```
LinksPlatform's Platform Collections Methods Class Library
./Platform.Collections.Methods/GenericCollectionMethodsBase.cs
   using System.Collections.Generic;
   using System.Runtime.CompilerServices;
2
   using Platform. Numbers;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods
8
        public abstract class GenericCollectionMethodsBase<TElement>
10
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
11
            protected virtual TElement GetZero() => Integer<TElement>.Zero;
13
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
14
            protected virtual bool EqualToZero(TElement value) => EqualityComparer.Equals(value,

    Zero);

16
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
17
            protected virtual bool AreEqual(TElement first, TElement second) =>

→ EqualityComparer.Equals(first, second);

19
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool GreaterThanZero(TElement value) => Comparer.Compare(value, Zero)
            \rightarrow > 0;
22
23
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool GreaterThan(TElement first, TElement second) =>
24

→ Comparer.Compare(first, second) > 0;

25
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
26
            protected virtual bool GreaterOrEqualThanZero(TElement value) => Comparer.Compare(value,
            \rightarrow Zero) >= 0;
2.8
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
2.9
            protected virtual bool GreaterOrEqualThan(TElement first, TElement second) =>
               Comparer.Compare(first, second) >= 0;
31
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
32
            protected virtual bool LessOrEqualThanZero(TElement value) => Comparer.Compare(value,
            \rightarrow Zero) <= 0;
34
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool LessOrEqualThan(TElement first, TElement second) =>
36

→ Comparer.Compare(first, second) <= 0;
</p>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool LessThanZero(TElement value) => Comparer.Compare(value, Zero) < 0;</pre>
39
40
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
41
            protected virtual bool LessThan(TElement first, TElement second) =>
42
                Comparer.Compare(first, second) < 0;</pre>
43
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
44
            protected virtual TElement Increment(TElement value) =>
45
               Arithmetic<TElement>.Increment(value);
46
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
47
            protected virtual TElement Decrement(TElement value) =>
            → Arithmetic<TElement>.Decrement(value);
49
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
50
            protected virtual TElement Add(TElement first, TElement second) =>
               Arithmetic<TElement>.Add(first, second);
52
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual TElement Subtract(TElement first, TElement second) =>
               Arithmetic<TElement>.Subtract(first, second);
55
            protected readonly TElement Zero;
protected readonly TElement One;
            protected readonly TElement Two;
protected readonly EqualityComparer<TElement> EqualityComparer;
58
            protected readonly Comparer<TElement> Comparer;
60
61
            protected GenericCollectionMethodsBase()
62
63
                EqualityComparer = EqualityComparer<TElement>.Default;
64
```

```
Comparer = Comparer<TElement>.Default;
6.5
                Zero = GetZero(); //-V3068
                One = Increment(Zero); //-V3068
67
                Two = Increment(One); //-V3068
68
            }
        }
70
7.1
./Platform.Collections.Methods/Lists/CircularDoublyLinkedListMethods.cs
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
3
4
        public abstract class CircularDoublyLinkedListMethods<TElement> :
           DoublyLinkedListMethodsBase<TElement>
6
            public void AttachBefore(TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
10
                SetNext(newElement, baseElement);
11
                if (AreEqual(baseElement, GetFirst()))
12
                {
13
                    SetFirst(newElement);
14
15
                SetNext(baseElementPrevious, newElement);
16
                SetPrevious(baseElement, newElement);
17
                IncrementSize();
            }
19
20
            public void AttachAfter(TElement baseElement, TElement newElement)
21
22
                var baseElementNext = GetNext(baseElement);
23
                SetPrevious(newElement, baseElement);
                SetNext(newElement, baseElementNext);
25
                if (AreEqual(baseElement, GetLast()))
26
27
                    SetLast(newElement);
28
29
                SetPrevious(baseElementNext, newElement);
30
                SetNext(baseElement, newElement);
                IncrementSize();
32
            }
33
34
            public void AttachAsFirst(TElement element)
35
36
                var first = GetFirst();
                if (EqualToZero(first))
38
39
                    SetFirst(element);
                    SetLast(element);
41
                    SetPrevious(element, element);
42
                    SetNext(element, element);
43
                    IncrementSize();
                }
45
                else
46
                {
47
                     AttachBefore(first, element);
48
            }
51
            public void AttachAsLast(TElement element)
53
                var last = GetLast();
54
                if (EqualToZero(last))
                {
56
                     AttachAsFirst(element);
57
                }
58
                else
59
                {
60
                     AttachAfter(last, element);
62
            }
63
64
            public void Detach(TElement element)
65
66
                var elementPrevious = GetPrevious(element);
                var elementNext = GetNext(element);
68
```

```
if (AreEqual(elementNext, element))
6.9
                    SetFirst(Zero);
7.1
                    SetLast(Zero);
72
                }
                else
74
75
                    SetNext(elementPrevious, elementNext);
76
                    SetPrevious(elementNext, elementPrevious);
77
                    if (AreEqual(element, GetFirst()))
78
                        SetFirst(elementNext);
80
                    }
81
                    if (AreEqual(element, GetLast()))
82
                        SetLast(elementPrevious);
84
85
                SetPrevious(element, Zero);
87
                SetNext(element, Zero);
88
                DecrementSize();
89
            }
       }
91
92
./Platform.Collections.Methods/Lists/DoublyLinkedListMethodsBase.cs
   using System.Runtime.CompilerServices;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
5
        /// <remarks>
       /// Based on <a href="https://en.wikipedia.org/wiki/Doubly_linked_list">doubly linked
           list</a> implementation.
        /// </remarks>
       public abstract class DoublyLinkedListMethodsBase<TElement> :
10
           GenericCollectionMethodsBase<TElement>
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetFirst();
13
14
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
15
            protected abstract TElement GetLast();
16
17
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
            protected abstract TElement GetPrevious(TElement element);
19
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
            protected abstract TElement GetNext(TElement element);
23
24
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetSize();
26
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract void SetFirst(TElement element);
28
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
30
            protected abstract void SetLast(TElement element);
31
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
33
            protected abstract void SetPrevious(TElement element, TElement previous);
34
35
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
36
            protected abstract void SetNext(TElement element, TElement next);
38
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
39
            protected abstract void SetSize(TElement size);
40
41
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected void IncrementSize() => SetSize(Increment(GetSize()));
43
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
45
            protected void DecrementSize() => SetSize(Decrement(GetSize()));
46
       }
47
   }
```

```
./Platform.Collections.Methods/Lists/OpenDoublyLinkedListMethods.cs
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Lists
   {
4
        public abstract class OpenDoublyLinkedListMethods<TElement> :
           DoublyLinkedListMethodsBase<TElement>
6
            public void AttachBefore(TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
10
                SetNext(newElement, baseElement);
11
12
                if (EqualToZero(baseElementPrevious))
                {
13
                    SetFirst(newElement);
14
                }
                else
16
                {
17
                    SetNext(baseElementPrevious, newElement);
18
19
                SetPrevious(baseElement, newElement);
20
                IncrementSize();
            }
22
23
            public void AttachAfter(TElement baseElement, TElement newElement)
25
                var baseElementNext = GetNext(baseElement);
26
                SetPrevious(newElement, baseElement);
                SetNext(newElement, baseElementNext);
28
                if (EqualToZero(baseElementNext))
29
30
                    SetLast(newElement);
31
                }
32
                else
                {
34
                    SetPrevious(baseElementNext, newElement);
35
36
                SetNext(baseElement, newElement);
37
                IncrementSize();
38
            }
39
40
            public void AttachAsFirst(TElement element)
41
42
                var first = GetFirst();
43
                if (EqualToZero(first))
44
45
                    SetFirst(element);
                    SetLast(element);
47
                    SetPrevious(element, Zero);
48
                    SetNext(element, Zero);
                    IncrementSize();
50
                }
51
                else
53
                     AttachBefore(first, element);
54
                }
            }
56
            public void AttachAsLast(TElement element)
59
                var last = GetLast()
60
                if (EqualToZero(last))
62
                     AttachAsFirst(element);
63
                }
                else
65
66
                     AttachAfter(last, element);
67
68
            }
69
70
            public void Detach(TElement element)
7.1
72
                var elementPrevious = GetPrevious(element);
73
                var elementNext = GetNext(element);
74
                if (EqualToZero(elementPrevious))
75
```

```
SetFirst(elementNext);
                }
                else
79
                {
                     SetNext(elementPrevious, elementNext);
81
82
                if (EqualToZero(elementNext))
83
                     SetLast(elementPrevious);
85
                }
86
                else
87
                {
88
                     SetPrevious(elementNext, elementPrevious);
89
                SetPrevious(element, Zero);
91
                SetNext(element, Zero);
92
                DecrementSize();
            }
94
        }
95
96
./Platform. Collections. Methods/Trees/Recursionless Size Balanced Tree Methods. cs
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Trees
3
4
        public abstract class RecursionlessSizeBalancedTreeMethods<TElement> :
5
           SizedBinaryTreeMethodsBase<TElement>
6
            protected override void AttachCore(ref TElement root, TElement node)
                while (true)
10
                     ref var left = ref GetLeftReference(root);
11
                     var leftSize = GetSizeOrZero(left);
                     ref var right = ref GetRightReference(root);
                     var rightSize = GetSizeOrZero(right);
14
                     if (FirstIsToTheLeftOfSecond(node, root)) // node.Key less than root.Key
15
16
                         if (EqualToZero(left))
17
                         {
18
                             IncrementSize(root);
19
                             SetSize(node, One);
                             left = node;
21
                             return;
22
23
                         if (FirstIsToTheLeftOfSecond(node, left)) // node.Key less than left.Key
25
                             if (GreaterThan(Increment(leftSize), rightSize))
26
27
                                  RightRotate(ref root);
28
                             }
29
                             else
31
                                  IncrementSize(root);
32
                                  root = ref left;
33
34
35
                               // node.Key greater than left.Key
                         else
37
                             var leftRightSize = GetSizeOrZero(GetRight(left));
38
                             if (GreaterThan(Increment(leftRightSize), rightSize))
39
40
                                  if (EqualToZero(leftRightSize) && EqualToZero(rightSize))
41
42
                                  {
                                      SetLeft(node, left);
44
                                      SetRight(node, root);
                                      SetSize(node, Add(leftSize, Two)); // Two (2) - node the size of
45
                                       \hookrightarrow root and a node itself
                                      SetLeft(root, Zero);
46
                                      SetSize(root, One);
47
                                      root = node;
                                      return;
49
                                  LeftRotate(ref left);
51
                                  RightRotate(ref root);
52
                             }
53
                             else
54
```

```
IncrementSize(root);
                    root = ref left;
                }
            }
        else // node.Key greater than root.Key
            if (EqualToZero(right))
                IncrementSize(root);
                SetSize(node, One);
                right = node;
                return;
            if (FirstIsToTheRightOfSecond(node, right)) // node.Key greater than
                right.Key
                if (GreaterThan(Increment(rightSize), leftSize))
                    LeftRotate(ref root);
                }
                else
                {
                    IncrementSize(root);
                    root = ref right;
            else // node.Key less than right.Key
                var rightLeftSize = GetSizeOrZero(GetLeft(right));
                   (GreaterThan(Increment(rightLeftSize), leftSize))
                    if (EqualToZero(rightLeftSize) && EqualToZero(leftSize))
                        SetLeft(node, root);
                        SetRight(node, right);
                        SetSize(node, Add(rightSize, Two)); // Two (2) - node the size
                            of root and a node itself
                        SetRight(root, Zero);
                        SetSize(root, One);
                        root = node;
                        return;
                    RightRotate(ref right);
                    LeftRotate(ref root);
                }
                else
                    IncrementSize(root);
                    root = ref right;
                }
            }
        }
    }
}
protected override void DetachCore(ref TElement root, TElement node)
    while (true)
        ref var left = ref GetLeftReference(root);
        var leftSize = GetSizeOrZero(left);
        ref var right = ref GetRightReference(root);
        var rightSize = GetSizeOrZero(right);
        if (FirstIsToTheLeftOfSecond(node, root)) // node.Key less than root.Key
            var decrementedLeftSize = Decrement(leftSize)
            if (GreaterThan(GetSizeOrZero(GetRight(right)), decrementedLeftSize))
            {
                LeftRotate(ref root);
            else if (GreaterThan(GetSizeOrZero(GetLeft(right)), decrementedLeftSize))
                RightRotate(ref right);
                LeftRotate(ref root);
            }
            else
            {
```

