

Contrastive Learning for Unpaired Image-to-Image Translation

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Abstract. In image-to-image translation, each patch in the output should reflect the *content* of the corresponding patch in the input, independent of domain. We propose a straightforward method for doing so – maximizing mutual information between the two, using a framework based on contrastive learning. The method encourages two elements (corresponding patches) to map to a similar point in a learned feature space, relative to other elements (other patches) in the dataset, referred to as negatives. We explore several critical design choices for making contrastive learning effective in the image synthesis setting. Notably, we use a multilayer, patch-based approach, rather than operate on entire images. Furthermore, we draw negatives from *within* the input image itself, rather than from the rest of the dataset. We demonstrate that our framework enables one-sided translation in the unpaired image-to-image translation setting, while improving quality and reducing training time. In addition, our method can even be extended to the training setting where each “domain” is only a single image.

Keywords: contrastive learning, noise contrastive estimation, mutual information, image generation

1 Introduction

Consider the image-to-image translation problem in Figure 1. We wish for the output to take on the *appearance* of the target domain (a zebra), while retaining the structure, or *content*, of the specific input horse. This is, fundamentally, a disentanglement problem: separating the content, which needs to be preserved across domains, from appearance, which must change. Typically, target appearance is enforced using an adversarial loss [19,28], while content is preserved using cycle-consistency [81,73,34]. However, cycle-consistency assumes that the relationship between the two domains is a bijection, which is often too restrictive. In this paper, we propose an alternative, rather straightforward way of maintaining correspondence in content but not appearance – by maximizing the mutual information between corresponding input and output patches.

In a successful result, given a specific patch on the output, for example, the generated zebra forehead highlighted in blue, one should have a good idea that it came from the horse forehead, and not the other parts of the horse or

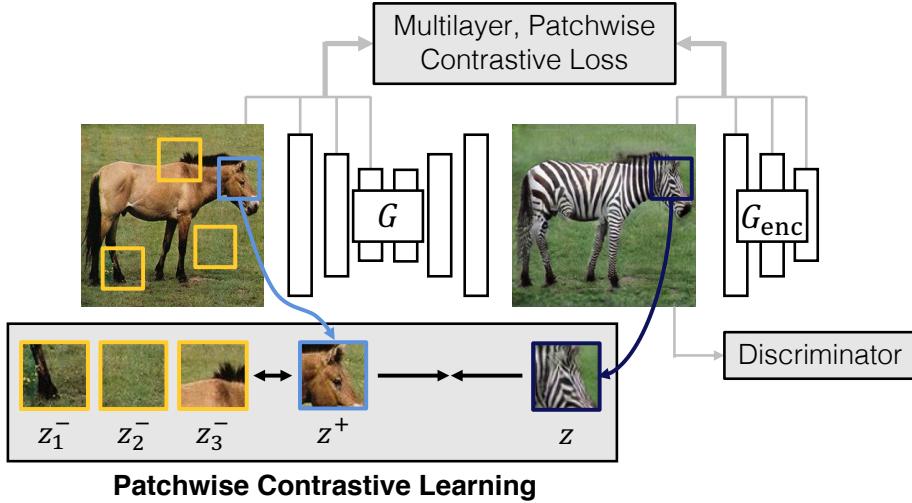


Fig. 1: **Patchwise Contrastive Learning for one-sided translation.** A generated **output patch** should appear closer to its **corresponding input patch**, in comparison to other **random patches**. We use a multilayer, patchwise contrastive loss, which maximizes **mutual information** between corresponding input and output patches. This enables one-sided translation in the unpaired setting.

the background vegetation. We achieve this by using a type of contrastive loss function, InfoNCE loss [53], which aims to learn an embedding or an encoder that *associates* corresponding patches to each other, while *disassociating* them from others. To do so, the encoder learns to pay attention to the commonalities between the two domains, such as object parts and shapes, while being invariant to the differences, such as the textures of the animals. The two networks, the generator and encoder, conspire together to generate an image such that patches can be easily traceable to the input.

