```
LinksPlatform's Platform Collections Methods Class Library
./Platform.Collections.Methods/GenericCollectionMethodsBase.cs
   using System.Collections.Generic;
   using System.Runtime.CompilerServices;
2
   using Platform.Numbers;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods
8
        public abstract class GenericCollectionMethodsBase<TElement>
10
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
11
            protected virtual TElement GetZero() => Integer<TElement>.Zero;
13
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
14
            protected virtual bool EqualToZero(TElement value) => EqualityComparer.Equals(value,

    Zero);

16
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
17
            protected virtual bool AreEqual(TElement first, TElement second) =>

→ EqualityComparer.Equals(first, second);

19
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool GreaterThanZero(TElement value) => Comparer.Compare(value, Zero)
            \rightarrow > 0;
22
23
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool GreaterThan(TElement first, TElement second) =>
24

→ Comparer.Compare(first, second) > 0;

25
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
26
            protected virtual bool GreaterOrEqualThanZero(TElement value) => Comparer.Compare(value,
            \rightarrow Zero) >= 0;
2.8
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
2.9
            protected virtual bool GreaterOrEqualThan(TElement first, TElement second) =>
               Comparer.Compare(first, second) >= 0;
31
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
32
            protected virtual bool LessOrEqualThanZero(TElement value) => Comparer.Compare(value,
            \rightarrow Zero) <= 0;
34
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool LessOrEqualThan(TElement first, TElement second) =>
36

→ Comparer.Compare(first, second) <= 0;
</p>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool LessThanZero(TElement value) => Comparer.Compare(value, Zero) < 0;</pre>
39
40
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
41
            protected virtual bool LessThan(TElement first, TElement second) =>
42
                Comparer.Compare(first, second) < 0;</pre>
43
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
44
            protected virtual TElement Increment(TElement value) =>
45
               Arithmetic<TElement>.Increment(value);
46
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
47
            protected virtual TElement Decrement(TElement value) =>
            → Arithmetic<TElement>.Decrement(value);
49
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
50
            protected virtual TElement Add(TElement first, TElement second) =>
               Arithmetic<TElement>.Add(first, second);
52
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual TElement Subtract(TElement first, TElement second) =>
               Arithmetic<TElement>.Subtract(first, second);
55
            protected readonly TElement Zero;
protected readonly TElement One;
            protected readonly TElement Two;
protected readonly EqualityComparer<TElement> EqualityComparer;
58
            protected readonly Comparer<TElement> Comparer;
60
61
            protected GenericCollectionMethodsBase()
62
63
                EqualityComparer = EqualityComparer<TElement>.Default;
64
```

```
Comparer = Comparer<TElement>.Default;
6.5
                Zero = GetZero(); //-V3068
                One = Increment(Zero); //-V3068
67
                Two = Increment(One); //-V3068
68
            }
        }
70
7.1
./Platform.Collections.Methods/Lists/CircularDoublyLinkedListMethods.cs
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
3
4
        public abstract class CircularDoublyLinkedListMethods<TElement> :
           DoublyLinkedListMethodsBase<TElement>
6
            public void AttachBefore(TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
10
                SetNext(newElement, baseElement);
11
                if (AreEqual(baseElement, GetFirst()))
12
                {
13
                    SetFirst(newElement);
14
15
                SetNext(baseElementPrevious, newElement);
16
                SetPrevious(baseElement, newElement);
17
                IncrementSize();
            }
19
20
            public void AttachAfter(TElement baseElement, TElement newElement)
21
22
                var baseElementNext = GetNext(baseElement);
23
                SetPrevious(newElement, baseElement);
                SetNext(newElement, baseElementNext);
25
                if (AreEqual(baseElement, GetLast()))
26
27
                    SetLast(newElement);
28
29
                SetPrevious(baseElementNext, newElement);
30
                SetNext(baseElement, newElement);
                IncrementSize();
32
            }
33
34
            public void AttachAsFirst(TElement element)
35
36
                var first = GetFirst();
                if (EqualToZero(first))
38
39
                    SetFirst(element);
                    SetLast(element);
41
                    SetPrevious(element, element);
42
                    SetNext(element, element);
43
                    IncrementSize();
                }
45
                else
46
                {
47
                     AttachBefore(first, element);
48
            }
51
            public void AttachAsLast(TElement element)
53
                var last = GetLast();
54
                if (EqualToZero(last))
                {
56
                     AttachAsFirst(element);
57
                }
58
                else
59
                {
60
                     AttachAfter(last, element);
62
            }
63
64
            public void Detach(TElement element)
65
66
                var elementPrevious = GetPrevious(element);
                var elementNext = GetNext(element);
68
```

```
if (AreEqual(elementNext, element))
6.9
                    SetFirst(Zero);
7.1
                    SetLast(Zero);
72
                }
                else
74
75
                    SetNext(elementPrevious, elementNext);
76
                    SetPrevious(elementNext, elementPrevious);
77
                    if (AreEqual(element, GetFirst()))
78
                        SetFirst(elementNext);
80
                    }
81
                    if (AreEqual(element, GetLast()))
82
                        SetLast(elementPrevious);
84
85
                SetPrevious(element, Zero);
87
                SetNext(element, Zero);
88
                DecrementSize();
89
            }
       }
91
92
./Platform.Collections.Methods/Lists/DoublyLinkedListMethodsBase.cs
   using System.Runtime.CompilerServices;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
5
        /// <remarks>
       /// Based on <a href="https://en.wikipedia.org/wiki/Doubly_linked_list">doubly linked
           list</a> implementation.
        /// </remarks>
       public abstract class DoublyLinkedListMethodsBase<TElement> :
10
           GenericCollectionMethodsBase<TElement>
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetFirst();
13
14
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
15
            protected abstract TElement GetLast();
16
17
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
            protected abstract TElement GetPrevious(TElement element);
19
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
            protected abstract TElement GetNext(TElement element);
23
24
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetSize();
26
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract void SetFirst(TElement element);
28
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
30
            protected abstract void SetLast(TElement element);
31
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
33
            protected abstract void SetPrevious(TElement element, TElement previous);
34
35
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
36
            protected abstract void SetNext(TElement element, TElement next);
38
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
39
            protected abstract void SetSize(TElement size);
40
41
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected void IncrementSize() => SetSize(Increment(GetSize()));
43
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
45
            protected void DecrementSize() => SetSize(Decrement(GetSize()));
46
       }
47
   }
```

```
./Platform.Collections.Methods/Lists/OpenDoublyLinkedListMethods.cs
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
   {
4
        public abstract class OpenDoublyLinkedListMethods<TElement> :
           DoublyLinkedListMethodsBase<TElement>
6
            public void AttachBefore(TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
10
                SetNext(newElement, baseElement);
11
12
                if (EqualToZero(baseElementPrevious))
                {
13
                    SetFirst(newElement);
14
                }
                else
16
                {
17
                    SetNext(baseElementPrevious, newElement);
18
19
                SetPrevious(baseElement, newElement);
20
                IncrementSize();
            }
22
23
            public void AttachAfter(TElement baseElement, TElement newElement)
25
                var baseElementNext = GetNext(baseElement);
26
                SetPrevious(newElement, baseElement);
                SetNext(newElement, baseElementNext);
28
                if (EqualToZero(baseElementNext))
29
30
                    SetLast(newElement);
31
                }
32
                else
                {
34
                    SetPrevious(baseElementNext, newElement);
35
36
                SetNext(baseElement, newElement);
37
                IncrementSize();
38
            }
39
40
            public void AttachAsFirst(TElement element)
41
42
                var first = GetFirst();
43
                if (EqualToZero(first))
44
45
                    SetFirst(element);
                    SetLast(element);
47
                    SetPrevious(element, Zero);
48
                    SetNext(element, Zero);
                    IncrementSize();
50
                }
51
                else
53
                     AttachBefore(first, element);
54
                }
            }
56
            public void AttachAsLast(TElement element)
59
                var last = GetLast()
60
                if (EqualToZero(last))
62
                     AttachAsFirst(element);
63
                }
                else
65
66
                     AttachAfter(last, element);
67
68
            }
69
70
            public void Detach(TElement element)
7.1
72
                var elementPrevious = GetPrevious(element);
73
                var elementNext = GetNext(element);
74
                if (EqualToZero(elementPrevious))
75
```

```
SetFirst(elementNext);
                }
                else
79
                {
                    SetNext(elementPrevious, elementNext);
81
82
                if (EqualToZero(elementNext))
83
84
                    SetLast(elementPrevious);
85
                }
86
87
                else
                {
88
                    SetPrevious(elementNext, elementPrevious);
89
                SetPrevious(element, Zero);
91
                SetNext(element, Zero);
92
                DecrementSize();
            }
94
        }
95
96
./Platform. Collections. Methods/Trees/Size Balanced Tree Methods 2.cs
   using System;
1
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Trees
5
        public abstract class SizeBalancedTreeMethods2<TElement> :
           SizedBinaryTreeMethodsBase<TElement>
            protected override void AttachCore(ref TElement root, TElement node)
9
10
11
                if (EqualToZero(root))
12
                    root = node;
13
                     IncrementSize(root);
                }
15
16
                else
17
                     IncrementSize(root);
18
                     if (FirstIsToTheLeftOfSecond(node, root))
20
                         AttachCore(ref GetLeftReference(root), node);
21
                         LeftMaintain(ref root);
22
                    }
23
                    else
24
                         AttachCore(ref GetRightReference(root), node);
26
                         RightMaintain(ref root);
27
                     }
28
                }
29
            }
30
            protected override void DetachCore(ref TElement root, TElement nodeToDetach)
32
33
                ref var currentNode = ref root;
34
                ref var parent = ref root;
35
                var replacementNode = Zero;
36
                while (!AreEqual(currentNode, nodeToDetach))
37
                    SetSize(currentNode, Decrement(GetSize(currentNode)));
39
                     if (FirstIsToTheLeftOfSecond(nodeToDetach, currentNode))
40
41
                         parent = ref currentNode;
42
                         currentNode = ref GetLeftReference(currentNode);
43
44
                    else if (FirstIsToTheRightOfSecond(nodeToDetach, currentNode))
45
46
                         parent = ref currentNode;
47
                         currentNode = ref GetRightReference(currentNode);
48
                     }
49
                    else
50
                     {
51
                         throw new InvalidOperationException("Duplicate link found in the tree.");
53
54
                var nodeToDetachLeft = GetLeft(nodeToDetach);
55
                var node = GetRight(nodeToDetach);
```

```
if (!EqualToZero(nodeToDetachLeft) && !EqualToZero(node))
        var minNode = node;
        var minNodeLeft = GetLeft(minNode);
        while (!EqualToZero(minNodeLeft))
            minNode = minNodeLeft;
            minNodeLeft = GetLeft(minNode);
        DetachCore(ref GetRightReference(nodeToDetach), minNode);
        SetLeft(minNode, nodeToDetachLeft);
        node = GetRight(nodeToDetach);
        if (!EqualToZero(node))
            SetRight(minNode, node);
            SetSize(minNode, Increment(Add(GetSize(nodeToDetachLeft), GetSize(node))));
        else
            SetSize(minNode, Increment(GetSize(nodeToDetachLeft)));
        replacementNode = minNode;
    }
    else if (!EqualToZero(nodeToDetachLeft))
        replacementNode = nodeToDetachLeft;
    }
    else if (!EqualToZero(node))
        replacementNode = node;
    if (AreEqual(root, nodeToDetach))
    {
        root = replacementNode;
    }
    else if (AreEqual(GetLeft(parent), nodeToDetach))
        SetLeft(parent, replacementNode);
    else if (AreEqual(GetRight(parent), nodeToDetach))
        SetRight(parent, replacementNode);
    ClearNode(nodeToDetach);
}
private void LeftMaintain(ref TElement root)
    if (!EqualToZero(root))
        var rootLeftNode = GetLeft(root);
        if (!EqualToZero(rootLeftNode))
            var rootRightNode = GetRight(root);
            var rootLeftNodeLeftNode = GetLeft(rootLeftNode);
            if (!EqualToZero(rootLeftNodeLeftNode) &&
                (EqualToZero(rootRightNode) ||
                    GreaterThan(GetSize(rootLeftNodeLeftNode), GetSize(rootRightNode))))
            {
                RightRotate(ref root);
            }
            else
            {
                var rootLeftNodeRightNode = GetRight(rootLeftNode);
                if (!EqualToZero(rootLeftNodeRightNode) &&
                    (EqualToZero(rootRightNode) ||
                        GreaterThan(GetSize(rootLeftNodeRightNode),
                        GetSize(rootRightNode))))
                {
                    LeftRotate(ref GetLeftReference(root));
                    RightRotate(ref root);
                else
                {
                    return;
                }
            LeftMaintain(ref GetLeftReference(root));
```

