```
LinksPlatform's Platform Collections Methods Class Library
./Platform.Collections.Methods/GenericCollectionMethodsBase.cs
   using System.Collections.Generic;
   using System.Runtime.CompilerServices;
2
   using Platform. Numbers;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods
8
        public abstract class GenericCollectionMethodsBase<TElement>
10
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
11
            protected virtual TElement GetZero() => Integer<TElement>.Zero;
13
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
14
            protected virtual bool EqualToZero(TElement value) => EqualityComparer.Equals(value,

    Zero);

16
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
17
            protected virtual bool AreEqual(TElement first, TElement second) =>

→ EqualityComparer.Equals(first, second);

19
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool GreaterThanZero(TElement value) => Comparer.Compare(value, Zero)
            \rightarrow > 0;
22
23
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool GreaterThan(TElement first, TElement second) =>
24

→ Comparer.Compare(first, second) > 0;

25
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
26
            protected virtual bool GreaterOrEqualThanZero(TElement value) => Comparer.Compare(value,
            \rightarrow Zero) >= 0;
2.8
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
2.9
            protected virtual bool GreaterOrEqualThan(TElement first, TElement second) =>
               Comparer.Compare(first, second) >= 0;
31
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
32
            protected virtual bool LessOrEqualThanZero(TElement value) => Comparer.Compare(value,
            \rightarrow Zero) <= 0;
34
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool LessOrEqualThan(TElement first, TElement second) =>
36

→ Comparer.Compare(first, second) <= 0;
</p>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool LessThanZero(TElement value) => Comparer.Compare(value, Zero) < 0;</pre>
39
40
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
41
            protected virtual bool LessThan(TElement first, TElement second) =>
42
                Comparer.Compare(first, second) < 0;</pre>
43
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
44
            protected virtual TElement Increment(TElement value) =>
45
               Arithmetic<TElement>.Increment(value);
46
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
47
            protected virtual TElement Decrement(TElement value) =>
            → Arithmetic<TElement>.Decrement(value);
49
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
50
            protected virtual TElement Add(TElement first, TElement second) =>
               Arithmetic<TElement>.Add(first, second);
52
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual TElement Subtract(TElement first, TElement second) =>
               Arithmetic<TElement>.Subtract(first, second);
55
            protected readonly TElement Zero;
protected readonly TElement One;
            protected readonly TElement Two;
protected readonly EqualityComparer<TElement> EqualityComparer;
58
            protected readonly Comparer<TElement> Comparer;
60
61
            protected GenericCollectionMethodsBase()
62
63
                EqualityComparer = EqualityComparer<TElement>.Default;
64
```

```
Comparer = Comparer<TElement>.Default;
6.5
                Zero = GetZero(); //-V3068
                One = Increment(Zero); //-V3068
67
                Two = Increment(One); //-V3068
68
            }
        }
70
7.1
./Platform.Collections.Methods/Lists/CircularDoublyLinkedListMethods.cs
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
3
4
        public abstract class CircularDoublyLinkedListMethods<TElement> :
           DoublyLinkedListMethodsBase<TElement>
6
            public void AttachBefore(TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
10
                SetNext(newElement, baseElement);
11
                if (AreEqual(baseElement, GetFirst()))
12
                {
13
                    SetFirst(newElement);
14
15
                SetNext(baseElementPrevious, newElement);
16
                SetPrevious(baseElement, newElement);
17
                IncrementSize();
            }
19
20
            public void AttachAfter(TElement baseElement, TElement newElement)
21
22
                var baseElementNext = GetNext(baseElement);
23
                SetPrevious(newElement, baseElement);
                SetNext(newElement, baseElementNext);
25
                if (AreEqual(baseElement, GetLast()))
26
27
                    SetLast(newElement);
28
29
                SetPrevious(baseElementNext, newElement);
30
                SetNext(baseElement, newElement);
                IncrementSize();
32
            }
33
34
            public void AttachAsFirst(TElement element)
35
36
                var first = GetFirst();
                if (EqualToZero(first))
38
39
                    SetFirst(element);
                    SetLast(element);
41
                    SetPrevious(element, element);
42
                    SetNext(element, element);
43
                    IncrementSize();
                }
45
                else
46
                {
47
                     AttachBefore(first, element);
48
            }
51
            public void AttachAsLast(TElement element)
53
                var last = GetLast();
54
                if (EqualToZero(last))
                {
56
                     AttachAsFirst(element);
57
                }
58
                else
59
                {
60
                     AttachAfter(last, element);
62
            }
63
64
            public void Detach(TElement element)
65
66
                var elementPrevious = GetPrevious(element);
                var elementNext = GetNext(element);
68
```

```
if (AreEqual(elementNext, element))
6.9
                    SetFirst(Zero);
7.1
                    SetLast(Zero);
72
                }
                else
74
75
                    SetNext(elementPrevious, elementNext);
76
                    SetPrevious(elementNext, elementPrevious);
77
                    if (AreEqual(element, GetFirst()))
78
                        SetFirst(elementNext);
80
                    }
81
                    if (AreEqual(element, GetLast()))
82
                        SetLast(elementPrevious);
84
85
                SetPrevious(element, Zero);
87
                SetNext(element, Zero);
88
                DecrementSize();
89
            }
       }
91
92
./Platform.Collections.Methods/Lists/DoublyLinkedListMethodsBase.cs
   using System.Runtime.CompilerServices;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
5
        /// <remarks>
       /// Based on <a href="https://en.wikipedia.org/wiki/Doubly_linked_list">doubly linked
           list</a> implementation.
        /// </remarks>
       public abstract class DoublyLinkedListMethodsBase<TElement> :
10
           GenericCollectionMethodsBase<TElement>
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetFirst();
13
14
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
15
            protected abstract TElement GetLast();
16
17
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
            protected abstract TElement GetPrevious(TElement element);
19
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
            protected abstract TElement GetNext(TElement element);
23
24
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetSize();
26
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract void SetFirst(TElement element);
28
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
30
            protected abstract void SetLast(TElement element);
31
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
33
            protected abstract void SetPrevious(TElement element, TElement previous);
34
35
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
36
            protected abstract void SetNext(TElement element, TElement next);
38
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
39
            protected abstract void SetSize(TElement size);
40
41
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected void IncrementSize() => SetSize(Increment(GetSize()));
43
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
45
            protected void DecrementSize() => SetSize(Decrement(GetSize()));
46
       }
47
   }
```

```
./Platform.Collections.Methods/Lists/OpenDoublyLinkedListMethods.cs
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
   {
4
        public abstract class OpenDoublyLinkedListMethods<TElement> :
           DoublyLinkedListMethodsBase<TElement>
6
            public void AttachBefore(TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
10
                SetNext(newElement, baseElement);
11
12
                if (EqualToZero(baseElementPrevious))
                {
13
                    SetFirst(newElement);
14
                }
                else
16
                {
17
                    SetNext(baseElementPrevious, newElement);
18
19
                SetPrevious(baseElement, newElement);
20
                IncrementSize();
            }
22
23
            public void AttachAfter(TElement baseElement, TElement newElement)
25
                var baseElementNext = GetNext(baseElement);
26
                SetPrevious(newElement, baseElement);
                SetNext(newElement, baseElementNext);
28
                if (EqualToZero(baseElementNext))
29
30
                    SetLast(newElement);
31
                }
32
                else
                {
34
                    SetPrevious(baseElementNext, newElement);
35
36
                SetNext(baseElement, newElement);
37
                IncrementSize();
38
            }
39
40
            public void AttachAsFirst(TElement element)
41
42
                var first = GetFirst();
43
                if (EqualToZero(first))
44
45
                    SetFirst(element);
                    SetLast(element);
47
                    SetPrevious(element, Zero);
48
                    SetNext(element, Zero);
                    IncrementSize();
50
                }
51
                else
53
                     AttachBefore(first, element);
54
                }
            }
56
            public void AttachAsLast(TElement element)
59
                var last = GetLast()
60
                if (EqualToZero(last))
62
                     AttachAsFirst(element);
63
                }
                else
65
66
                     AttachAfter(last, element);
67
68
            }
69
70
            public void Detach(TElement element)
7.1
72
                var elementPrevious = GetPrevious(element);
73
                var elementNext = GetNext(element);
74
                if (EqualToZero(elementPrevious))
75
```

```
SetFirst(elementNext);
                }
                else
79
                {
                    SetNext(elementPrevious, elementNext);
81
82
                if (EqualToZero(elementNext))
83
84
                    SetLast(elementPrevious);
85
                }
86
87
                else
                {
88
                    SetPrevious(elementNext, elementPrevious);
89
                SetPrevious(element, Zero);
91
                SetNext(element, Zero);
92
                DecrementSize();
            }
94
        }
95
96
./Platform. Collections. Methods/Trees/Size Balanced Tree Methods 2.cs
   using System;
1
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Trees
5
        public abstract class SizeBalancedTreeMethods2<TElement> :
           SizedBinaryTreeMethodsBase<TElement>
            protected override void AttachCore(ref TElement root, TElement node)
9
10
11
                if (EqualToZero(root))
12
                    root = node;
13
                     IncrementSize(root);
                }
15
16
                else
17
                     IncrementSize(root);
18
                     if (FirstIsToTheLeftOfSecond(node, root))
20
                         AttachCore(ref GetLeftReference(root), node);
21
                         LeftMaintain(ref root);
22
                    }
23
                    else
24
                         AttachCore(ref GetRightReference(root), node);
26
                         RightMaintain(ref root);
27
                     }
28
                }
29
            }
30
            protected override void DetachCore(ref TElement root, TElement nodeToDetach)
32
33
                ref var currentNode = ref root;
34
                ref var parent = ref root;
35
                var replacementNode = Zero;
36
                while (!AreEqual(currentNode, nodeToDetach))
37
                    SetSize(currentNode, Decrement(GetSize(currentNode)));
39
                     if (FirstIsToTheLeftOfSecond(nodeToDetach, currentNode))
40
41
                         parent = ref currentNode;
42
                         currentNode = ref GetLeftReference(currentNode);
43
44
                    else if (FirstIsToTheRightOfSecond(nodeToDetach, currentNode))
45
46
                         parent = ref currentNode;
47
                         currentNode = ref GetRightReference(currentNode);
48
                     }
49
                    else
50
                     {
51
                         throw new InvalidOperationException("Duplicate link found in the tree.");
53
54
                var nodeToDetachLeft = GetLeft(nodeToDetach);
55
                var node = GetRight(nodeToDetach);
```

```
if (!EqualToZero(nodeToDetachLeft) && !EqualToZero(node))
        var minNode = node;
        var minNodeLeft = GetLeft(minNode);
        while (!EqualToZero(minNodeLeft))
            minNode = minNodeLeft;
            minNodeLeft = GetLeft(minNode);
        DetachCore(ref GetRightReference(nodeToDetach), minNode);
        SetLeft(minNode, nodeToDetachLeft);
        node = GetRight(nodeToDetach);
        if (!EqualToZero(node))
            SetRight(minNode, node);
            SetSize(minNode, Increment(Add(GetSize(nodeToDetachLeft), GetSize(node))));
        else
            SetSize(minNode, Increment(GetSize(nodeToDetachLeft)));
        replacementNode = minNode;
    }
    else if (!EqualToZero(nodeToDetachLeft))
        replacementNode = nodeToDetachLeft;
    }
    else if (!EqualToZero(node))
        replacementNode = node;
    if (AreEqual(root, nodeToDetach))
    {
        root = replacementNode;
    }
    else if (AreEqual(GetLeft(parent), nodeToDetach))
        SetLeft(parent, replacementNode);
    else if (AreEqual(GetRight(parent), nodeToDetach))
        SetRight(parent, replacementNode);
    ClearNode(nodeToDetach);
}
private void LeftMaintain(ref TElement root)
    if (!EqualToZero(root))
        var rootLeftNode = GetLeft(root);
        if (!EqualToZero(rootLeftNode))
            var rootRightNode = GetRight(root);
            var rootLeftNodeLeftNode = GetLeft(rootLeftNode);
            if (!EqualToZero(rootLeftNodeLeftNode) &&
                (EqualToZero(rootRightNode) ||
                    GreaterThan(GetSize(rootLeftNodeLeftNode), GetSize(rootRightNode))))
            {
                RightRotate(ref root);
            }
            else
            {
                var rootLeftNodeRightNode = GetRight(rootLeftNode);
                if (!EqualToZero(rootLeftNodeRightNode) &&
                    (EqualToZero(rootRightNode) ||
                        GreaterThan(GetSize(rootLeftNodeRightNode),
                        GetSize(rootRightNode))))
                {
                    LeftRotate(ref GetLeftReference(root));
                    RightRotate(ref root);
                else
                {
                    return;
                }
            LeftMaintain(ref GetLeftReference(root));
```

