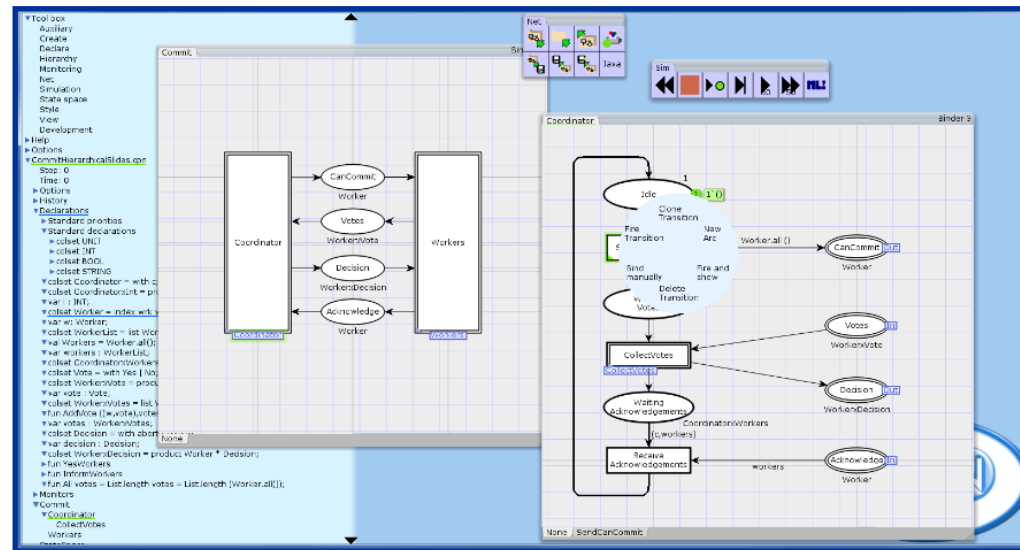


# Theory and Tool | Part 1d

## Hierarchical Coloured Petri Nets with Modules



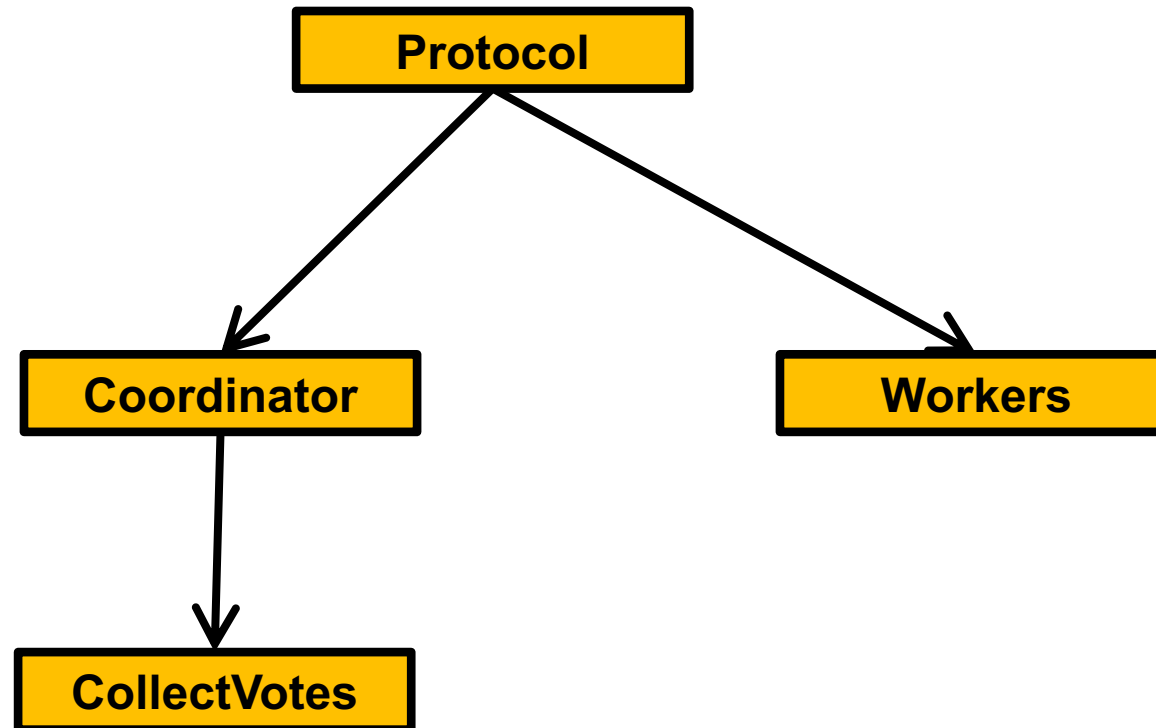
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Department of Computer Science, Electrical Engineering, and Mathematical Sciences  
Western Norway University of Applied Sciences  
Email: [lmkr@hvl.no](mailto:lmkr@hvl.no)