Contrastive learning has been an effective tool in unsupervised visual representation learning [7,21,53,72]. In this work, we demonstrate its effectiveness in a conditional image synthesis setting and systematically study several key factors to make it successful. We find it pertinent to use it on a multilayer, patchwise fashion. In addition, we find that drawing negatives *internally* from within the input image, rather than externally from other images in the dataset, forces the patches to better preserve the content of the input. Our method requires neither memory bank [72,21] nor specialized architectures [22,2].

Extensive experiments show that our faster, lighter model outperforms both prior one-sided translation methods [3,16] and state-of-the-art models that rely on several auxiliary networks and multiple loss functions. Furthermore, since our contrastive representation is formulated within the same image, our method can even be trained on single images. Our code and models are available at [GitHub](#).

2 Related Work

Image translation and cycle-consistency. Paired image-to-image translation [28] maps an image from input to output domain using an adversarial loss [19], in conjunction with a reconstruction loss between the result and target. In unpaired translation settings, corresponding examples from domains are not available. In such cases, *cycle-consistency* has become the de facto method for enforcing correspondence [81,73,34], which learns an inverse mapping from the output domain back to the input and checks if the input can be reconstructed. Alternatively, UNIT [40] and MUNIT [27] propose to learn a shared intermediate “content” latent space. Recent works further enable multiple domains and multi-modal synthesis [8,82,1,37,41] and improve the quality of results [65,80,18,71,39]. In all of the above examples, *cycle-consistency* is used, often in multiple aspects, between (a) two image domains [34,73,81] (b) image to latent [8,27,37,40,82], or (c) latent to image [27,82]. While effective, the underlying bijective assumption behind cycle-consistency is sometimes too restrictive. Perfect reconstruction is difficult to achieve, especially when images from one domain have additional information compared to the other domain.

Relationship preservation. An interesting alternative approach is to encourage relationships present in the input be analogously reflected in the output. For example, perceptually similar patches *within* an input image should be similar in the output [80], output and input images share similar content regarding a pre-defined distance [4,62,64], distances *between* input images should be consistent in output images [3], the network should be equivariant to geometric transformations [16]. Among them, DistanceGAN [3] and GcGAN [16] enable one-way translation and bypass cycle-consistency. However, both still rely on a pre-specified distance function. Here we seek to replace cycle-consistency by instead preserving the relationship *between input and output* through information maximization. Critically, our method learns a cross-domain similarity function between input and output patches, without relying on a pre-specified distance.

Emergent perceptual similarity in deep network embeddings. Defining a “perceptual” distance function between high-dimensional signals, e.g., images, has been a longstanding problem in computer vision and image processing. The majority of image translation work mentioned uses a per-pixel reconstruction metric, such as ℓ_1 . Such metrics do not reflect human perceptual preferences and can lead to blurry results. Recently, the deep learning community has found that the VGG classification network [63] trained on ImageNet dataset [12] can be re-purposed as a “perceptual loss” [14,17,31,67,79,48], which can be used in paired image translation tasks [6,55,69], and was known to outperform traditional metrics such as SSIM [70] and FSIM [76] on human perceptual tests [79]. In particular, the Contextual Loss [48] boosts the perceptual quality of pretrained VGG features, validated by human perceptual judgments [47]. In these cases, the frozen network weights cannot adapt to the data on hand. Furthermore, the frozen similarity function may not be appropriate when comparing data *across* two domains, depending on the pairing. By posing our constraint via mutual

information, our method makes use of negative samples from the data, allowing the cross-domain similarity function to adapt to the particular input and output domains, and bypass using a pre-defined similarity function.

Contrastive representation learning. Traditional unsupervised learning has sought to learn a compressed code which can effectively reconstruct the input [24]. Data imputation – holding one subset of raw data to predict from another – has emerged as a more effective family of pretext tasks, including denoising [68], context prediction [13,56], colorization [36,77], cross-channel encoding [78], frame prediction [42,51], and multi-sensory prediction [52,54]. However, such methods suffer from the same issue as before — the need for a pre-specified, hand-designed loss function to measure predictive performance.