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 $\frac{125}{126}$

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129

```
DecrementSize(root);
132
                               root = ref left;
133
                          }
134
                      else if (FirstIsToTheRightOfSecond(node, root)) // node.Key greater than root.Key
136
137
                          var decrementedRightSize = Decrement(rightSize);
138
                          if (GreaterThan(GetSizeOrZero(GetLeft(left)), decrementedRightSize))
139
140
                               RightRotate(ref root);
141
                          }
142
                          else if (GreaterThan(GetSizeOrZero(GetRight(left)), decrementedRightSize))
144
                               LeftRotate(ref left);
145
                               RightRotate(ref root);
                          }
147
                          else
148
                          {
149
                               DecrementSize(root);
150
                               root = ref right;
151
152
153
                      else // key equals to root.Key
155
                          if (GreaterThanZero(leftSize) && GreaterThanZero(rightSize))
156
157
                               TElement replacement;
158
                               if (GreaterThan(leftSize, rightSize))
159
                                   replacement = GetRightest(left);
161
                                   DetachCore(ref left, replacement);
162
                               }
163
                               else
164
165
                                   replacement = GetLeftest(right);
                                   DetachCore(ref right, replacement);
167
168
169
                               SetLeft(replacement, left)
                               SetRight(replacement, right);
170
                               SetSize(replacement, Add(leftSize, rightSize));
171
172
                               root = replacement;
173
                          else if (GreaterThanZero(leftSize))
174
                               root = left;
176
                          }
                          else if (GreaterThanZero(rightSize))
178
                          {
179
180
                               root = right;
                          }
181
                          else
183
                          {
                               root = Zero;
185
                          ClearNode(node);
186
                          return;
187
                      }
188
                 }
189
             }
190
        }
191
192
./Platform. Collections. Methods/Trees/SizeBalancedTreeMethods.cs\\
    using System;
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
    namespace Platform.Collections.Methods.Trees
 5
    {
 6
        public abstract class SizeBalancedTreeMethods<TElement> :
            SizedBinaryTreeMethodsBase<TElement>
 8
             protected override void AttachCore(ref TElement root, TElement node)
{
10
                 if (EqualToZero(root))
11
                 {
                      root = node;
13
                      IncrementSize(root);
14
                 }
```

```
else
        IncrementSize(root);
        if (FirstIsToTheLeftOfSecond(node, root))
            AttachCore(ref GetLeftReference(root), node);
            LeftMaintain(ref root);
        else
        ₹
            AttachCore(ref GetRightReference(root), node);
            RightMaintain(ref root);
    }
}
protected override void DetachCore(ref TElement root, TElement nodeToDetach)
    ref var currentNode = ref root;
    ref var parent = ref root;
    var replacementNode = Zero;
    while (!AreEqual(currentNode, nodeToDetach))
        DecrementSize(currentNode);
        if (FirstIsToTheLeftOfSecond(nodeToDetach, currentNode))
        {
            parent = ref currentNode;
            currentNode = ref GetLeftReference(currentNode);
        else if (FirstIsToTheRightOfSecond(nodeToDetach, currentNode))
            parent = ref currentNode;
            currentNode = ref GetRightReference(currentNode);
        }
        else
        {
            throw new InvalidOperationException("Duplicate link found in the tree.");
    }
    var nodeToDetachLeft = GetLeft(nodeToDetach);
    var node = GetRight(nodeToDetach);
    if (!EqualToZero(nodeToDetachLeft) && !EqualToZero(node))
        var leftestNode = GetLeftest(node);
        DetachCore(ref GetRightReference(nodeToDetach), leftestNode);
        SetLeft(leftestNode, nodeToDetachLeft);
        node = GetRight(nodeToDetach);
        if (!EqualToZero(node))
            SetRight(leftestNode, node);
            SetSize(leftestNode, Increment(Add(GetSize(nodeToDetachLeft),

   GetSize(node))));
        else
            SetSize(leftestNode, Increment(GetSize(nodeToDetachLeft)));
        replacementNode = leftestNode;
    }
    else if (!EqualToZero(nodeToDetachLeft))
        replacementNode = nodeToDetachLeft;
    }
    else if (!EqualToZero(node))
        replacementNode = node;
    if (AreEqual(root, nodeToDetach))
    {
        root = replacementNode;
    else if (AreEqual(GetLeft(parent), nodeToDetach))
        SetLeft(parent, replacementNode);
    else if (AreEqual(GetRight(parent), nodeToDetach))
        SetRight(parent, replacementNode);
    }
```