# Motivation and concepts

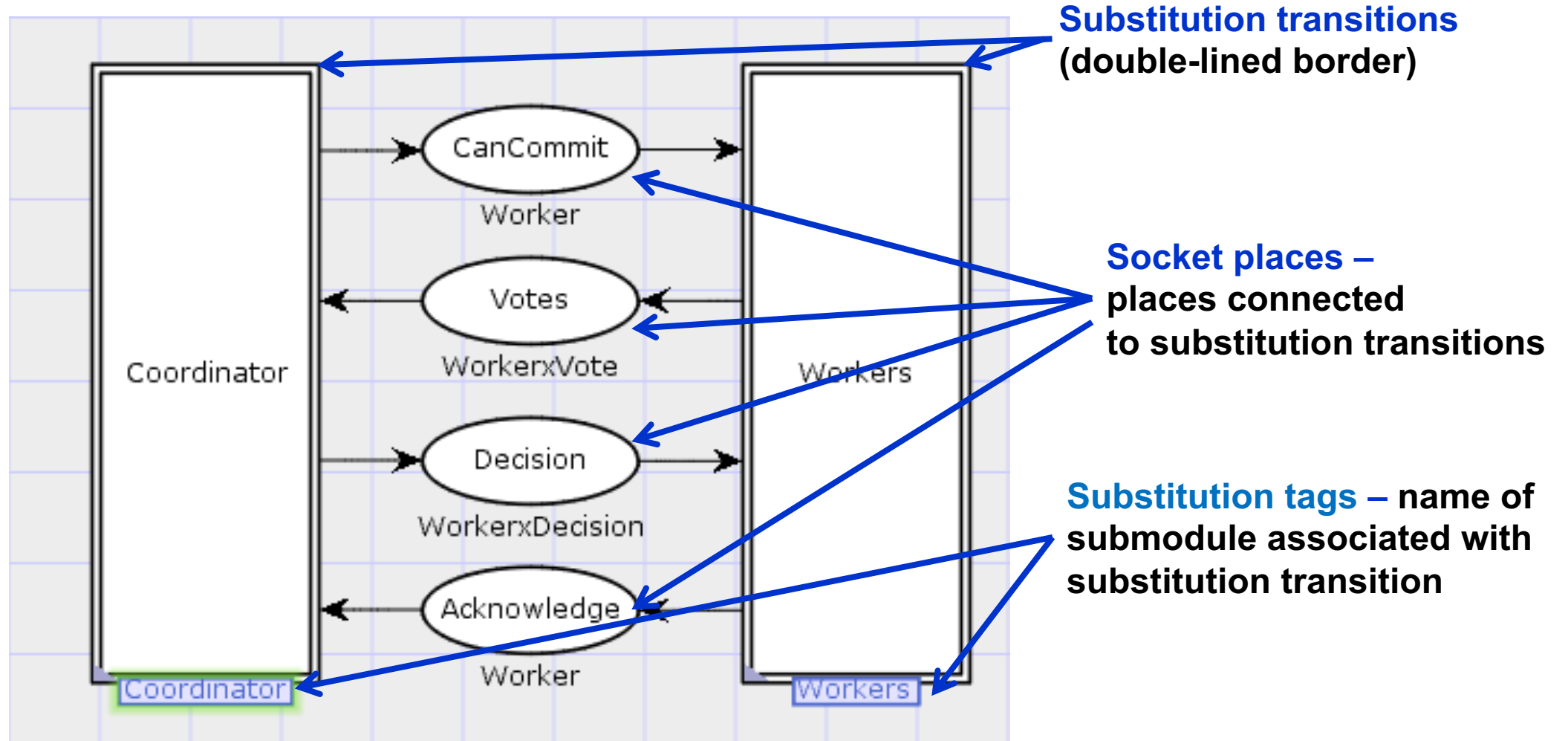
- **Important to be able to split a large CPN models into a set of modules with interfaces**
  - To support construction of large CPN models
  - To support reuse of modules and maintainability
  - To support abstraction and management of details
- **Key concepts of hierarchical CPN modules**
  - A **module** exchange tokens with its environment using input/output **port places**
  - **Substitution transitions** have associated **submodules**
  - **Port-socket relation** associates socket places of substitution transitions with the port places in the associated submodule