Recently, a family of methods based on *maximizing mutual information* has emerged to bypass the above issue [7,21,22,25,43,50,53,66,72]. These methods make use of noise contrastive estimation [20], learning an embedding where associated signals are brought together, in *contrast* to other samples in the dataset (note that similar ideas go back to classic work on metric learning with Siamese nets [10]). Associated signals can be an image with itself [45,61,15,21,72], an image with its downstream representation [25,43], neighboring patches within an image [30,22,53], or multiple views of the input image [66], and most successfully, an image with a set of transformed versions of itself [7,50]. The design choices of the InfoNCE loss, such as the number of negatives and how to sample them, hyperparameter settings, and data augmentations all play a critical role and need to be carefully studied. We are the first to use InfoNCE loss for the conditional image synthesis tasks. As such, we draw on these important insights, and find additional pertinent factors, unique to image synthesis.

3 Methods

We wish to translate images from input domain $\mathcal{X} \subset \mathbb{R}^{H \times W \times C}$ to appear like an image from the output domain $\mathcal{Y} \subset \mathbb{R}^{H \times W \times 3}$. We are given a dataset of unpaired instances $X = \{\mathbf{x} \in \mathcal{X}\}, Y = \{\mathbf{y} \in \mathcal{Y}\}$. Our method can operate even when X and Y only contain a single image each.

Our method only requires learning the mapping in one direction and avoids using inverse auxiliary generators and discriminators. This can largely simplify the training procedure and reduce training time. We break up our generator function G into two components, an encoder G_{enc} followed by a decoder G_{dec} , which are applied sequentially to produce output image $\hat{\mathbf{y}} = G(\mathbf{z}) = G_{\text{dec}}(G_{\text{enc}}(\mathbf{x}))$.

Adversarial loss. We use an adversarial loss [19], to encourage the output to be visually similar to images from the target domain, as follows:

$$\mathcal{L}_{\text{GAN}}(G, D, X, Y) = \mathbb{E}_{\mathbf{y} \sim Y} \log D(\mathbf{y}) + \mathbb{E}_{\mathbf{x} \sim X} \log(1 - D(G(\mathbf{x}))). \quad (1)$$

Mutual information maximization. We use a noise contrastive estimation framework [53] to maximize mutual information between input and output. The idea of contrastive learning is to associate two signals, a “query” and its “positive”

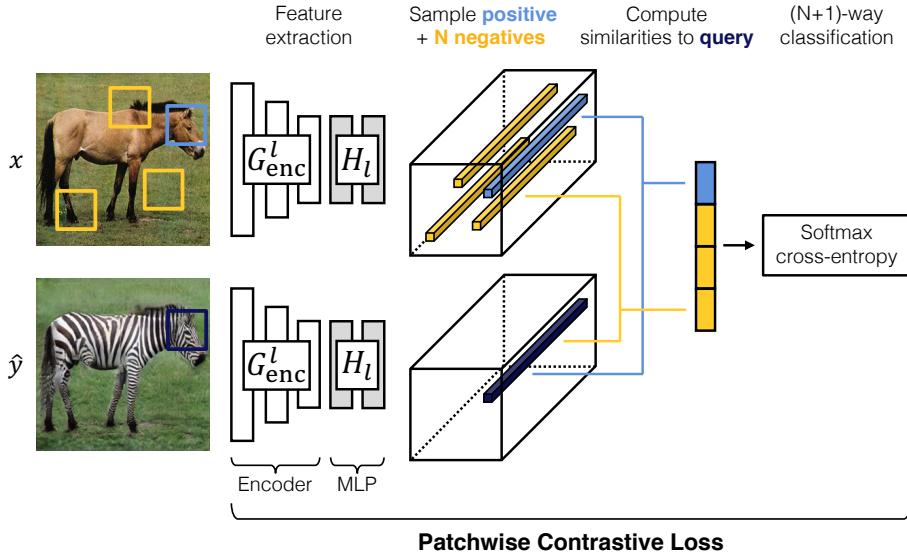


Fig. 2: **Patchwise Contrastive Loss.** Both images, x and \hat{y} , are encoded into feature tensor. We sample a **query** patch from the output \hat{y} and compare it to the input patch at the same location. We set up an $(N+1)$ -way classification problem, where N negative patches are sampled from the same input image at different locations. We reuse the encoder part G_{enc} of our generator and add a two-layer MLP network. This network learns to project both the input and output patch to a shared embedding space.

