node))
                return GetLeftest(current);
            return current;
        }
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected override TElement GetPrevious(TElement node)
            var current = GetLeft(node);
            if (GetLeftIsChild(node))
                return GetRightest(current);
            return current;
        }
        protected override void DetachCore(ref TElement root, TElement node)
            unchecked
#if USEARRAYPOOL
                var path = ArrayPool.Allocate<TElement>(MaxPath);
                var pathPosition = 0;
```

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 $355 \\ 356$

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372 373

```
path[pathPosition++] = default;
var path = new TElement[_maxPath];
var pathPosition = 1;
var currentNode = root;
while (true)
    if (FirstIsToTheLeftOfSecond(node, currentNode))
    {
        if (!GetLeftIsChild(currentNode))
        {
            throw new InvalidOperationException("Cannot find a node.");
        DecrementSize(currentNode);
        path[pathPosition++] = currentNode;
        currentNode = GetLeft(currentNode);
    else if (FirstIsToTheRightOfSecond(node, currentNode))
        if (!GetRightIsChild(currentNode))
        {
            throw new InvalidOperationException("Cannot find a node.");
        DecrementSize(currentNode);
        path[pathPosition++] = currentNode;
        currentNode = GetRight(currentNode);
    }
    else
    {
        break;
    }
}
var parent = path[--pathPosition];
var balanceNode = parent;
var isLeftNode = !AreEqual(parent, default) && AreEqual(currentNode,
    GetLeft(parent));
if (!GetLeftIsChild(currentNode))
    if (!GetRightIsChild(currentNode)) // node has no children
        if (AreEqual(parent, default))
            root = Zero;
        else if (isLeftNode)
            SetLeftIsChild(parent, false);
            SetLeft(parent, GetLeft(currentNode));
            IncrementBalance(parent);
        }
        else
            SetRightIsChild(parent, false);
            SetRight(parent, GetRight(currentNode));
            DecrementBalance(parent);
    else // node has a right child
        var successor = GetNext(currentNode);
        SetLeft(successor, GetLeft(currentNode));
        var right = GetRight(currentNode);
        if (AreEqual(parent, default))
        {
            root = right;
        else if (isLeftNode)
            SetLeft(parent, right);
            IncrementBalance(parent);
        else
            SetRight(parent, right);
            DecrementBalance(parent);
        }
    }
```

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400

401

402 403

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422 423

424

426

427

428

429 430 431

433

434

435

436

437

438 439

440

441 442

443

444

446

448

449 450 #else

#endif

```
else // node has a left child
    if (!GetRightIsChild(currentNode))
        var predecessor = GetPrevious(currentNode);
        SetRight(predecessor, GetRight(currentNode));
        var leftValue = GetLeft(currentNode);
        if (AreEqual(parent, default))
        {
            root = leftValue;
        }
        else if (isLeftNode)
            SetLeft(parent, leftValue);
            IncrementBalance(parent);
        else
            SetRight(parent, leftValue);
            DecrementBalance(parent);
    else // node has a both children (left and right)
        var predecessor = GetLeft(currentNode);
        var successor = GetRight(currentNode);
        var successorParent = currentNode;
        int previousPathPosition = ++pathPosition;
        // find the immediately next node (and its parent)
        while (GetLeftIsChild(successor))
            path[++pathPosition] = successorParent = successor;
            successor = GetLeft(successor);
            if (!AreEqual(successorParent, currentNode))
            {
                DecrementSize(successorParent);
        }
        path[previousPathPosition] = successor;
        balanceNode = path[pathPosition];
        // remove 'successor' from the tree
        if (!AreEqual(successorParent, currentNode))
            if (!GetRightIsChild(successor))
                SetLeftIsChild(successorParent, false);
            }
            else
            {
                SetLeft(successorParent, GetRight(successor));
            IncrementBalance(successorParent);
            SetRightIsChild(successor, true);
            SetRight(successor, GetRight(currentNode));
        else
        {
            DecrementBalance(currentNode);
        // set the predecessor's successor link to point to the right place
        while (GetRightIsChild(predecessor))
            predecessor = GetRight(predecessor);
        SetRight(predecessor, successor);
        // prepare 'successor' to replace 'node'
        var left = GetLeft(currentNode);
        SetLeftIsChild(successor, true);
        SetLeft(successor, left);
        SetBalance(successor, GetBalance(currentNode));
        FixSize(successor);
        if (AreEqual(parent, default))
        {
            root = successor;
        else if (isLeftNode)
```

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522

523

524

525

526 527

