```
LinksPlatform's Platform Collections Methods Class Library
     ./csharp/Platform. Collections. Methods/Generic Collection Methods Base.cs\\
   using System.Collections.Generic;
using System.Runtime.CompilerServices;
2
   using Platform. Numbers;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods
        /// <summary>
9
        /// <para>Represents a range between minimum and maximum values.</para>
10
        /// <para>Представляет диапазон между минимальным и максимальным значениями.</para>
11
        /// </summary>
12
        /// <remarks>
13
        /// <para>Based on <a href="http://stackoverflow.com/questions/5343006/is-there-a-c-sharp-ty|
        _{\hookrightarrow} pe-for-representing-an-integer-range">the question at
           StackOverflow</a>.</para>
        /// <para>Ochobaho ha <a href="http://stackoverflow.com/questions/5343006/is-there-a-c-sharp_
15
            -type-for-representing-an-integer-range">вопросе в
           StackOverflow</a>.</para>
        /// </remarks>
       public abstract class GenericCollectionMethodsBase<TElement>
            /// <summary>
19
            /// <para>Returns minimum value of the range.</para>
20
            /// <para>Возвращает минимальное значение диапазона.</para>
21
            /// </summary>
22
            /// <summary>
24
            /// <para>Presents the Range in readable format.</para>
25
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
26
            /// </summary>
27
            /// <returns><para>String representation of the Range.</para><para>Строковое
28
               представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
29
            protected virtual TElement GetZero() => default;
            /// <summary>
31
            /// <para>Returns minimum value of the range.</para>
32
            /// <para>Возвращает минимальное значение диапазона.</para>
33
            /// </summary>
35
            /// <summary>
            /// <para>Presents the Range in readable format.</para>
37
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
38
            /// </summary>
39
            /// <returns><para>String representation of the Range.</para><para>Строковое
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool EqualToZero(TElement value) => EqualityComparer.Equals(value,
42

    Zero);

            /// <summary>
43
            /// <para>Returns minimum value of the range.</para>
            /// <para>Возвращает минимальное значение диапазона.</para>
45
            /// </summary>
46
47
            /// <summary>
48
            /// <para>Presents the Range in readable format.</para>
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
50
            /// </summary>
51
            /// <returns><para>String representation of the Range.</para><para>Строковое
52
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool AreEqual(TElement first, TElement second) =>
                EqualityComparer.Equals(first, second);
            /// <summary>
55
            /// <para>Returns minimum value of the range.</para>
56
            /// <para>Возвращает минимальное значение диапазона.</para>
            /// <\bar{\summary>
58
            /// <summary>
60
            /// <para>Presents the Range in readable format.</para>
61
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
62
            /// </summary>
            /// <returns><para>String representation of the Range.</para><para>Строковое
64
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
65
```

```
protected virtual bool GreaterThanZero(TElement value) => Comparer.Compare(value, Zero)
66
               > 0;
            /// <summary>
            /// <para>Returns minimum value of the range.</para>
68
            /// <para>Возвращает минимальное значение диапазона.</para>
69
            /// </summary>
71
            /// <summary>
72
            /// <para>Presents the Range in readable format.</para>
73
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
74
75
            /// <returns><para>String representation of the Range.</para><para>Строковое

    представление диапазона.
</returns>

            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool GreaterThan(TElement first, TElement second) =>
78
                Comparer.Compare(first, second) > 0;
            /// <summary>
            /// <para>Returns minimum value of the range.</para>
            /// <para>Возвращает минимальное значение диапазона.</para>
81
            /// </summary>
83
            /// <summary>
84
            /// <para>Presents the Range in readable format.</para>
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
86
            /// </summary>
            /// <returns><para>String representation of the Range.</para><para>Строковое
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool GreaterOrEqualThanZero(TElement value) => Comparer.Compare(value,
90
             \rightarrow Zero) >= 0;
            /// <summary>
91
            /// <para>Returns minimum value of the range.</para>
92
            /// <para>Возвращает минимальное значение диапазона.</para>
            /// </summary>
94
            /// <summary>
96
            /// <para>Presents the Range in readable format.</para>
97
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
            /// </summary>
            /// <returns><para>String representation of the Range.</para><para>Строковое
100
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
101
            protected virtual bool GreaterOrEqualThan(TElement first, TElement second) =>
102

→ Comparer.Compare(first, second) >= 0;
            /// <summary>
103
            /// <para>Returns minimum value of the range.</para>
104
            /// <para>Возвращает минимальное значение диапазона.</para>
105
            /// </summary>
107
            /// <summary>
            /// <para>Presents the Range in readable format.</para>
109
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
110
            /// </summary>
111
            /// <returns><para>String representation of the Range.</para><para>Строковое
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
113
            protected virtual bool LessOrEqualThanZero(TElement value) => Comparer.Compare(value,
114
                Zero) <= 0;
            /// <summary>
115
            /// <para>Returns minimum value of the range.</para>
            /// <para>Возвращает минимальное значение диапазона.</para>
117
            /// </summary>
118
119
            /// <summary>
120
            /// <para>Presents the Range in readable format.</para>
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
            /// </summary>
123
            /// <returns><para>String representation of the Range.</para><para>Строковое
124
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool LessOrEqualThan(TElement first, TElement second) =>
126
                Comparer.Compare(first, second) <= 0;</pre>
            /// <summary>
127
            /// <para>Returns minimum value of the range.</para>
128
            /// <para>Возвращает минимальное значение диапазона.</para>
            /// </summary>
130
```

```
/// <summary>
132
            /// <para>Presents the Range in readable format.</para>
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
134
            /// </summary>
135
            /// <returns><para>String representation of the Range.</para><para>Строковое
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual bool LessThanZero(TElement value) => Comparer.Compare(value, Zero) < 0;</pre>
138
            /// <summary>
139
            /// <para>Returns minimum value of the range.</para>
140
            /// <para>Возвращает минимальное значение диапазона.</para>
141
            /// </summary>
142
            /// <summary>
144
            /// <para>Presents the Range in readable format.</para>
145
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
            /// </summary>
147
            /// <returns><para>String representation of the Range.</para><para>Строковое
148
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
149
            protected virtual bool LessThan(TElement first, TElement second) =>
                Comparer.Compare(first, second) < 0;</pre>
            /// <summary>
151
            /// <para>Returns minimum value of the range.</para>
152
            /// <para>Возвращает минимальное значение диапазона.</para>
153
            /// </summary>
155
            /// <summary>
            /// <para>Presents the Range in readable format.</para>
157
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
158
            /// </summary>
            /// <returns><para>String representation of the Range.</para>Строковое
160
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
161
            protected virtual TElement Increment(TElement value) =>
162
                Arithmetic<TElement>.Increment(value);
            /// <summary>
            /// <para>Returns minimum value of the range.</para>
164
            /// <para>Возвращает минимальное значение диапазона.</para>
165
            /// </summary>
166
167
            /// <summary>
168
            /// <para>Presents the Range in readable format.</para>
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
170
            /// </summary>
171
172
            /// <returns><para>String representation of the Range.</para><para>Строковое
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual TElement Decrement(TElement value) =>
174
                Arithmetic<TElement>.Decrement(value);
            /// <summary>
175
            /// <para>Returns minimum value of the range.</para>
            /// <para>Возвращает минимальное значение диапазона.</para>
177
            /// </summary>
178
179
            /// <summary>
180
            /// <para>Presents the Range in readable format.</para>
181
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
            /// </summary>
183
            /// <returns><para>String representation of the Range.</para><para>Строковое
184
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
185
            protected virtual TElement Add(TElement first, TElement second) =>
                Arithmetic<TElement>.Add(first, second);
            /// <summary>
187
            /// <para>Returns minimum value of the range.</para>
188
            /// <para>Возвращает минимальное значение диапазона.</para>
189
            /// </summary>
191
            /// <summary>
            /// <para>Presents the Range in readable format.</para>
193
            /// <para>Представляет диапазон в удобном для чтения формате.</para>
194
            /// </summary>
            /// <returns><para>String representation of the Range.</para><para>Строковое
                представление диапазона.</para></returns>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
197
```

```
protected virtual TElement Subtract(TElement first, TElement second) =>
198
                Arithmetic<TElement>.Subtract(first, second);
199
             /// <summary>
200
             /// <para>Returns minimum value of the range.</para>
201
             /// <para>Возвращает минимальное значение диапазона.</para>
202
             /// </summary>
203
             /// <summary>
205
             /// <para>Presents the Range in readable format.</para>
206
             /// <para>Представляет диапазон в удобном для чтения формате.</para>
             /// </summary>
             /// <returns><para>String representation of the Range.</para><para>Строковое
209
             → представление диапазона.</para></returns>
            protected readonly TElement Zero;
protected readonly TElement One;
protected readonly TElement Two;
protected readonly EqualityComparerTElement> EqualityComparer;
210
211
212
213
             protected readonly Comparer<TElement> Comparer;
214
215
             /// <summary>
216
             /// <para>Presents the Range in readable format.</para>
217
             /// <para>Представляет диапазон в удобном для чтения формате.</para>
             /// </summary>
219
             /// <returns><para>String representation of the Range.</para>Строковое
220
             → представление диапазона.</para></returns>
             protected GenericCollectionMethodsBase()
221
                 EqualityComparer = EqualityComparer<TElement>.Default;
223
                 Comparer = Comparer<TElement>.Default;
224
                 Zero = GetZero(); //-V3068
225
                 One = Increment(Zero); //-V3068
                 Two = Increment(One); //-V3068
227
             }
228
        }
229
230
     ./csharp/Platform.Collections.Methods/Lists/AbsoluteCircularDoublyLinkedListMethods.cs
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
 2
    namespace Platform.Collections.Methods.Lists
 3
 4
        public abstract class AbsoluteCircularDoublyLinkedListMethods<TElement> :
            AbsoluteDoublyLinkedListMethodsBase<TElement>
 6
             public void AttachBefore(TElement baseElement, TElement newElement)
                 var baseElementPrevious = GetPrevious(baseElement);
                 SetPrevious(newElement, baseElementPrevious);
10
                 SetNext(newElement, baseElement);
11
                 if (AreEqual(baseElement, GetFirst()))
                 {
13
                     SetFirst(newElement);
14
15
                 SetNext(baseElementPrevious, newElement);
16
                 SetPrevious(baseElement, newElement);
17
                 IncrementSize();
18
             }
20
             public void AttachAfter(TElement baseElement, TElement newElement)
21
22
                 var baseElementNext = GetNext(baseElement);
23
                 SetPrevious(newElement, baseElement);
                 SetNext(newElement, baseElementNext);
26
                 if (AreEqual(baseElement, GetLast()))
27
                     SetLast(newElement);
28
29
                 SetPrevious(baseElementNext, newElement);
30
                 SetNext(baseElement, newElement);
31
                 IncrementSize();
32
33
             public void AttachAsFirst(TElement element)
35
36
                 var first = GetFirst();
                 if (EqualToZero(first))
39
                     SetFirst(element);
```

```
SetLast(element);
41
                    SetPrevious(element, element);
43
                    SetNext(element, element);
                    IncrementSize();
44
                }
                else
46
                {
47
                    AttachBefore(first, element);
                }
49
            }
50
51
            public void AttachAsLast(TElement element)
52
53
                var last = GetLast()
                if (EqualToZero(last))
55
56
                    AttachAsFirst(element);
                }
                else
59
                {
60
                    AttachAfter(last, element);
61
                }
62
            }
64
            public void Detach(TElement element)
66
                var elementPrevious = GetPrevious(element);
67
                var elementNext = GetNext(element);
68
                if (AreEqual(elementNext, element))
70
                    SetFirst(Zero);
71
                    SetLast(Zero);
                }
73
                else
                {
                    SetNext(elementPrevious, elementNext);
76
                    SetPrevious(elementNext, elementPrevious);
77
                    if (AreEqual(element, GetFirst()))
79
                         SetFirst(elementNext);
80
                    }
81
                       (AreEqual(element, GetLast()))
83
                         SetLast(elementPrevious);
84
86
                SetPrevious(element, Zero);
87
                SetNext(element, Zero);
                DecrementSize();
89
            }
90
        }
91
   }
92
1.3
     ./csharp/Platform.Collections.Methods/Lists/AbsoluteDoublyLinkedListMethodsBase.cs
   using System.Runtime.CompilerServices;
2
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
4
   namespace Platform.Collections.Methods.Lists
5
6
       public abstract class AbsoluteDoublyLinkedListMethodsBase<TElement> :
           DoublyLinkedListMethodsBase<TElement>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetFirst();
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetLast();
13
14
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
15
            protected abstract TElement GetSize();
16
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
            protected abstract void SetFirst(TElement element);
19
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
            protected abstract void SetLast(TElement element);
23
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
```

```
protected abstract void SetSize(TElement size);
25
26
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
27
            protected void IncrementSize() => SetSize(Increment(GetSize()));
29
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
30
            protected void DecrementSize() => SetSize(Decrement(GetSize()));
31
        }
32
33
1.4
     ./csharp/Platform. Collections. Methods/Lists/AbsoluteOpenDoublyLinkedListMethods.cs\\
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
1
2
   namespace Platform.Collections.Methods.Lists
3
4
        public abstract class AbsoluteOpenDoublyLinkedListMethods<TElement> :
5
            AbsoluteDoublyLinkedListMethodsBase<TElement>
            public void AttachBefore(TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
                SetNext(newElement, baseElement);
1.1
                if (EqualToZero(baseElementPrevious))
12
13
                    SetFirst(newElement);
14
                }
15
                else
                {
17
                    SetNext(baseElementPrevious, newElement);
18
19
                SetPrevious(baseElement, newElement);
20
                IncrementSize();
2.1
            }
23
            public void AttachAfter(TElement baseElement, TElement newElement)
24
                var baseElementNext = GetNext(baseElement);
26
                SetPrevious(newElement, baseElement);
27
                SetNext(newElement, baseElementNext);
28
29
                if (EqualToZero(baseElementNext))
30
                    SetLast(newElement);
31
                }
32
                else
33
                {
                    SetPrevious(baseElementNext, newElement);
35
36
37
                SetNext(baseElement, newElement);
38
                IncrementSize();
            }
39
            public void AttachAsFirst(TElement element)
41
42
                var first = GetFirst();
43
                if (EqualToZero(first))
44
45
                    SetFirst(element);
46
                    SetLast(element);
                    SetPrevious(element, Zero);
48
                    SetNext(element, Zero);
49
                     IncrementSize();
50
                }
51
                else
                {
                     AttachBefore(first, element);
54
55
            }
57
            public void AttachAsLast(TElement element)
59
                var last = GetLast()
60
                if (EqualToZero(last))
61
62
                     AttachAsFirst(element);
63
                }
64
                else
66
                    AttachAfter(last, element);
```

```
68
            }
70
            public void Detach(TElement element)
79
                var elementPrevious = GetPrevious(element);
73
                var elementNext = GetNext(element);
74
                if (EqualToZero(elementPrevious))
75
                {
76
                    SetFirst(elementNext);
77
                }
                else
79
                {
80
                    SetNext(elementPrevious, elementNext);
81
82
                if (EqualToZero(elementNext))
83
                    SetLast(elementPrevious);
85
86
                else
87
                {
88
                    SetPrevious(elementNext, elementPrevious);
89
                SetPrevious(element, Zero);
91
                SetNext(element, Zero);
92
93
                DecrementSize();
            }
94
       }
95
   }
96
     ./csharp/Platform.Collections.Methods/Lists/DoublyLinkedListMethodsBase.cs
1.5
   using System.Runtime.CompilerServices;
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
3
   namespace Platform.Collections.Methods.Lists
5
        /// <remarks>
        /// Based on <a href="https://en.wikipedia.org/wiki/Doubly_linked_list">doubly linked
        → list</a> implementation.
/// </remarks`
9
       public abstract class DoublyLinkedListMethodsBase<TElement> :
10
           GenericCollectionMethodsBase<TElement>
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract Telement GetPrevious(Telement element);
13
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
15
            protected abstract TElement GetNext(TElement element);
16
17
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
19
            protected abstract void SetPrevious(TElement element, TElement previous);
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
            protected abstract void SetNext(TElement element, TElement next);
        }
23
24
     ./csharp/Platform.Collections.Methods/Lists/RelativeCircularDoublyLinkedListMethods.cs
1.6
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
2
   namespace Platform.Collections.Methods.Lists
3
4
       public abstract class RelativeCircularDoublyLinkedListMethods<TElement> :
           RelativeDoublyLinkedListMethodsBase<TElement>
6
            public void AttachBefore(TElement headElement, TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
10
                SetNext(newElement, baseElement);
                if (AreEqual(baseElement, GetFirst(headElement)))
12
                {
13
14
                    SetFirst(headElement, newElement);
15
                SetNext(baseElementPrevious, newElement);
16
                SetPrevious(baseElement, newElement);
17
                IncrementSize(headElement);
```

```
19
20
            public void AttachAfter(TElement headElement, TElement baseElement, TElement newElement)
21
                var baseElementNext = GetNext(baseElement);
23
                SetPrevious(newElement, baseElement);
24
                SetNext(newElement, baseElementNext);
25
                if (AreEqual(baseElement, GetLast(headElement)))
26
27
                    SetLast(headElement, newElement);
28
                SetPrevious(baseElementNext, newElement);
                SetNext(baseElement, newElement);
31
                IncrementSize(headElement);
32
            }
34
            public void AttachAsFirst(TElement headElement, TElement element)
36
                var first = GetFirst(headElement);
37
                if (EqualToZero(first))
38
39
                    SetFirst(headElement, element);
40
                    SetLast(headElement, element);
41
                    SetPrevious(element, element);
                    SetNext(element, element);
43
                     IncrementSize(headElement);
44
                }
45
                else
46
                {
47
                     AttachBefore(headElement, first, element);
49
            }
50
51
            public void AttachAsLast(TElement headElement, TElement element)
52
                var last = GetLast(headElement);
                if (EqualToZero(last))
55
56
                     AttachAsFirst(headElement, element);
                }
                else
59
                {
60
                     AttachAfter(headElement, last, element);
61
62
            }
64
            public void Detach(TElement headElement, TElement element)
                var elementPrevious = GetPrevious(element);
67
                var elementNext = GetNext(element)
68
                if (AreEqual(elementNext, element))
7.0
                    SetFirst(headElement, Zero);
71
                    SetLast(headElement, Zero);
                }
73
                else
74
75
                    SetNext(elementPrevious, elementNext);
76
                    SetPrevious(elementNext, elementPrevious);
77
                     if (AreEqual(element, GetFirst(headElement)))
                     {
79
                         SetFirst(headElement, elementNext);
80
                     }
81
                        (AreEqual(element, GetLast(headElement)))
82
                     {
83
                         SetLast(headElement, elementPrevious);
84
86
                SetPrevious(element, Zero);
87
                SetNext(element, Zero);
88
                DecrementSize(headElement);
            }
90
        }
91
```

```
#pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
3
   namespace Platform.Collections.Methods.Lists
   {
       public abstract class RelativeDoublyLinkedListMethodsBase<TElement> :
           DoublyLinkedListMethodsBase<TElement>
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected abstract TElement GetFirst(TElement headElement);
10
11
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
12
           protected abstract TElement GetLast(TElement headElement);
13
14
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
15
           protected abstract TElement GetSize(TElement headElement);
16
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
           protected abstract void SetFirst(TElement headElement, TElement element);
19
20
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
           protected abstract void SetLast(TElement headElement, TElement element);
22
23
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
24
           protected abstract void SetSize(TElement headElement, TElement size);
26
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
27
            protected void IncrementSize(TElement headElement) => SetSize(headElement,
            → Increment(GetSize(headElement)));
2.9
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
           protected void DecrementSize(TElement headElement) => SetSize(headElement,
31
            → Decrement(GetSize(headElement)));
32
   }
33
1.8
     ./csharp/Platform.Collections.Methods/Lists/RelativeOpenDoublyLinkedListMethods.cs
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
1
   namespace Platform.Collections.Methods.Lists
3
       public abstract class RelativeOpenDoublyLinkedListMethods<TElement> :
5
           RelativeDoublyLinkedListMethodsBase<TElement>
           public void AttachBefore(TElement headElement, TElement baseElement, TElement newElement)
                var baseElementPrevious = GetPrevious(baseElement);
                SetPrevious(newElement, baseElementPrevious);
10
                SetNext(newElement, baseElement);
11
12
                if (EqualToZero(baseElementPrevious))
                {
13
                    SetFirst(headElement, newElement);
14
                }
15
                else
16
                {
17
                    SetNext(baseElementPrevious, newElement);
18
19
                SetPrevious(baseElement, newElement);
20
                IncrementSize(headElement);
            }
23
           public void AttachAfter(TElement headElement, TElement baseElement, TElement newElement)
24
25
                var baseElementNext = GetNext(baseElement);
26
                SetPrevious(newElement, baseElement);
                SetNext(newElement, baseElementNext);
29
                if (EqualToZero(baseElementNext))
30
                    SetLast(headElement, newElement);
31
                }
32
                else
33
                {
34
                    SetPrevious(baseElementNext, newElement);
35
36
                SetNext(baseElement, newElement);
                IncrementSize(headElement);
38
            }
39
           public void AttachAsFirst(TElement headElement, TElement element)
41
```

```
var first = GetFirst(headElement);
43
                if (EqualToZero(first))
45
                     SetFirst(headElement, element);
46
                    SetLast(headElement, element);
                    SetPrevious(element, Zero);
48
                    SetNext(element, Zero);
49
                     IncrementSize(headElement);
50
                }
                else
52
                {
                     AttachBefore(headElement, first, element);
                }
55
            }
56
57
            public void AttachAsLast(TElement headElement, TElement element)
58
                var last = GetLast(headElement);
60
                if (EqualToZero(last))
61
62
                     AttachAsFirst(headElement, element);
63
                }
64
                else
                {
66
                     AttachAfter(headElement, last, element);
67
68
            }
70
            public void Detach(TElement headElement, TElement element)
72
                var elementPrevious = GetPrevious(element);
73
                var elementNext = GetNext(element);
                if (EqualToZero(elementPrevious))
75
                {
76
                    SetFirst(headElement, elementNext);
                }
                else
79
                    SetNext(elementPrevious, elementNext);
81
82
                if (EqualToZero(elementNext))
83
                    SetLast(headElement, elementPrevious);
85
                }
86
87
                else
                {
88
                    SetPrevious(elementNext, elementPrevious);
90
                SetPrevious(element, Zero);
91
                SetNext(element, Zero);
92
93
                DecrementSize(headElement);
            }
94
        }
95
   }
96
     ./csharp/Platform.Collections.Methods/Trees/RecursionlessSizeBalancedTreeMethods.cs
1.9
   #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
   namespace Platform.Collections.Methods.Trees
4
        public abstract class RecursionlessSizeBalancedTreeMethods<TElement> :
5
            SizedBinaryTreeMethodsBase<TElement>
6
            protected override void AttachCore(ref TElement root, TElement node)
                while (true)
10
                     ref var left = ref GetLeftReference(root);
11
                     var leftSize = GetSizeOrZero(left);
12
                    ref var right = ref GetRightReference(root);
13
                     var rightSize = GetSizeOrZero(right);
14
                     if (FirstIsToTheLeftOfSecond(node, root)) // node.Key less than root.Key
16
                         if (EqualToZero(left))
17
                         {
18
                             IncrementSize(root);
19
                             SetSize(node, One);
20
21
                             left = node;
                             return;
```

```
if (FirstIsToTheLeftOfSecond(node, left)) // node.Key less than left.Key
        if (GreaterThan(Increment(leftSize), rightSize))
            RightRotate(ref root);
        else
        {
            IncrementSize(root);
            root = ref left;
    }
    else
         // node.Key greater than left.Key
        var leftRightSize = GetSizeOrZero(GetRight(left));
        if (GreaterThan(Increment(leftRightSize), rightSize))
            if (EqualToZero(leftRightSize) && EqualToZero(rightSize))
                SetLeft(node, left);
                SetRight(node, root);
                SetSize(node, Add(leftSize, Two)); // Two (2) - node the size of

→ root and a node itself

                SetLeft(root, Zero);
                SetSize(root, One);
                root = node;
                return;
            LeftRotate(ref left);
            RightRotate(ref root);
        }
        else
        {
            IncrementSize(root);
            root = ref left;
    }
else // node.Key greater than root.Key
    if (EqualToZero(right))
    {
        IncrementSize(root);
        SetSize(node, One);
        right = node;
        return;
    if (FirstIsToTheRightOfSecond(node, right)) // node.Key greater than
       right.Key
    {
        if (GreaterThan(Increment(rightSize), leftSize))
        {
            LeftRotate(ref root);
        }
        else
        {
            IncrementSize(root);
            root = ref right;
        }
    }
    else // node.Key less than right.Key
        var rightLeftSize = GetSizeOrZero(GetLeft(right));
        if (GreaterThan(Increment(rightLeftSize), leftSize))
            if (EqualToZero(rightLeftSize) && EqualToZero(leftSize))
                SetLeft(node, root);
                SetRight(node, right);
                SetSize(node, Add(rightSize, Two)); // Two (2) - node the size

→ of root and a node itself

                SetRight(root, Zero);
                SetSize(root, One);
                root = node;
                return;
            RightRotate(ref right);
            LeftRotate(ref root);
```