example, in contrast to other points within the dataset, referred to as “negatives”. The **query**, **positive**, and N **negatives** are mapped to K -dimensional vectors $\mathbf{v}, \mathbf{v}^+ \in \mathbb{R}^K$ and $\mathbf{v}^- \in \mathbb{R}^{N \times K}$, respectively. $\mathbf{v}_n^- \in \mathbb{R}^K$ denotes the n -th negative. We normalize vectors onto a unit sphere to prevent the space from collapsing or expanding. An $(N + 1)$ -way classification problem is set up, where the distances between the query and other examples are scaled by a temperature $\tau = 0.07$ and passed as logits [72, 21]. The cross-entropy loss is calculated, representing the probability of the positive example being selected over negatives.

$$\ell(\mathbf{v}, \mathbf{v}^+, \mathbf{v}^-) = -\log \left[\frac{\exp(\mathbf{v} \cdot \mathbf{v}^+ / \tau)}{\exp(\mathbf{v} \cdot \mathbf{v}^+ / \tau) + \sum_{n=1}^N \exp(\mathbf{v} \cdot \mathbf{v}_n^- / \tau)} \right]. \quad (2)$$

Our goal is to associate the input and output data. In our context, query refers to an output. positive and negatives are corresponding and noncorresponding input. Below, we explore several important design choices, including how to map the images into vectors and how to sample the negatives.

Multilayer, patchwise contrastive learning. In the unsupervised learning setting, contrastive learning has been used both on an image and patch level [2, 22]. For our application, we note that not only should the whole images share content, but also corresponding patches between the input and output images. For example,

given a patch showing the legs of an output zebra, one should be able to more strongly associate it to the corresponding legs of the input horse, more so than the other patches of the horse image. Even at the pixel level, the colors of a zebra body (black and white) can be more strongly associated to the color of a horse body than to the background shades of grass. Thus, we employ a *multilayer, patch-based learning objective*.

Since the encoder G_{enc} is computed to produce the image translation, its feature stack is readily available, and we take advantage. Each layer and spatial location within this feature stack represents a patch of the input image, with deeper layers corresponding to bigger patches. We select L layers of interest and pass the feature maps through a small two-layer MLP network H_l , as used in SimCLR [7], producing a stack of features $\{\mathbf{z}_l\}_L = \{H_l(G_{\text{enc}}^l(\mathbf{x}))\}_L$, where G_{enc}^l represents the output of the l -th chosen layer. We index into layers $l \in \{1, 2, \dots, L\}$ and denote $s \in \{1, \dots, S_l\}$, where S_l is the number of spatial locations in each layer. We refer to the corresponding feature as $\mathbf{z}_l^s \in \mathbb{R}^{C_l}$ and the other features as $\mathbf{z}_l^{S_l \setminus s} \in \mathbb{R}^{(S_l - 1) \times C_l}$, where C_l is the number of channels at each layer. Similarly, we encode the output image $\hat{\mathbf{y}}$ into $\{\hat{\mathbf{z}}_l\}_L = \{H_l(G_{\text{enc}}^l(G(\mathbf{x})))\}_L$.

We aim to match corresponding input-output patches at a specific location. We can leverage the other patches *within* the input as negatives. For example, a zebra leg should be more closely associated with an input horse leg than the other patches of the same input, such as other horse parts or the background sky and vegetation. We name it as the *PatchNCE* loss, as illustrated in Figure 2. Appendix C provides pseudocode.

$$\mathcal{L}_{\text{PatchNCE}}(G, H, X) = \mathbb{E}_{\mathbf{x} \sim X} \sum_{l=1}^L \sum_{s=1}^{S_l} \ell(\mathbf{z}_l^s, \hat{\mathbf{z}}_l^s, \mathbf{z}_l^{S_l \setminus s}). \quad (3)$$