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123

 $\frac{124}{125}$

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```
RightMaintain(ref GetRightReference(root));
132
                          LeftMaintain(ref root)
                          RightMaintain(ref root);
134
135
                 }
136
            }
137
138
            private void RightMaintain(ref TElement root)
139
140
                 if (!EqualToZero(root))
141
142
                     var rootRightNode = GetRight(root);
                     if (!EqualToZero(rootRightNode))
144
145
                          var rootLeftNode = GetLeft(root);
                          var rootRightNodeRightNode = GetRight(rootRightNode);
147
                          if (!EqualToZero(rootRightNodeRightNode) &&
148
                              (EqualToZero(rootLeftNode) |
149
                                 GreaterThan(GetSize(rootRightNodeRightNode), GetSize(rootLeftNode))))
                          {
150
                              LeftRotate(ref root);
151
152
                          else
153
                          {
154
                              var rootRightNodeLeftNode = GetLeft(rootRightNode);
                              if (!EqualToZero(rootRightNodeLeftNode) &&
156
                                  (EqualToZero(rootLeftNode) ||
157
                                      GreaterThan(GetSize(rootRightNodeLeftNode),
                                      GetSize(rootLeftNode))))
                              {
158
                                  RightRotate(ref GetRightReference(root));
                                  LeftRotate(ref root);
160
                              }
161
                              else
162
                              {
163
                                  return;
164
                              }
165
166
                         LeftMaintain(ref GetLeftReference(root));
                         RightMaintain(ref GetRightReference(root));
168
                          LeftMaintain(ref root);
169
170
                          RightMaintain(ref root);
                     }
171
                 }
172
            }
173
        }
    }
175
./Platform.Collections.Methods/Trees/SizeBalancedTreeMethods.cs
    using System;
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
    namespace Platform.Collections.Methods.Trees
 6
        public abstract class SizeBalancedTreeMethods<TElement> :
            SizedBinaryTreeMethodsBase<TElement>
            protected override void AttachCore(ref TElement root, TElement node)
10
                 while (true)
11
12
                     ref var left = ref GetLeftReference(root);
13
                     var leftSize = GetSizeOrZero(left);
14
                     ref var right = ref GetRightReference(root);
15
                     var rightSize = GetSizeOrZero(right);
                     if (FirstIsToTheLeftOfSecond(node, root)) // node.Key less than root.Key
17
                     {
18
                          if (EqualToZero(left))
19
                          {
20
                              IncrementSize(root);
21
                              SetSize(node, One);
22
23
                              left = node;
24
                              return;
25
                          if (FirstIsToTheLeftOfSecond(node, left)) // node.Key less than left.Key
26
27
                              if (GreaterThan(Increment(leftSize), rightSize))
```