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```
else
                    IncrementSize(root);
                    root = ref right;
                }
            }
        }
   }
}
protected override void DetachCore(ref TElement root, TElement node)
    while (true)
        ref var left = ref GetLeftReference(root);
        var leftSize = GetSizeOrZero(left);
        ref var right = ref GetRightReference(root);
        var rightSize = GetSizeOrZero(right);
        if (FirstIsToTheLeftOfSecond(node, root)) // node.Key less than root.Key
            var decrementedLeftSize = Decrement(leftSize);
            if (GreaterThan(GetSizeOrZero(GetRightOrDefault(right)),
               decrementedLeftSize))
            {
                LeftRotate(ref root);
            else if (GreaterThan(GetSizeOrZero(GetLeftOrDefault(right)),
                decrementedLeftSize))
            {
                RightRotate(ref right);
                LeftRotate(ref root);
            }
            else
                DecrementSize(root);
                root = ref left;
            }
        else if (FirstIsToTheRightOfSecond(node, root)) // node.Key greater than root.Key
            var decrementedRightSize = Decrement(rightSize);
            if (GreaterThan(GetSizeOrZero(GetLeftOrDefault(left)), decrementedRightSize))
            {
                RightRotate(ref root);
            else if (GreaterThan(GetSizeOrZero(GetRightOrDefault(left)),
                decrementedRightSize))
            {
                LeftRotate(ref left);
                RightRotate(ref root);
            }
            else
                DecrementSize(root);
                root = ref right;
        else // key equals to root.Key
            if (GreaterThanZero(leftSize) && GreaterThanZero(rightSize))
            {
                TElement replacement;
                if (GreaterThan(leftSize, rightSize))
                    replacement = GetRightest(left);
                    DetachCore(ref left, replacement);
                }
                else
                    replacement = GetLeftest(right);
                    DetachCore(ref right, replacement);
                SetLeft(replacement, left);
                SetRight(replacement, right);
                SetSize(replacement, Add(leftSize, rightSize));
                root = replacement;
            }
```

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 $\frac{123}{124}$

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151 152 153

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162

 $\frac{163}{164}$

165

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167 168

169

170

 $171 \\ 172$