Alternatively, we can also leverage image patches from the rest of the dataset. We encode a random negative image from the dataset $\tilde{\mathbf{x}}$ into $\{\tilde{\mathbf{z}}_l\}_L$, and use the following *external* NCE loss. In this variant, we maintain a large, consistent dictionary of negatives using an auxiliary moving-averaged encoder, following MoCo [21]. MoCo enables negatives to be sampled from a longer history, and performs more effective than end-to-end updates [53, 22] and memory bank [72].

$$\mathcal{L}_{\text{external}}(G, H, X) = \mathbb{E}_{\mathbf{x} \sim X} \mathbb{E}_{\tilde{\mathbf{z}} \sim Z^-} \sum_{l=1}^L \sum_{s=1}^{S_l} \ell(\mathbf{z}_l^s, \hat{\mathbf{z}}_l^s, \tilde{\mathbf{z}}_l), \quad (4)$$

where dataset negatives $\tilde{\mathbf{z}}_l$ are sampled from an external dictionary Z^- , whose data are computed using a moving-averaged encoder \hat{H}_l and moving-averaged MLP \hat{H} . We refer our readers to the original work for more details [21].

In Section 4.1, we show that our encoder G_{enc} learns to capture domain-invariant concepts, such as animal body, grass, and sky for horse \rightarrow zebra, while our decoder G_{dec} learns to synthesize domain-specific features such as zebra stripes. Interestingly, through systematic evaluations, we find that using internal patches only outperforms using external patches. We hypothesize that by using internal statistics, our encoder does not need to model large intra-class variation

such as white horse vs. brown horse, which is not necessary for generating output zebras. Single image internal statistics has been proven effective in many vision tasks such as segmentation [29], super-resolution, and denoising [83,60].

Final objective. Our final objective is as follows. The generated image should be realistic, while patches in the input and output images should share correspondence. Figure 1 illustrates our minimax learning objective. Additionally, we may utilize PatchNCE loss $\mathcal{L}_{\text{PatchNCE}}(G, H, Y)$ on images from domain \mathcal{Y} to prevent the generator from making unnecessary changes. This loss is essentially a learnable, domain-specific version of the identity loss, commonly used by previous unpaired translation methods [64,81].

$$\mathcal{L}_{\text{GAN}}(G, D, X, Y) + \lambda_X \mathcal{L}_{\text{PatchNCE}}(G, H, X) + \lambda_Y \mathcal{L}_{\text{PatchNCE}}(G, H, Y). \quad (5)$$

We choose $\lambda_X = 1$ when we jointly train with the identity loss $\lambda_Y = 1$, and choose a larger value $\lambda_X = 10$ without the identity loss ($\lambda_Y = 0$) to compensate for the absence of the regularizer. We find that the former configuration, named *Contrastive Unpaired Translation (CUT)* hereafter, achieves superior performance to existing methods, whereas the latter, named *FastCUT*, can be thought as a faster and lighter version of CycleGAN. Our model is relatively simple compared to recent methods that often use 5-10 losses and hyper-parameters.

Discussion. Li et al. [38] has shown that cycle-consistency loss is the upper bound of conditional entropy $H(X|Y)$ (and $H(Y|X)$). Therefore, minimizing cycle-consistency loss encourages the output \hat{y} to be more dependent on input x . This is related to our objective of maximizing the mutual information $I(X, Y)$, as $I(X, Y) = H(X) - H(X|Y)$. As entropy $H(X)$ is a constant and independent of the generator G , maximizing mutual information is equivalent to minimizing the conditional entropy. Notably, using contrastive learning, we can achieve a similar goal without introducing inverse mapping networks and additional discriminators. In the unconditional modeling scenario, InfoGAN [5] shows that simple losses (e.g., L2 or cross-entropy) can serve as a lower bound for maximizing mutual information between an image and a low-dimensional code. In our setting, we maximize the mutual information between two high-dimensional image spaces, where simple losses are no longer effective. Liang et al. [39] proposes an adversarial loss based on Siamese networks that encourages the output to be closer to the target domain than to its source domain. The above method still builds on cycle-consistency and two-way translations. Different from the above work, we use contrastive learning to enforce content consistency, rather than to improve the adversarial loss itself. To measure the similarity between two distributions, the Contextual Loss [48] used softmax over cosine distances of features extracted from pre-trained networks. In contrast, we learn the encoder with the NCE loss to associate the input and output patches at the same location.