```
{
            RightRotate(ref root);
        }
        else
        {
            IncrementSize(root);
            root = ref left;
          // node.Key greater than left.Key
        var leftRightSize = GetSizeOrZero(GetRight(left));
        if (GreaterThan(Increment(leftRightSize), rightSize))
            if (EqualToZero(leftRightSize) && EqualToZero(rightSize))
                SetLeft(node, left);
                SetRight(node, root)
                {\tt SetSize(node,\ Add(leftSize,\ Two));\ //\ Two\ (2)\ -\ node\ the\ size\ of}
                    root and a node itself
                SetLeft(root, Zero);
                SetSize(root, One);
                root = node;
                return;
            LeftRotate(ref left);
            RightRotate(ref root);
        }
        else
            IncrementSize(root);
            root = ref left;
    }
else // node.Key greater than root.Key
    if (EqualToZero(right))
    {
        IncrementSize(root);
        SetSize(node, One);
        right = node;
        return;
    if (FirstIsToTheRightOfSecond(node, right)) // node.Key greater than
    {
        if (GreaterThan(Increment(rightSize), leftSize))
            LeftRotate(ref root);
        }
        else
            IncrementSize(root);
            root = ref right;
    else // node.Key less than right.Key
        var rightLeftSize = GetSizeOrZero(GetLeft(right));
        if (GreaterThan(Increment(rightLeftSize), leftSize))
            if (EqualToZero(rightLeftSize) && EqualToZero(leftSize))
                SetLeft(node, root);
                SetRight(node, right);
                SetSize(node, Add(rightSize, Two)); // Two (2) - node the size

→ of root and a node itself

                SetRight(root, Zero);
                SetSize(root, One);
                root = node;
                return;
            RightRotate(ref right);
            LeftRotate(ref root);
        }
        else
            IncrementSize(root);
```

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```
root = ref right;
                }
            }
        }
    }
}
protected override void DetachCore(ref TElement root, TElement node)
    while (true)
        ref var left = ref GetLeftReference(root);
        var leftSize = GetSizeOrZero(left);
        ref var right = ref GetRightReference(root);
        var rightSize = GetSizeOrZero(right);
        if (FirstIsToTheLeftOfSecond(node, root)) // node.Key less than root.Key
            var decrementedLeftSize = Decrement(leftSize);
            if (GreaterThan(GetSizeOrZero(GetRight(right)), decrementedLeftSize))
                LeftRotate(ref root);
            }
            else if (GreaterThan(GetSizeOrZero(GetLeft(right)), decrementedLeftSize))
                RightRotate(ref right);
                LeftRotate(ref root);
            }
            else
            {
                DecrementSize(root);
                root = ref left;
        else if (FirstIsToTheRightOfSecond(node, root)) // node.Key greater than root.Key
            var decrementedRightSize = Decrement(rightSize);
            if (GreaterThan(GetSizeOrZero(GetLeft(left)), decrementedRightSize))
                RightRotate(ref root);
            else if (GreaterThan(GetSizeOrZero(GetRight(left)), decrementedRightSize))
                LeftRotate(ref left);
                RightRotate(ref root);
            else
            {
                DecrementSize(root);
                root = ref right;
        else // key equals to root.Key
               (GreaterThanZero(leftSize) && GreaterThanZero(rightSize))
            {
                TElement replacement;
                if (GreaterThan(leftSize, rightSize))
                    replacement = left;
                    var replacementRight = GetRight(replacement);
                    while (!EqualToZero(replacementRight))
                        replacement = replacementRight;
                        replacementRight = GetRight(replacement);
                    DetachCore(ref left, replacement);
                }
                else
                    replacement = right;
                    var replacementLeft = GetLeft(replacement);
                    while (!EqualToZero(replacementLeft))
                        replacement = replacementLeft;
                        replacementLeft = GetLeft(replacement);
                    DetachCore(ref right, replacement);
                }
```