```
else if (GreaterThanZero(leftSize))
174
                              root = left;
176
                          }
                          else if (GreaterThanZero(rightSize))
178
                          {
179
                              root = right;
180
                          }
181
                          else
                          {
183
                              root = Zero;
184
185
                         ClearNode(node);
186
                          return;
187
                     }
188
                }
189
            }
        }
191
192
       ./csharp/Platform.Collections.Methods/Trees/SizeBalancedTreeMethods.cs
1.10
    using System;
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
 4
    namespace Platform.Collections.Methods.Trees
 7
        public abstract class SizeBalancedTreeMethods<TElement> :
            SizedBinaryTreeMethodsBase<TElement>
             protected override void AttachCore(ref TElement root, TElement node)
10
                 if (EqualToZero(root))
11
                 {
                     root = node;
13
14
                     IncrementSize(root);
                 }
15
                 else
16
                 {
                     IncrementSize(root);
18
                     if (FirstIsToTheLeftOfSecond(node, root))
19
20
                          AttachCore(ref GetLeftReference(root), node);
21
                         LeftMaintain(ref root);
22
                     }
24
                     else
25
                          AttachCore(ref GetRightReference(root), node);
                          RightMaintain(ref root);
27
28
                 }
             }
30
31
             protected override void DetachCore(ref TElement root, TElement nodeToDetach)
33
                 ref var currentNode = ref root;
                 ref var_parent = ref root;
35
                 var replacementNode = Zero;
36
                 while (!AreEqual(currentNode, nodeToDetach))
37
38
                     DecrementSize(currentNode);
                     if (FirstIsToTheLeftOfSecond(nodeToDetach, currentNode))
40
41
                          parent = ref currentNode;
42
                         currentNode = ref GetLeftReference(currentNode);
43
44
                     else if (FirstIsToTheRightOfSecond(nodeToDetach, currentNode))
46
                         parent = ref currentNode;
                          currentNode = ref GetRightReference(currentNode);
48
                     }
49
                     else
                     {
51
                          throw new InvalidOperationException("Duplicate link found in the tree.");
52
                 }
54
                 var nodeToDetachLeft = GetLeft(nodeToDetach);
55
                 var node = GetRight(nodeToDetach);
56
                 if (!EqualToZero(nodeToDetachLeft) && !EqualToZero(node))
```