# Hierarchical modules

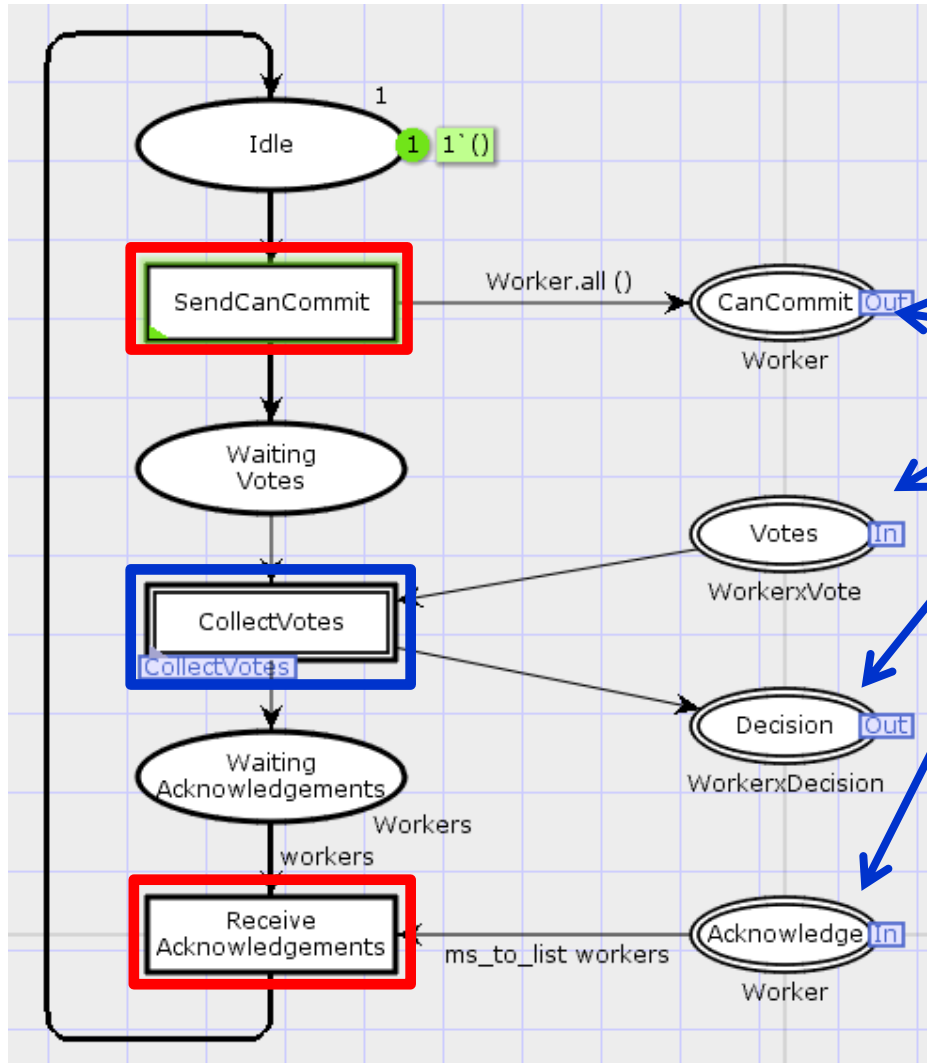
- Model is comprised of a collection of **modules** that are hierarchically organised into levels
- **Example:** the two-phase commit protocol