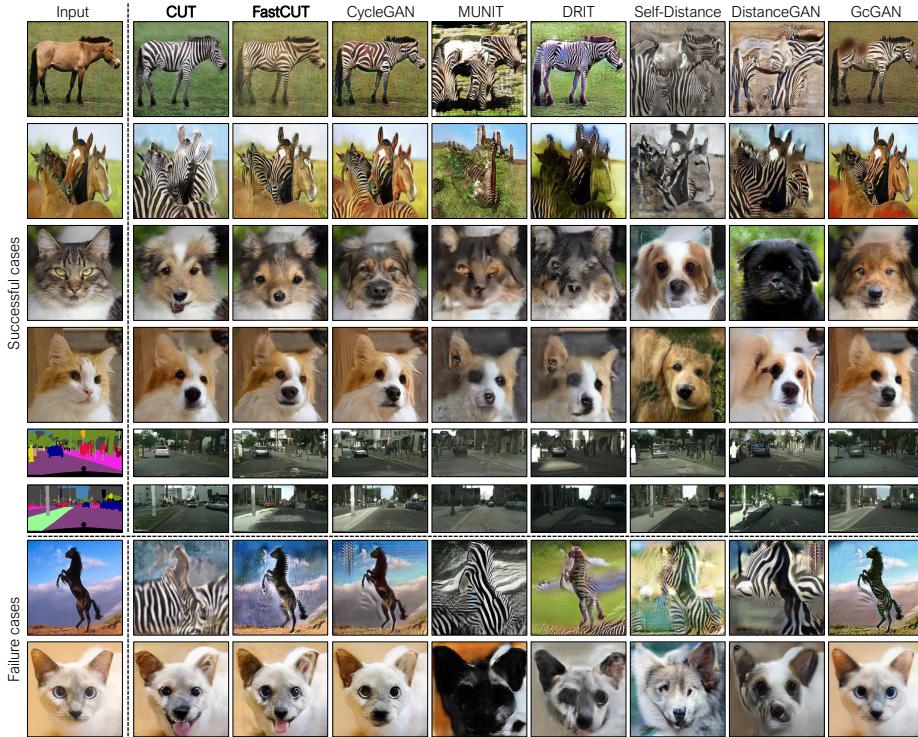


Fig. 3: **Results.** We compare our methods (CUT and FastCUT) with existing methods on the horse→zebra, cat→dog, and Cityscapes datasets. CycleGAN [81], MUNIT [40], and DRIT [37], are two-sided methods, while SelfDistance, DistanceGAN [3], and GcGAN [16] are one-sided. We show successful cases above the dotted lines. Our full version CUT is able to add the zebra texture to the horse bodies. Our fast variant, FastCUT can also generate competitive results at the least computational cost of training. The final rows show failure cases. In the first, we are unable to identify the unfamiliar pose of the horse and instead add texture to the background. In the second, the method hallucinates a tongue.

4 Experiments

We test across several datasets. We first show that our method improves upon baselines in unpaired image translation. We then show that our method can extend to *single-image* training. Full results are available at our [website](#).

Training details. We follow the setting of CycleGAN [81], except that the ℓ_1 cycle-consistency loss is replaced with our contrastive loss. In detail, we used LSGAN [46] and Resnet-based generator [31] with PatchGAN [28]. We define our encoder as the first half of the generator, and accordingly extract our multilayer features from five evenly distributed points of the encoder. For single image translation, we use a StyleGAN2-based generator [33]. To embed the encoder’s