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181

```
SetLeft(replacement, left);
183
                              SetRight(replacement, right);
                              SetSize(replacement, Add(leftSize, rightSize));
185
                              root = replacement;
186
                          }
187
                          else if (GreaterThanZero(leftSize))
188
189
                              root = left;
190
                          }
191
                          else if (GreaterThanZero(rightSize))
                          {
193
194
                              root = right;
                          }
                          else
196
                          {
                              root = Zero;
198
199
                          ClearNode(node);
200
201
                          return;
                     }
202
                 }
203
            }
204
        }
205
    }
206
./Platform.Collections.Methods/Trees/SizedAndThreadedAVLBalancedTreeMethods.cs
    using System;
    using System. Runtime. Compiler Services;
    using System.Text;
#if USEARRAYPOOL
    using Platform.Collections;
 5
    #endif
 7
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
    namespace Platform.Collections.Methods.Trees
10
11
        /// <summary>
12
        /// Combination of Size, Height (AVL), and threads.
13
        /// </summary>
14
        /// <remarks>
15
        /// Based on: <a href="https://github.com/programmatom/TreeLib/blob/master/TreeLib/TreeLib/G|
16
            enerated/AVLTreeList.cs">TreeLib.AVLTreeList</a>.
        /// Which itself based on: <a
         → href="https://github.com/GNOME/glib/blob/master/glib/gtree.c">GNOME/glib/gtree</a>.
        /// </remarks>
18
        public abstract class SizedAndThreadedAVLBalancedTreeMethods<TElement> :
19
            SizedBinaryTreeMethodsBase<TElement>
20
             // TODO: Link with size of TElement
21
             private const int MaxPath = 92;
22
             public override bool Contains (TElement node, TElement root)
24
25
                 while (!EqualToZero(root))
26
                 {
27
                     if (FirstIsToTheLeftOfSecond(node, root)) // node.Key < root.Key</pre>
28
29
                          root = GetLeftOrDefault(root);
31
                     else if (FirstIsToTheRightOfSecond(node, root)) // node.Key > root.Key
32
                          root = GetRightOrDefault(root);
34
35
                     else // node.Key == root.Key
36
                          return true;
38
40
                 return false;
41
             }
42
43
             protected override void PrintNode(TElement node, StringBuilder sb, int level)
45
                 base.PrintNode(node, sb, level);
46
                 sb.Append(' ');
47
                 sb.Append(GetLeftIsChild(node) ? 'l' : 'L');
                 sb.Append(GetRightIsChild(node) ? 'r' : 'R');
49
                 sb.Append(' ');
50
```

```
sb.Append(GetBalance(node));
             }
5.3
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected void IncrementBalance(TElement node) => SetBalance(node,
                (sbyte)(GetBalance(node) + 1));
56
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected void DecrementBalance(TElement node) => SetBalance(node,
                (sbyte)(GetBalance(node) - 1));
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected override TElement GetLeftOrDefault(TElement node) => GetLeftIsChild(node) ?
61
             \;\hookrightarrow\;\; \texttt{GetLeft(node)}\;:\; \textcolor{red}{\texttt{default;}}
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected override TElement GetRightOrDefault(TElement node) => GetRightIsChild(node) ?
64
                GetRight(node) : default;
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
66
            protected abstract bool GetLeftIsChild(TElement node);
67
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
69
            protected abstract void SetLeftIsChild(TElement node, bool value);
71
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
73
            protected abstract bool GetRightIsChild(TElement node);
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
76
            protected abstract void SetRightIsChild(TElement node, bool value);
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
78
            protected abstract sbyte GetBalance(TElement node);
79
80
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
81
            protected abstract void SetBalance(TElement node, sbyte value);
82
83
            protected override void AttachCore(ref TElement root, TElement node)
84
85
                 unchecked
86
                 {
87
                     // TODO: Check what is faster to use simple array or array from array pool
                     // TODO: Try to use stackalloc as an optimization (requires code generation,
89
                         because of generics)
    #if USEARRAYPOOL
90
                     var path = ArrayPool.Allocate<TElement>(MaxPath);
91
                     var pathPosition = 0;
92
93
                     path[pathPosition++] = default;
    #else
94
                     var path = new TElement[MaxPath];
                     var pathPosition = 1;
96
    #endif
97
                     var currentNode = root;
98
                     while (true)
99
100
                             (FirstIsToTheLeftOfSecond(node, currentNode))
101
102
103
                              if (GetLeftIsChild(currentNode))
104
                                  IncrementSize(currentNode);
105
                                  path[pathPosition++] = currentNode;
                                  currentNode = GetLeft(currentNode);
107
108
                              else
109
110
                                  // Threads
                                  SetLeft(node, GetLeft(currentNode));
112
                                  SetRight(node, currentNode);
113
                                  SetLeft(currentNode, node);
114
                                  SetLeftIsChild(currentNode,
                                                                true);
                                  DecrementBalance(currentNode);
116
                                  SetSize(node, One);
117
                                  FixSize(currentNode); // Should be incremented already
118
                                  break;
119
120
122
                          else if (FirstIsToTheRightOfSecond(node, currentNode))
123
                              if (GetRightIsChild(currentNode))
```

```
{
125
                                   IncrementSize(currentNode);
                                   path[pathPosition++] = currentNode;
127
                                   currentNode = GetRight(currentNode);
128
                               else
130
131
                                    // Threads
132
                                   SetRight(node, GetRight(currentNode));
133
                                   SetLeft(node, currentNode);
134
                                   SetRight(currentNode, node);
135
                                   SetRightIsChild(currentNode, true);
136
                                   IncrementBalance(currentNode);
137
138
                                   SetSize(node, One);
139
                                   FixSize(currentNode); // Should be incremented already
                                   break;
140
                               }
                          }
142
                           else
143
144
                               throw new InvalidOperationException("Node with the same key already
145
                               → attached to a tree.");
                          }
146
                      // Restore balance. This is the goodness of a non-recursive
148
                      // implementation, when we are done with balancing we 'break'
149
150
                      // the loop and we are done.
                      while (true)
151
152
                           var parent = path[--pathPosition];
153
                          var isLeftNode = !AreEqual(parent, default) && AreEqual(currentNode,

   GetLeft(parent));
                          var currentNodeBalance = GetBalance(currentNode);
155
                          if (currentNodeBalance < -1 || currentNodeBalance > 1)
156
157
                               currentNode = Balance(currentNode);
159
                               if (AreEqual(parent, default))
                               {
160
                                   root = currentNode;
161
                               }
162
                               else if (isLeftNode)
163
164
                                   SetLeft(parent, currentNode);
165
                                   FixSize(parent);
166
                               else
168
169
                                   SetRight(parent, currentNode);
170
                                   FixSize(parent);
171
                          currentNodeBalance = GetBalance(currentNode);
174
                          if (currentNodeBalance == 0 || AreEqual(parent, default))
175
176
                               break;
177
178
                             (isLeftNode)
179
                           {
180
                               DecrementBalance(parent);
181
                          else
183
                          {
184
                               IncrementBalance(parent);
185
186
                           currentNode = parent;
187
188
    #if USEARRAYPOOL
189
                      ArrayPool.Free(path);
190
    #endif
191
                 }
192
             }
193
             private TElement Balance(TElement node)
195
196
                 unchecked
197
                 {
198
                      var rootBalance = GetBalance(node);
199
                      if (rootBalance < -1)</pre>
```

```
var left = GetLeft(node);
            if (GetBalance(left) > 0)
                SetLeft(node, LeftRotateWithBalance(left));
                FixSize(node);
            node = RightRotateWithBalance(node);
        else if (rootBalance > 1)
            var right = GetRight(node);
            if (GetBalance(right) < 0)</pre>
                SetRight(node, RightRotateWithBalance(right));
                FixSize(node);
            }
            node = LeftRotateWithBalance(node);
        return node;
    }
}
protected TElement LeftRotateWithBalance(TElement node)
    unchecked
        var right = GetRight(node);
        if (GetLeftIsChild(right))
            SetRight(node, GetLeft(right));
        }
        else
            SetRightIsChild(node, false);
            SetLeftIsChild(right, true);
        SetLeft(right, node);
        // Fix size
        SetSize(right, GetSize(node));
        FixSize(node);
        // Fix balance
        var rootBalance = GetBalance(node);
        var rightBalance = GetBalance(right);
        if (rightBalance <= 0)</pre>
            if (rootBalance >= 1)
            {
                SetBalance(right, (sbyte)(rightBalance - 1));
            }
            else
            {
                SetBalance(right, (sbyte)(rootBalance + rightBalance - 2));
            SetBalance(node, (sbyte)(rootBalance - 1));
        else
            if (rootBalance <= rightBalance)</pre>
                SetBalance(right, (sbyte)(rootBalance - 2));
            }
            else
            {
                SetBalance(right, (sbyte)(rightBalance - 1));
            SetBalance(node, (sbyte)(rootBalance - rightBalance - 1));
        return right;
    }
}
protected TElement RightRotateWithBalance(TElement node)
    unchecked
    {
        var left = GetLeft(node);
        if (GetRightIsChild(left))
```

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265 266 267

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270

271

273 274 275

```
SetLeft(node, GetRight(left));
        }
        else
        {
            SetLeftIsChild(node, false);
            SetRightIsChild(left, true);
        SetRight(left, node);
        // Fix size
        SetSize(left, GetSize(node));
        FixSize(node);
        // Fix balance
        var rootBalance = GetBalance(node);
        var leftBalance = GetBalance(left);
        if (leftBalance <= 0)</pre>
            if (leftBalance > rootBalance)
                SetBalance(left, (sbyte)(leftBalance + 1));
            else
            {
                SetBalance(left, (sbyte)(rootBalance + 2));
            SetBalance(node, (sbyte)(rootBalance - leftBalance + 1));
        else
            if (rootBalance <= -1)</pre>
            {
                SetBalance(left, (sbyte)(leftBalance + 1));
            }
            else
            {
                SetBalance(left, (sbyte)(rootBalance + leftBalance + 2));
            SetBalance(node, (sbyte)(rootBalance + 1));
        return left;
    }
}
protected TElement GetNext(TElement node)
    unchecked
    {
        var current = GetRight(node);
        if (GetRightIsChild(node))
            while (GetLeftIsChild(current))
                 current = GetLeft(current);
        return current;
    }
}
protected TElement GetPrevious(TElement node)
    unchecked
        var current = GetLeft(node);
        if (GetLeftIsChild(node))
            while (GetRightIsChild(current))
                current = GetRight(current);
            }
        return current;
    }
}
protected override void DetachCore(ref TElement root, TElement node)
    unchecked
```