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```
ClearNode(nodeToDetach);
}
private void LeftMaintain(ref TElement root)
    if (!EqualToZero(root))
        var rootLeftNode = GetLeft(root);
        if (!EqualToZero(rootLeftNode))
            var rootRightNode = GetRight(root);
            var rootRightNodeSize = GetSize(rootRightNode);
            var rootLeftNodeLeftNode = GetLeft(rootLeftNode);
            if (!EqualToZero(rootLeftNodeLeftNode) &&
                (EqualToZero(rootRightNode)
                    GreaterThan(GetSize(rootLeftNodeLeftNode), rootRightNodeSize)))
            {
                RightRotate(ref root);
            }
            else
                var rootLeftNodeRightNode = GetRight(rootLeftNode);
                if (!EqualToZero(rootLeftNodeRightNode) &&
                     (EqualToZero(rootRightNode) ||
                       GreaterThan(GetSize(rootLeftNodeRightNode), rootRightNodeSize)))
                    LeftRotate(ref GetLeftReference(root));
                    RightRotate(ref root);
                }
                else
                {
                    return;
            LeftMaintain(ref GetLeftReference(root));
            RightMaintain(ref GetRightReference(root));
            LeftMaintain(ref root);
            RightMaintain(ref root);
        }
    }
}
private void RightMaintain(ref TElement root)
    if (!EqualToZero(root))
        var rootRightNode = GetRight(root);
        if (!EqualToZero(rootRightNode))
            var rootLeftNode = GetLeft(root);
            var rootLeftNodeSize = GetSize(rootLeftNode);
            var rootRightNodeRightNode = GetRight(rootRightNode);
            if (!EqualToZero(rootRightNodeRightNode) &&
                (EqualToZero(rootLeftNode)
                    GreaterThan(GetSize(rootRightNodeRightNode), rootLeftNodeSize)))
            {
                LeftRotate(ref root);
            }
            else
                var rootRightNodeLeftNode = GetLeft(rootRightNode);
                if (!EqualToZero(rootRightNodeLeftNode) &&
                     (EqualToZero(rootLeftNode) ||
                        GreaterThan(GetSize(rootRightNodeLeftNode), rootLeftNodeSize)))
                    RightRotate(ref GetRightReference(root));
                    LeftRotate(ref root);
                }
                else
                {
                    return;
                }
            LeftMaintain(ref GetLeftReference(root));
            RightMaintain(ref GetRightReference(root));
            LeftMaintain(ref root);
            RightMaintain(ref root);
        }
```

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161 162 163

164

165

```
168
            }
        }
170
171
./Platform.Collections.Methods/Trees/SizedAndThreadedAVLBalancedTreeMethods.cs
    using System;
    using System.Runtime.CompilerServices;
    using System.Text;
#if USEARRAYPOOL
 3
    using Platform.Collections;
    #endif
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
    namespace Platform.Collections.Methods.Trees
10
11
        /// <summary>
12
        /// Combination of Size, Height (AVL), and threads.
13
        /// </summary>
14
        /// <remarks>
        /// Based on: <a href="https://github.com/programmatom/TreeLib/blob/master/TreeLib/TreeLib/G_
            enerated/AVLTreeList.cs">TreeLib.AVLTreeList</a>.
        /// Which itself based on: <a
17
            href="https://github.com/GNOME/glib/blob/master/glib/gtree.c">GNOME/glib/gtree</a>.
        /// </remarks>
18
        public abstract class SizedAndThreadedAVLBalancedTreeMethods<TElement> :
19
            SizedBinaryTreeMethodsBase<TElement>
20
            private const int MaxPath = 92;
21
22
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
23
            protected override TElement GetRightest(TElement current)
2.4
                 var currentRight = GetRightOrDefault(current);
                 while (!EqualToZero(currentRight))
27
28
                     current = currentRight;
29
                     currentRight = GetRightOrDefault(current);
30
                 return current;
32
             }
33
34
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected override TElement GetLeftest(TElement current)
37
                 var currentLeft = GetLeftOrDefault(current);
38
                 while (!EqualToZero(currentLeft))
39
40
                     current = currentLeft;
41
                     currentLeft = GetLeftOrDefault(current);
43
                 return current;
            }
45
46
            public override bool Contains(TElement node, TElement root)
47
48
                 while (!EqualToZero(root))
49
                     if (FirstIsToTheLeftOfSecond(node, root)) // node.Key < root.Key</pre>
52
                         root = GetLeftOrDefault(root);
                     else if (FirstIsToTheRightOfSecond(node, root)) // node.Key > root.Key
55
56
                         root = GetRightOrDefault(root);
57
58
                     else // node.Key == root.Key
59
                         return true;
61
62
                 return false;
64
            }
66
67
            protected override void PrintNode(TElement node, StringBuilder sb, int level)
                 base.PrintNode(node, sb, level);
69
                 sb.Append(' ');
```

```
sb.Append(GetLeftIsChild(node) ? 'l' : 'L')
                sb.Append(GetRightIsChild(node) ? 'r' : 'R');
                sb.Append('');
73
                sb.Append(GetBalance(node));
74
76
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
77
            protected void IncrementBalance(TElement node) => SetBalance(node,
                (sbyte)(GetBalance(node) + 1));
79
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
80
            protected void DecrementBalance(TElement node) => SetBalance(node,
             82
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected override TElement GetLeftOrDefault(TElement node) => GetLeftIsChild(node) ?
84

→ GetLeft(node) : default;

            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected override TElement GetRightOrDefault(TElement node) => GetRightIsChild(node) ?
87

   GetRight(node) : default;