61 62

63

64 65

66

67

68

69 70

7.1

72

74

76 77

79

80 81

82

83

85

86 87

88

90

91

93

94

96 97

98

100

101 102

103 104

106

107

109

110

111

112

113

114

116

117

119

120 121

122

123

 $\frac{124}{125}$

126

128

130

```
RightMaintain(ref GetRightReference(root));
132
                          LeftMaintain(ref root)
                          RightMaintain(ref root);
134
135
                 }
136
            }
137
138
            private void RightMaintain(ref TElement root)
139
140
                 if (!EqualToZero(root))
141
142
                     var rootRightNode = GetRight(root);
                     if (!EqualToZero(rootRightNode))
144
145
                          var rootLeftNode = GetLeft(root);
                          var rootRightNodeRightNode = GetRight(rootRightNode);
147
                          if (!EqualToZero(rootRightNodeRightNode) &&
148
                              (EqualToZero(rootLeftNode) |
149
                                 GreaterThan(GetSize(rootRightNodeRightNode), GetSize(rootLeftNode))))
                          {
150
                              LeftRotate(ref root);
151
152
                          else
153
                          {
154
                              var rootRightNodeLeftNode = GetLeft(rootRightNode);
                              if (!EqualToZero(rootRightNodeLeftNode) &&
156
                                  (EqualToZero(rootLeftNode) ||
157
                                      GreaterThan(GetSize(rootRightNodeLeftNode),
                                      GetSize(rootLeftNode))))
                              {
158
                                  RightRotate(ref GetRightReference(root));
                                  LeftRotate(ref root);
160
                              }
161
                              else
162
                              {
163
                                  return;
164
                              }
165
166
                         LeftMaintain(ref GetLeftReference(root));
                         RightMaintain(ref GetRightReference(root));
168
                          LeftMaintain(ref root);
169
170
                          RightMaintain(ref root);
                     }
171
                 }
172
            }
173
        }
    }
175
./Platform.Collections.Methods/Trees/SizeBalancedTreeMethods.cs
    using System;
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
    namespace Platform.Collections.Methods.Trees
 6
        public abstract class SizeBalancedTreeMethods<TElement> :
            SizedBinaryTreeMethodsBase<TElement>
            protected override void AttachCore(ref TElement root, TElement node)
10
                 while (true)
11
12
                     ref var left = ref GetLeftReference(root);
13
                     var leftSize = GetSizeOrZero(left);
14
                     ref var right = ref GetRightReference(root);
15
                     var rightSize = GetSizeOrZero(right);
                     if (FirstIsToTheLeftOfSecond(node, root)) // node.Key less than root.Key
17
                     {
18
                          if (EqualToZero(left))
19
                          {
20
                              IncrementSize(root);
21
                              SetSize(node, One);
22
23
                              left = node;
24
                              return;
25
                          if (FirstIsToTheLeftOfSecond(node, left)) // node.Key less than left.Key
26
27
                              if (GreaterThan(Increment(leftSize), rightSize))
```

```
{
            RightRotate(ref root);
        }
        else
        {
            IncrementSize(root);
            root = ref left;
          // node.Key greater than left.Key
        var leftRightSize = GetSizeOrZero(GetRight(left));
        if (GreaterThan(Increment(leftRightSize), rightSize))
            if (EqualToZero(leftRightSize) && EqualToZero(rightSize))
                SetLeft(node, left);
                SetRight(node, root)
                {\tt SetSize(node,\ Add(leftSize,\ Two));\ //\ Two\ (2)\ -\ node\ the\ size\ of}
                    root and a node itself
                SetLeft(root, Zero);
                SetSize(root, One);
                root = node;
                return;
            LeftRotate(ref left);
            RightRotate(ref root);
        }
        else
            IncrementSize(root);
            root = ref left;
    }
else // node.Key greater than root.Key
    if (EqualToZero(right))
    {
        IncrementSize(root);
        SetSize(node, One);
        right = node;
        return;
    if (FirstIsToTheRightOfSecond(node, right)) // node.Key greater than
    {
        if (GreaterThan(Increment(rightSize), leftSize))
            LeftRotate(ref root);
        }
        else
            IncrementSize(root);
            root = ref right;
    else // node.Key less than right.Key
        var rightLeftSize = GetSizeOrZero(GetLeft(right));
        if (GreaterThan(Increment(rightLeftSize), leftSize))
            if (EqualToZero(rightLeftSize) && EqualToZero(leftSize))
                SetLeft(node, root);
                SetRight(node, right);
                SetSize(node, Add(rightSize, Two)); // Two (2) - node the size

→ of root and a node itself

                SetRight(root, Zero);
                SetSize(root, One);
                root = node;
                return;
            RightRotate(ref right);
            LeftRotate(ref root);
        }
        else
            IncrementSize(root);
```