```
SetLeft(parent, successor);
530
                               }
                               else
532
                               {
                                   SetRight(parent, successor);
534
535
                          }
536
537
                      // restore balance
538
                         (!AreEqual(balanceNode, default))
539
540
                          while (true)
541
542
543
                               var balanceParent = path[--pathPosition];
                               isLeftNode = !AreEqual(balanceParent, default) && AreEqual(balanceNode,
544
                                  GetLeft(balanceParent));
                               var currentNodeBalance = GetBalance(balanceNode);
545
                               if (currentNodeBalance < -1 || currentNodeBalance > 1)
546
547
                                   balanceNode = Balance(balanceNode);
                                   if (AreEqual(balanceParent, default))
549
550
                                        root = balanceNode;
551
552
                                   else if (isLeftNode)
                                   {
554
                                       SetLeft(balanceParent, balanceNode);
555
                                   }
556
                                   else
557
                                   {
558
                                        SetRight(balanceParent, balanceNode);
560
561
562
                               currentNodeBalance = GetBalance(balanceNode);
                               if (currentNodeBalance != 0 || AreEqual(balanceParent, default))
563
                               {
564
                                   break;
565
                               }
566
                               if (isLeftNode)
567
568
                                   IncrementBalance(balanceParent);
569
                               }
570
                               else
                               {
572
                                   DecrementBalance(balanceParent);
573
574
                               balanceNode = balanceParent;
575
                          }
576
577
                      ClearNode(node);
578
    #if USEARRAYPOOL
579
                      ArrayPool.Free(path);
580
    #endif
581
582
                 }
583
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
585
             protected override void ClearNode(TElement node)
586
                 SetLeft(node, Zero)
588
                 SetRight(node, Zero);
589
                 SetSize(node, Zero);
590
                 SetLeftIsChild(node, false);
591
                 SetRightIsChild(node, false);
592
                 SetBalance(node, 0);
593
594
             }
         }
595
596
1.8
     ./csharp/Platform.Collections.Methods/Trees/SizedBinaryTreeMethodsBase.cs
    //#define ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
    using System;
 3
    using System. Diagnostics;
          System.Runtime.CompilerServices;
    using
    using System. Text;
    using Platform. Numbers;
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
```

```
namespace Platform.Collections.Methods.Trees
11
12
       public abstract class SizedBinaryTreeMethodsBase<TElement> :
13
           GenericCollectionMethodsBase<TElement>
14
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract ref TElement GetLeftReference(TElement node);
16
17
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
            protected abstract ref TElement GetRightReference(TElement node);
19
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
            protected abstract TElement GetLeft(TElement node);
22
23
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
2.4
            protected abstract TElement GetRight(TElement node);
26
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetSize(TElement node);
29
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract void SetLeft(TElement node, TElement left);
31
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
33
            protected abstract void SetRight(TElement node, TElement right);
34
35
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
36
            protected abstract void SetSize(TElement node, TElement size);
37
38
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
39
            protected abstract bool FirstIsToTheLeftOfSecond(TElement first, TElement second);
40
41
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
42
            protected abstract bool FirstIsToTheRightOfSecond(TElement first, TElement second);
44
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual TElement GetLeftOrDefault(TElement node) => AreEqual(node, default) ?
46