```
var leftestNode = GetLeftest(node);
        DetachCore(ref GetRightReference(nodeToDetach), leftestNode);
        SetLeft(leftestNode, nodeToDetachLeft);
        node = GetRight(nodeToDetach);
        if (!EqualToZero(node))
            SetRight(leftestNode, node);
            SetSize(leftestNode, Increment(Add(GetSize(nodeToDetachLeft),

   GetSize(node)));

        }
        else
        {
            SetSize(leftestNode, Increment(GetSize(nodeToDetachLeft)));
        replacementNode = leftestNode;
    }
    else if (!EqualToZero(nodeToDetachLeft))
        replacementNode = nodeToDetachLeft;
    else if (!EqualToZero(node))
    {
        replacementNode = node;
    if (AreEqual(root, nodeToDetach))
    {
        root = replacementNode;
    }
    else if (AreEqual(GetLeft(parent), nodeToDetach))
        SetLeft(parent, replacementNode);
    }
    else if (AreEqual(GetRight(parent), nodeToDetach))
        SetRight(parent, replacementNode);
    ClearNode(nodeToDetach);
}
private void LeftMaintain(ref TElement root)
    if (!EqualToZero(root))
        var rootLeftNode = GetLeft(root);
        if (!EqualToZero(rootLeftNode))
            var rootRightNode = GetRight(root);
            var rootRightNodeSize = GetSize(rootRightNode);
            var rootLeftNodeLeftNode = GetLeft(rootLeftNode);
            if (!EqualToZero(rootLeftNodeLeftNode) &&
                (EqualToZero(rootRightNode)
                    GreaterThan(GetSize(rootLeftNodeLeftNode), rootRightNodeSize)))
            {
                RightRotate(ref root);
            }
            else
                var rootLeftNodeRightNode = GetRight(rootLeftNode);
                if (!EqualToZero(rootLeftNodeRightNode) &&
                     (EqualToZero(rootRightNode) ||
                        GreaterThan(GetSize(rootLeftNodeRightNode), rootRightNodeSize)))
                    LeftRotate(ref GetLeftReference(root));
                    RightRotate(ref root);
                }
                else
                {
                    return;
            LeftMaintain(ref GetLeftReference(root));
            RightMaintain(ref GetRightReference(root));
            LeftMaintain(ref root);
            RightMaintain(ref root);
        }
    }
}
```

5.8

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121

 $\frac{122}{123}$

124 125

126

127

128

130

131

```
133
             private void RightMaintain(ref TElement root)
135
                 if (!EqualToZero(root))
136
                     var rootRightNode = GetRight(root);
138
                     if (!EqualToZero(rootRightNode))
139
140
                          var rootLeftNode = GetLeft(root);
                         var rootLeftNodeSize = GetSize(rootLeftNode);
142
                          var rootRightNodeRightNode = GetRight(rootRightNode);
143
                          if (!EqualToZero(rootRightNodeRightNode) &&
144
                              (EqualToZero(rootLeftNode) | |
                                 GreaterThan(GetSize(rootRightNodeRightNode), rootLeftNodeSize)))
                          {
146
                              LeftRotate(ref root);
147
                          }
148
                          else
149
                          {
150
                              var rootRightNodeLeftNode = GetLeft(rootRightNode);
                              if (!EqualToZero(rootRightNodeLeftNode) &&
152
                                  (EqualToZero(rootLeftNode)
153
                                      GreaterThan(GetSize(rootRightNodeLeftNode), rootLeftNodeSize)))
                                  RightRotate(ref GetRightReference(root));
155
                                  LeftRotate(ref root);
156
                              }
157
                              else
158
                              {
159
                                  return;
160
                              }
161
162
                         LeftMaintain(ref GetLeftReference(root));
                         RightMaintain(ref GetRightReference(root));
164
                          LeftMaintain(ref root);
165
                          RightMaintain(ref root);
                     }
167
                }
168
            }
169
        }
170
171
1.11
       ./csharp/Platform.Collections.Methods/Trees/SizedAndThreadedAVLBalancedTreeMethods.cs
    using System;
    using System. Runtime. Compiler Services;
    using System.Text;
#if USEARRAYPOOL
    using Platform.Collections;
    #endif
    using Platform.Reflection;
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
10
    namespace Platform.Collections.Methods.Trees
11
12
        /// <summary>
13
        /// Combination of Size, Height (AVL), and threads.
14
        /// </summary>
15
        /// <remarks>
        /// Based on: <a href="https://github.com/programmatom/TreeLib/blob/master/TreeLib/TreeLib/G<sub>|</sub>
17
            enerated/AVLTreeList.cs">TreeLib.AVLTreeList</a>.
        /// Which itself based on: <a
18
            href="https://github.com/GNOME/glib/blob/master/glib/gtree.c">GNOME/glib/gtree</a>.
            </remarks>
19
        public abstract class SizedAndThreadedAVLBalancedTreeMethods<TElement> :
20
            SizedBinaryTreeMethodsBase<TElement>
21
            private static readonly int _maxPath = 11 * NumericType<TElement>.BytesSize + 4;
22
23
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
24
            protected override TElement GetRightest(TElement current)
25
                 var currentRight = GetRightOrDefault(current);
27
                 while (!EqualToZero(currentRight))
28
                     current = currentRight;
30
                     currentRight = GetRightOrDefault(current);
31
                 return current;
```

```
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected override TElement GetLeftest(TElement current)
    var currentLeft = GetLeftOrDefault(current);
    while (!EqualToZero(currentLeft))
        current = currentLeft;
        currentLeft = GetLeftOrDefault(current);
    return current;
}
public override bool Contains(TElement node, TElement root)
    while (!EqualToZero(root))
        if (FirstIsToTheLeftOfSecond(node, root)) // node.Key < root.Key</pre>
            root = GetLeftOrDefault(root);
        else if (FirstIsToTheRightOfSecond(node, root)) // node.Key > root.Key
            root = GetRightOrDefault(root);
        }
        else // node.Key == root.Key
            return true;
    return false;
}
protected override void PrintNode(TElement node, StringBuilder sb, int level)
    base.PrintNode(node, sb, level);
    sb.Append(' ');
    sb.Append(GetLeftIsChild(node) ? 'l' : 'L');
    sb.Append(GetRightIsChild(node) ? 'r' : 'R');
    sb.Append(' ')
    sb.Append(GetBalance(node));
}
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected void IncrementBalance(TElement node) => SetBalance(node,
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected void DecrementBalance(TElement node) => SetBalance(node,
   (sbyte)(GetBalance(node) - 1));
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected override TElement GetLeftOrDefault(TElement node) => GetLeftIsChild(node) ?

   GetLeft(node) : default;

[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected override TElement GetRightOrDefault(TElement node) => GetRightIsChild(node) ?