# Top-level: Protocol module



# Coordinator module



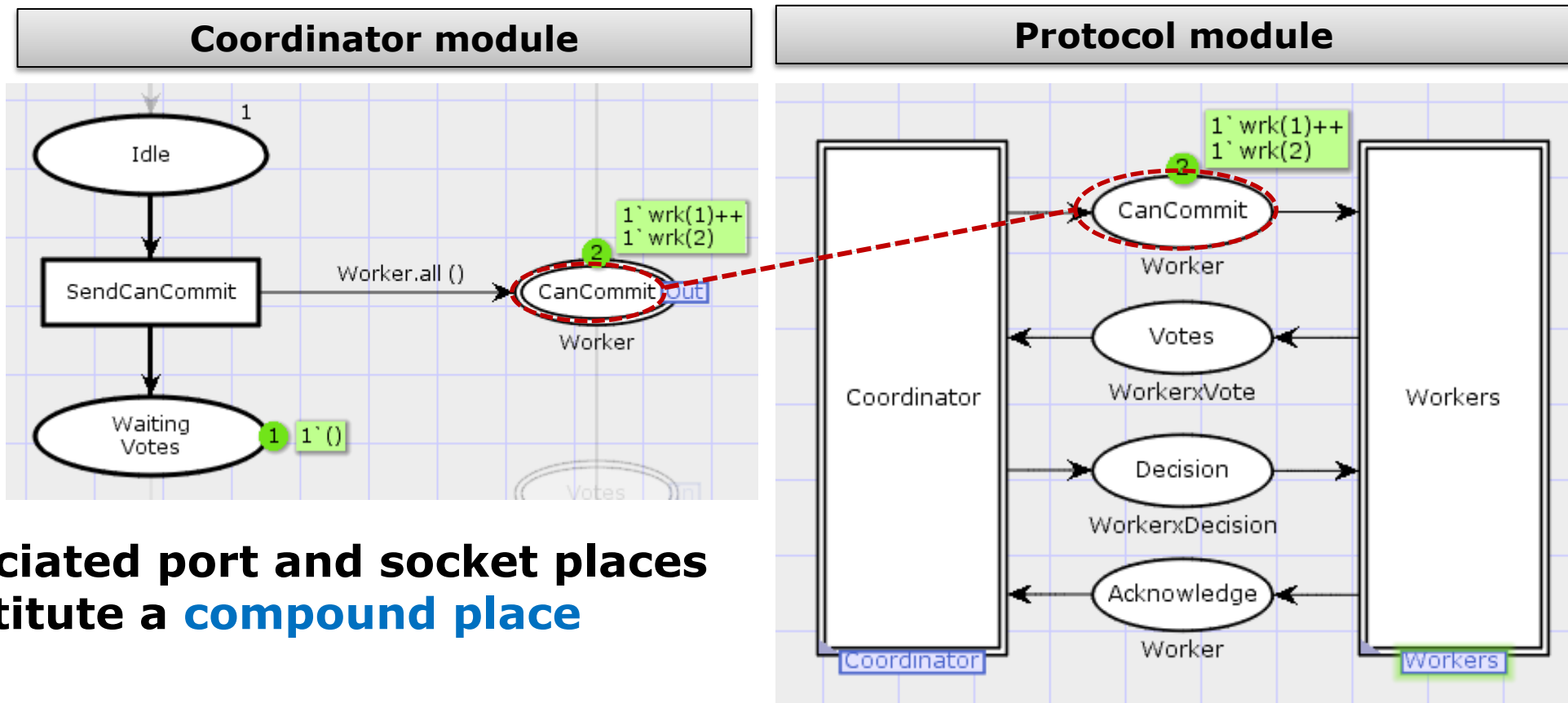
**Port place** - used for exchanging tokens with the upper-level module (IN,OUT,IN/OUT)