            [MethodImpl(MethodImplOptions.AggressiveInlining)]
89
            protected abstract bool GetLeftIsChild(TElement node);
90
91
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
92
            protected abstract void SetLeftIsChild(TElement node, bool value);
93
94
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
95
            protected abstract bool GetRightIsChild(TElement node);
97
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
98
            protected abstract void SetRightIsChild(TElement node, bool value);
qq
100
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract sbyte GetBalance(TElement node);
102
103
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
104
            protected abstract void SetBalance(TElement node, sbyte value);
105
106
            protected override void AttachCore(ref TElement root, TElement node)
107
108
                unchecked
109
                {
110
                     // TODO: Check what is faster to use simple array or array from array pool
111
                     // TODO: Try to use stackalloc as an optimization (requires code generation,
                       because of generics)
    #if USEARRAYPOOL
113
                     var path = ArrayPool.Allocate<TElement>(MaxPath);
114
                     var pathPosition = 0;
115
                    path[pathPosition++] = default;
116
    #else
117
                     var path = new TElement[MaxPath];
118
                     var pathPosition = 1;
119
    #endif
120
                     var currentNode = root;
121
                    while (true)
122
123
                           (FirstIsToTheLeftOfSecond(node, currentNode))
124
                         {
                             if (GetLeftIsChild(currentNode))
127
                                 IncrementSize(currentNode);
128
                                 path[pathPosition++] = currentNode;
                                 currentNode = GetLeft(currentNode);
130
131
                             else
132
133
134
                                  // Threads
                                 SetLeft(node, GetLeft(currentNode));
135
                                 SetRight(node, currentNode);
136
                                 SetLeft(currentNode, node);
137
                                 SetLeftIsChild(currentNode, true);
138
139
                                 DecrementBalance(currentNode);
                                 SetSize(node, One);
140
                                 FixSize(currentNode); // Should be incremented already
141
142
                                 break;
                             }
143
                         }
```

```
else if (FirstIsToTheRightOfSecond(node, currentNode))
145
                               if (GetRightIsChild(currentNode))
147
148
                                   IncrementSize(currentNode);
                                   path[pathPosition++] = currentNode;
150
                                   currentNode = GetRight(currentNode);
151
152
                               else
153
                               {
154
                                    // Threads
155
                                   SetRight(node, GetRight(currentNode));
156
                                   SetLeft(node, currentNode);
157
                                   SetRight(currentNode, node);
158
159
                                   SetRightIsChild(currentNode,
                                                                   true);
160
                                   IncrementBalance(currentNode);
                                   SetSize(node, One);
161
                                   FixSize(currentNode); // Should be incremented already
                                   break;
163
                               }
164
                          }
165
                          else
166
                          {
                               throw new InvalidOperationException("Node with the same key already
168
                               → attached to a tree.");
169
170
                      // Restore balance. This is the goodness of a non-recursive
171
                      // implementation, when we are done with balancing we 'break'
172
                      // the loop and we are done.
173
                      while (true)
175
                          var parent = path[--pathPosition];
176
                          var isLeftNode = !AreEqual(parent, default) && AreEqual(currentNode,
177
                              GetLeft(parent));
                          var currentNodeBalance = GetBalance(currentNode);
                          if (currentNodeBalance < -1 || currentNodeBalance > 1)
179
                           {
180
                               currentNode = Balance(currentNode);
182
                               if (AreEqual(parent, default))
183
                                   root = currentNode;
184
                               }
185
                               else if (isLeftNode)
186
188
                                   SetLeft(parent, currentNode);
                                   FixSize(parent);
189
                               }
190
                               else
191
192
                                   SetRight(parent, currentNode);
194
                                   FixSize(parent);
                               }
195
                          }
196
                          currentNodeBalance = GetBalance(currentNode);
197
                           if (currentNodeBalance == 0 || AreEqual(parent, default))
198
                           {
199
                               break;
200
201
                           if (isLeftNode)
                           {
203
                               DecrementBalance(parent);
204
                          }
205
                          else
206
                           {
207
                               IncrementBalance(parent);
208
                          }
209
210
                           currentNode = parent;
211
    #if USEARRAYPOOL
212
                      ArrayPool.Free(path);
213
    #endif
214
                  }
215
             }
216
217
             private TElement Balance(TElement node)
218
219
                  unchecked
```

```
var rootBalance = GetBalance(node);
        if (rootBalance < -1)</pre>
            var left = GetLeft(node);
            if (GetBalance(left) > 0)
                 SetLeft(node, LeftRotateWithBalance(left));
                 FixSize(node);
            node = RightRotateWithBalance(node);
        else if (rootBalance > 1)
            var right = GetRight(node);
            if (GetBalance(right) < 0)</pre>
                 SetRight(node, RightRotateWithBalance(right));
                 FixSize(node);
            node = LeftRotateWithBalance(node);
        return node;
    }
}
protected TElement LeftRotateWithBalance(TElement node)
    unchecked
    {
        var right = GetRight(node);
        if (GetLeftIsChild(right))
            SetRight(node, GetLeft(right));
        else
        {
            SetRightIsChild(node, false);
            SetLeftIsChild(right, true);
        SetLeft(right, node);
        // Fix size
        SetSize(right, GetSize(node));
        FixSize(node);
        // Fix balance
        var rootBalance = GetBalance(node);
        var rightBalance = GetBalance(right);
        if (rightBalance <= 0)</pre>
            if (rootBalance >= 1)
                 SetBalance(right, (sbyte)(rightBalance - 1));
            }
            else
            {
                 SetBalance(right, (sbyte)(rootBalance + rightBalance - 2));
            SetBalance(node, (sbyte)(rootBalance - 1));
        else
            if (rootBalance <= rightBalance)</pre>
            {
                 SetBalance(right, (sbyte)(rootBalance - 2));
            }
            else
            {
                 SetBalance(right, (sbyte)(rightBalance - 1));
            SetBalance(node, (sbyte)(rootBalance - rightBalance - 1));
        return right;
    }
}
protected TElement RightRotateWithBalance(TElement node)
    unchecked
```

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 $\frac{229}{230}$

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276 277

 $\frac{278}{279}$

280 281

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290 291

292

294

```
var left = GetLeft(node);
                if (GetRightIsChild(left))
                    SetLeft(node, GetRight(left));
                }
                else
                    SetLeftIsChild(node, false);
                    SetRightIsChild(left, true);
                SetRight(left, node);
                // Fix size
                SetSize(left, GetSize(node));
                FixSize(node);
                // Fix balance
                var rootBalance = GetBalance(node);
                var leftBalance = GetBalance(left);
                if (leftBalance <= 0)</pre>
                    if (leftBalance > rootBalance)
                         SetBalance(left, (sbyte)(leftBalance + 1));
                    }
                    else
                    {
                         SetBalance(left, (sbyte)(rootBalance + 2));
                    SetBalance(node, (sbyte)(rootBalance - leftBalance + 1));
                else
                    if (rootBalance <= -1)</pre>
                         SetBalance(left, (sbyte)(leftBalance + 1));
                    else
                    {
                         SetBalance(left, (sbyte)(rootBalance + leftBalance + 2));
                    SetBalance(node, (sbyte)(rootBalance + 1));
                return left;
            }
        }
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected override TElement GetNext(TElement node)
            var current = GetRight(node);
            if (GetRightIsChild(node))
            {
                return GetLeftest(current);
            return current;
        }
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected override TElement GetPrevious(TElement node)
            var current = GetLeft(node);
            if (GetLeftIsChild(node))
            {
                return GetRightest(current);
            return current;
        protected override void DetachCore(ref TElement root, TElement node)
            unchecked
#if USEARRAYPOOL
                var path = ArrayPool.Allocate<TElement>(MaxPath);
                var pathPosition = 0;
                path[pathPosition++] = default;
#else
                var path = new TElement[MaxPath];
                var pathPosition = 1;
```

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 $\frac{327}{328}$

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362 363 364

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367 368

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371

372

373

 $\frac{374}{375}$