   GetRight(node) : default;

[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected abstract bool GetLeftIsChild(TElement node);
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected abstract void SetLeftIsChild(TElement node, bool value);
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected abstract bool GetRightIsChild(TElement node);
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected abstract void SetRightIsChild(TElement node, bool value);
[MethodImpl(MethodImplOptions.AggressiveInlining)]
protected abstract sbyte GetBalance(TElement node);
[{\tt MethodImpl}({\tt MethodImpl}{\tt Options.AggressiveInlining}) \, \rfloor \,
protected abstract void SetBalance(TElement node, sbyte value);
protected override void AttachCore(ref TElement root, TElement node)
```

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100 101

102

103 104

105

106 107

```
109
                 unchecked
110
111
                      // TODO: Check what is faster to use simple array or array from array pool
                     // TODO: Try to use stackalloc as an optimization (requires code generation,
113

→ because of generics)

    #if USEARRAYPOOL
114
                     var path = ArrayPool.Allocate<TElement>(MaxPath);
115
                     var pathPosition = 0;
116
                     path[pathPosition++] = default;
117
    #else
118
                     var path = new TElement[_maxPath];
119
                     var pathPosition = 1;
120
    #endif
                     var currentNode = root;
122
                     while (true)
124
                          if (FirstIsToTheLeftOfSecond(node, currentNode))
125
126
                              if (GetLeftIsChild(currentNode))
127
128
                                  IncrementSize(currentNode);
129
                                  path[pathPosition++] = currentNode;
                                  currentNode = GetLeft(currentNode);
131
                              }
132
                              else
133
134
                                   // Threads
135
                                  SetLeft(node, GetLeft(currentNode));
137
                                  SetRight(node, currentNode);
                                  SetLeft(currentNode, node);
138
                                  SetLeftIsChild(currentNode, true);
                                  DecrementBalance(currentNode);
140
                                  SetSize(node, One);
141
                                  FixSize(currentNode); // Should be incremented already
142
143
                                  break;
                              }
144
                          else if (FirstIsToTheRightOfSecond(node, currentNode))
146
147
                              if (GetRightIsChild(currentNode))
148
149
                                  IncrementSize(currentNode);
150
                                  path[pathPosition++] = currentNode;
151
                                  currentNode = GetRight(currentNode);
154
                              else
155
                                  // Threads
156
                                  SetRight(node, GetRight(currentNode));
157
                                  SetLeft(node, currentNode);
159
                                  SetRight(currentNode, node);
                                  SetRightIsChild(currentNode, true);
160
                                   IncrementBalance(currentNode);
161
                                  SetSize(node, One);
                                  FixSize(currentNode); // Should be incremented already
163
                              }
165
                          }
166
                          else
167
                          {
168
                              throw new InvalidOperationException("Node with the same key already
169
                               → attached to a tree.");
                          }
170
171
                     // Restore balance. This is the goodness of a non-recursive
172
                        implementation, when we are done with balancing we 'break'
173
                     // the loop and we are done.
174
                     while (true)
175
176
                          var parent = path[--pathPosition];
                         var isLeftNode = !AreEqual(parent, default) && AreEqual(currentNode,
178

   GetLeft(parent));
                          var currentNodeBalance = GetBalance(currentNode);
179
                          if (currentNodeBalance < -1 || currentNodeBalance > 1)
180
                              currentNode = Balance(currentNode);
182
                              if (AreEqual(parent, default))
183
```

```
{
184
                                    root = currentNode;
185
                                }
186
                                else if (isLeftNode)
188
                                     SetLeft(parent, currentNode);
189
                                     FixSize(parent);
190
                                }
191
                                else
192
                                {
                                     SetRight(parent, currentNode);
194
                                    FixSize(parent);
195
196
                                }
                           }
197
                           currentNodeBalance = GetBalance(currentNode);
198
                           if (currentNodeBalance == 0 || AreEqual(parent, default))
199
                                break:
201
                           if (isLeftNode)
203
                            {
204
                                DecrementBalance(parent);
205
                           }
                           else
207
208
                            {
                                IncrementBalance(parent);
209
                           }
210
211
                           currentNode = parent;
212
    #if USEARRAYPOOL
213
                       ArrayPool.Free(path);
214
215
    #endif
                  }
216
              }
217
218
              private TElement Balance(TElement node)
219
220
221
                  unchecked
                  {
222
                       var rootBalance = GetBalance(node);
223
                       if (rootBalance < -1)</pre>
224
225
                           var left = GetLeft(node);
226
                           if (GetBalance(left) > 0)
227
228
                                SetLeft(node, LeftRotateWithBalance(left));
229
230
                                FixSize(node);
                           }
231
                           node = RightRotateWithBalance(node);
232
233
                       else if (rootBalance > 1)
235
                           var right = GetRight(node);
236
                           if (GetBalance(right) < 0)</pre>
237
238
                                SetRight(node, RightRotateWithBalance(right));
239
240
                                FixSize(node);
                           node = LeftRotateWithBalance(node);
242
243
^{244}
                       return node;
                  }
245
             }
246
247
             protected TElement LeftRotateWithBalance(TElement node)
248
249
                  unchecked
250
                  {
                       var right = GetRight(node);
252
                       if (GetLeftIsChild(right))
253
                       {
254
                           SetRight(node, GetLeft(right));
255
                       }
256
257
                       else
258
                           SetRightIsChild(node, false);
259
                           SetLeftIsChild(right, true);
260
261
                       SetLeft(right, node);
262
```

```
// Fix size
        SetSize(right, GetSize(node));
        FixSize(node);
        // Fix balance
        var rootBalance = GetBalance(node);
        var rightBalance = GetBalance(right);
        if (rightBalance <= 0)</pre>
            if (rootBalance >= 1)
            {
                 SetBalance(right, (sbyte)(rightBalance - 1));
            }
            else
            {
                 SetBalance(right, (sbyte)(rootBalance + rightBalance - 2));
            SetBalance(node, (sbyte)(rootBalance - 1));
        else
            if (rootBalance <= rightBalance)</pre>
            {
                 SetBalance(right, (sbyte)(rootBalance - 2));
            else
            {
                 SetBalance(right, (sbyte)(rightBalance - 1));
            SetBalance(node, (sbyte)(rootBalance - rightBalance - 1));
        return right;
    }
}
protected TElement RightRotateWithBalance(TElement node)
    unchecked
        var left = GetLeft(node);
        if (GetRightIsChild(left))
            SetLeft(node, GetRight(left));
        }
        else
            SetLeftIsChild(node, false);
            SetRightIsChild(left, true);
        SetRight(left, node);
        // Fix size
        SetSize(left, GetSize(node));
        FixSize(node);
        // Fix balance
        var rootBalance = GetBalance(node);
        var leftBalance = GetBalance(left);
        if (leftBalance <= 0)</pre>
            if (leftBalance > rootBalance)
            {
                 SetBalance(left, (sbyte)(leftBalance + 1));
            }
            else
            {
                 SetBalance(left, (sbyte)(rootBalance + 2));
            SetBalance(node, (sbyte)(rootBalance - leftBalance + 1));
        else
            if (rootBalance <= -1)</pre>
            {
                 SetBalance(left, (sbyte)(leftBalance + 1));
            }
            else
            {
                 SetBalance(left, (sbyte)(rootBalance + leftBalance + 2));
            SetBalance(node, (sbyte)(rootBalance + 1));
```

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 $\frac{275}{276}$

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 $\frac{326}{327}$

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337

```
return left;
                }
            }
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected override TElement GetNext(TElement node)
                var current = GetRight(node);
                if (GetRightIsChild(node))
                    return GetLeftest(current);
                return current;
354
            }
356
            [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected override TElement GetPrevious(TElement node)
                var current = GetLeft(node);
                if (GetLeftIsChild(node))
                {
                    return GetRightest(current);
                return current;
            }
            protected override void DetachCore(ref TElement root, TElement node)
                unchecked
    #if USEARRAYPOOL
                     var path = ArrayPool.Allocate<TElement>(MaxPath);
                     var pathPosition = 0;
374
                    path[pathPosition++] = default;
    #else
                     var path = new TElement[_maxPath];
                     var pathPosition = 1;
    #endif
379
                     var currentNode = root;
380
                    while (true)
                         if (FirstIsToTheLeftOfSecond(node, currentNode))
                             if (!GetLeftIsChild(currentNode))
385
                             {
                                 throw new InvalidOperationException("Cannot find a node.");
                             DecrementSize(currentNode);
                             path[pathPosition++] = currentNode;
                             currentNode = GetLeft(currentNode);
                         else if (FirstIsToTheRightOfSecond(node, currentNode))
394
                             if (!GetRightIsChild(currentNode))
                             {
                                 throw new InvalidOperationException("Cannot find a node.");
                             DecrementSize(currentNode);
                             path[pathPosition++] = currentNode;
                             currentNode = GetRight(currentNode);
                         else
                         {
                             break;
                         }
                     var parent = path[--pathPosition];
                     var balanceNode = parent;
                     var isLeftNode = !AreEqual(parent, default) && AreEqual(currentNode,
410
                        GetLeft(parent));
                     if (!GetLeftIsChild(currentNode))
                         if (!GetRightIsChild(currentNode)) // node has no children
                             if (AreEqual(parent, default))
                             {
                                 root = Zero;
                             }
```

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```
else if (isLeftNode)
            SetLeftIsChild(parent, false);
            SetLeft(parent, GetLeft(currentNode));
            IncrementBalance(parent);
        else
            SetRightIsChild(parent, false);
            SetRight(parent, GetRight(currentNode));
            DecrementBalance(parent);
    }
    else // node has a right child
        var successor = GetNext(currentNode);
        SetLeft(successor, GetLeft(currentNode));
        var right = GetRight(currentNode);
        if (AreEqual(parent, default))
            root = right;
        else if (isLeftNode)
            SetLeft(parent, right);
            IncrementBalance(parent);
        }
        else
        {
            SetRight(parent, right);
            DecrementBalance(parent);
    }
else // node has a left child
       (!GetRightIsChild(currentNode))
        var predecessor = GetPrevious(currentNode)
        SetRight(predecessor, GetRight(currentNode));
        var leftValue = GetLeft(currentNode);
        if (AreEqual(parent, default))
            root = leftValue;
        else if (isLeftNode)
            SetLeft(parent, leftValue);
            IncrementBalance(parent);
        }
        else
            SetRight(parent, leftValue);
            DecrementBalance(parent);
    else // node has a both children (left and right)
        var predecessor = GetLeft(currentNode);
        var successor = GetRight(currentNode);
        var successorParent = currentNode;
        int previousPathPosition = ++pathPosition;
        // find the immediately next node (and its parent)
        while (GetLeftIsChild(successor))
            path[++pathPosition] = successorParent = successor;
            successor = GetLeft(successor);
            if (!AreEqual(successorParent, currentNode))
            {
                DecrementSize(successorParent);
        path[previousPathPosition] = successor;
        balanceNode = path[pathPosition];
        // remove 'successor' from the tree
        if (!AreEqual(successorParent, currentNode))
            if (!GetRightIsChild(successor))
```