31

33

34

35 36 37

38 39

40

41 42

43 44

46

47

48

49

51 52

53

54

55 56

57

58

59 60

61 62

63

65

66

67

69 70

71

73

74 75

76

77 78

79

80

81 82

84 85

86

87 88

89

91

92

93

94

95

96

98

99 100

101

```
root = ref right;
                }
            }
        }
    }
}
protected override void DetachCore(ref TElement root, TElement node)
    while (true)
        ref var left = ref GetLeftReference(root);
        var leftSize = GetSizeOrZero(left);
        ref var right = ref GetRightReference(root);
        var rightSize = GetSizeOrZero(right);
        if (FirstIsToTheLeftOfSecond(node, root)) // node.Key less than root.Key
            var decrementedLeftSize = Decrement(leftSize);
            if (GreaterThan(GetSizeOrZero(GetRight(right)), decrementedLeftSize))
                LeftRotate(ref root);
            }
            else if (GreaterThan(GetSizeOrZero(GetLeft(right)), decrementedLeftSize))
                RightRotate(ref right);
                LeftRotate(ref root);
            }
            else
            {
                DecrementSize(root);
                root = ref left;
        else if (FirstIsToTheRightOfSecond(node, root)) // node.Key greater than root.Key
            var decrementedRightSize = Decrement(rightSize);
            if (GreaterThan(GetSizeOrZero(GetLeft(left)), decrementedRightSize))
                RightRotate(ref root);
            else if (GreaterThan(GetSizeOrZero(GetRight(left)), decrementedRightSize))
                LeftRotate(ref left);
                RightRotate(ref root);
            else
            {
                DecrementSize(root);
                root = ref right;
        else // key equals to root.Key
               (GreaterThanZero(leftSize) && GreaterThanZero(rightSize))
            {
                TElement replacement;
                if (GreaterThan(leftSize, rightSize))
                    replacement = left;
                    var replacementRight = GetRight(replacement);
                    while (!EqualToZero(replacementRight))
                        replacement = replacementRight;
                        replacementRight = GetRight(replacement);
                    DetachCore(ref left, replacement);
                }
                else
                    replacement = right;
                    var replacementLeft = GetLeft(replacement);
                    while (!EqualToZero(replacementLeft))
                        replacement = replacementLeft;
                        replacementLeft = GetLeft(replacement);
                    DetachCore(ref right, replacement);
                }
```