**SendCanCommit** and **ReceiveAcknowledgement** are ordinary transitions

**CollectVotes** is a substitution transition

# Port-socket place relation

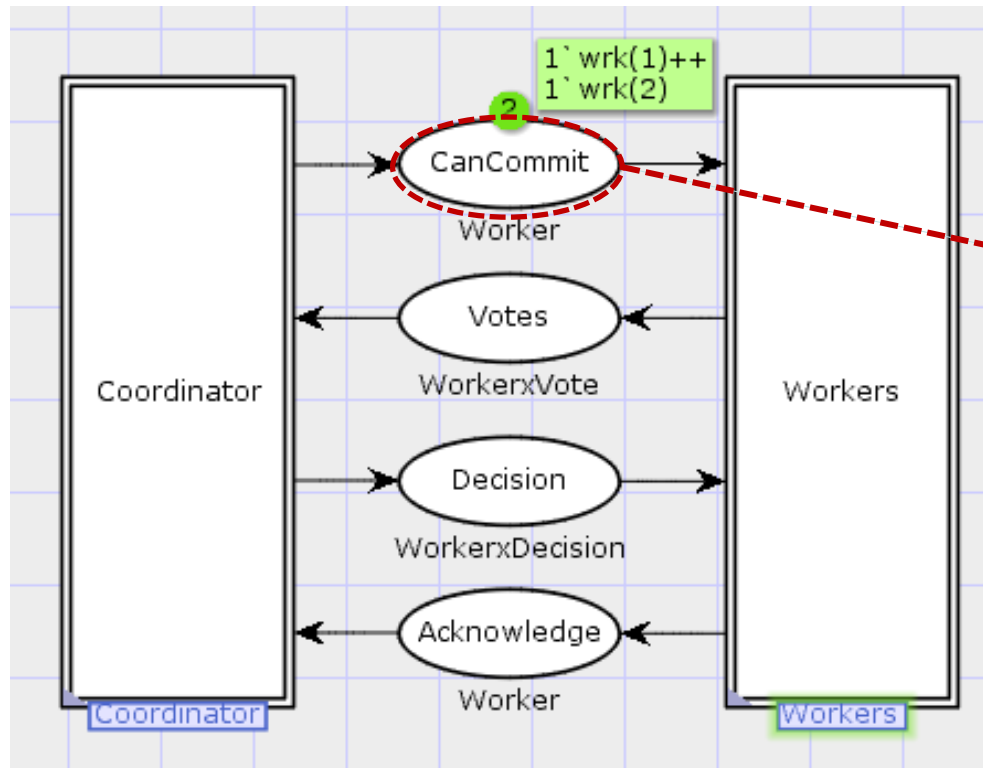
- **Tokens added (removed) on a port place are added (removed) on the associated socket place**