```
var currentNode = root;
while (true)
    if (FirstIsToTheLeftOfSecond(node, currentNode))
        if (!GetLeftIsChild(currentNode))
            throw new InvalidOperationException("Cannot find a node.");
        DecrementSize(currentNode);
        path[pathPosition++] = currentNode;
        currentNode = GetLeft(currentNode);
    else if (FirstIsToTheRightOfSecond(node, currentNode))
        if (!GetRightIsChild(currentNode))
        {
            throw new InvalidOperationException("Cannot find a node.");
        DecrementSize(currentNode);
        path[pathPosition++] = currentNode;
        currentNode = GetRight(currentNode);
    }
    else
    {
        break;
    }
}
var parent = path[--pathPosition];
var balanceNode = parent;
   isLeftNode = !AreEqual(parent, default) && AreEqual(currentNode,
    GetLeft(parent));
   (!GetLeftIsChild(currentNode))
    if (!GetRightIsChild(currentNode)) // node has no children
        if (AreEqual(parent, default))
            root = Zero;
        else if (isLeftNode)
            SetLeftIsChild(parent, false);
            SetLeft(parent, GetLeft(currentNode));
            IncrementBalance(parent);
        }
        else
        {
            SetRightIsChild(parent, false);
            SetRight(parent, GetRight(currentNode));
            DecrementBalance(parent);
        }
    }
    else // node has a right child
        var successor = GetNext(currentNode);
        SetLeft(successor, GetLeft(currentNode));
        var right = GetRight(currentNode);
        if (AreEqual(parent, default))
        {
            root = right;
        }
        else if (isLeftNode)
            SetLeft(parent, right)
            IncrementBalance(parent);
        }
        else
            SetRight(parent, right);
            DecrementBalance(parent);
    }
else // node has a left child
    if (!GetRightIsChild(currentNode))
```

#endif

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451

```
var predecessor = GetPrevious(currentNode);
   SetRight(predecessor, GetRight(currentNode));
   var leftValue = GetLeft(currentNode);
   if (AreEqual(parent, default))
    {
        root = leftValue;
   }
   else if (isLeftNode)
        SetLeft(parent, leftValue);
        IncrementBalance(parent);
   }
    else
    {
        SetRight(parent, leftValue);
        DecrementBalance(parent);
else // node has a both children (left and right)
   var predecessor = GetLeft(currentNode);
   var successor = GetRight(currentNode);
   var successorParent = currentNode;
   int previousPathPosition = ++pathPosition;
   // find the immediately next node (and its parent)
   while (GetLeftIsChild(successor))
       path[++pathPosition] = successorParent = successor;
        successor = GetLeft(successor);
        if (!AreEqual(successorParent, currentNode))
            DecrementSize(successorParent);
   path[previousPathPosition] = successor;
   balanceNode = path[pathPosition];
    // remove 'successor' from the tree
   if (!AreEqual(successorParent, currentNode))
   {
        if (!GetRightIsChild(successor))
        {
            SetLeftIsChild(successorParent, false);
        }
        else
        {
            SetLeft(successorParent, GetRight(successor));
        IncrementBalance(successorParent);
        SetRightIsChild(successor, true);
        SetRight(successor, GetRight(currentNode));
   }
   else
    {
        DecrementBalance(currentNode);
    // set the predecessor's successor link to point to the right place
   while (GetRightIsChild(predecessor))
       predecessor = GetRight(predecessor);
   SetRight(predecessor, successor);
   // prepare 'successor' to replace 'node'
   var left = GetLeft(currentNode);
   SetLeftIsChild(successor, true);
   SetLeft(successor, left)
   SetBalance(successor, GetBalance(currentNode));
   FixSize(successor);
   if (AreEqual(parent, default))
        root = successor;
   else if (isLeftNode)
        SetLeft(parent, successor);
    else
```

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509 510

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521

523 524

525 526

527

529

530

```
SetRight(parent, successor);
533
                               }
                          }
535
536
                         restore balance
                      if (!AreEqual(balanceNode, default))
538
539
                           while (true)
540
                               var balanceParent = path[--pathPosition];
542
                               isLeftNode = !AreEqual(balanceParent, default) && AreEqual(balanceNode,
543

   GetLeft(balanceParent));
                               var currentNodeBalance = GetBalance(balanceNode);
544
                               if (currentNodeBalance < -1 || currentNodeBalance > 1)
545
546
                                   balanceNode = Balance(balanceNode);
547
548
                                   if (AreEqual(balanceParent, default))
                                    {
549
                                        root = balanceNode;
550
                                   }
551
                                   else if (isLeftNode)
552
553
                                        SetLeft(balanceParent, balanceNode);
                                   }
555
                                   else
                                   {
557
                                        SetRight(balanceParent, balanceNode);
558
                                   }
559
                               }
560
                               currentNodeBalance = GetBalance(balanceNode);
561
                               if (currentNodeBalance != 0 || AreEqual(balanceParent, default))
562
563
                                   break:
564
565
                               if (isLeftNode)
                               {
567
                                   IncrementBalance(balanceParent);
568
                               }
                               else
570
                               {
572
                                   DecrementBalance(balanceParent);
573
                               balanceNode = balanceParent;
574
                           }
575
576
                      ClearNode(node);
577
    #if USEARRAYPOOL
578
                      ArrayPool.Free(path);
579
    #endif
580
                  }
581
             }
583
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected override void ClearNode(TElement node)
585
586
                  SetLeft(node, Zero);
587
                 SetRight(node, Zero);
SetSize(node, Zero);
589
                  SetLeftIsChild(node, false);
590
                  SetRightIsChild(node, false);
                 SetBalance(node, 0);
592
             }
593
         }
594
595
./Platform.Collections.Methods/Trees/SizedBinaryTreeMethodsBase.cs
    using System;
    using System.Runtime.CompilerServices;
    using System. Text;
 3
    using Platform. Numbers;
    //#define ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
    namespace Platform.Collections.Methods.Trees
 9
    {
10
         public abstract class SizedBinaryTreeMethodsBase<TElement> :
11
             GenericCollectionMethodsBase<TElement>
12
```

```
[MethodImpl(MethodImplOptions.AggressiveInlining)]
13
            protected abstract ref TElement GetLeftReference(TElement node);
15
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected abstract ref TElement GetRightReference(TElement node);
17
18
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
19
           protected abstract TElement GetLeft(TElement node);
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
22
           protected abstract TElement GetRight(TElement node);
23
24
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
25
           protected abstract TElement GetSize(TElement node);
26
27
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
28
           protected abstract void SetLeft(TElement node, TElement left);
30
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
31
           protected abstract void SetRight(TElement node, TElement right);
32
33
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected abstract void SetSize(TElement node, TElement size);
35
36
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
37
           protected abstract bool FirstIsToTheLeftOfSecond(TElement first, TElement second);
38
39
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
40
           protected abstract bool FirstIsToTheRightOfSecond(TElement first, TElement second);
41
42
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
43
           protected virtual TElement GetLeftOrDefault(TElement node) => AreEqual(node, default) ?
               default : GetLeft(node);
45
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
46
           protected virtual TElement GetRightOrDefault(TElement node) => AreEqual(node, default) ?