107

108

110 111

113

114 115

117

118 119

120 121

123 124

125

126

127 128

130

131

132

133

134 135

136 137

138 139

140

142

143 144

145 146

147

149

151

152

153 154 155

156 157

158

159

160

161

163

165

166

167

168 169

171

172 173

174

176 177

178

179 180

181

```
SetLeft(replacement, left);
183
                              SetRight(replacement, right);
                              SetSize(replacement, Add(leftSize, rightSize));
185
                              root = replacement;
186
                          }
187
                          else if (GreaterThanZero(leftSize))
188
189
                              root = left;
190
                          }
191
                          else if (GreaterThanZero(rightSize))
                          {
193
194
                              root = right;
                          }
                          else
196
                          {
                              root = Zero;
198
199
                          ClearNode(node);
200
201
                          return;
                     }
202
                 }
203
            }
204
        }
205
    }
206
./Platform.Collections.Methods/Trees/SizedAndThreadedAVLBalancedTreeMethods.cs
    using System;
    using System. Runtime. Compiler Services;
    using System.Text;
#if USEARRAYPOOL
    using Platform.Collections;
 5
    #endif
 7
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
    namespace Platform.Collections.Methods.Trees
10
11
        /// <summary>
12
        /// Combination of Size, Height (AVL), and threads.
13
        /// </summary>
14
        /// <remarks>
15
        /// Based on: <a href="https://github.com/programmatom/TreeLib/blob/master/TreeLib/TreeLib/G|
16
            enerated/AVLTreeList.cs">TreeLib.AVLTreeList</a>.
        /// Which itself based on: <a
         → href="https://github.com/GNOME/glib/blob/master/glib/gtree.c">GNOME/glib/gtree</a>.
        /// </remarks>
18
        public abstract class SizedAndThreadedAVLBalancedTreeMethods<TElement> :
19
            SizedBinaryTreeMethodsBase<TElement>
20
             // TODO: Link with size of TElement
21
             private const int MaxPath = 92;
22
             public override bool Contains (TElement node, TElement root)
24
25
                 while (!EqualToZero(root))
26
                 {
27
                     if (FirstIsToTheLeftOfSecond(node, root)) // node.Key < root.Key</pre>
28
29
                          root = GetLeftOrDefault(root);
31
                     else if (FirstIsToTheRightOfSecond(node, root)) // node.Key > root.Key
32
                          root = GetRightOrDefault(root);
34
35
                     else // node.Key == root.Key
36
                          return true;
38
40
                 return false;
41
             }
42
43
             protected override void PrintNode(TElement node, StringBuilder sb, int level)
45
                 base.PrintNode(node, sb, level);
46
                 sb.Append(' ');
47
                 sb.Append(GetLeftIsChild(node) ? 'l' : 'L');
                 sb.Append(GetRightIsChild(node) ? 'r' : 'R');
49
                 sb.Append(' ');
50
```

```
sb.Append(GetBalance(node));
             }
5.3
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected void IncrementBalance(TElement node) => SetBalance(node,
                (sbyte)(GetBalance(node) + 1));
56
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected void DecrementBalance(TElement node) => SetBalance(node,
                (sbyte)(GetBalance(node) - 1));
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected override TElement GetLeftOrDefault(TElement node) => GetLeftIsChild(node) ?
61
             \;\hookrightarrow\;\; \texttt{GetLeft(node)}\;:\; \textcolor{red}{\texttt{default;}}
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected override TElement GetRightOrDefault(TElement node) => GetRightIsChild(node) ?
64
                GetRight(node) : default;
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
66
            protected abstract bool GetLeftIsChild(TElement node);
67
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
69
            protected abstract void SetLeftIsChild(TElement node, bool value);
71
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
73
            protected abstract bool GetRightIsChild(TElement node);
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
76
            protected abstract void SetRightIsChild(TElement node, bool value);
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
78
            protected abstract sbyte GetBalance(TElement node);
79
80
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
81
            protected abstract void SetBalance(TElement node, sbyte value);
82
83
            protected override void AttachCore(ref TElement root, TElement node)
84
85
                 unchecked
86
                 {
87
                     // TODO: Check what is faster to use simple array or array from array pool
                     // TODO: Try to use stackalloc as an optimization (requires code generation,
89
                         because of generics)
    #if USEARRAYPOOL
90
                     var path = ArrayPool.Allocate<TElement>(MaxPath);
91
                     var pathPosition = 0;
92
93
                     path[pathPosition++] = default;
    #else
94
                     var path = new TElement[MaxPath];
                     var pathPosition = 1;
96
    #endif
97
                     var currentNode = root;
98
                     while (true)
99
100
                             (FirstIsToTheLeftOfSecond(node, currentNode))
101
102
103
                              if (GetLeftIsChild(currentNode))
104
                                  IncrementSize(currentNode);
105
                                  path[pathPosition++] = currentNode;
                                  currentNode = GetLeft(currentNode);
107
108
                              else
109
110
                                  // Threads
                                  SetLeft(node, GetLeft(currentNode));
112
                                  SetRight(node, currentNode);
113
                                  SetLeft(currentNode, node);
114
                                  SetLeftIsChild(currentNode,
                                                                true);
                                  DecrementBalance(currentNode);
116
                                  SetSize(node, One);
117
                                  FixSize(currentNode); // Should be incremented already
118
                                  break;
119
120
122
                          else if (FirstIsToTheRightOfSecond(node, currentNode))
123
                              if (GetRightIsChild(currentNode))
```

```
{
125
                                   IncrementSize(currentNode);
                                   path[pathPosition++] = currentNode;
127
                                   currentNode = GetRight(currentNode);
128
                               else
130
131
                                    // Threads
132
                                   SetRight(node, GetRight(currentNode));
133
                                   SetLeft(node, currentNode);
134
                                   SetRight(currentNode, node);
135
                                   SetRightIsChild(currentNode, true);
136
                                   IncrementBalance(currentNode);
137
138
                                   SetSize(node, One);
139
                                   FixSize(currentNode); // Should be incremented already
                                   break;
140
                               }
                          }
142
                           else
143
144
                               throw new InvalidOperationException("Node with the same key already
145
                               → attached to a tree.");
                          }
146
                      // Restore balance. This is the goodness of a non-recursive
148
                      // implementation, when we are done with balancing we 'break'
149
150
                      // the loop and we are done.
                      while (true)
151
152
                           var parent = path[--pathPosition];
153
                          var isLeftNode = !AreEqual(parent, default) && AreEqual(currentNode,

   GetLeft(parent));
                          var currentNodeBalance = GetBalance(currentNode);
155
                          if (currentNodeBalance < -1 || currentNodeBalance > 1)
156
157
                               currentNode = Balance(currentNode);
159
                               if (AreEqual(parent, default))
                               {
160
                                   root = currentNode;
161
                               }
162
                               else if (isLeftNode)
163
164
                                   SetLeft(parent, currentNode);
165
                                   FixSize(parent);
166
                               else
168
169
                                   SetRight(parent, currentNode);
170
                                   FixSize(parent);
171
                          currentNodeBalance = GetBalance(currentNode);
174
                          if (currentNodeBalance == 0 || AreEqual(parent, default))
175
176
                               break;
177
178
                             (isLeftNode)
179
                           {
180
                               DecrementBalance(parent);
181
                          else
183
                          {
184
                               IncrementBalance(parent);
185
186
                           currentNode = parent;
187
188
    #if USEARRAYPOOL
189
                      ArrayPool.Free(path);
190
    #endif
191
                 }
192
             }
193
             private TElement Balance(TElement node)
195
196
                 unchecked
197
                 {
198
                      var rootBalance = GetBalance(node);
199
                      if (rootBalance < -1)</pre>
```

```
var left = GetLeft(node);
            if (GetBalance(left) > 0)
                SetLeft(node, LeftRotateWithBalance(left));
                FixSize(node);
            node = RightRotateWithBalance(node);
        else if (rootBalance > 1)
            var right = GetRight(node);
            if (GetBalance(right) < 0)</pre>
                SetRight(node, RightRotateWithBalance(right));
                FixSize(node);
            }
            node = LeftRotateWithBalance(node);
        return node;
    }
}
protected TElement LeftRotateWithBalance(TElement node)
    unchecked
        var right = GetRight(node);
        if (GetLeftIsChild(right))
            SetRight(node, GetLeft(right));
        }
        else
            SetRightIsChild(node, false);
            SetLeftIsChild(right, true);
        SetLeft(right, node);
        // Fix size
        SetSize(right, GetSize(node));
        FixSize(node);
        // Fix balance
        var rootBalance = GetBalance(node);
        var rightBalance = GetBalance(right);
        if (rightBalance <= 0)</pre>
            if (rootBalance >= 1)
            {
                SetBalance(right, (sbyte)(rightBalance - 1));
            }
            else
            {
                SetBalance(right, (sbyte)(rootBalance + rightBalance - 2));
            SetBalance(node, (sbyte)(rootBalance - 1));
        else
            if (rootBalance <= rightBalance)</pre>
                SetBalance(right, (sbyte)(rootBalance - 2));
            }
            else
            {
                SetBalance(right, (sbyte)(rightBalance - 1));
            SetBalance(node, (sbyte)(rootBalance - rightBalance - 1));
        return right;
    }
}
protected TElement RightRotateWithBalance(TElement node)
    unchecked
    {
        var left = GetLeft(node);
        if (GetRightIsChild(left))
```

203 204

206 207

208

210 211

212

213 214 215

216

217

 $\frac{218}{219}$

220

221

 $\frac{222}{223}$

 $\frac{225}{226}$

227

228

229 230

231

 $\frac{232}{233}$

234

236 237

238

240

241

242

243

244

245

247

248

249

250

251

253 254

256

257

259 260

262

263

264

265 266 267

268

269

270

271

273 274 275

```
SetLeft(node, GetRight(left));
        }
        else
        {
            SetLeftIsChild(node, false);
            SetRightIsChild(left, true);
        SetRight(left, node);
        // Fix size
        SetSize(left, GetSize(node));
        FixSize(node);
        // Fix balance
        var rootBalance = GetBalance(node);
        var leftBalance = GetBalance(left);
        if (leftBalance <= 0)</pre>
            if (leftBalance > rootBalance)
                SetBalance(left, (sbyte)(leftBalance + 1));
            else
            {
                SetBalance(left, (sbyte)(rootBalance + 2));
            SetBalance(node, (sbyte)(rootBalance - leftBalance + 1));
        else
            if (rootBalance <= -1)</pre>
            {
                SetBalance(left, (sbyte)(leftBalance + 1));
            }
            else
            {
                SetBalance(left, (sbyte)(rootBalance + leftBalance + 2));
            SetBalance(node, (sbyte)(rootBalance + 1));
        return left;
    }
}
protected TElement GetNext(TElement node)
    unchecked
    {
        var current = GetRight(node);
        if (GetRightIsChild(node))
            while (GetLeftIsChild(current))
                 current = GetLeft(current);
        return current;
    }
}
protected TElement GetPrevious(TElement node)
    unchecked
        var current = GetLeft(node);
        if (GetLeftIsChild(node))
            while (GetRightIsChild(current))
                current = GetRight(current);
            }
        return current;
    }
}
protected override void DetachCore(ref TElement root, TElement node)
    unchecked
```