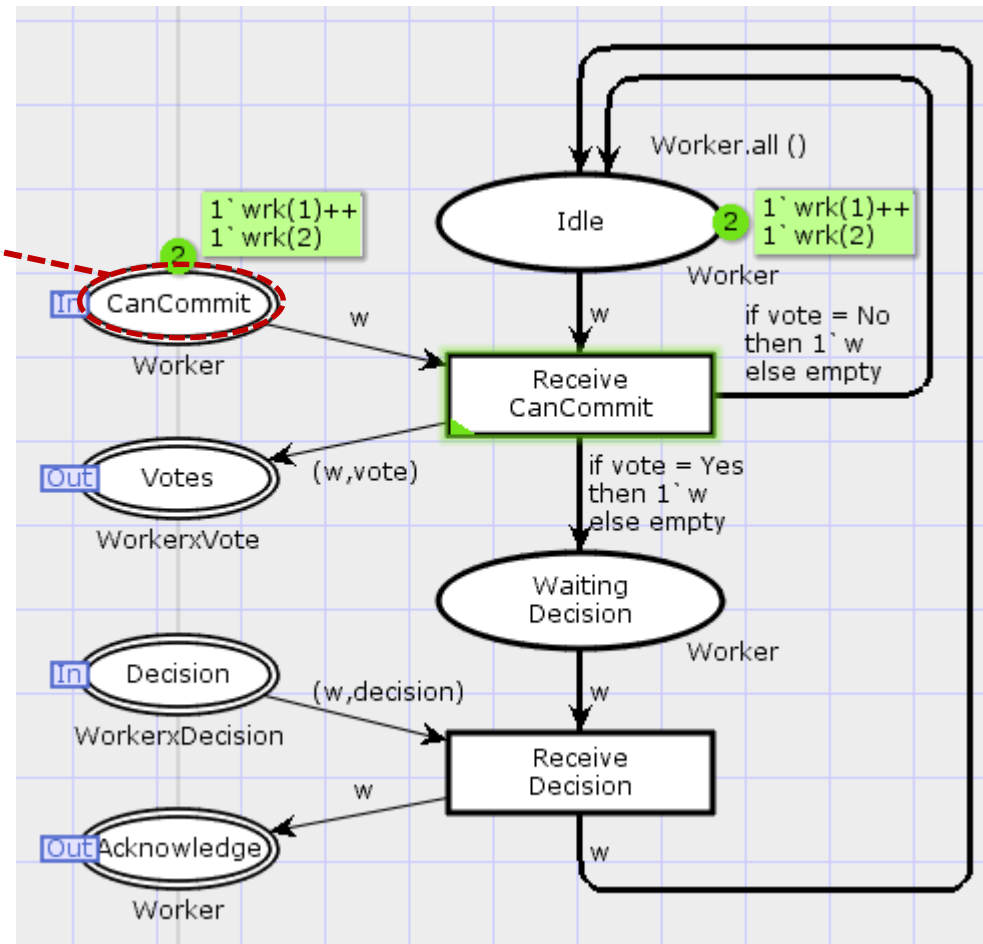
- **Associated port and socket places constitute a compound place**

# Workers module

## Protocol module



## Workers module



# CPN Tools demo

`part1d-cpnmodules.cpn`

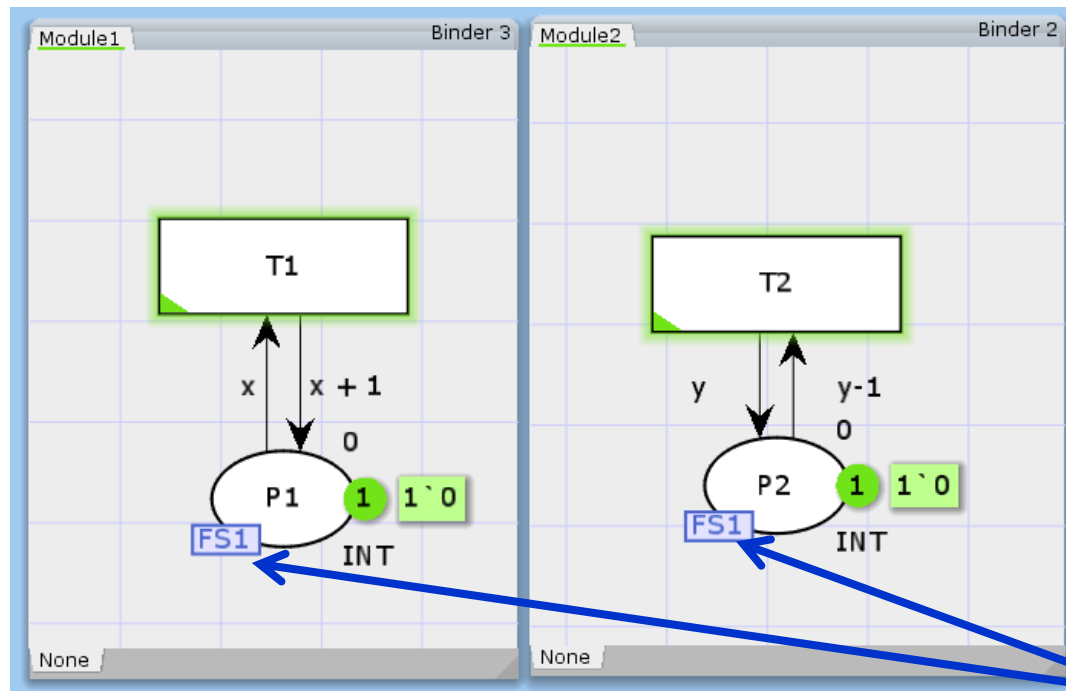
- **Hierarchical CPN models**
  - Navigating hierarchical models
  - Simulation of hierarchical models
  - Editing of modules: top-down and bottom-up development