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 $\frac{285}{286}$

287

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293

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 $\frac{348}{349}$

350

351

352 353

354 355 356

```
#if USEARRAYPOOL
358
                      var path = ArrayPool.Allocate<TElement>(MaxPath);
                      var pathPosition = 0;
360
                      path[pathPosition++] = default;
361
    #else
362
                      var path = new TElement[MaxPath];
363
                      var pathPosition = 1;
364
    #endif
365
                      var currentNode = root;
366
                      while (true)
367
368
                          if (FirstIsToTheLeftOfSecond(node, currentNode))
369
370
                               if (!GetLeftIsChild(currentNode))
372
                                   throw new InvalidOperationException("Cannot find a node.");
373
                               DecrementSize(currentNode);
375
                               path[pathPosition++] = currentNode;
376
                               currentNode = GetLeft(currentNode);
377
378
                          else if (FirstIsToTheRightOfSecond(node, currentNode))
379
380
                               if (!GetRightIsChild(currentNode))
                               {
382
                                   throw new InvalidOperationException("Cannot find a node.");
383
384
                               DecrementSize(currentNode);
385
                               path[pathPosition++] = currentNode;
386
                               currentNode = GetRight(currentNode);
387
                          else
389
                          {
390
                               break;
391
                          }
392
                      }
393
                      var parent = path[--pathPosition];
394
                      var balanceNode = parent;
                      var isLeftNode = !AreEqual(parent, default) && AreEqual(currentNode,
396
                          GetLeft(parent));
                      if (!GetLeftIsChild(currentNode))
397
398
                          if (!GetRightIsChild(currentNode)) // node has no children
400
                               if (AreEqual(parent, default))
401
                               {
402
                                   root = Zero;
403
                               }
404
                               else if (isLeftNode)
405
406
                                   SetLeftIsChild(parent, false);
407
                                   SetLeft(parent, GetLeft(currentNode));
408
409
                                   IncrementBalance(parent);
410
                               else
411
                               {
412
                                   SetRightIsChild(parent, false);
413
                                   SetRight(parent, GetRight(currentNode));
                                   DecrementBalance(parent);
415
416
417
                          else // node has a right child
418
419
                               var successor = GetNext(currentNode);
420
421
                               SetLeft(successor, GetLeft(currentNode));
422
                               var right = GetRight(currentNode);
                               if (AreEqual(parent, default))
423
424
                                   root = right;
425
                               }
426
                               else if (isLeftNode)
427
428
429
                                   SetLeft(parent, right);
                                   IncrementBalance(parent);
                               }
431
432
                               else
                               {
433
                                   SetRight(parent, right);
434
```

```
DecrementBalance(parent);
    }
else // node has a left child
    if (!GetRightIsChild(currentNode))
        var predecessor = GetPrevious(currentNode);
        SetRight(predecessor, GetRight(currentNode));
        var leftValue = GetLeft(currentNode);
        if (AreEqual(parent, default))
            root = leftValue;
        }
        else if (isLeftNode)
            SetLeft(parent, leftValue);
            IncrementBalance(parent);
        else
            SetRight(parent, leftValue);
            DecrementBalance(parent);
    }
    else // node has a both children (left and right)
        var predecessor = GetLeft(currentNode);
        var successor = GetRight(currentNode);
        var successorParent = currentNode
        int previousPathPosition = ++pathPosition;
        // find the immediately next node (and its parent)
        while (GetLeftIsChild(successor))
            path[++pathPosition] = successorParent = successor;
            successor = GetLeft(successor);
            if (!AreEqual(successorParent, currentNode))
                DecrementSize(successorParent);
        path[previousPathPosition] = successor;
        balanceNode = path[pathPosition];
        // remove 'successor' from the tree
           (!AreEqual(successorParent, currentNode))
            if (!GetRightIsChild(successor))
            {
                SetLeftIsChild(successorParent, false);
            }
            else
            {
                SetLeft(successorParent, GetRight(successor));
            IncrementBalance(successorParent);
            SetRightIsChild(successor, true);
            SetRight(successor, GetRight(currentNode));
        else
        {
            DecrementBalance(currentNode);
        // set the predecessor's successor link to point to the right place
        while (GetRightIsChild(predecessor))
            predecessor = GetRight(predecessor);
        SetRight(predecessor, successor);
        // prepare 'successor' to replace 'node'
        var left = GetLeft(currentNode);
        SetLeftIsChild(successor, true);
        SetLeft(successor, left);
        SetBalance(successor, GetBalance(currentNode));
        FixSize(successor);
        if (AreEqual(parent, default))
        {
            root = successor;
```