→ default : GetLeft(node);
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual TElement GetRightOrDefault(TElement node) => AreEqual(node, default) ?
49
            → default : GetRight(node);
50
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected void IncrementSize(TElement node) => SetSize(node, Increment(GetSize(node)));
52
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
54
            protected void DecrementSize(TElement node) => SetSize(node, Decrement(GetSize(node)));
55
56
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
57
            protected TElement GetLeftSize(TElement node) => GetSizeOrZero(GetLeftOrDefault(node));
58
59
60
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected TElement GetRightSize(TElement node) => GetSizeOrZero(GetRightOrDefault(node));
61
62
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
63
            protected TElement GetSizeOrZero(TElement node) => EqualToZero(node) ? Zero :
64

→ GetSize(node);

            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected void FixSize(TElement node) => SetSize(node, Increment(Add(GetLeftSize(node),

→ GetRightSize(node))));
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
69
            protected void LeftRotate(ref TElement root) => root = LeftRotate(root);
70
7.1
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
72
            protected TElement LeftRotate(TElement root)
73
   var right = GetRight(root);
#if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
7.5
76
                if (EqualToZero(right))
77
                {
78
                    throw new InvalidOperationException("Right is null.");
79
                }
80
   #endif
81
                SetRight(root, GetLeft(right));
82
                SetLeft(right, root);
83
```

```
SetSize(right, GetSize(root));
                 FixSize(root);
                 return right;
86
             }
88
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
89
             protected void RightRotate(ref TElement root) => root = RightRotate(root);
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected TElement RightRotate(TElement root)
93
94
                 var left = GetLeft(root)
95
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
96
                 if (EqualToZero(left))
97
                      throw new InvalidOperationException("Left is null.");
99
                 }
100
    #endif
101
                 SetLeft(root, GetRight(left));
102
                 SetRight(left, root);
103
                 SetSize(left, GetSize(root));
                 FixSize(root);
105
                 return left;
             }
107
108
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
109
             protected virtual TElement GetRightest(TElement current)
110
111
                 var currentRight = GetRight(current);
112
                 while (!EqualToZero(currentRight))
113
114
                     current = currentRight;
115
                     currentRight = GetRight(current);
116
117
                 return current;
118
             }
119
120
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
121
             protected virtual TElement GetLeftest(TElement current)
122
123
                 var currentLeft = GetLeft(current);
124
                 while (!EqualToZero(currentLeft))
125
                 {
                     current = currentLeft;
127
                     currentLeft = GetLeft(current);
129
                 return current;
             }
131
132
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
133
             protected virtual TElement GetNext(TElement node) => GetLeftest(GetRight(node));
134
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
136
             protected virtual TElement GetPrevious(TElement node) => GetRightest(GetLeft(node));
137
138
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
139
             public virtual bool Contains(TElement node, TElement root)
140
141
                 while (!EqualToZero(root))
142
143
                      if (FirstIsToTheLeftOfSecond(node, root)) // node.Key < root.Key</pre>
144
145
                          root = GetLeft(root);
146
147
                     else if (FirstIsToTheRightOfSecond(node, root)) // node.Key > root.Key
                     {
149
                          root = GetRight(root);
150
                     }
                     else // node.Key == root.Key
152
153
154
                          return true;
155
156
                 return false;
157
158
159
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
160
             protected virtual void ClearNode(TElement node)
161
162
```