283

284

 $\frac{285}{286}$

287

288

289

290

291 292

293

294 295

297

298 299

300

301

303

 $304 \\ 305$

306 307

309

310

311

312

313

314

316

318

319

 $\frac{320}{321}$

322 323

 $\frac{324}{325}$

 $\frac{326}{327}$

328

329 330

332 333

334

335

336 337

338 339

 $\frac{340}{341}$

343 344

 $\frac{345}{346}$

347

 $\frac{348}{349}$

350

351

352 353

354 355 356

```
#if USEARRAYPOOL
358
                      var path = ArrayPool.Allocate<TElement>(MaxPath);
                      var pathPosition = 0;
360
                      path[pathPosition++] = default;
361
    #else
362
                      var path = new TElement[MaxPath];
363
                      var pathPosition = 1;
364
    #endif
365
                      var currentNode = root;
366
                      while (true)
367
368
                          if (FirstIsToTheLeftOfSecond(node, currentNode))
369
370
                               if (!GetLeftIsChild(currentNode))
372
                                   throw new InvalidOperationException("Cannot find a node.");
373
                               DecrementSize(currentNode);
375
                               path[pathPosition++] = currentNode;
376
                               currentNode = GetLeft(currentNode);
377
378
                          else if (FirstIsToTheRightOfSecond(node, currentNode))
379
380
                               if (!GetRightIsChild(currentNode))
                               {
382
                                   throw new InvalidOperationException("Cannot find a node.");
383
384
                               DecrementSize(currentNode);
385
                               path[pathPosition++] = currentNode;
386
                               currentNode = GetRight(currentNode);
387
                          else
389
                          {
390
                               break;
391
                          }
392
                      }
393
                      var parent = path[--pathPosition];
394
                      var balanceNode = parent;
                      var isLeftNode = !AreEqual(parent, default) && AreEqual(currentNode,
396
                          GetLeft(parent));
                      if (!GetLeftIsChild(currentNode))
397
398
                          if (!GetRightIsChild(currentNode)) // node has no children
400
                               if (AreEqual(parent, default))
401
                               {
402
                                   root = Zero;
403
                               }
404
                               else if (isLeftNode)
405
406
                                   SetLeftIsChild(parent, false);
407
                                   SetLeft(parent, GetLeft(currentNode));
408
409
                                   IncrementBalance(parent);
410
                               else
411
                               {
412
                                   SetRightIsChild(parent, false);
413
                                   SetRight(parent, GetRight(currentNode));
                                   DecrementBalance(parent);
415
416
417
                          else // node has a right child
418
419
                               var successor = GetNext(currentNode);
420
421
                               SetLeft(successor, GetLeft(currentNode));
422
                               var right = GetRight(currentNode);
                               if (AreEqual(parent, default))
423
424
                                   root = right;
425
                               }
426
                               else if (isLeftNode)
427
428
429
                                   SetLeft(parent, right);
                                   IncrementBalance(parent);
                               }
431
432
                               else
                               {
433
                                   SetRight(parent, right);
434
```

```
DecrementBalance(parent);
    }
else // node has a left child
    if (!GetRightIsChild(currentNode))
        var predecessor = GetPrevious(currentNode);
        SetRight(predecessor, GetRight(currentNode));
        var leftValue = GetLeft(currentNode);
        if (AreEqual(parent, default))
            root = leftValue;
        }
        else if (isLeftNode)
            SetLeft(parent, leftValue);
            IncrementBalance(parent);
        else
            SetRight(parent, leftValue);
            DecrementBalance(parent);
    }
    else // node has a both children (left and right)
        var predecessor = GetLeft(currentNode);
        var successor = GetRight(currentNode);
        var successorParent = currentNode
        int previousPathPosition = ++pathPosition;
        // find the immediately next node (and its parent)
        while (GetLeftIsChild(successor))
            path[++pathPosition] = successorParent = successor;
            successor = GetLeft(successor);
            if (!AreEqual(successorParent, currentNode))
                DecrementSize(successorParent);
        path[previousPathPosition] = successor;
        balanceNode = path[pathPosition];
        // remove 'successor' from the tree
           (!AreEqual(successorParent, currentNode))
            if (!GetRightIsChild(successor))
            {
                SetLeftIsChild(successorParent, false);
            }
            else
            {
                SetLeft(successorParent, GetRight(successor));
            IncrementBalance(successorParent);
            SetRightIsChild(successor, true);
            SetRight(successor, GetRight(currentNode));
        else
        {
            DecrementBalance(currentNode);
        // set the predecessor's successor link to point to the right place
        while (GetRightIsChild(predecessor))
            predecessor = GetRight(predecessor);
        SetRight(predecessor, successor);
        // prepare 'successor' to replace 'node'
        var left = GetLeft(currentNode);
        SetLeftIsChild(successor, true);
        SetLeft(successor, left);
        SetBalance(successor, GetBalance(currentNode));
        FixSize(successor);
        if (AreEqual(parent, default))
        {
            root = successor;
```