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511

```
513
                                else if (isLeftNode)
515
                                    SetLeft(parent, successor);
516
                               }
                               else
518
                                {
519
                                    SetRight(parent, successor);
520
                               }
521
                           }
522
523
                       // restore balance
524
                      if (!AreEqual(balanceNode, default))
525
526
527
                           while (true)
528
                                var balanceParent = path[--pathPosition];
529
                               isLeftNode = !AreEqual(balanceParent, default) && AreEqual(balanceNode,
530
                                   GetLeft(balanceParent));
                               var currentNodeBalance = GetBalance(balanceNode);
531
                               if (currentNodeBalance < -1 || currentNodeBalance > 1)
532
533
                                    balanceNode = Balance(balanceNode);
                                    if (AreEqual(balanceParent, default))
535
                                    {
536
                                        root = balanceNode;
537
                                    }
538
                                    else if (isLeftNode)
539
540
                                        SetLeft(balanceParent, balanceNode);
541
542
543
                                    else
                                    {
544
545
                                         SetRight(balanceParent, balanceNode);
546
547
                               currentNodeBalance = GetBalance(balanceNode);
548
                                   (currentNodeBalance != 0 || AreEqual(balanceParent, default))
550
                                    break;
                               }
552
                                   (isLeftNode)
                               i f
553
                                {
554
                                    IncrementBalance(balanceParent);
                               }
556
557
                                else
                                {
558
                                    DecrementBalance(balanceParent);
559
560
                               balanceNode = balanceParent;
561
                           }
562
563
                      ClearNode(node);
564
    #if USEARRAYPOOL
565
                      ArrayPool.Free(path);
566
    #endif
567
                  }
568
             }
569
              [MethodImpl(MethodImplOptions.AggressiveInlining)]
571
             protected override void ClearNode(TElement node)
572
573
                  SetLeft(node, Zero);
                  SetRight(node, Zero);
575
                  SetSize(node, Zero);
576
577
                  SetLeftIsChild(node, false);
578
                  SetRightIsChild(node, false);
                  SetBalance(node, 0);
579
580
         }
581
582
./Platform.Collections.Methods/Trees/SizedBinaryTreeMethodsBase.cs
    using System;
    using System.Runtime.CompilerServices;
using System.Text;
 3
    using Platform. Numbers;
    //#define ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
```

```
#pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Trees
10
   {
       public abstract class SizedBinaryTreeMethodsBase<TElement> :
11
           GenericCollectionMethodsBase<TElement>
12
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
13
           protected abstract ref TElement GetLeftReference(TElement node);
14
15
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
16
           protected abstract ref TElement GetRightReference(TElement node);
17
18
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected abstract TElement GetLeft(TElement node);
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
22
           protected abstract TElement GetRight(TElement node);
23
24
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
25
           protected abstract TElement GetSize(TElement node);
26
27
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
28
           protected abstract void SetLeft(TElement node, TElement left);
30
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
31
           protected abstract void SetRight(TElement node, TElement right);
32
33
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected abstract void SetSize(TElement node, TElement size);
3.5
36
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
37
           protected abstract bool FirstIsToTheLeftOfSecond(TElement first, TElement second);
38
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
40
           protected abstract bool FirstIsToTheRightOfSecond(TElement first, TElement second);
41
42
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
43
           protected virtual TElement GetLeftOrDefault(TElement node) => AreEqual(node, default) ?

→ default : GetLeft(node);
45
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
46
           protected virtual TElement GetRightOrDefault(TElement node) => AreEqual(node, default) ?
47
               default : GetRight(node);
48
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected void IncrementSize(TElement node) => SetSize(node, Increment(GetSize(node)));
50
51
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected void DecrementSize(TElement node) => SetSize(node, Decrement(GetSize(node)));
53
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
55
           protected TElement GetLeftSize(TElement node) => GetSizeOrZero(GetLeftOrDefault(node));
56
57
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
58
           protected TElement GetRightSize(TElement node) => GetSizeOrZero(GetRightOrDefault(node));
59
60
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
61
           protected TElement GetSizeOrZero(TElement node) => EqualToZero(node) ? Zero :

→ GetSize(node);

63
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
64
           protected void FixSize(TElement node) => SetSize(node, Increment(Add(GetLeftSize(node),

→ GetRightSize(node)));
66
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected void LeftRotate(ref TElement root) => root = LeftRotate(root);
69
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
70
           protected TElement LeftRotate(TElement root)
7.1
72
                var right = GetRight(root)
73
   #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
74
                if (EqualToZero(right))
75
                {
76
                    throw new Exception("Right is null.");
77
                }
78
   #endif
79
                SetRight(root, GetLeft(right));
80
```

```
SetLeft(right, root);
                 SetSize(right, GetSize(root));
                 FixSize(root);
83
                 return right;
            }
85
86
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
87
            protected void RightRotate(ref TElement root) => root = RightRotate(root);
88
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
90
            protected TElement RightRotate(TElement root)
91
92
                 var left = GetLeft(root)
93
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
94
                 if (EqualToZero(left))
96
                     throw new Exception("Left is null.");
97
98
    #endif
99
                 SetLeft(root, GetRight(left));
100
                 SetRight(left, root);
                 SetSize(left, GetSize(root));
102
                 FixSize(root);
103
104
                 return left;
            }
105
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
107
            public virtual bool Contains(TElement node, TElement root)
108
109
                 while (!EqualToZero(root))
110
111
                     if (FirstIsToTheLeftOfSecond(node, root)) // node.Key < root.Key</pre>
                     {
                         root = GetLeft(root);
114
                     }
115
                     else if (FirstIsToTheRightOfSecond(node, root)) // node.Key > root.Key
117
                         root = GetRight(root);
118
                     else // node.Key == root.Key
120
121
                         return true;
122
123
124
                 return false;
125
126
127
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
128
            protected virtual void ClearNode(TElement node)
129
                 SetLeft(node, Zero);
131
                 SetRight(node, Zero);
SetSize(node, Zero);
132
            }
134
135
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            public void Attach(ref TElement root, TElement node)
137
138
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
139
                 ValidateSizes(root);
140
                 Debug.WriteLine("--BeforeAttach--");
141
                 Debug.WriteLine(PrintNodes(root));
142
                 Debug.WriteLine("----"):
143
                 var sizeBefore = GetSize(root);
144
    #endif
145
                 if (EqualToZero(root))
146
                 {
148
                     SetSize(node, One);
                     root = node;
149
                     return;
150
151
    153
154
                 Debug.WriteLine(PrintNodes(root));
155
                 Debug.WriteLine("----");
156
                 ValidateSizes(root);
                 var sizeAfter = GetSize(root);
                 if (!IsEquals(MathHelpers.Increment(sizeBefore), sizeAfter))
159
```

```
160
                     throw new Exception("Tree was broken after attach.");
162
    #endif
163
164
165
             protected abstract void AttachCore(ref TElement root, TElement node);
166
167
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             public void Detach(ref TElement root, TElement node)
169
170
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
171
                 ValidateSizes(root);
172
                 Debug.WriteLine("--BeforeDetach--");