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494 495

```
{
                SetLeftIsChild(successorParent, false);
            }
            else
            {
                SetLeft(successorParent, GetRight(successor));
            IncrementBalance(successorParent);
            SetRightIsChild(successor, true);
            SetRight(successor, GetRight(currentNode));
        else
        {
            DecrementBalance(currentNode);
        // set the predecessor's successor link to point to the right place
        while (GetRightIsChild(predecessor))
            predecessor = GetRight(predecessor);
        SetRight(predecessor, successor);
        // prepare 'successor' to replace 'node'
        var left = GetLeft(currentNode);
        SetLeftIsChild(successor, true);
        SetLeft(successor, left);
        SetBalance(successor, GetBalance(currentNode));
        FixSize(successor);
        if (AreEqual(parent, default))
        {
            root = successor;
        }
        else if (isLeftNode)
            SetLeft(parent, successor);
        }
        else
        {
            SetRight(parent, successor);
    }
// restore balance
if (!AreEqual(balanceNode, default))
    while (true)
        var balanceParent = path[--pathPosition];
        isLeftNode = !AreEqual(balanceParent, default) && AreEqual(balanceNode,

   GetLeft(balanceParent));
        var currentNodeBalance = GetBalance(balanceNode);
        if (currentNodeBalance < -1 || currentNodeBalance > 1)
            balanceNode = Balance(balanceNode);
            if (AreEqual(balanceParent, default))
            {
                root = balanceNode;
            }
            else if (isLeftNode)
                SetLeft(balanceParent, balanceNode);
            }
            else
            {
                SetRight(balanceParent, balanceNode);
        currentNodeBalance = GetBalance(balanceNode);
        if (currentNodeBalance != 0 || AreEqual(balanceParent, default))
            break;
        if (isLeftNode)
            IncrementBalance(balanceParent);
        }
        else
            DecrementBalance(balanceParent);
```

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```
574
                              balanceNode = balanceParent;
575
576
                     ClearNode(node);
578
    #if USEARRAYPOOL
579
                     ArrayPool.Free(path);
580
    #endif
581
                 }
             }
583
584
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
585
            protected override void ClearNode(TElement node)
586
587
                 SetLeft(node, Zero);
588
                 SetRight(node, Zero);
SetSize(node, Zero);
589
590
                 SetLeftIsChild(node, false);
591
                 SetRightIsChild(node, false);
592
                 SetBalance(node, 0);
593
             }
594
        }
595
596
1.12
       ./csharp/Platform.Collections.Methods/Trees/SizedBinaryTreeMethodsBase.cs
    //#define ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
 2
    using System;
    using System Diagnostics;
 4
    using System.Runtime.CompilerServices;
    using System.Text;
    using Platform. Numbers;
    #pragma warning disable CS1591 // Missing XML comment for publicly visible type or member
10
    namespace Platform.Collections.Methods.Trees
11
12
        public abstract class SizedBinaryTreeMethodsBase<TElement> :
13
            GenericCollectionMethodsBase<TElement>
14
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
15
            protected abstract ref TElement GetLeftReference(TElement node);
16
17
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
18
            protected abstract ref TElement GetRightReference(TElement node);
19
20
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
21
            protected abstract TElement GetLeft(TElement node);
22
23
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected abstract TElement GetRight(TElement node);
25
26
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
27
            protected abstract TElement GetSize(TElement node);
2.8
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
30
            protected abstract void SetLeft(TElement node, TElement left);
31
32
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
33
            protected abstract void SetRight(TElement node, TElement right);
34
35
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
36
            protected abstract void SetSize(TElement node, TElement size);
38
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
39
            protected abstract bool FirstIsToTheLeftOfSecond(TElement first, TElement second);
41
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
42
            protected abstract bool FirstIsToTheRightOfSecond(TElement first, TElement second);
43
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual TElement GetLeftOrDefault(TElement node) => AreEqual(node, default) ?
46
                default : GetLeft(node);
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual TElement GetRightOrDefault(TElement node) => AreEqual(node, default) ?
49
                default : GetRight(node);
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
51
            protected void IncrementSize(TElement node) => SetSize(node, Increment(GetSize(node)));
```

```
5.3
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected void DecrementSize(TElement node) => SetSize(node, Decrement(GetSize(node)));
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
57
            protected TElement GetLeftSize(TElement node) => GetSizeOrZero(GetLeftOrDefault(node));
58
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
60
            protected TElement GetRightSize(TElement node) => GetSizeOrZero(GetRightOrDefault(node));
61
62
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
63
            protected TElement GetSizeOrZero(TElement node) => EqualToZero(node) ? Zero :
64
                GetSize(node);
65
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
66
            protected void FixSize(TElement node) => SetSize(node, Increment(Add(GetLeftSize(node),

   GetRightSize(node))));
68
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
69
             protected void LeftRotate(ref TElement root) => root = LeftRotate(root);
70
71
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             protected TElement LeftRotate(TElement root)
73
74
                 var right = GetRight(root)
75
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
76
                 if (EqualToZero(right))
77
                 {
                     throw new InvalidOperationException("Right is null.");
79
                 }
80
    #endif
81
                 SetRight(root, GetLeft(right));
82
                 SetLeft(right, root);
83
                 SetSize(right, GetSize(root));
                 FixSize(root);
85
                 return right;
             }
87
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
89
             protected void RightRotate(ref TElement root) => root = RightRotate(root);
90
91
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
92
            protected TElement RightRotate(TElement root)
93
    var left = GetLeft(root);
#if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
95
96
                 if (EqualToZero(left))
97
                 {
98
                     throw new InvalidOperationException("Left is null.");
99
                 }
100
    #endif
101
                 SetLeft(root, GetRight(left));
                 SetRight(left, root);
103
                 SetSize(left, GetSize(root));
104
                 FixSize(root);
105
                 return left;
106
             }
107
108
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
109
            protected virtual TElement GetRightest(TElement current)
110
111
                 var currentRight = GetRight(current);
112
                 while (!EqualToZero(currentRight))
113
114
                     current = currentRight;
115
                     currentRight = GetRight(current);
117
118
                 return current;
             }
119
120
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
            protected virtual TElement GetLeftest(TElement current)
122
123
124
                 var currentLeft = GetLeft(current);
125
                 while (!EqualToZero(currentLeft))
126
                     current = currentLeft;
127
                     currentLeft = GetLeft(current);
128
                 }
129
```

```
return current;
130
             }
132
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
134
             protected virtual TElement GetNext(TElement node) => GetLeftest(GetRight(node));
135
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
136
             protected virtual TElement GetPrevious(TElement node) => GetRightest(GetLeft(node));
137
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
139
             public virtual bool Contains(TElement node, TElement root)
140
141
142
                 while (!EqualToZero(root))
143
                        (FirstIsToTheLeftOfSecond(node, root)) // node.Key < root.Key
144
145
                          root = GetLeft(root);
146
147
                     else if (FirstIsToTheRightOfSecond(node, root)) // node.Key > root.Key
148
149
                          root = GetRight(root);
150
                     }
151
                     else // node.Key == root.Key
                     {
153
154
                          return true;
155
                 }
156
                 return false;
157
158
159
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
160
             protected virtual void ClearNode(TElement node)
161
162
                 SetLeft(node, Zero)
163
                 SetRight(node, Zero);
SetSize(node, Zero);
164
165
             }
167
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
169
             public void Attach(ref TElement root, TElement node)
170
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
171
                 ValidateSizes(root);
172
                 Debug.WriteLine("--BeforeAttach--");
173
                 Debug.WriteLine(PrintNodes(root));
174
                 Debug.WriteLine("----");
175
                 var sizeBefore = GetSize(root);
176
    #endif
177
                 if (EqualToZero(root))
178
179
                     SetSize(node, One);
                     root = node;
181
182
                     return:
183
                 AttachCore(ref root, node);
184
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
185
                 Debug.WriteLine("--AfterAttach--");
186
                 Debug.WriteLine(PrintNodes(root));
                 Debug.WriteLine("-----");
188
                 ValidateSizes(root);
189
                 var sizeAfter = GetSize(root);
190
                 if (!AreEqual(Arithmetic.Increment(sizeBefore), sizeAfter))
191
192
                     throw new InvalidOperationException("Tree was broken after attach.");
193
                 }
194
    #endif
195
             }
196
197
             protected abstract void AttachCore(ref TElement root, TElement node);
198
199
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
200
             public void Detach(ref TElement root, TElement node)
201
202
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
203
204
                 ValidateSizes(root);
                 Debug.WriteLine("--BeforeDetach--");
205
                 Debug.WriteLine(PrintNodes(root));
206
                 Debug.WriteLine("----");
207
                 var sizeBefore = GetSize(root);
208
```