# Place Fusion Sets

- Group of places to be treated as one compound (global) place



Any change in the marking of P1 will be reflected on P2 (and vice versa)

Similar to global variables  
- should be used with care

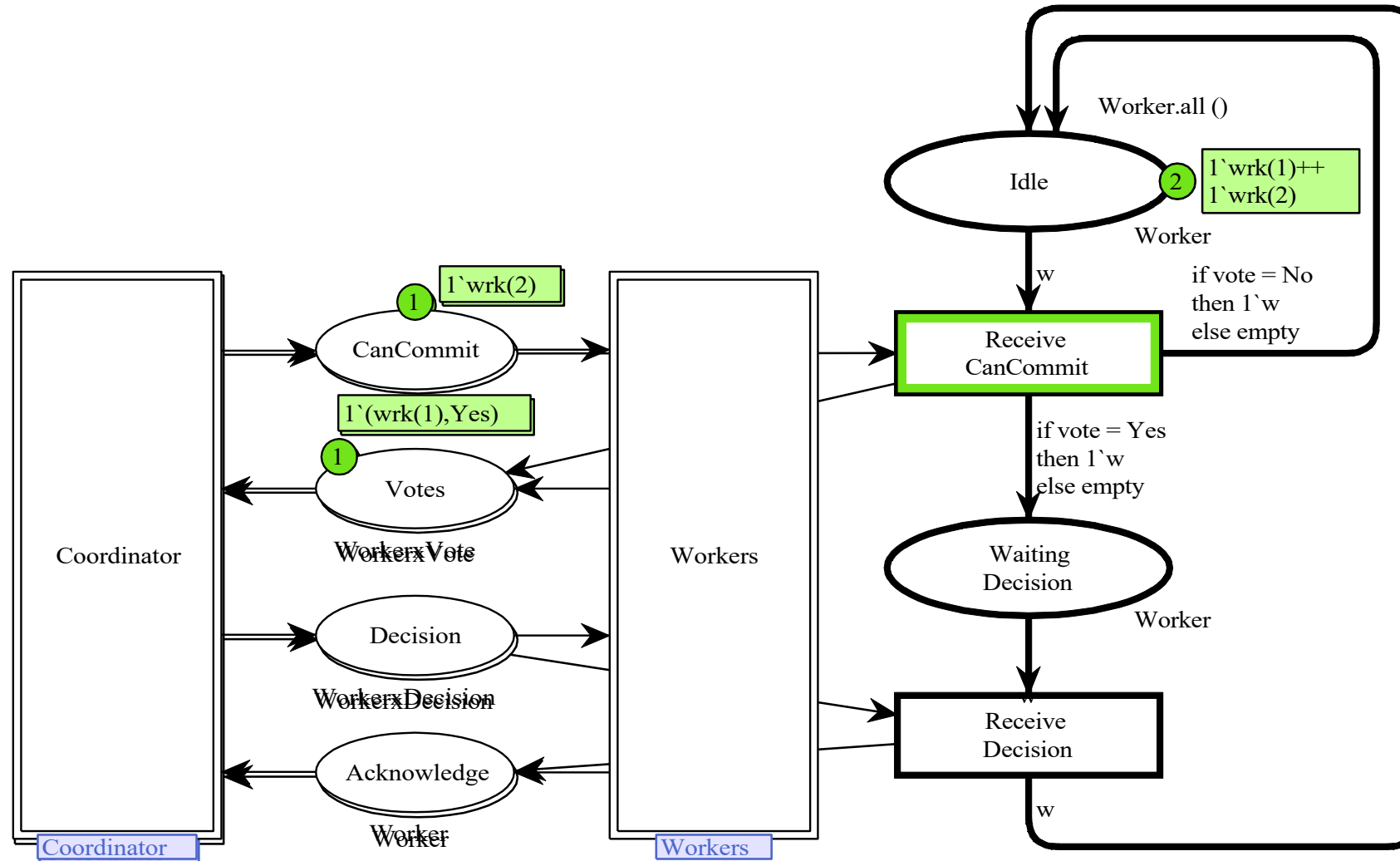
P1 and P2 are fusion places belonging to fusion set FS1