→ default : GetRight(node);

48
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
49
           protected void IncrementSize(TElement node) => SetSize(node, Increment(GetSize(node)));
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected void DecrementSize(TElement node) => SetSize(node, Decrement(GetSize(node)));
53
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
55
           protected TElement GetLeftSize(TElement node) => GetSizeOrZero(GetLeftOrDefault(node));
56
57
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
58
           protected TElement GetRightSize(TElement node) => GetSizeOrZero(GetRightOrDefault(node));
59
60
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
61
           protected TElement GetSizeOrZero(TElement node) => EqualToZero(node) ? Zero :

   GetSize(node);
63
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
64
           protected void FixSize(TElement node) => SetSize(node, Increment(Add(GetLeftSize(node),
65
               GetRightSize(node))));
66
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected void LeftRotate(ref TElement root) => root = LeftRotate(root);
69
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
70
           protected TElement LeftRotate(TElement root)
7.1
72
                var right = GetRight(root)
73
   #if ENABLE TREE AUTO DEBUG AND VALIDATION
74
                if (EqualToZero(right))
75
                {
76
                    throw new Exception("Right is null.");
77
                }
78
   #endif
79
                SetRight(root, GetLeft(right));
80
                SetLeft(right, root);
81
                SetSize(right, GetSize(root));
82
                FixSize(root);
83
                return right;
85
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
87
```

```
protected void RightRotate(ref TElement root) => root = RightRotate(root);
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected TElement RightRotate(TElement root)
var left = GetLeft(root);
#if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
            if (EqualToZero(left))
                throw new Exception("Left is null.");
            }
#endif
            SetLeft(root, GetRight(left));
            SetRight(left, root);
            SetSize(left, GetSize(root));
            FixSize(root);
            return left;
        }
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected virtual TElement GetRightest(TElement current)
            var currentRight = GetRight(current);
            while (!EqualToZero(currentRight))
                current = currentRight;
                currentRight = GetRight(current);
            return current;
        }
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected virtual TElement GetLeftest(TElement current)
            var currentLeft = GetLeft(current);
            while (!EqualToZero(currentLeft))
            {
                current = currentLeft;
                currentLeft = GetLeft(current);
            return current;
        }
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected virtual TElement GetNext(TElement node) => GetLeftest(GetRight(node));
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected virtual TElement GetPrevious(TElement node) => GetRightest(GetLeft(node));
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        public virtual bool Contains (TElement node, TElement root)
            while (!EqualToZero(root))
            {
                if (FirstIsToTheLeftOfSecond(node, root)) // node.Key < root.Key</pre>
                {
                    root = GetLeft(root);
                else if (FirstIsToTheRightOfSecond(node, root)) // node.Key > root.Key
                    root = GetRight(root);
                else // node.Key == root.Key
                    return true;
            return false;
        }
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
        protected virtual void ClearNode(TElement node)
            SetLeft(node, Zero)
            SetRight(node, Zero);
            SetSize(node, Zero);
        [MethodImpl(MethodImplOptions.AggressiveInlining)]
```

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159 160 161

162

163 164 165

```
public void Attach(ref TElement root, TElement node)
167
168
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
169
                 ValidateSizes(root);
170
                 Debug.WriteLine("--BeforeAttach--");
171
                 Debug.WriteLine(PrintNodes(root));
172
                 Debug.WriteLine("----");
173
                 var sizeBefore = GetSize(root);
174
    #endif
175
                 if (EqualToZero(root))
176
177
                     SetSize(node, One);
178
179
                     root = node;
                     return;
180
181
                 AttachCore(ref root, node)
182
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
183
                 Debug.WriteLine("--AfterAttach--");
184
                 Debug .WriteLine(PrintNodes(root));
185
                 Debug.WriteLine("----");
186
                 ValidateSizes(root);
187
                 var sizeAfter = GetSize(root);
188
                 if (!IsEquals(MathHelpers.Increment(sizeBefore), sizeAfter))
189
                      throw new Exception("Tree was broken after attach.");
191
                 }
192
    #endif
193
194
195
             protected abstract void AttachCore(ref TElement root, TElement node);
196
198
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             public void Detach(ref TElement root, TElement node)
199
200
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
201
                 ValidateSizes(root);
202
                 Debug.WriteLine("--BeforeDetach--");
203
                 Debug.WriteLine(PrintNodes(root));
204
                 Debug.WriteLine("----");
205
                 var sizeBefore = GetSize(root);
206
                 if (ValueEqualToZero(root))
207
                 {
208
                      throw new Exception($"Элемент с {node} не содержится в дереве.");
209
210
                 }
    #endif
211
    DetachCore(ref root, node);
#if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
212
213
                 Debug.WriteLine("--AfterDetach--");
214
                 Debug.WriteLine(PrintNodes(root));
215
                 Debug.WriteLine("----"):
216
217
                 ValidateSizes(root);
                 var sizeAfter = GetSize(root);
218
                 if (!IsEquals(MathHelpers.Decrement(sizeBefore), sizeAfter))
220
                      throw new Exception("Tree was broken after detach.");
221
                 }
222
    #endif
223
             }
224
225
             protected abstract void DetachCore(ref TElement root, TElement node);
226
227
             public void FixSizes(TElement node)
228
229
                 if (AreEqual(node, default))
230
                 {
231
                     return;
233
                 FixSizes(GetLeft(node)):
234
                 FixSizes(GetRight(node));
235
236
                 FixSize(node);
             }
237
238
             public void ValidateSizes(TElement node)
239
240
241
                 if (AreEqual(node, default))
                 {
242
                     return;
243
244
                 var size = GetSize(node);
245
```

```
var leftSize = GetLeftSize(node)
246
                 var rightSize = GetRightSize(node);
                 var expectedSize = Arithmetic.Increment(Arithmetic.Add(leftSize, rightSize));
248
                 if (!AreEqual(size, expectedSize))
249
                     throw new InvalidOperationException($\sigmu$"Size of \{node\} is not valid. Expected
                        size: {expectedSize}, actual size: {size}.");
                 ValidateSizes(GetLeft(node));
253
                 ValidateSizes(GetRight(node));
254
256
             public void ValidateSize(TElement node)
257
258
                 var size = GetSize(node);
259
                 var leftSize = GetLeftSize(node)
260
                 var rightSize = GetRightSize(node);
                 var expectedSize = Arithmetic.Increment(Arithmetic.Add(leftSize, rightSize));
262
                 if (!AreEqual(size, expectedSize))
263
264
                     throw new InvalidOperationException(|$|"Size of {node} is not valid. Expected
265

    size: {expectedSize}, actual size: {size}.");
266
                 }
             }
267
268
             public string PrintNodes(TElement node)
269
270
                 var sb = new StringBuilder();
                 PrintNodes(node, sb);
272
                 return sb.ToString();
273
             }
274
275
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
276
             public void PrintNodes(TElement node, StringBuilder sb) => PrintNodes(node, sb, 0);
277
278
             public void PrintNodes(TElement node, StringBuilder sb, int level)
279
280
                 if (AreEqual(node, default))
281
                 {
282
283
                     return;
284
285
                 PrintNodes(GetLeft(node), sb, level + 1);
286
                 PrintNode(node, sb, level);
                 sb.AppendLine()
287
                 PrintNodes(GetRight(node), sb, level + 1);
288
             }
289
290
             public string PrintNode(TElement node)
292
                 var sb = new StringBuilder();
293
                 PrintNode(node, sb);
294
                 return sb.ToString();
295
             }
296
297
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
298
             protected void PrintNode(TElement node, StringBuilder sb) => PrintNode(node, sb, 0);
299
300
             protected virtual void PrintNode(TElement node, StringBuilder sb, int level)
301
302
                 sb.Append('\t'
                                 level);
303
                 sb.Append(node);
304
                 PrintNodeValue(node, sb);
305
                 sb.Append(' ');
                 sb.Append('s')
307
                 sb.Append(GetSize(node));
308
309
310
             protected abstract void PrintNodeValue(TElement node, StringBuilder sb);
311
        }
./Platform.Collections.Methods.Tests/RecursionlessSizeBalancedTree.cs
    using System;
    using System.Collections.Generic;
    using System.Text;
          Platform.Numbers;
    using
    using Platform.Collections.Methods.Trees;
    namespace Platform.Collections.Methods.Tests
```