437 438

440

441 442

443

444

445

446 447

448

449

450 451

453 454

455 456

457

459

460 461

462

463

464

465

466

467

468 469

470

471

472

474 475 476

477

478

479

480 481

482

483

484

485 486

487

488 489

490

491

492 493

494

496 497

498

500

501 502 503

504

505

507

508

510

511

```
513
                                else if (isLeftNode)
515
                                    SetLeft(parent, successor);
516
                               }
                               else
518
                                {
519
                                    SetRight(parent, successor);
520
                               }
521
                           }
522
523
                       // restore balance
524
                      if (!AreEqual(balanceNode, default))
525
526
527
                           while (true)
528
                                var balanceParent = path[--pathPosition];
529
                               isLeftNode = !AreEqual(balanceParent, default) && AreEqual(balanceNode,
530
                                   GetLeft(balanceParent));
                               var currentNodeBalance = GetBalance(balanceNode);
531
                               if (currentNodeBalance < -1 || currentNodeBalance > 1)
532
533
                                    balanceNode = Balance(balanceNode);
                                    if (AreEqual(balanceParent, default))
535
                                    {
536
                                        root = balanceNode;
537
                                    }
538
                                    else if (isLeftNode)
539
540
                                        SetLeft(balanceParent, balanceNode);
541
542
543
                                    else
                                    {
544
545
                                         SetRight(balanceParent, balanceNode);
546
547
                               currentNodeBalance = GetBalance(balanceNode);
548
                                   (currentNodeBalance != 0 || AreEqual(balanceParent, default))
550
                                    break;
                               }
552
                                   (isLeftNode)
                               i f
553
                                {
554
                                    IncrementBalance(balanceParent);
                               }
556
557
                                else
                                {
558
                                    DecrementBalance(balanceParent);
559
560
                               balanceNode = balanceParent;
561
                           }
562
563
                      ClearNode(node);
564
    #if USEARRAYPOOL
565
                      ArrayPool.Free(path);
566
    #endif
567
                  }
568
             }
569
              [MethodImpl(MethodImplOptions.AggressiveInlining)]
571
             protected override void ClearNode(TElement node)
572
573
                  SetLeft(node, Zero);
                  SetRight(node, Zero);
575
                  SetSize(node, Zero);
576
577
                  SetLeftIsChild(node, false);
578
                  SetRightIsChild(node, false);
                  SetBalance(node, 0);
579
580
         }
581
582
./Platform.Collections.Methods/Trees/SizedBinaryTreeMethodsBase.cs
    using System;
    using System.Runtime.CompilerServices;
using System.Text;
 3
    using Platform. Numbers;
    //#define ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
```

```
#pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Trees
10
   {
       public abstract class SizedBinaryTreeMethodsBase<TElement> :
11
           GenericCollectionMethodsBase<TElement>
12
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
13
           protected abstract ref TElement GetLeftReference(TElement node);
14
15
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
16
           protected abstract ref TElement GetRightReference(TElement node);
17
18
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected abstract TElement GetLeft(TElement node);
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
22
           protected abstract TElement GetRight(TElement node);
23
24
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
25
           protected abstract TElement GetSize(TElement node);
26
27
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
28
           protected abstract void SetLeft(TElement node, TElement left);
30
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
31
           protected abstract void SetRight(TElement node, TElement right);
32
33
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected abstract void SetSize(TElement node, TElement size);
3.5
36
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
37
           protected abstract bool FirstIsToTheLeftOfSecond(TElement first, TElement second);
38
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
40
           protected abstract bool FirstIsToTheRightOfSecond(TElement first, TElement second);
41
42
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
43
           protected virtual TElement GetLeftOrDefault(TElement node) => AreEqual(node, default) ?

→ default : GetLeft(node);
45
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
46
           protected virtual TElement GetRightOrDefault(TElement node) => AreEqual(node, default) ?
47
               default : GetRight(node);
48
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected void IncrementSize(TElement node) => SetSize(node, Increment(GetSize(node)));
50
51
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected void DecrementSize(TElement node) => SetSize(node, Decrement(GetSize(node)));
5.3
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
55
           protected TElement GetLeftSize(TElement node) => GetSizeOrZero(GetLeftOrDefault(node));
56
57
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
58
           protected TElement GetRightSize(TElement node) => GetSizeOrZero(GetRightOrDefault(node));
59
60
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
61
           protected TElement GetSizeOrZero(TElement node) => EqualToZero(node) ? Zero :

→ GetSize(node);

63
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
64
           protected void FixSize(TElement node) => SetSize(node, Increment(Add(GetLeftSize(node),

→ GetRightSize(node)));
66
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected void LeftRotate(ref TElement root) => root = LeftRotate(root);
69
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
70
           protected TElement LeftRotate(TElement root)
7.1
72
                var right = GetRight(root)
73
   #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
74
                if (EqualToZero(right))
75
                {
76
                    throw new Exception("Right is null.");
77
                }
78
   #endif
79
                SetRight(root, GetLeft(right));
80
```

```
SetLeft(right, root);
                 SetSize(right, GetSize(root));
                 FixSize(root);
83
                 return right;
            }
85
86
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
87
            protected void RightRotate(ref TElement root) => root = RightRotate(root);
88
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
90
            protected TElement RightRotate(TElement root)
91
92
                 var left = GetLeft(root)
93
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
94
                 if (EqualToZero(left))
96
                     throw new Exception("Left is null.");
97
98
    #endif
99
                 SetLeft(root, GetRight(left));
100
                 SetRight(left, root);
                 SetSize(left, GetSize(root));
102
                 FixSize(root);
103
104
                 return left;
            }
105
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
107
            public virtual bool Contains(TElement node, TElement root)
108
109
                 while (!EqualToZero(root))
110
111
                     if (FirstIsToTheLeftOfSecond(node, root)) // node.Key < root.Key</pre>
                     {
                         root = GetLeft(root);
114
                     }
115
                     else if (FirstIsToTheRightOfSecond(node, root)) // node.Key > root.Key
117
                         root = GetRight(root);
118
                     else // node.Key == root.Key
120
121
                         return true;
122
123
124
                 return false;
125
126
127
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
128
            protected virtual void ClearNode(TElement node)
129
                 SetLeft(node, Zero);
131
                 SetRight(node, Zero);
SetSize(node, Zero);
132
            }
134
135
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public void Attach(ref TElement root, TElement node)
137
138
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
139
                 ValidateSizes(root);
140
                 Debug.WriteLine("--BeforeAttach--");
141
                 Debug.WriteLine(PrintNodes(root));
142
                 Debug.WriteLine("----"):
143
                 var sizeBefore = GetSize(root);
144
    #endif
145
                 if (EqualToZero(root))
146
                 {
148
                     SetSize(node, One);
                     root = node;
149
                     return;
150
151
    153
154
                 Debug.WriteLine(PrintNodes(root));
155
                 Debug.WriteLine("----");
156
                 ValidateSizes(root);
                 var sizeAfter = GetSize(root);
                 if (!IsEquals(MathHelpers.Increment(sizeBefore), sizeAfter))
159
```

```
160
                     throw new Exception("Tree was broken after attach.");
162
    #endif
163
164
165
             protected abstract void AttachCore(ref TElement root, TElement node);
166
167
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             public void Detach(ref TElement root, TElement node)
169
170