```
SetLeft(node, Zero);
163
                 SetRight(node, Zero);
                 SetSize(node, Zero);
165
166
167
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
168
             public void Attach(ref TElement root, TElement node)
169
170
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
171
                 ValidateSizes(root);
172
                 Debug.WriteLine("--BeforeAttach--");
173
                 Debug.WriteLine(PrintNodes(root));
174
                 Debug.WriteLine("-----");
175
176
                 var sizeBefore = GetSize(root);
    #endif
177
                 if (EqualToZero(root))
178
179
                      SetSize(node, One);
180
                     root = node;
181
182
                     return;
183
                 AttachCore(ref root, node)
184
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
185
                 Debug.WriteLine("--AfterAttach--");
186
                 Debug.WriteLine(PrintNodes(root));
187
                 Debug.WriteLine("----"):
188
                 ValidateSizes(root);
189
                 var sizeAfter = GetSize(root);
190
                 if (!AreEqual(Arithmetic.Increment(sizeBefore), sizeAfter))
191
192
                      throw new InvalidOperationException("Tree was broken after attach.");
193
                 }
194
    #endif
195
             }
196
197
             protected abstract void AttachCore(ref TElement root, TElement node);
198
200
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             public void Detach(ref TElement root, TElement node)
201
202
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
203
204
                 ValidateSizes(root);
                 Debug.WriteLine("--BeforeDetach--");
205
                 Debug.WriteLine(PrintNodes(root));
206
                 Debug.WriteLine("----");
207
                 var sizeBefore = GetSize(root);
                 if (EqualToZero(root))
209
                 {
210
                      throw new InvalidOperationException($"Элемент с {node} не содержится в
211
                      → дереве.");
212
    #endif
213
    DetachCore(ref root, node);
#if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
214
215
                 Debug.WriteLine("--AfterDetach--");
216
                 Debug.WriteLine(PrintNodes(root));
217
                 Debug.WriteLine("-----");
218
                 ValidateSizes(root);
219
                 var sizeAfter = GetSize(root);
220
                 if (!AreEqual(Arithmetic.Decrement(sizeBefore), sizeAfter))
221
                 {
222
                      throw new InvalidOperationException("Tree was broken after detach.");
223
                 }
224
    #endif
225
226
227
             protected abstract void DetachCore(ref TElement root, TElement node);
228
229
             public void FixSizes(TElement node)
230
231
                 if (AreEqual(node, default))
232
                 {
233
                     return;
235
                 FixSizes(GetLeft(node));
236
237
                 FixSizes(GetRight(node));
                 FixSize(node);
238
             }
239
```

```
public void ValidateSizes(TElement node)
^{241}
                 if (AreEqual(node, default))
243
                 {
244
                     return;
245
246
                 var size = GetSize(node);
247
                 var leftSize = GetLeftSize(node);
                 var rightSize = GetRightSize(node);
249
                 var expectedSize = Arithmetic.Increment(Arithmetic.Add(leftSize, rightSize));
250
                 if (!AreEqual(size, expectedSize))
251
252
                      throw new InvalidOperationException($\sigma"Size of \{node\} is not valid. Expected
253

    size: {expectedSize}, actual size: {size}.");

254
                 ValidateSizes(GetLeft(node))
255
                 ValidateSizes(GetRight(node));
             }
257
258
             public void ValidateSize(TElement node)
259
260
                 var size = GetSize(node);
261
                 var leftSize = GetLeftSize(node);
                 var rightSize = GetRightSize(node);
263
                 var expectedSize = Arithmetic.Increment(Arithmetic.Add(leftSize, rightSize));
264
                 if (!AreEqual(size, expectedSize))
                 {
266
                      throw new InvalidOperationException($ "Size of {node} is not valid. Expected
267

    size: {expectedSize}, actual size: {size}.");
                 }
268
             }
269
270
             public string PrintNodes(TElement node)
271
272
273
                 var sb = new StringBuilder();
                 PrintNodes(node, sb);
274
275
                 return sb.ToString();
276
277
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             public void PrintNodes(TElement node, StringBuilder sb) => PrintNodes(node, sb, 0);
279
280
             public void PrintNodes(TElement node, StringBuilder sb, int level)
281
282
                 if (AreEqual(node, default))
283
                 {
                     return;
285
                 PrintNodes(GetLeft(node), sb, level + 1);
287
                 PrintNode(node, sb, level);
288
                 sb.AppendLine();
289
                 PrintNodes(GetRight(node), sb, level + 1);
290
             }
291
292
             public string PrintNode(TElement node)
293
294
                 var sb = new StringBuilder();
                 PrintNode(node, sb)
296
                 return sb.ToString();
297
298
299
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
300
             protected void PrintNode(TElement node, StringBuilder sb) => PrintNode(node, sb, 0);
302
             protected virtual void PrintNode(TElement node, StringBuilder sb, int level)
303
304
                 sb.Append('\t', level);
305
                 sb.Append(node);
306
                 PrintNodeValue(node, sb);
                 sb.Append(' ');
308
                 sb.Append('s')
309
                 sb.Append(GetSize(node));
310
311
312
             protected abstract void PrintNodeValue(TElement node, StringBuilder sb);
313
        }
314
    }
315
```