173
                 Debug.WriteLine(PrintNodes(root));
174
                 Debug.WriteLine("----"):
175
                 var sizeBefore = GetSize(root);
176
                 if (ValueEqualToZero(root))
177
178
                     throw new Exception($"Элемент с {node} не содержится в дереве.");
179
180
    #endif
181
                 DetachCore(ref root, node)
182
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
183
                 Debug.WriteLine("--AfterDetach--");
184
                 Debug.WriteLine(PrintNodes(root));
185
                 Debug.WriteLine("-----');
186
                 ValidateSizes(root);
187
                 var sizeAfter = GetSize(root);
188
                 if (!IsEquals(MathHelpers.Decrement(sizeBefore), sizeAfter))
189
190
                     throw new Exception("Tree was broken after detach.");
191
                 }
192
    #endif
193
194
             protected abstract void DetachCore(ref TElement root, TElement node);
196
             public void FixSizes(TElement node)
198
199
                 if (AreEqual(node, default))
200
                 {
201
                     return;
202
                 FixSizes(GetLeft(node))
204
                 FixSizes(GetRight(node));
205
                 FixSize(node);
             }
207
208
             public void ValidateSizes(TElement node)
209
210
                 if (AreEqual(node, default))
211
212
                     return;
213
                 }
214
                 var size = GetSize(node);
215
                 var leftSize = GetLeftSize(node);
216
217
                 var rightSize = GetRightSize(node);
                 var expectedSize = Arithmetic.Increment(Arithmetic.Add(leftSize, rightSize));
                 if (!AreEqual(size, expectedSize))
219
                 {
220
                     throw new InvalidOperationException($|"Size of {node} is not valid. Expected
221

    size: {expectedSize}, actual size: {size}.");
223
                 ValidateSizes(GetLeft(node));
                 ValidateSizes(GetRight(node));
224
             }
225
226
             public void ValidateSize(TElement node)
227
229
                 var size = GetSize(node);
                 var leftSize = GetLeftSize(node);
230
                 var rightSize = GetRightSize(node);
231
                 var expectedSize = Arithmetic.Increment(Arithmetic.Add(leftSize, rightSize));
232
                 if (!AreEqual(size, expectedSize))
233
                 {
234
                     throw new InvalidOperationException(S Size of {node} is not valid. Expected
235

    size: {expectedSize}, actual size: {size}.");
```

```
236
237
238
             public string PrintNodes(TElement node)
240
                 var sb = new StringBuilder();
241
                 PrintNodes(node, sb);
242
                 return sb.ToString();
243
244
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
246
             public void PrintNodes(TElement node, StringBuilder sb) => PrintNodes(node, sb, 0);
247
248
             public void PrintNodes(TElement node, StringBuilder sb, int level)
249
250
                 if (AreEqual(node, default))
                 {
252
                     return;
253
254
                 PrintNodes(GetLeft(node), sb, level + 1);
255
                 PrintNode(node, sb, level);
256
                 sb.AppendLine();
257
                 PrintNodes(GetRight(node), sb, level + 1);
258
259
260
             public string PrintNode(TElement node)
261
262
                 var sb = new StringBuilder();
263
                 PrintNode(node, sb);
264
                 return sb.ToString();
265
267
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected void PrintNode(TElement node, StringBuilder sb) => PrintNode(node, sb, 0);
269
270
             protected virtual void PrintNode(TElement node, StringBuilder sb, int level)
271
272
                 sb.Append('\t', level);
273
                 sb.Append(node);
275
                 PrintNodeValue(node, sb);
                 sb.Append(' ');
276
                 sb.Append('s');
277
                 sb.Append(GetSize(node));
278
279
             protected abstract void PrintNodeValue(TElement node, StringBuilder sb);
281
        }
282
./Platform.Collections.Methods.Tests/SizeBalancedTree2.cs
    using System;
using System.Collections.Generic;
    using System.Text;
    using Platform. Numbers:
    using Platform.Collections.Methods.Trees;
    namespace Platform.Collections.Methods.Tests
 8
         internal class SizeBalancedTree2<TElement> : SizeBalancedTreeMethods2<TElement>
 9
10
             private struct TreeElement
12
                 public TElement Size;
 13
                 public TElement Left;
14
                 public TElement Right;
                 public sbyte Balance;
16
                 public bool LeftIsChild;
17
                 public bool RightIsChild;
19
             private readonly TreeElement[] _elements;
21
             private TElement _allocated;
23
             public TElement Root;
24
25
             public TElement Count => GetSizeOrZero(Root);
27
             public SizeBalancedTree2(int capacity) => (_elements, _allocated) = (new
             → TreeElement[capacity], Integer<TElement>.One);
29
```

```
public TElement Allocate()
30
                var newNode = _allocated;
32
                if (IsEmpty(newNode))
34
                    _allocated = Arithmetic.Increment(_allocated);
35
                    return newNode;
36
                }
37
                else
                {
39
                    throw new InvalidOperationException("Allocated tree element is not empty.");
40
                }
41
           }
43
           public void Free(TElement node)
45
                while (!EqualityComparer.Equals(_allocated, Integer<TElement>.One) && IsEmpty(node))
46
47
                    var lastNode = Arithmetic.Decrement(_allocated);
                    if (EqualityComparer.Equals(lastNode, node))
49
50
                        _allocated = lastNode;
51
                        node = Arithmetic.Decrement(node);
52
                    }
                    else
54
                    {
56
                        return;
57
                }
           }
59
           public bool IsEmpty(TElement node) =>
61
            Gefault.Equals(GetElement(node), default);
62
           protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
               Comparer.Compare(first, second) < 0;</pre>
64
           protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>

→ Comparer.Compare(first, second) > 0;

66
           protected override ref TElement GetLeftReference(TElement node) => ref
67

   GetElement(node).Left;
68
           protected override TElement GetLeft(TElement node) => GetElement(node).Left;
69
70
           protected override ref TElement GetRightReference(TElement node) => ref
7.1

   GetElement(node).Right;
           protected override TElement GetRight(TElement node) => GetElement(node).Right;
7.3
           protected override TElement GetSize(TElement node) => GetElement(node).Size;
7.5
           protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
77

⇒ sb.Append(node);

           protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
            → left;
80
           protected override void SetRight(TElement node, TElement right) =>

   GetElement(node).Right = right;

82
           protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =

→ size;

           private ref TreeElement GetElement(TElement node) => ref
               _elements[(Integer<TElement>)node];
       }
86
87
./Platform.Collections.Methods.Tests/SizeBalancedTree.cs
   using System;
   using System.Collections.Generic;
   using System. Text;
3
   using Platform. Numbers;
   using Platform.Collections.Methods.Trees;
   namespace Platform.Collections.Methods.Tests
   {
       internal class SizeBalancedTree<TElement> : SizeBalancedTreeMethods<TElement>
```

```
private struct TreeElement
    public TElement Size;
    public TElement Left;
    public TElement Right;
    public sbyte Balance;
    public bool LeftIsChild
    public bool RightIsChild;
}
private readonly TreeElement[] _elements;
private TElement _allocated;
public TElement Root;
public TElement Count => GetSizeOrZero(Root);
public SizeBalancedTree(int capacity) => (_elements, _allocated) = (new
→ TreeElement[capacity], Integer<TElement>.One);
public TElement Allocate()
    var newNode = _allocated;
    if (IsEmpty(newNode))
        _allocated = Arithmetic.Increment(_allocated);
        return newNode;
    }
    else
        throw new InvalidOperationException("Allocated tree element is not empty.");
    }
}
public void Free(TElement node)
    while (!EqualityComparer.Equals(_allocated, Integer<TElement>.One) && IsEmpty(node))
        var lastNode = Arithmetic.Decrement(_allocated);
        if (EqualityComparer.Equals(lastNode, node))
            _allocated = lastNode;
            node = Arithmetic.Decrement(node);
        }
        else
        {
            return;
        }
    }
}
public bool IsEmpty(TElement node) =>
Gefault.Equals(GetElement(node), default);
protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
→ Comparer.Compare(first, second) < 0;</pre>
protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>

→ Comparer.Compare(first, second) > 0;

protected override ref TElement GetLeftReference(TElement node) => ref

→ GetElement(node).Left;

protected override TElement GetLeft(TElement node) => GetElement(node).Left;
protected override ref TElement GetRightReference(TElement node) => ref

   GetElement(node).Right;
protected override TElement GetRight(TElement node) => GetElement(node).Right;
protected override TElement GetSize(TElement node) => GetElement(node).Size;
protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
\rightarrow sb.Append(node);
protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
→ left;
```