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
171
                 ValidateSizes(root);
172
                 Debug.WriteLine("--BeforeDetach--");
173
                 Debug.WriteLine(PrintNodes(root));
174
                 Debug.WriteLine("----"):
175
                 var sizeBefore = GetSize(root);
176
                 if (ValueEqualToZero(root))
177
178
                     throw new Exception($"Элемент с {node} не содержится в дереве.");
179
180
    #endif
181
                 DetachCore(ref root, node)
182
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
183
                 Debug.WriteLine("--AfterDetach--");
184
                 Debug.WriteLine(PrintNodes(root));
185
                 Debug.WriteLine("-----');
186
                 ValidateSizes(root);
187
                 var sizeAfter = GetSize(root);
188
                 if (!IsEquals(MathHelpers.Decrement(sizeBefore), sizeAfter))
189
190
                     throw new Exception("Tree was broken after detach.");
191
                 }
192
    #endif
193
194
             protected abstract void DetachCore(ref TElement root, TElement node);
196
             public void FixSizes(TElement node)
198
199
                 if (AreEqual(node, default))
200
                 {
201
                     return;
202
                 FixSizes(GetLeft(node))
204
                 FixSizes(GetRight(node));
205
                 FixSize(node);
             }
207
208
             public void ValidateSizes(TElement node)
209
210
                 if (AreEqual(node, default))
211
212
                     return;
213
                 }
214
                 var size = GetSize(node);
215
                 var leftSize = GetLeftSize(node);
216
217
                 var rightSize = GetRightSize(node);
                 var expectedSize = Arithmetic.Increment(Arithmetic.Add(leftSize, rightSize));
                 if (!AreEqual(size, expectedSize))
219
                 {
220
                     throw new InvalidOperationException($|"Size of {node} is not valid. Expected
221

    size: {expectedSize}, actual size: {size}.");
223
                 ValidateSizes(GetLeft(node));
                 ValidateSizes(GetRight(node));
224
             }
225
226
             public void ValidateSize(TElement node)
227
229
                 var size = GetSize(node);
                 var leftSize = GetLeftSize(node);
230
                 var rightSize = GetRightSize(node);
231
                 var expectedSize = Arithmetic.Increment(Arithmetic.Add(leftSize, rightSize));
232
                 if (!AreEqual(size, expectedSize))
233
                 {
234
                     throw new InvalidOperationException(S Size of {node} is not valid. Expected
235

    size: {expectedSize}, actual size: {size}.");
```

```
236
237
238
             public string PrintNodes(TElement node)
240
                 var sb = new StringBuilder();
241
                 PrintNodes(node, sb);
242
                 return sb.ToString();
243
244
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
246
             public void PrintNodes(TElement node, StringBuilder sb) => PrintNodes(node, sb, 0);
247
248
             public void PrintNodes(TElement node, StringBuilder sb, int level)
249
250
                 if (AreEqual(node, default))
                 {
252
                     return;
253
254
                 PrintNodes(GetLeft(node), sb, level + 1);
255
                 PrintNode(node, sb, level);
256
                 sb.AppendLine();
257
                 PrintNodes(GetRight(node), sb, level + 1);
258
259
260
             public string PrintNode(TElement node)
261
262
                 var sb = new StringBuilder();
263
                 PrintNode(node, sb);
264
                 return sb.ToString();
265
267
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected void PrintNode(TElement node, StringBuilder sb) => PrintNode(node, sb, 0);
269
270
             protected virtual void PrintNode(TElement node, StringBuilder sb, int level)
271
272
                 sb.Append('\t', level);
273
                 sb.Append(node);
275
                 PrintNodeValue(node, sb);
                 sb.Append(' ');
276
                 sb.Append('s');
277
                 sb.Append(GetSize(node));
278
279
             protected abstract void PrintNodeValue(TElement node, StringBuilder sb);
281
        }
282
./Platform.Collections.Methods.Tests/SizeBalancedTree2.cs
    using System;
using System.Collections.Generic;
    using System.Text;
    using Platform. Numbers:
    using Platform.Collections.Methods.Trees;
    namespace Platform.Collections.Methods.Tests
 8
        public class SizeBalancedTree2<TElement> : SizeBalancedTreeMethods2<TElement>
 9
10
             private struct TreeElement
12
                 public TElement Size;
 13
                 public TElement Left;
14
                 public TElement Right;
                 public sbyte Balance;
16
                 public bool LeftIsChild;
17
                 public bool RightIsChild;
19
             private readonly TreeElement[] _elements;
21
             private TElement _allocated;
23
             public TElement Root;
25
             public TElement Count => GetSizeOrZero(Root);
27
             public SizeBalancedTree2(int capacity) => (_elements, _allocated) = (new
             → TreeElement[capacity], Integer<TElement>.One);
29
```

```
public TElement Allocate()
30
                var newNode = _allocated;
32
                if (IsEmpty(newNode))
34
                    _allocated = Arithmetic.Increment(_allocated);
35
                    return newNode;
36
                }
37
                else
                {
39
                    throw new InvalidOperationException("Allocated tree element is not empty.");
40
                }
41
           }
43
           public void Free(TElement node)
45
                while (!EqualityComparer.Equals(_allocated, Integer<TElement>.One) && IsEmpty(node))
46
47
                    var lastNode = Arithmetic.Decrement(_allocated);
                    if (EqualityComparer.Equals(lastNode, node))
49
50
                        _allocated = lastNode;
51
                        node = Arithmetic.Decrement(node);
52
                    }
                    else
54
                    {
56
                        return;
57
                }
           }
59
           public bool IsEmpty(TElement node) =>
61
            Gefault.Equals(GetElement(node), default);
62
           protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
               Comparer.Compare(first, second) < 0;</pre>
64
           protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>

→ Comparer.Compare(first, second) > 0;

66
           protected override ref TElement GetLeftReference(TElement node) => ref
67

   GetElement(node).Left;
68
           protected override TElement GetLeft(TElement node) => GetElement(node).Left;
69
70
           protected override ref TElement GetRightReference(TElement node) => ref
7.1

   GetElement(node).Right;
           protected override TElement GetRight(TElement node) => GetElement(node).Right;
7.3
           protected override TElement GetSize(TElement node) => GetElement(node).Size;
7.5
           protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
77

⇒ sb.Append(node);

           protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
            → left;
80
           protected override void SetRight(TElement node, TElement right) =>

→ GetElement(node).Right = right;

82
           protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =

→ size;

           private ref TreeElement GetElement(TElement node) => ref
               _elements[(Integer<TElement>)node];
       }
86
87
./Platform.Collections.Methods.Tests/SizeBalancedTree.cs
   using System;
   using System.Collections.Generic;
   using System. Text;
3
   using Platform. Numbers;
   using Platform.Collections.Methods.Trees;
   namespace Platform.Collections.Methods.Tests
       public class SizeBalancedTree<TElement> : SizeBalancedTreeMethods<TElement>
```

```
private struct TreeElement
    public TElement Size;
    public TElement Left;
    public TElement Right;
    public sbyte Balance;
    public bool LeftIsChild
    public bool RightIsChild;
}
private readonly TreeElement[] _elements;
private TElement _allocated;
public TElement Root;
public TElement Count => GetSizeOrZero(Root);
public SizeBalancedTree(int capacity) => (_elements, _allocated) = (new
→ TreeElement[capacity], Integer<TElement>.One);
public TElement Allocate()
    var newNode = _allocated;
    if (IsEmpty(newNode))
        _allocated = Arithmetic.Increment(_allocated);
        return newNode;
    }
    else
        throw new InvalidOperationException("Allocated tree element is not empty.");
    }
}
public void Free(TElement node)
    while (!EqualityComparer.Equals(_allocated, Integer<TElement>.One) && IsEmpty(node))
        var lastNode = Arithmetic.Decrement(_allocated);
        if (EqualityComparer.Equals(lastNode, node))
            _allocated = lastNode;
            node = Arithmetic.Decrement(node);
        }
        else
        {
            return;
        }
    }
}
public bool IsEmpty(TElement node) =>
Gefault.Equals(GetElement(node), default);
protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
→ Comparer.Compare(first, second) < 0;</pre>
protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>

→ Comparer.Compare(first, second) > 0;

protected override ref TElement GetLeftReference(TElement node) => ref

→ GetElement(node).Left;

protected override TElement GetLeft(TElement node) => GetElement(node).Left;
protected override ref TElement GetRightReference(TElement node) => ref

   GetElement(node).Right;
protected override TElement GetRight(TElement node) => GetElement(node).Right;
protected override TElement GetSize(TElement node) => GetElement(node).Size;
protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
\rightarrow sb.Append(node);
protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
→ left;
```