```
{
    public class RecursionlessSizeBalancedTree<TElement> :
       RecursionlessSizeBalancedTreeMethods<TElement>
        private struct TreeElement
            public TElement Size;
            public TElement Left;
            public TElement Right;
        private readonly TreeElement[] _elements;
        private TElement _allocated;
        public TElement Root;
        public TElement Count => GetSizeOrZero(Root);
        public RecursionlessSizeBalancedTree(int capacity) => (_elements, _allocated) = (new
        → TreeElement[capacity], Integer<TElement>.One);
        public TElement Allocate()
            var newNode = _allocated;
            if (IsEmpty(newNode))
                 _allocated = Arithmetic.Increment(_allocated);
                return newNode;
            }
            else
            {
                throw new InvalidOperationException("Allocated tree element is not empty.");
        }
        public void Free(TElement node)
            while (!EqualityComparer.Equals(_allocated, Integer<TElement>.One) && IsEmpty(node))
                var lastNode = Arithmetic.Decrement(_allocated);
                if (EqualityComparer.Equals(lastNode, node))
                    _allocated = lastNode;
                    node = Arithmetic.Decrement(node);
                else
                {
                    return;
                }
            }
        }
        public bool IsEmpty(TElement node) =>
           EqualityComparer<TreeElement>.Default.Equals(GetElement(node), default);
        protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>

→ Comparer.Compare(first, second) < 0;
</p>
        protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>
        → Comparer.Compare(first, second) > 0;
        protected override ref TElement GetLeftReference(TElement node) => ref

   GetElement(node).Left;
        protected override TElement GetLeft(TElement node) => GetElement(node).Left;
        protected override ref TElement GetRightReference(TElement node) => ref

   GetElement(node).Right;

        protected override TElement GetRight(TElement node) => GetElement(node).Right;
        protected override TElement GetSize(TElement node) => GetElement(node).Size;
        protected override void PrintNodeValue(TElement node, StringBuilder sb) =>

⇒ sb.Append(node);

        protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
          left;
```

10

11 12

13

15 16 17

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21 22

 $\frac{23}{24}$

25

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39 40

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43 44

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73

74

7.5

76

```
protected override void SetRight(TElement node, TElement right) =>
78

   GetElement(node).Right = right;
79
           protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =
80

    size;

81
           private ref TreeElement GetElement(TElement node) => ref
82

    _elements[(Integer<TElement>)node];
       }
   }
84
./Platform.Collections.Methods.Tests/SizeBalancedTree.cs
   using System;
   using System.Collections.Generic;
   using System. Text;
   using Platform. Numbers;
   using Platform.Collections.Methods.Trees;
   namespace Platform.Collections.Methods.Tests
7
       public class SizeBalancedTree<TElement> : SizeBalancedTreeMethods<TElement>
9
10
           private struct TreeElement
11
12
                public TElement Size;
13
                public TElement Left;
14
                public TElement Right;
15
16
17
           private readonly TreeElement[] _elements;
18
           private TElement _allocated;
19
20
           public TElement Root;
21
22
           public TElement Count => GetSizeOrZero(Root);
23
24
           public SizeBalancedTree(int capacity) => (_elements, _allocated) = (new
25

→ TreeElement[capacity], Integer<TElement>.One);
           public TElement Allocate()
27
28
                var newNode = _allocated;
29
                if (IsEmpty(newNode))
30
3.1
                    _allocated = Arithmetic.Increment(_allocated);
                   return newNode;
33
                }
34
                else
35
                {
36
                    throw new InvalidOperationException("Allocated tree element is not empty.");
                }
38
           }
39
40
           public void Free(TElement node)
41
                while (!EqualityComparer.Equals(_allocated, Integer<TElement>.One) && IsEmpty(node))
43
44
                    var lastNode = Arithmetic.Decrement(_allocated);
45
                    if (EqualityComparer.Equals(lastNode, node))
46
47
                        _allocated = lastNode;
                       node = Arithmetic.Decrement(node);
49
                   }
50
                    else
51
                    {
52
                        return;
                    }
54
                }
55
56
57
           public bool IsEmpty(TElement node) =>
58
            5.9
           protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
60
            → Comparer.Compare(first, second) < 0;</p>
           protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>
62
            → Comparer.Compare(first, second) > 0;
```

```
protected override ref TElement GetLeftReference(TElement node) => ref
64
               GetElement(node).Left;
65
            protected override TElement GetLeft(TElement node) => GetElement(node).Left;
66
67
            protected override ref TElement GetRightReference(TElement node) => ref
68

   GetElement(node).Right;

            protected override TElement GetRight(TElement node) => GetElement(node).Right;
7.0
71
            protected override TElement GetSize(TElement node) => GetElement(node).Size;
72
73
            protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
             \rightarrow sb.Append(node);
7.5
            protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
            → left;
            protected override void SetRight(TElement node, TElement right) =>

   GetElement(node).Right = right;
79
            protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =

→ size;

81
            private ref TreeElement GetElement(TElement node) => ref
            → _elements[(Integer<TElement>)node];
        }
83
   }
84
./Platform.Collections.Methods.Tests/SizedAndThreadedAVLBalancedTree.cs
   using System;
   using System Collections Generic;
   using System.Text;
using Platform.Numbers;
3
   using Platform.Collections.Methods.Trees;
   namespace Platform.Collections.Methods.Tests
       public class SizedAndThreadedAVLBalancedTree<TElement> :
           SizedAndThreadedAVLBalancedTreeMethods<TElement>
10
            private struct TreeElement
11
12
                public TElement Size;
13
                public TElement Left;
public TElement Right;
14
15
                public sbyte Balance;
16
                public bool LeftIsChild
17
                public bool RightIsChild;
            }
19
            private readonly TreeElement[] _elements;
2.1
22
            private TElement _allocated;
23
            public TElement Root;
25
            public TElement Count => GetSizeOrZero(Root);
27
            public SizedAndThreadedAVLBalancedTree(int capacity) => (_elements, _allocated) = (new
28
            → TreeElement[capacity], Integer<TElement>.One);
29
            public TElement Allocate()
30
                var newNode = _allocated;
32
                if (IsEmpty(newNode))
34
                     _allocated = Arithmetic.Increment(_allocated);
35
                    return newNode;
36
                }
37
                else
                {
39
                    throw new InvalidOperationException("Allocated tree element is not empty.");
40
41
            }
42
43
            public void Free(TElement node)
45
                while (!EqualityComparer.Equals(_allocated, Integer<TElement>.One) && IsEmpty(node))
46
47
                    var lastNode = Arithmetic.Decrement(_allocated);
```