```
if (EqualToZero(root))
209
                      throw new InvalidOperationException($"Элемент с {node} не содержится в
211
                      → дереве.");
212
    #endif
213
                 DetachCore(ref root, node)
214
    #if ENABLE_TREE_AUTO_DEBUG_AND_VALIDATION
215
                 Debug.WriteLine("--AfterDetach--");
                 Debug.WriteLine(PrintNodes(root));
217
                 Debug.WriteLine("----");
218
                 ValidateSizes(root);
219
                 var sizeAfter = GetSize(root);
220
                 if (!AreEqual(Arithmetic.Decrement(sizeBefore), sizeAfter))
221
222
                      throw new InvalidOperationException("Tree was broken after detach.");
223
                 }
224
    #endif
225
226
227
             protected abstract void DetachCore(ref TElement root, TElement node);
228
229
             public void FixSizes(TElement node)
231
                 if (AreEqual(node, default))
232
233
                     return;
234
235
                 FixSizes(GetLeft(node));
                 FixSizes(GetRight(node));
237
                 FixSize(node);
238
             }
239
240
             public void ValidateSizes(TElement node)
241
242
                 if (AreEqual(node, default))
243
244
245
                     return;
                 }
246
                 var size = GetSize(node);
248
                 var leftSize = GetLeftSize(node)
                 var rightSize = GetRightSize(node);
249
                 var expectedSize = Arithmetic.Increment(Arithmetic.Add(leftSize, rightSize));
250
                 if (!AreEqual(size, expectedSize))
251
252
                     throw new InvalidOperationException($\sigma"Size of \{node\} is not valid. Expected
253

    size: {expectedSize}, actual size: {size}.");
254
                 ValidateSizes(GetLeft(node));
                 ValidateSizes(GetRight(node));
256
             }
257
258
             public void ValidateSize(TElement node)
259
260
                 var size = GetSize(node);
                 var leftSize = GetLeftSize(node);
262
                 var rightSize = GetRightSize(node);
263
                 var expectedSize = Arithmetic.Increment(Arithmetic.Add(leftSize, rightSize));
264
                 if (!AreEqual(size, expectedSize))
266
                     throw new InvalidOperationException($\sigmu$"Size of \{node\} is not valid. Expected
267

    size: {expectedSize}, actual size: {size}.");
                 }
268
             }
270
             public string PrintNodes(TElement node)
271
272
                 var sb = new StringBuilder();
273
                 PrintNodes(node, sb);
274
275
                 return sb.ToString();
276
277
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
             public void PrintNodes(TElement node, StringBuilder sb) => PrintNodes(node, sb, 0);
279
             public void PrintNodes(TElement node, StringBuilder sb, int level)
281
282
                 if (AreEqual(node, default))
```

```
{
284
285
                      return;
                  }
286
                 PrintNodes(GetLeft(node), sb, level + 1);
                 PrintNode(node, sb, level);
288
                  sb.AppendLine()
289
                 PrintNodes(GetRight(node), sb, level + 1);
290
             }
291
292
             public string PrintNode(TElement node)
294
                  var sb = new StringBuilder();
295
                 PrintNode(node, sb)
296
297
                  return sb.ToString();
298
             [MethodImpl(MethodImplOptions.AggressiveInlining)]
300
             protected void PrintNode(TElement node, StringBuilder sb) => PrintNode(node, sb, 0);
301
302
             protected virtual void PrintNode(TElement node, StringBuilder sb, int level)
303
304
                  sb.Append('\t', level);
                  sb.Append(node);
306
                  PrintNodeValue(node, sb);
307
                  sb.Append(' ');
308
                  sb.Append('s');
309
                  sb.Append(GetSize(node));
310
             }
311
312
             protected abstract void PrintNodeValue(TElement node, StringBuilder sb);
313
         }
314
    }
315
1.13
       ./csharp/Platform.Collections.Methods.Tests/RecursionlessSizeBalancedTree.cs
    using System;
    using System.Collections.Generic;
    using System. Text;
    using Platform Numbers;
    using Platform.Collections.Methods.Trees;
 5
    using Platform.Converters;
    namespace Platform.Collections.Methods.Tests
 8
 9
         public class RecursionlessSizeBalancedTree<TElement> :
10
             RecursionlessSizeBalancedTreeMethods<TElement>
11
             private struct TreeElement
12
13
                 public TElement Size;
public TElement Left;
14
15
                 public TElement Right;
16
             }
17
18
             private readonly TreeElement[] _elements;
private TElement _allocated;
19
20
             public TElement Root;
22
23
             public TElement Count => GetSizeOrZero(Root);
24
             public RecursionlessSizeBalancedTree(int capacity) => (_elements, _allocated) = (new
26
                TreeElement[capacity], One);
27
             public TElement Allocate()
29
                  var newNode = _allocated;
                  if (IsEmpty(newNode))
31
32
                      _allocated = Arithmetic.Increment(_allocated);
33
                      return newNode;
34
                  }
                  else
36
                  {
37
                      throw new InvalidOperationException("Allocated tree element is not empty.");
                  }
39
             }
40
41
             public void Free(TElement node)
42
43
                  while (!EqualityComparer.Equals(_allocated, One) && IsEmpty(node))
```

```
45
                     var lastNode = Arithmetic.Decrement(_allocated);
46
                     if (EqualityComparer.Equals(lastNode, node))
47
48
                         _allocated = lastNode;
49
                         node = Arithmetic.Decrement(node):
50
51
                     else
52
                     {
53
                         return;
54
                     }
55
                }
56
            }
57
5.8
            public bool IsEmpty(TElement node) =>

→ EqualityComparer<TreeElement>.Default.Equals(GetElement(node), default);

60
            protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>

→ Comparer.Compare(first, second) < 0;
</p>
62
            protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>
63

→ Comparer.Compare(first, second) > 0;

64
            protected override ref TElement GetLeftReference(TElement node) => ref
65

    GetElement(node).Left;

            protected override TElement GetLeft(TElement node) => GetElement(node).Left;
67
            protected override ref TElement GetRightReference(TElement node) => ref
69

   GetElement(node).Right;
70
            protected override TElement GetRight(TElement node) => GetElement(node).Right;
71
72
            protected override TElement GetSize(TElement node) => GetElement(node).Size;
73
74
            protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
             \rightarrow sb.Append(node);
76
            protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
77
             → left;
            protected override void SetRight(TElement node, TElement right) =>

    GetElement(node).Right = right;

80
            protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =
81

    size;

82
            private ref TreeElement GetElement(TElement node) => ref
83
             -- _elements[UncheckedConverter<TElement, long>.Default.Convert(node)];
        }
84
   }
85
      ./csharp/Platform.Collections.Methods.Tests/SizeBalancedTree.cs
1.14
   using System;
   using System.Collections.Generic;
   using System.Text;
using Platform.Numbers;
3
   using Platform.Collections.Methods.Trees;
   using Platform.Converters;
   namespace Platform.Collections.Methods.Tests
   {
        public class SizeBalancedTree<TElement> : SizeBalancedTreeMethods<TElement>
1.0
11
            private struct TreeElement
12
13
                public TElement Size;
public TElement Left;
14
15
                public TElement Right;
16
17
18
            private readonly TreeElement[] _elements;
private TElement _allocated;
19
20
            public TElement Root;
22
23
            public TElement Count => GetSizeOrZero(Root);
24
            public SizeBalancedTree(int capacity) => (_elements, _allocated) = (new
             → TreeElement[capacity], One);
```

```
public TElement Allocate()
29
                var newNode = _allocated;
                if (IsEmpty(newNode))
31
32
                    _allocated = Arithmetic.Increment(_allocated);
33
                    return newNode;
34
                }
35
                else
36
                {
37
                    throw new InvalidOperationException("Allocated tree element is not empty.");
38
                }
39
           }
40
41
           public void Free(TElement node)
42
43
                while (!EqualityComparer.Equals(_allocated, One) && IsEmpty(node))
44
45
                    var lastNode = Arithmetic.Decrement(_allocated);
46
                    if (EqualityComparer.Equals(lastNode, node))
47
                        _allocated = lastNode;
49
                        node = Arithmetic.Decrement(node);
                    }
51
                    else
                    {
                        return;
54
                    }
                }
56
           }
57
           public bool IsEmpty(TElement node) =>
59
            Gefault.Equals(GetElement(node), default);
           protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
61
            → Comparer.Compare(first, second) < 0;</p>
           protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>
63

→ Comparer.Compare(first, second) > 0;

64
           protected override ref TElement GetLeftReference(TElement node) => ref

→ GetElement(node).Left;

66
           protected override TElement GetLeft(TElement node) => GetElement(node).Left;
68
           protected override ref TElement GetRightReference(TElement node) => ref
69

   GetElement(node).Right;

70
           protected override TElement GetRight(TElement node) => GetElement(node).Right;
71
72
           protected override TElement GetSize(TElement node) => GetElement(node).Size;
73
74
           protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
75

    sb.Append(node);
           protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
77
            → left;
           protected override void SetRight(TElement node, TElement right) =>
79