# Unfolding Coloured Petri Nets to Place/Transition Nets

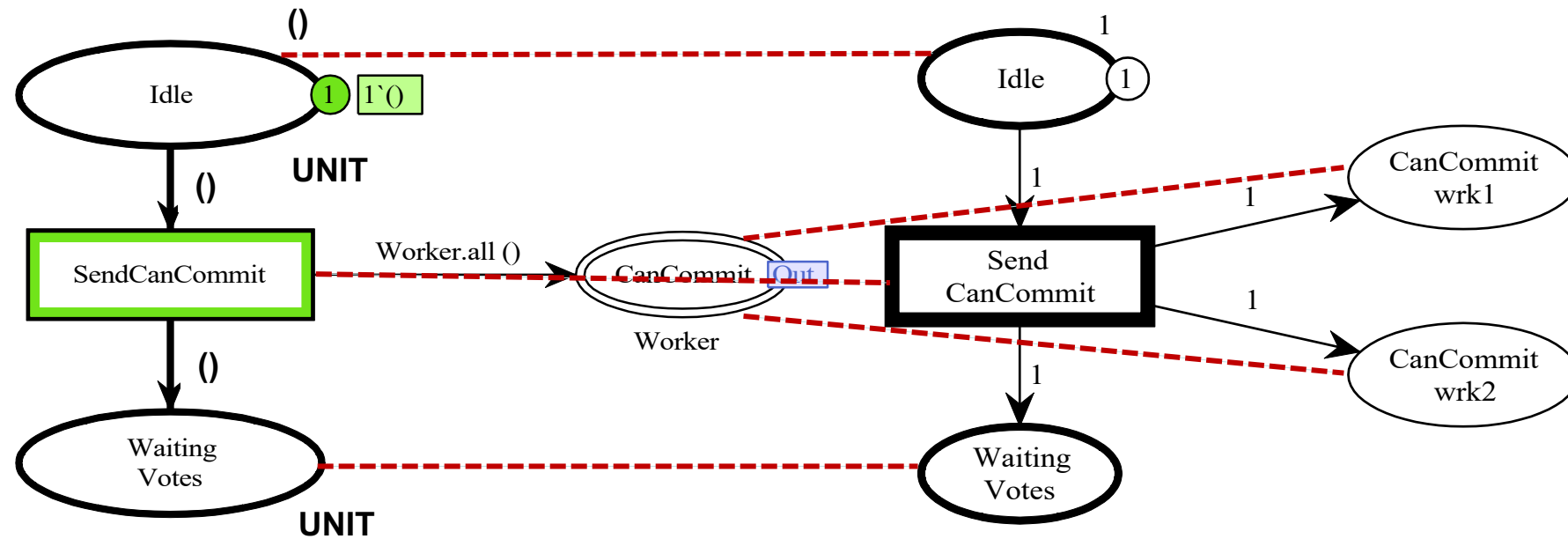
# Unfolding Coloured Petri Nets

- **A hierarchical CPN model can be unfolded to a **non-hierarchical Coloured Petri Net****
  - Recursively replace each substitution transition with its associated submodule
  - Associated port and socket places are merged into a single place
- **A **non-hierarchical Coloured Petri Net** can be unfolded into a Place/Transition Net (PTN)**
  - Replace each CPN place with one PTN place for each colour in the colour set of the CPN place
  - Replace each CPN transition with one PTN transition for each possible binding of the CPN transition

# Unfolding hierarchical CPNs



# Unfolding CPN places



# Unfolding CPN transitions