```
./csharp/Platform.Collections.Methods.Tests/RecursionlessSizeBalancedTree.cs
   using System;
   using System.Collections.Generic;
2
   using System.Text;
using Platform.Numbers
3
   using Platform.Collections.Methods.Trees;
   using Platform.Converters;
   namespace Platform.Collections.Methods.Tests
        public class RecursionlessSizeBalancedTree<TElement> :
10
            RecursionlessSizeBalancedTreeMethods<TElement>
11
            private struct TreeElement
12
13
                public TElement Size;
14
                public
                        TElement Left;
15
                public TElement Right;
16
            }
17
18
            private readonly TreeElement[] _elements;
private TElement _allocated;
19
20
21
            public TElement Root;
22
23
            public TElement Count => GetSizeOrZero(Root);
24
            public RecursionlessSizeBalancedTree(int capacity) => (_elements, _allocated) = (new
26
             → TreeElement[capacity], One);
27
            public TElement Allocate()
28
29
                var newNode = _allocated;
                if (IsEmpty(newNode))
31
32
33
                     _allocated = Arithmetic.Increment(_allocated);
                     return newNode;
34
                }
35
36
                else
                {
37
                     throw new InvalidOperationException("Allocated tree element is not empty.");
                }
39
            }
40
41
            public void Free(TElement node)
42
43
44
                while (!EqualityComparer.Equals(_allocated, One) && IsEmpty(node))
45
                     var lastNode = Arithmetic.Decrement(_allocated);
46
                     if (EqualityComparer.Equals(lastNode, node))
48
                         _allocated = lastNode;
49
                         node = Arithmetic.Decrement(node);
                     }
51
                     else
                     {
53
                         return;
54
                     }
55
                }
56
            }
57
5.8
            public bool IsEmpty(TElement node) =>
59
             EqualityComparer<TreeElement>.Default.Equals(GetElement(node), default);
60
            protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
61

→ Comparer.Compare(first, second) < 0;
</p>
            protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>
63
             → Comparer.Compare(first, second) > 0;
64
            protected override ref TElement GetLeftReference(TElement node) => ref

→ GetElement(node).Left;

66
            protected override TElement GetLeft(TElement node) => GetElement(node).Left;
68
            protected override ref TElement GetRightReference(TElement node) => ref

   GetElement(node).Right;

7.0
            protected override TElement GetRight(TElement node) => GetElement(node).Right;
71
72
```

```
protected override TElement GetSize(TElement node) => GetElement(node).Size;
7.3
7.4
            protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
75

    sb.Append(node);
76
            protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
77
            → left;
            protected override void SetRight(TElement node, TElement right) =>
79

   GetElement(node).Right = right;
80
            protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =
81

    size;

82
            private ref TreeElement GetElement(TElement node) => ref
83
               _elements[UncheckedConverter<TElement, long>.Default.Convert(node)];
        }
   }
     ./csharp/Platform.Collections.Methods.Tests/SizeBalancedTree.cs
1.10
   using System;
   using System.Collections.Generic;
   using System. Text;
   using Platform. Numbers;
   using Platform.Collections.Methods.Trees;
   using Platform.Converters;
   namespace Platform.Collections.Methods.Tests
9
        public class SizeBalancedTree<TElement> : SizeBalancedTreeMethods<TElement>
10
11
            private struct TreeElement
12
13
                public TElement Size;
14
                public TElement Left;
15
                public TElement Right;
17
18
            private readonly TreeElement[] _elements;
19
            private TElement _allocated;
20
21
            public TElement Root;
22
23
            public TElement Count => GetSizeOrZero(Root);
25
            public SizeBalancedTree(int capacity) => (_elements, _allocated) = (new
26