    GetElement(node).Right = right;

           protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =
81

→ size;

           private ref TreeElement GetElement(TElement node) => ref
83
            - _ elements[UncheckedConverter<TElement, long>.Default.Convert(node)];
       }
84
   }
      ./csharp/Platform.Collections.Methods.Tests/SizedAndThreadedAVLBalancedTree.cs
1.15
   using System;
   using System Collections Generic;
   using System. Text;
   using Platform. Numbers:
4
   using Platform.Collections.Methods.Trees;
   using Platform.Converters;
   namespace Platform.Collections.Methods.Tests
```

```
{
   public class SizedAndThreadedAVLBalancedTree<TElement> :
       SizedAndThreadedAVLBalancedTreeMethods<TElement>
       private struct TreeElement
           public TElement Size;
           public TElement Left;
           public TElement Right;
           public sbyte Balance;
           public bool LeftIsChild
           public bool RightIsChild;
       private readonly TreeElement[] _elements;
       private TElement _allocated;
       public TElement Root;
       public TElement Count => GetSizeOrZero(Root);
       public SizedAndThreadedAVLBalancedTree(int capacity) => (_elements, _allocated) = (new
        → TreeElement[capacity], One);
       public TElement Allocate()
           var newNode = _allocated;
           if (IsEmpty(newNode))
               _allocated = Arithmetic.Increment(_allocated);
               return newNode;
           }
           else
           {
               throw new InvalidOperationException("Allocated tree element is not empty.");
           }
       }
       public void Free(TElement node)
           while (!EqualityComparer.Equals(_allocated, One) && IsEmpty(node))
               var lastNode = Arithmetic.Decrement(_allocated);
               if (EqualityComparer.Equals(lastNode, node))
                   _allocated = lastNode;
                   node = Arithmetic.Decrement(node);
               }
               else
               {
                   return;
               }
           }
       }
       public bool IsEmpty(TElement node) =>
        protected override bool FirstIsToTheLeftOfSecond(TElement first, TElement second) =>
        → Comparer.Compare(first, second) < 0;</p>
       protected override bool FirstIsToTheRightOfSecond(TElement first, TElement second) =>

→ Comparer.Compare(first, second) > 0;

       protected override sbyte GetBalance(TElement node) => GetElement(node).Balance;
       protected override bool GetLeftIsChild(TElement node) => GetElement(node).LeftIsChild;
       protected override ref TElement GetLeftReference(TElement node) => ref

→ GetElement(node).Left;

       protected override TElement GetLeft(TElement node) => GetElement(node).Left;
       protected override bool GetRightIsChild(TElement node) => GetElement(node).RightIsChild;
       protected override ref TElement GetRightReference(TElement node) => ref

   GetElement(node).Right;

       protected override TElement GetRight(TElement node) => GetElement(node).Right;
```

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70 71

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75

76 77

78

79

```
protected override TElement GetSize(TElement node) => GetElement(node).Size;
83
            protected override void PrintNodeValue(TElement node, StringBuilder sb) =>
84

⇒ sb.Append(node);

            protected override void SetBalance(TElement node, sbyte value) =>
86

    GetElement(node).Balance = value;

            protected override void SetLeft(TElement node, TElement left) => GetElement(node).Left =
            → left:
            protected override void SetLeftIsChild(TElement node, bool value) =>
90

→ GetElement(node).LeftIsChild = value;
            protected override void SetRight(TElement node, TElement right) =>

   GetElement(node).Right = right;
            protected override void SetRightIsChild(TElement node, bool value) =>

    GetElement(node).RightIsChild = value;

95
            protected override void SetSize(TElement node, TElement size) => GetElement(node).Size =

→ size;

            private ref TreeElement GetElement(TElement node) => ref
98
            _ _ elements[UncheckedConverter<TElement, long>.Default.Convert(node)];
        }
99
100
      /csharp/Platform.Collections.Methods.Tests/TestExtensions.cs
1.16
   using System;
   using
         System.Collections.Generic;
   using Xunit;
   using Platform.Collections.Methods.Trees;
   using Platform.Converters;
   namespace Platform.Collections.Methods.Tests
        public static class TestExtensions
9
10
            public static void TestMultipleCreationsAndDeletions<TElement>(this
                SizedBinaryTreeMethodsBase<TElement> tree, Func<TElement> allocate, Action<TElement>
                free, ref TElement root, Func<TElement> treeCount, int maximumOperationsPerCycle)
12
                for (var N = 1; N < maximumOperationsPerCycle; N++)</pre>
13
14
                     var currentCount = 0;
15
                    for (var i = 0; i < N; i++)</pre>
16
17
                         var node = allocate();
18
                        tree.Attach(ref root, node);
                         currentCount++;
20
                         Assert.Equal(currentCount, (int)UncheckedConverter<TElement,
                         → int>.Default.Convert(treeCount()));
22
                    for (var i = 1; i <= N; i++)</pre>
23
                        TElement node = UncheckedConverter<int, TElement>.Default.Convert(i);
                         if (tree.Contains(node, root))
26
27
                             tree.Detach(ref root, node);
28
                             free(node);
29
                             currentCount--;
30
                             Assert.Equal(currentCount, (int)UncheckedConverter<TElement,

→ int>.Default.Convert(treeCount()));
                         }
32
                    }
33
                }
34
            }
36
            public static void TestMultipleRandomCreationsAndDeletions<TElement>(this
               SizedBinaryTreeMethodsBase<TElement> tree, ref TElement root, Func<TElement>
                treeCount, int maximumOperationsPerCycle)
38
                var random = new System.Random(0)
                var added = new HashSet<TElement>();
40
                var currentCount = 0;
41
                for (var N = 1; N < maximumOperationsPerCycle; N++)</pre>
43
                    for (var i = 0; i < N; i++)</pre>
```

```
45
                        var node = UncheckedConverter<int, TElement>.Default.Convert(random.Next(1,
                            N));
                        if (added.Add(node))
47
                        {
48
                            tree.Attach(ref root, node);
49
                            currentCount++:
50
                            Assert.Equal(currentCount, (int)UncheckedConverter<TElement,
51
                                int>.Default.Convert(treeCount()));
                        }
53
                    for (var i = 1; i <= N; i++)</pre>
54
55
                        TElement node = UncheckedConverter<int,
56
                            TElement>.Default.Convert(random.Next(1, N));
                        if (tree.Contains(node, root))
57
58
                            tree.Detach(ref root, node);
                            currentCount--;
60
                            Assert.Equal(currentCount, (int)UncheckedConverter<TElement,
                             → int>.Default.Convert(treeCount()));
                            added.Remove(node);
62
                        }
63
                    }
64
               }
           }
66
       }
67
1.17
      ./csharp/Platform.Collections.Methods.Tests/TreesTests.cs
   using Xunit;
2
3
   namespace Platform.Collections.Methods.Tests
4
       public static class TreesTests
            private const int _n = 500;
            public static void RecursionlessSizeBalancedTreeMultipleAttachAndDetachTest()
11
                var recursionlessSizeBalancedTree = new RecursionlessSizeBalancedTree<uint>(10000);
12
13
                recursionlessSizeBalancedTree.TestMultipleCreationsAndDeletions(recursionlessSizeBal
                    ancedTree.Allocate, recursionlessSizeBalancedTree.Free, ref
                    recursionlessSizeBalancedTree.Root, () => recursionlessSizeBalancedTree.Count,
                    n);
            }
14
15
            [Fact]
16
            public static void SizeBalancedTreeMultipleAttachAndDetachTest()
                var sizeBalancedTree = new SizeBalancedTree<uint>(10000);
19
                sizeBalancedTree.TestMultipleCreationsAndDeletions(sizeBalancedTree.Allocate,
20

→ sizeBalancedTree.Free, ref sizeBalancedTree.Root, () => sizeBalancedTree.Count,

                    _n);
            }
21
            [Fact]
23
            public static void SizedAndThreadedAVLBalancedTreeMultipleAttachAndDetachTest()
2.4
                var avlTree = new SizedAndThreadedAVLBalancedTree<uint>(10000);
26
                avlTree.TestMultipleCreationsAndDeletions(avlTree.Allocate, avlTree.Free, ref
27
                → avlTree.Root, () => avlTree.Count, _n);
            }
29
            [Fact]
30
            public static void RecursionlessSizeBalancedTreeMultipleRandomAttachAndDetachTest()
32
                var recursionlessSizeBalancedTree = new RecursionlessSizeBalancedTree<uint>(10000);
33
                recursionlessSizeBalancedTree.TestMultipleRandomCreationsAndDeletions(ref
                recursionlessSizeBalancedTree.Root, () => recursionlessSizeBalancedTree.Count,
                    _n);
            }
35
36
            [Fact]
37
            public static void SizeBalancedTreeMultipleRandomAttachAndDetachTest()
39
                var sizeBalancedTree = new SizeBalancedTree<uint>(10000);
40
```

```
\verb|sizeBalancedTree.TestMultipleRandomCreationsAndDeletions| (\verb|ref| sizeBalancedTree.Root|, | and | 
41
                                                                                               }
43
                                                                   public static void SizedAndThreadedAVLBalancedTreeMultipleRandomAttachAndDetachTest()
{
44
^{45}
46
                                                                                             var avlTree = new SizedAndThreadedAVLBalancedTree<uint>(10000);
47
                                                                                             avlTree.TestMultipleRandomCreationsAndDeletions(ref avlTree.Root, () =>

→ avlTree.Count, _n);
                                                                    }
49
                                             }
50
                    }
```

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