11 12

13

14

15

17

18

19 20

21 22 23

24

26

29

31

33 34

35

36

37

38 39

40

41

42 43

44 45

46 47

48

49

51

52

53

56

57

58

59 60

61

63

65

66

68

70

71

72

73 74

75 76

77

79

```
protected override void SetRight(TElement node, TElement right) =>
81

   GetElement(node).Right = right;
            protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =
83

    size;

84
            private ref TreeElement GetElement(TElement node) => ref
85

    _elements[(Integer<TElement>)node];
        }
   }
87
./Platform.Collections.Methods.Tests/SizedAndThreadedAVLBalancedTree.cs
   using System;
   using System.Collections.Generic;
   using System. Text;
   using Platform Numbers;
   using Platform.Collections.Methods.Trees;
   namespace Platform.Collections.Methods.Tests
7
       public class SizedAndThreadedAVLBalancedTree<TElement> :
9
           SizedAndThreadedAVLBalancedTreeMethods<TElement>
10
            private struct TreeElement
11
12
                public TElement Size;
13
                public TElement Left;
public TElement Right;
15
                public sbyte Balance;
16
                public bool LeftIsChild
                public bool RightIsChild;
18
            }
20
            private readonly TreeElement[] _elements;
            private TElement _allocated;
22
23
            public TElement Root;
24
25
            public TElement Count => GetSizeOrZero(Root);
26
27
            public SizedAndThreadedAVLBalancedTree(int capacity) => (_elements, _allocated) = (new
28
            → TreeElement[capacity], Integer<TElement>.One);
            public TElement Allocate()
30
31
                var newNode = _allocated;
32
                if (IsEmpty(newNode))
33
                    _allocated = Arithmetic.Increment(_allocated);
                    return newNode;
36
                }
                else
38
                {
                    throw new InvalidOperationException("Allocated tree element is not empty.");
41
            }
42
43
            public void Free(TElement node)
44
                while (!EqualityComparer.Equals(_allocated, Integer<TElement>.One) && IsEmpty(node))
46
47
                    var lastNode = Arithmetic.Decrement(_allocated);
48
                    if (EqualityComparer.Equals(lastNode, node))
49
50
                         _allocated = lastNode;
                        node = Arithmetic.Decrement(node);
52
53
                    else
54
                    {
55
                        return;
                    }
57
                }
58
            }
60
            public bool IsEmpty(TElement node) =>
61
            Gefault.Equals(GetElement(node), default);
62
            protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
63

→ Comparer.Compare(first, second) < 0;
</p>
64
```

```
protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>
6.5

→ Comparer.Compare(first, second) > 0;

66
            protected override sbyte GetBalance(TElement node) => GetElement(node).Balance;
67
            protected override bool GetLeftIsChild(TElement node) => GetElement(node).LeftIsChild;
69
70
            protected override ref TElement GetLeftReference(TElement node) => ref
7.1

   GetElement(node).Left;
            protected override TElement GetLeft(TElement node) => GetElement(node).Left;
73
            protected override bool GetRightIsChild(TElement node) => GetElement(node).RightIsChild;
76
            protected override ref TElement GetRightReference(TElement node) => ref

   GetElement(node).Right;
78
            protected override TElement GetRight(TElement node) => GetElement(node).Right;
80
            protected override TElement GetSize(TElement node) => GetElement(node).Size;
81
82
            protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
83

    sb.Append(node);
84
            protected override void SetBalance(TElement node, sbyte value) =>
85

    GetElement(node).Balance = value;

            protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
87
            → left:
            protected override void SetLeftIsChild(TElement node, bool value) =>
89

    GetElement(node).LeftIsChild = value;

90
            protected override void SetRight(TElement node, TElement right) =>
91

   GetElement(node).Right = right;
            protected override void SetRightIsChild(TElement node, bool value) =>
93

→ GetElement(node).RightIsChild = value;

            protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =

    size;

96
            private ref TreeElement GetElement(TElement node) => ref
97
               _elements[(Integer<TElement>)node];
       }
98
99
./Platform.Collections.Methods.Tests/TestExtensions.cs
   using System;
1
   using System.Collections.Generic;
   using Xunit;
3
   using Platform. Numbers;
   using Platform.Collections.Methods.Trees;
   namespace Platform.Collections.Methods.Tests
8
       public static class TestExtensions
10
            public static void TestMultipleCreationsAndDeletions<TElement>(this
11
                SizedBinaryTreeMethodsBase<TElement> tree, Func<TElement> allocate, Action<TElement>
               free, ref TElement root, Func<TElement> treeCount, int maximumOperationsPerCycle)
12
                for (var N = 1; N < maximumOperationsPerCycle; N++)</pre>
13
                {
14
                    var currentCount = 0;
15
                    for (var i = 0; i < N; i++)</pre>
16
17
                        var node = allocate();
18
                        tree.Attach(ref root, node);
19
                        currentCount++;
20
                        Assert.Equal(currentCount, (int)(Integer<TElement>)treeCount());
21
22
                    for (var i = 1; i <= N; i++)</pre>
23
24
                        TElement node = (Integer<TElement>)i;
25
                        if (tree.Contains(node, root))
26
                        {
27
                             tree.Detach(ref root, node);
28
                             free(node);
29
```

```
currentCount--;
30
                                                       Assert.Equal(currentCount, (int)(Integer<TElement>)treeCount());
                                               }
32
                                       }
33
                               }
                       }
35
36
                       public static void TestMultipleRandomCreationsAndDeletions<TElement>(this
                               SizedBinaryTreeMethodsBase<TElement> tree, ref TElement root, Func<TElement>
                               treeCount, int maximumOperationsPerCycle)
38
                               var random = new System.Random(0);
                               var added = new HashSet<TElement>();
40
                               var currentCount = 0;
41
                               for (var N = 1; N < maximumOperationsPerCycle; N++)</pre>
42
43
                                       for (var i = 0; i < N; i++)</pre>
44
45
                                                var node = (Integer<TElement>)random.Next(1, N);
46
                                                if (added.Add(node))
47
48
                                                       tree.Attach(ref root, node);
49
                                                       currentCount++;
50
                                                       Assert.Equal(currentCount, (int)(Integer<TElement>)treeCount());
                                                }
52
53
                                       for (var i = 1; i <= N; i++)
55
                                               TElement node = (Integer<TElement>)random.Next(1, N);
56
                                                if (tree.Contains(node, root))
                                                       tree.Detach(ref root, node);
5.9
60
                                                       currentCount--
                                                       Assert.Equal(currentCount, (int)(Integer<TElement>)treeCount());
61
                                                       added.Remove(node);
62
                                               }
63
                                       }
64
                              }
65
                      }
66
               }
       }
68
./Platform.Collections.Methods.Tests/TreesTests.cs
      using Xunit;
 1
      namespace Platform.Collections.Methods.Tests
 3
               public static class TreesTests
 5
                       private const int _n = 500;
                       [Fact]
 9
                       public static void SizeBalancedTreeMultipleAttachAndDetachTest()
10
                               var sizeBalancedTree = new SizeBalancedTree<uint>(10000);
12
                               sizeBalancedTree.TestMultipleCreationsAndDeletions(sizeBalancedTree.Allocate,
13

→ sizeBalancedTree.Free, ref sizeBalancedTree.Root, () => sizeBalancedTree.Count,

                                       _n);
                       }
14
                       [Fact]
16
                       public static void SizeBalancedTree2MultipleAttachAndDetachTest()
17
18
19
                               var sizeBalancedTree2 = new SizeBalancedTree2<uint>(10000);
                               sizeBalancedTree2.TestMultipleCreationsAndDeletions(sizeBalancedTree2.Allocate, and a sizeBalancedTree2.Allocate, and a sizeBalancedTree3.Allocate, and a sizeBalancedTree3.Al
20
                                       sizeBalancedTree2.Free, ref sizeBalancedTree2.Root, () =>
                                       sizeBalancedTree2.Count, _n);
                       }
                       [Fact]
23
                       public static void SizedAndThreadedAVLBalancedTreeMultipleAttachAndDetachTest()
24
25
                               var avlTree = new SizedAndThreadedAVLBalancedTree<uint>(10000);
                               avlTree.TestMultipleCreationsAndDeletions(avlTree.Allocate, avlTree.Free, ref
27
                                      avlTree.Root, () => avlTree.Count, _n);
                       }
28
                       [Fact]
30
                       public static void SizeBalancedTreeMultipleRandomAttachAndDetachTest()
```

```
{
32
                 var sizeBalancedTree = new SizeBalancedTree<uint>(10000);
                 {\tt sizeBalancedTree.TestMultipleRandomCreationsAndDeletions} ( {\tt ref} \ {\tt sizeBalancedTree.Root}, \\
34
                 }
35
            public static void SizeBalancedTree2MultipleRandomAttachAndDetachTest()
{
37
38
                 var sizeBalancedTree2 = new SizeBalancedTree2<uint>(10000);
40
                 {\tt sizeBalancedTree2.TestMultipleRandomCreationsAndDeletions} ( {\tt refine} \\
41

    sizeBalancedTree2.Root, () => sizeBalancedTree2.Count, _n);

             }
42
43
             [Fact]
44
            \begin{array}{ll} public \  \  static \  \  void \  \, SizedAndThreadedAVLBalancedTreeMultipleRandomAttachAndDetachTest() \\ \{ \end{array}
45
46
                 var avlTree = new SizedAndThreadedAVLBalancedTree<uint>(10000);
47
                 avlTree.TestMultipleRandomCreationsAndDeletions(ref avlTree.Root, () =>
48
                  → avlTree.Count, _n);
            }
49
        }
50
   }
51
```

Index

```
./Platform.Collections.Methods.Tests/SizeBalancedTree.cs, 22
./Platform.Collections.Methods.Tests/SizeBalancedTree2.cs, 21
./Platform.Collections.Methods.Tests/SizedAndThreadedAVLBalancedTree.cs, 24
./Platform.Collections.Methods.Tests/TestExtensions.cs, 25
./Platform.Collections.Methods.Tests/TreesTests.cs, 26
./Platform.Collections.Methods/GenericCollectionMethodsBase.cs, 1
./Platform.Collections.Methods/Lists/CircularDoublyLinkedListMethods.cs, 2
./Platform.Collections.Methods/Lists/DoublyLinkedListMethodsBase.cs, 3
./Platform.Collections.Methods/Lists/OpenDoublyLinkedListMethods.cs, 3
./Platform.Collections.Methods/Trees/SizeBalancedTreeMethods2.cs, 5
./Platform.Collections.Methods/Trees/SizeBalancedTreeMethods2.cs, 5
./Platform.Collections.Methods/Trees/SizeBalancedTreeMethodsBase.cs, 10
./Platform.Collections.Methods/Trees/SizedBinaryTreeMethodsBase.cs, 17
```