→ TreeElement[capacity], One);
27
            public TElement Allocate()
28
                var newNode = _allocated;
30
31
                if (IsEmpty(newNode))
32
                     _allocated = Arithmetic.Increment(_allocated);
33
                    return newNode;
35
                else
36
                {
37
                    throw new InvalidOperationException("Allocated tree element is not empty.");
38
                }
39
            }
40
41
            public void Free(TElement node)
42
43
                while (!EqualityComparer.Equals(_allocated, One) && IsEmpty(node))
44
45
                    var lastNode = Arithmetic.Decrement(_allocated);
                    if (EqualityComparer.Equals(lastNode, node))
47
48
                         _allocated = lastNode;
49
                         node = Arithmetic.Decrement(node);
50
                    }
                    else
52
                         return;
54
                    }
55
                }
            }
57
```

```
public bool IsEmpty(TElement node) =>
5.9
               EqualityComparer<TreeElement>.Default.Equals(GetElement(node), default);
60
            protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
               Comparer.Compare(first, second) < 0;</pre>
            protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>
63
            → Comparer.Compare(first, second) > 0;
            protected override ref TElement GetLeftReference(TElement node) => ref

   GetElement(node).Left;
66
            protected override TElement GetLeft(TElement node) => GetElement(node).Left;
68
            protected override ref TElement GetRightReference(TElement node) => ref
69

→ GetElement(node).Right;

70
            protected override TElement GetRight(TElement node) => GetElement(node).Right;
72
            protected override TElement GetSize(TElement node) => GetElement(node).Size;
7.3
7.4
            protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
7.5

    sb.Append(node);
76
            protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
77
            → left;
            protected override void SetRight(TElement node, TElement right) =>
79
            → GetElement(node).Right = right;
            protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =
81

    size;

82
            private ref TreeElement GetElement(TElement node) => ref
83
               _elements[UncheckedConverter<TElement, long>.Default.Convert(node)];
       }
   }
85
      ./csharp/Platform.Collections.Methods.Tests/SizedAndThreadedAVLBalancedTree.cs
1.11
   using System;
         System.Collections.Generic;
   using
   using System. Text;
   using Platform. Numbers;
   using Platform.Collections.Methods.Trees;
5
   using Platform.Converters;
   namespace Platform.Collections.Methods.Tests
9
       public class SizedAndThreadedAVLBalancedTree<TElement> :
10
           SizedAndThreadedAVLBalancedTreeMethods<TElement>
1.1
            private struct TreeElement
12
13
                public TElement Size;
                public TElement Left;
15
                public TElement Right;
16
                public sbyte Balance;
17
                public bool LeftIsChild
18
                public bool RightIsChild;
20
21
            private readonly TreeElement[] _elements;
22
            private TElement _allocated;
^{24}
            public TElement Root;
25
26
            public TElement Count => GetSizeOrZero(Root);
27
28
            public SizedAndThreadedAVLBalancedTree(int capacity) => (_elements, _allocated) = (new
            → TreeElement[capacity], One);
30
            public TElement Allocate()
                var newNode = _allocated;
33
                if (IsEmpty(newNode))
35
                     _allocated = Arithmetic.Increment(_allocated);
36
                    return newNode;
37
38
                else
39
```

```
40
                    throw new InvalidOperationException("Allocated tree element is not empty.");
                }
42
            }
43
44
            public void Free(TElement node)
45
46
                while (!EqualityComparer.Equals(_allocated, One) && IsEmpty(node))
47
48
                    var lastNode = Arithmetic.Decrement(_allocated);
49
                    if (EqualityComparer.Equals(lastNode, node))
50
                        _allocated = lastNode;
52
                        node = Arithmetic.Decrement(node);
                    }
54
                    else
                    {
56
                        return;
                    }
58
                }
59
            }
60
61
            public bool IsEmpty(TElement node) =>
62
            Gefault.Equals(GetElement(node), default);
63
            protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
64