11 12

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73 74

75 76

77

79

```
protected override void SetRight(TElement node, TElement right) =>
81

   GetElement(node).Right = right;
            protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =
83

    size;

84
            private ref TreeElement GetElement(TElement node) => ref
85

    _elements[(Integer<TElement>)node];
        }
   }
87
./Platform.Collections.Methods.Tests/SizedAndThreadedAVLBalancedTree.cs
   using System;
   using System.Collections.Generic;
   using System. Text;
   using Platform Numbers;
   using Platform.Collections.Methods.Trees;
   namespace Platform.Collections.Methods.Tests
7
        internal class SizedAndThreadedAVLBalancedTree<TElement> :
9
           SizedAndThreadedAVLBalancedTreeMethods<TElement>
10
            private struct TreeElement
11
12
                public TElement Size;
13
                public TElement Left;
public TElement Right;
15
                public sbyte Balance;
16
                public bool LeftIsChild
                public bool RightIsChild;
18
            }
20
            private readonly TreeElement[] _elements;
            private TElement _allocated;
22
23
            public TElement Root;
24
25
            public TElement Count => GetSizeOrZero(Root);
26
27
            public SizedAndThreadedAVLBalancedTree(int capacity) => (_elements, _allocated) = (new
28
            → TreeElement[capacity], Integer<TElement>.One);
            public TElement Allocate()
30
31
                var newNode = _allocated;
32
                if (IsEmpty(newNode))
33
                    _allocated = Arithmetic.Increment(_allocated);
                    return newNode;
36
                }
                else
38
                {
                    throw new InvalidOperationException("Allocated tree element is not empty.");
41
            }
42
43
            public void Free(TElement node)
44
                while (!EqualityComparer.Equals(_allocated, Integer<TElement>.One) && IsEmpty(node))
46
47
                    var lastNode = Arithmetic.Decrement(_allocated);
48
                    if (EqualityComparer.Equals(lastNode, node))
49
50
                         _allocated = lastNode;
                        node = Arithmetic.Decrement(node);
52
53
                    else
54
                    {
55
                        return;
                    }
57
                }
58
            }
60
            public bool IsEmpty(TElement node) =>
61
            Gefault.Equals(GetElement(node), default);
62
            protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
63

→ Comparer.Compare(first, second) < 0;
</p>
64
```

```
protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>
65

→ Comparer.Compare(first, second) > 0;

66
            protected override sbyte GetBalance(TElement node) => GetElement(node).Balance;
67
            protected override bool GetLeftIsChild(TElement node) => GetElement(node).LeftIsChild;
69
70
            protected override ref TElement GetLeftReference(TElement node) => ref
7.1

   GetElement(node).Left;
            protected override TElement GetLeft(TElement node) => GetElement(node).Left;
73
            protected override bool GetRightIsChild(TElement node) => GetElement(node).RightIsChild;
76
            protected override ref TElement GetRightReference(TElement node) => ref

   GetElement(node).Right;
78
            protected override TElement GetRight(TElement node) => GetElement(node).Right;
80
            protected override TElement GetSize(TElement node) => GetElement(node).Size;
81
82
            protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
83

    sb.Append(node);
84
            protected override void SetBalance(TElement node, sbyte value) =>
85

   GetElement(node).Balance = value;

            protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
87
            → left:
            protected override void SetLeftIsChild(TElement node, bool value) =>
89

    GetElement(node).LeftIsChild = value;

90
            protected override void SetRight(TElement node, TElement right) =>
91

   GetElement(node).Right = right;
            protected override void SetRightIsChild(TElement node, bool value) =>
93

→ GetElement(node).RightIsChild = value;

            protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =

    size;

96
            private ref TreeElement GetElement(TElement node) => ref
97
              _elements[(Integer<TElement>)node];
       }
98
99
./Platform.Collections.Methods.Tests/TestExtensions.cs
   using System;
1
   using System.Collections.Generic;
   using Xunit;
3
   using Platform. Numbers;
   using Platform.Collections.Methods.Trees;
   namespace Platform.Collections.Methods.Tests
8
       internal static class TestExtensions
        {
10
            public static void TestMultipleCreationsAndDeletions<TElement>(this
11
                SizedBinaryTreeMethodsBase<TElement> tree, Func<TElement> allocate, Action<TElement>
               free, ref TElement root, Func<TElement> treeCount, int maximumOperationsPerCycle)
12
                for (var N = 1; N < maximumOperationsPerCycle; N++)</pre>
13
                {
14
                    var currentCount = 0;
15
                    for (var i = 0; i < N; i++)</pre>
16
17
                        var node = allocate();
18
                        tree.Attach(ref root, node);
19
                        currentCount++;
20
                        Assert.Equal(currentCount, (int)(Integer<TElement>)treeCount());
21
22
                    for (var i = 1; i <= N; i++)</pre>
23
24
                        TElement node = (Integer<TElement>)i;
25
                        if (tree.Contains(node, root))
26
                        {
27
                             tree.Detach(ref root, node);
28
                             free(node);
29
```

```
currentCount--;
30
                                                       Assert.Equal(currentCount, (int)(Integer<TElement>)treeCount());
                                               }
32
                                       }
33
                               }
                       }
35
36
                       public static void TestMultipleRandomCreationsAndDeletions<TElement>(this
                               SizedBinaryTreeMethodsBase<TElement> tree, ref TElement root, Func<TElement>
                               treeCount, int maximumOperationsPerCycle)
38
                               var random = new System.Random(0);
                               var added = new HashSet<TElement>();
40
                               var currentCount = 0;
41
                               for (var N = 1; N < maximumOperationsPerCycle; N++)</pre>
42
43
                                       for (var i = 0; i < N; i++)</pre>
44
45
                                                var node = (Integer<TElement>)random.Next(1, N);
46
                                                if (added.Add(node))
47
48
                                                       tree.Attach(ref root, node);
49
                                                       currentCount++;
50
                                                       Assert.Equal(currentCount, (int)(Integer<TElement>)treeCount());
                                                }
52
53
                                       for (var i = 1; i <= N; i++)
55
                                               TElement node = (Integer<TElement>)random.Next(1, N);
56
                                                if (tree.Contains(node, root))
                                                       tree.Detach(ref root, node);
5.9
60
                                                       currentCount--
                                                       Assert.Equal(currentCount, (int)(Integer<TElement>)treeCount());
61
                                                       added.Remove(node);
62
                                               }
63
                                       }
64
                              }
65
                      }
66
               }
       }
68
./Platform.Collections.Methods.Tests/TreesTests.cs
      using Xunit;
 1
      namespace Platform.Collections.Methods.Tests
 3
               public static class TreesTests
 5
                       private const int _n = 100;
                       [Fact]
 9
                       public static void SizeBalancedTreeMultipleAttachAndDetachTest()
10
                               var sizeBalancedTree = new SizeBalancedTree<uint>(10000);
12
                               sizeBalancedTree.TestMultipleCreationsAndDeletions(sizeBalancedTree.Allocate,
13

→ sizeBalancedTree.Free, ref sizeBalancedTree.Root, () => sizeBalancedTree.Count,

                                       _n);
                       }
14
                       [Fact]
16
                       public static void SizeBalancedTree2MultipleAttachAndDetachTest()
17
18
19
                               var sizeBalancedTree2 = new SizeBalancedTree2<uint>(10000);
                               sizeBalancedTree2.TestMultipleCreationsAndDeletions(sizeBalancedTree2.Allocate, and a sizeBalancedTree2.Allocate, and a sizeBalancedTree3.Allocate, and a sizeBalancedTree3.Al
20
                                       sizeBalancedTree2.Free, ref sizeBalancedTree2.Root, () =>
                                       sizeBalancedTree2.Count, _n);
                       }
                       [Fact]
23
                       public static void SizedAndThreadedAVLBalancedTreeMultipleAttachAndDetachTest()
24
25
                               var avlTree = new SizedAndThreadedAVLBalancedTree<uint>(10000);
                               avlTree.TestMultipleCreationsAndDeletions(avlTree.Allocate, avlTree.Free, ref
27
                                      avlTree.Root, () => avlTree.Count, _n);
                       }
28
                       [Fact]
30
                       public static void SizeBalancedTreeMultipleRandomAttachAndDetachTest()
```

```
{
32
                 var sizeBalancedTree = new SizeBalancedTree<uint>(10000);
                 {\tt sizeBalancedTree.TestMultipleRandomCreationsAndDeletions} ( {\tt ref} \ {\tt sizeBalancedTree.Root}, \\
34
                 }
35
            public static void SizeBalancedTree2MultipleRandomAttachAndDetachTest()
{
37
38
                 var sizeBalancedTree2 = new SizeBalancedTree2<uint>(10000);
40
                 {\tt sizeBalancedTree2.TestMultipleRandomCreationsAndDeletions} ( {\tt refine} \\
41

    sizeBalancedTree2.Root, () ⇒ sizeBalancedTree2.Count, _n);

             }
42
43
             [Fact]
44
            \begin{array}{ll} public \  \  static \  \  void \  \, SizedAndThreadedAVLBalancedTreeMultipleRandomAttachAndDetachTest() \\ \{ \end{array}
45
46
                 var avlTree = new SizedAndThreadedAVLBalancedTree<uint>(10000);
47
                 avlTree.TestMultipleRandomCreationsAndDeletions(ref avlTree.Root, () =>
48
                  → avlTree.Count, _n);
            }
49
        }
50
   }
51
```

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