```
if (EqualityComparer.Equals(lastNode, node))
49
                         _allocated = lastNode;
5.1
                        node = Arithmetic.Decrement(node);
53
                    else
54
                    {
55
                        return;
56
                    }
                }
58
            }
59
60
            public bool IsEmpty(TElement node) =>
61
               EqualityComparer<TreeElement>.Default.Equals(GetElement(node), default);
            protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
63
            → Comparer.Compare(first, second) < 0;</p>
            protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>

→ Comparer.Compare(first, second) > 0;

66
            protected override sbyte GetBalance(TElement node) => GetElement(node).Balance;
68
            protected override bool GetLeftIsChild(TElement node) => GetElement(node).LeftIsChild;
69
70
            protected override ref TElement GetLeftReference(TElement node) => ref
71

    GetElement(node).Left;

72
            protected override TElement GetLeft(TElement node) => GetElement(node).Left;
73
74
            protected override bool GetRightIsChild(TElement node) => GetElement(node).RightIsChild;
75
76
            protected override ref TElement GetRightReference(TElement node) => ref
77

   GetElement(node).Right;
            protected override TElement GetRight(TElement node) => GetElement(node).Right;
79
            protected override TElement GetSize(TElement node) => GetElement(node).Size;
81
82
            protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
83
            \rightarrow sb.Append(node);
84
            protected override void SetBalance(TElement node, sbyte value) =>
85
               GetElement(node) . Balance = value;
86
            protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
            → left;
            protected override void SetLeftIsChild(TElement node, bool value) =>

    GetElement(node).LeftIsChild = value;

90
            protected override void SetRight(TElement node, TElement right) =>
91

   GetElement(node).Right = right;
92
            protected override void SetRightIsChild(TElement node, bool value) =>
93

    GetElement(node).RightIsChild = value;

94
            protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =
95

    size;

96
            private ref TreeElement GetElement(TElement node) => ref
97
               _elements[(Integer<TElement>)node];
        }
   }
./Platform. Collections. Methods. Tests/Test Extensions. cs\\
   using System;
   using System.Collections.Generic;
using Xunit;
2
   using Platform. Numbers;
   using Platform.Collections.Methods.Trees;
   namespace Platform.Collections.Methods.Tests
        public static class TestExtensions
9
10
            public static void TestMultipleCreationsAndDeletions<TElement>(this
               SizedBinaryTreeMethodsBase<TElement> tree, Func<TElement> allocate, Action<TElement>
               free, ref TElement root, Func<TElement> treeCount, int maximumOperationsPerCycle)
```

```
12
                for (var N = 1; N < maximumOperationsPerCycle; N++)</pre>
13
14
                     var currentCount = 0;
                     for (var i = 0; i < N; i++)</pre>
16
                     {
17
                         var node = allocate();
18
                         tree.Attach(ref root, node);
19
                         currentCount++;
20
                         Assert.Equal(currentCount, (int)(Integer<TElement>)treeCount());
22
                     for (var i = 1; i <= N; i++)
23
24
25
                         TElement node = (Integer<TElement>)i;
26
                         if (tree.Contains(node, root))
27
                             tree.Detach(ref root, node);
                             free(node);
29
                             currentCount--;
30
                             Assert.Equal(currentCount, (int)(Integer<TElement>)treeCount());
31
                         }
32
                     }
33
                }
            }
35
36
            public static void TestMultipleRandomCreationsAndDeletions<TElement>(this
37
                SizedBinaryTreeMethodsBase<TElement> tree, ref TElement root, Func<TElement>
                treeCount, int maximumOperationsPerCycle)
38
                var random = new System.Random(0);
39
                var added = new HashSet<TElement>();
40
                var currentCount = 0;
41
                for (var N = 1; N < maximumOperationsPerCycle; N++)</pre>
42
                {
43
                     for (var i = 0; i < N; i++)</pre>
                         var node = (Integer<TElement>)random.Next(1, N);
46
                         if (added.Add(node))
47
                             tree.Attach(ref root, node);
49
                             currentCount++;
                             Assert.Equal(currentCount, (int)(Integer<TElement>)treeCount());
51
52
53
                     for (var i = 1; i <= N; i++)</pre>
55
                         TElement node = (Integer<TElement>)random.Next(1, N);
56
                         if (tree.Contains(node, root))
                         {
                             tree.Detach(ref root, node);
59
                             currentCount--
                             Assert.Equal(currentCount, (int)(Integer<TElement>)treeCount());
61
                             added.Remove(node);
62
                         }
                     }
64
               }
65
            }
66
        }
67
68
./Platform.Collections.Methods.Tests/TreesTests.cs
   using Xunit;
1
   namespace Platform.Collections.Methods.Tests
3
4
        public static class TreesTests
5
6
            private const int _n = 500;
            [Fact]
            public static void RecursionlessSizeBalancedTreeMultipleAttachAndDetachTest()
10
11
                var recursionlessSizeBalancedTree = new RecursionlessSizeBalancedTree<uint>(10000);
12
                recursionlessSizeBalancedTree.TestMultipleCreationsAndDeletions(recursionlessSizeBal
13
                    ancedTree.Allocate, recursionlessSizeBalancedTree.Free, ref
                    recursionlessSizeBalancedTree.Root, () => recursionlessSizeBalancedTree.Count,
                    _n);
            }
```

```
[Fact]
16
                                  public static void SizeBalancedTreeMultipleAttachAndDetachTest()
17
18
                                              var sizeBalancedTree = new SizeBalancedTree<uint>(10000);
19
                                              sizeBalancedTree.TestMultipleCreationsAndDeletions(sizeBalancedTree.Allocate,

→ sizeBalancedTree.Free, ref sizeBalancedTree.Root, () => sizeBalancedTree.Count,

                                                         _n);
                                  }
21
22
                                  [Fact]
23
                                  public static void SizedAndThreadedAVLBalancedTreeMultipleAttachAndDetachTest()
25
                                              var avlTree = new SizedAndThreadedAVLBalancedTree<uint>(10000);
26
27
                                              avlTree.TestMultipleCreationsAndDeletions(avlTree.Allocate, avlTree.Free, ref
                                                        avlTree.Root, () => avlTree.Count, _n);
                                  }
29
                                  [Fact]
30
                                  public static void RecursionlessSizeBalancedTreeMultipleRandomAttachAndDetachTest()
31
32
                                              var recursionlessSizeBalancedTree = new RecursionlessSizeBalancedTree<uint>(10000);
33
                                              {\tt recursionlessSizeBalancedTree.TestMultipleRandomCreationsAndDeletions} (\textbf{refine} and \textbf{refine} and \textbf{refine}
                                               recursionlessSizeBalancedTree.Root, () => recursionlessSizeBalancedTree.Count,
                                                         _n);
                                  }
36
                                  [Fact]
                                  public static void SizeBalancedTreeMultipleRandomAttachAndDetachTest()
39
                                              var sizeBalancedTree = new SizeBalancedTree<uint>(10000);
40
                                              sizeBalancedTree.TestMultipleRandomCreationsAndDeletions(ref sizeBalancedTree.Root,
41
                                               }
42
43
                                  [Fact]
                                  public static void SizedAndThreadedAVLBalancedTreeMultipleRandomAttachAndDetachTest()
45
46
                                              var avlTree = new SizedAndThreadedAVLBalancedTree<uint>(10000);
47
                                              avlTree.TestMultipleRandomCreationsAndDeletions(ref avlTree.Root, () =>
                                               \rightarrow avlTree.Count, _n);
                                  }
49
                      }
50
          }
51
```

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