→ Comparer.Compare(first, second) < 0;
</p>
            protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>
66
            → Comparer.Compare(first, second) > 0;
            protected override sbyte GetBalance(TElement node) => GetElement(node).Balance;
            protected override bool GetLeftIsChild(TElement node) => GetElement(node).LeftIsChild;
70
71
            protected override ref TElement GetLeftReference(TElement node) => ref
72

→ GetElement(node).Left;

7.3
            protected override TElement GetLeft(TElement node) => GetElement(node).Left;
75
            protected override bool GetRightIsChild(TElement node) => GetElement(node).RightIsChild;
76
77
            protected override ref TElement GetRightReference(TElement node) => ref
78

   GetElement(node).Right;

79
            protected override TElement GetRight(TElement node) => GetElement(node).Right;
80
            protected override TElement GetSize(TElement node) => GetElement(node).Size;
82
            protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
84

    sb.Append(node);
            protected override void SetBalance(TElement node, sbyte value) =>

   GetElement(node).Balance = value;

            protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
            → left;
            protected override void SetLeftIsChild(TElement node, bool value) =>

    GetElement(node).LeftIsChild = value;

            protected override void SetRight(TElement node, TElement right) =>

   GetElement(node).Right = right;

93
            protected override void SetRightIsChild(TElement node, bool value) =>

    GetElement(node).RightIsChild = value;

95
            protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =
96

    size;

97
            private ref TreeElement GetElement(TElement node) => ref
98
            _ _ elements[UncheckedConverter<TElement, long>.Default.Convert(node)];
        }
   }
100
      ./csharp/Platform.Collections.Methods.Tests/TestExtensions.cs
1.12
   using System;
1
   using System.Collections.Generic;
```

using Xunit;

```
using Platform.Collections.Methods.Trees;
4
   using Platform.Converters;
5
   namespace Platform.Collections.Methods.Tests
7
        public static class TestExtensions
9
10
            public static void TestMultipleCreationsAndDeletions<TElement>(this
                SizedBinaryTreeMethodsBase<TElement> tree, Func<TElement> allocate, Action<TElement>
                free, ref TElement root, Func<TElement> treeCount, int maximumOperationsPerCycle)
12
                for (var N = 1; N < maximumOperationsPerCycle; N++)</pre>
13
                     var currentCount = 0;
15
                     for (var i = 0; i < N; i++)
17
                         var node = allocate();
18
                         tree.Attach(ref root, node);
19
                         currentCount++;
20
                         Assert.Equal(currentCount, (int)UncheckedConverter<TElement,
21
                            int>.Default.Convert(treeCount()));
22
                     for (var i = 1; i <= N; i++)</pre>
23
24
                         TElement node = UncheckedConverter<int, TElement>.Default.Convert(i);
25
                         if (tree.Contains(node, root))
26
                         {
27
                             tree.Detach(ref root, node);
28
                             free(node);
29
                             currentCount--;
30
                             Assert.Equal(currentCount, (int)UncheckedConverter<TElement,
                              → int>.Default.Convert(treeCount()));
                         }
32
                     }
33
                }
            }
36
            public static void TestMultipleRandomCreationsAndDeletions<TElement>(this
37
                SizedBinaryTreeMethodsBase<TElement> tree, ref TElement root, Func<TElement>
                treeCount, int maximumOperationsPerCycle)
38
                var random = new System.Random(0);
                var added = new HashSet<TElement>();
40
                var currentCount = 0;
41
                for (var N = 1; N < maximumOperationsPerCycle; N++)</pre>
42
43
                     for (var i = 0; i < N; i++)</pre>
44
                         var node = UncheckedConverter<int, TElement>.Default.Convert(random.Next(1,
46
                         \rightarrow N));
                         if (added.Add(node))
47
48
                             tree.Attach(ref root, node);
                             currentCount++;
50
                             Assert.Equal(currentCount, (int)UncheckedConverter<TElement,
                                int>.Default.Convert(treeCount()));
                         }
52
53
                     for (var i = 1; i <= N; i++)</pre>
54
                         TElement node = UncheckedConverter<int,
56
                             TElement > . Default . Convert (random . Next(1, N));
                         if (tree.Contains(node, root))
                         {
58
                             tree.Detach(ref root, node);
59
                             currentCount--;
                             Assert.Equal(currentCount, (int)UncheckedConverter<TElement,
61
                                  int>.Default.Convert(treeCount()));
                             added.Remove(node);
62
                         }
                     }
64
                }
65
            }
66
        }
67
   }
68
```

```
./csharp/Platform.Collections.Methods.Tests/TreesTests.cs
       using Xunit;
 2
       namespace Platform.Collections.Methods.Tests
 3
 4
                  public static class TreesTests
 5
 6
                           private const int _n = 500;
                            [Fact]
                            public static void RecursionlessSizeBalancedTreeMultipleAttachAndDetachTest()
10
11
                                      var recursionlessSizeBalancedTree = new RecursionlessSizeBalancedTree<uint>(10000);
12
                                      recursionlessSizeBalancedTree.TestMultipleCreationsAndDeletions(recursionlessSizeBal
                                               ancedTree.Allocate, recursionlessSizeBalancedTree.Free, ref
                                               recursionlessSizeBalancedTree.Root, () => recursionlessSizeBalancedTree.Count,
                                               _n);
                            }
15
                            [Fact]
16
                           public static void SizeBalancedTreeMultipleAttachAndDetachTest()
18
                                      var sizeBalancedTree = new SizeBalancedTree<uint>(10000);
19
                                      sizeBalancedTree.TestMultipleCreationsAndDeletions(sizeBalancedTree.Allocate,
                                               sizeBalancedTree.Free, ref sizeBalancedTree.Root, () => sizeBalancedTree.Count,
                                               _n);
                            }
21
22
                            [Fact]
2.3
                           public static void SizedAndThreadedAVLBalancedTreeMultipleAttachAndDetachTest()
25
                                      var avlTree = new SizedAndThreadedAVLBalancedTree<uint>(10000);
26
                                      avlTree.TestMultipleCreationsAndDeletions(avlTree.Allocate, avlTree.Free, ref
27
                                               avlTree.Root, () => avlTree.Count, _n);
                            }
29
                            [Fact]
30
                           public static void RecursionlessSizeBalancedTreeMultipleRandomAttachAndDetachTest()
31
32
                                      var recursionlessSizeBalancedTree = new RecursionlessSizeBalancedTree<uint>(10000);
33
                                      {\tt recursionlessSizeBalancedTree.TestMultipleRandomCreationsAndDeletions} (\textbf{refine} and \textbf{refine} and \textbf{refine}
                                       recursionlessSizeBalancedTree.Root, () => recursionlessSizeBalancedTree.Count,
                                               _n);
                            }
36
                            [Fact]
                            public static void SizeBalancedTreeMultipleRandomAttachAndDetachTest()
39
                                      var sizeBalancedTree = new SizeBalancedTree<uint>(10000);
40
                                      sizeBalancedTree.TestMultipleRandomCreationsAndDeletions(ref sizeBalancedTree.Root,

→ () => sizeBalancedTree.Count, _n);
                            }
42
43
                            [Fact]
                           public static void SizedAndThreadedAVLBalancedTreeMultipleRandomAttachAndDetachTest()
45
46
                                      var avlTree = new SizedAndThreadedAVLBalancedTree<uint>(10000);
                                      avlTree.TestMultipleRandomCreationsAndDeletions(ref avlTree.Root, () =>
48
                                      → avlTree.Count, _n);
                            }
49
                  }
50
        }
```

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