Method	Cityscapes				Cat→Dog		Horse→Zebra		
	mAP↑	pixAcc↑	classAcc↑	FID↓	FID↓	sec/iter↓	Mem(GB)↓		
CycleGAN [81]	20.4	55.9	25.4	76.3	85.9	77.2	0.40	4.81	
MUNIT [40]	16.9	56.5	22.5	91.4	104.4	133.8	0.39	3.84	
DRIT [37]	17.0	58.7	22.2	155.3	123.4	140.0	0.70	4.85	
Distance [3]	8.4	42.2	12.6	81.8	155.3	72.0	0.15	2.72	
SelfDistance [3]	15.3	56.9	20.6	78.8	144.4	80.8	0.16	2.72	
GCGAN [16]	21.2	63.2	26.6	105.2	96.6	86.7	0.26	2.67	
CUT	24.7	68.8	30.7	56.4	76.2	45.5	0.24	3.33	
FastCUT	19.1	59.9	24.3	68.8	94.0	73.4	0.15	2.25	

Table 1: **Comparison with baselines** We compare our methods across datasets on common evaluation metrics. CUT denotes our model trained with the identity loss ($\lambda_X = \lambda_Y = 1$), and FastCUT without it ($\lambda_X = 10, \lambda_Y = 0$). We show FID, a measure of image quality [23] (lower is better). For Cityscapes, we show the semantic segmentation scores (mAP, pixAcc, classAcc) to assess the discovered correspondence (higher is better for all metrics). Based on quantitative measures, CUT produces higher quality and more accurate generations with light footprint in terms of training speed (seconds per sample) and GPU memory usage. Our variant FastCUT also produces competitive results with even lighter computation cost of training.

features, we apply a two-layer MLP with 256 units at each layer. We normalize the vector by its L2 norm. See Appendix C for more training details.

4.1 Unpaired image translation

Datasets We conduct experiments on the following datasets.

- *Cat→Dog* contains 5,000 training and 500 val images from AFHQ Dataset [9].
- *Horse→Zebra* contains 2,403 training and 260 zebra images from ImageNet [12] and was introduced in CycleGAN [81].
- *Cityscapes* [11] contains street scenes from German cities, with 2,975 training and 500 validation images. We train models at 256×256 resolution. Unlike previous datasets listed, this does have corresponding labels. We can leverage this to measure how well our unpaired algorithm discovers correspondences.

Evaluation protocol. We adopt the evaluation protocols from [23,81], aimed at assessing *visual quality* and *discovered correspondence*. For the first, we utilize the widely-used *Fréchet Inception Distance (FID)* metric, which empirically estimates the distribution of real and generated images in a deep network space and computes the divergence between them. Intuitively, if the generated images are realistic, they should have similar summary statistics as real images, in any feature space. For *Cityscapes* specifically, we have ground truth of paired label maps. If accurate correspondences are discovered, the algorithm should generate images that are recognizable as the correct class. Using an off-the-shelf network to test “semantic interpretability” of image translation results has been commonly used [77,28]. We use the pretrained semantic segmentation network DRN[75]. We train the DRN at 256x128 resolution, and compute mean average precision

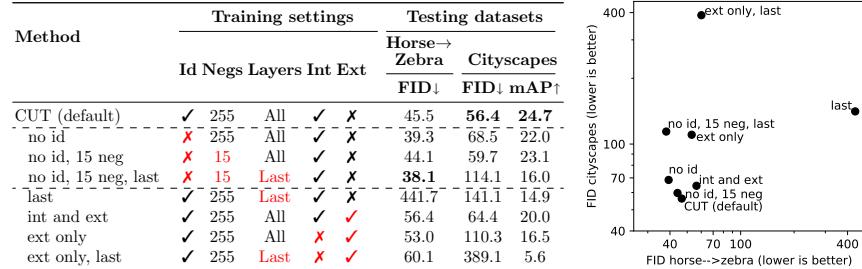


Fig. 4: **Ablations.** The PatchNCE loss is trained with negatives from each layer output of the same (internal) image, with the identity preservation regularization. (*Left*) We try removing the identity loss [**Id**], using less negatives [**Negs**], using only the last layer of the encoder [**Layers**], and varying where patches are sampled, internal [**Int**] vs external [**Ext**]. (*Right*) We plot the FIDs on horse→zebra and Cityscapes dataset. Removing the identity loss (no **id**) and reducing negatives (no **id**, 15 **neg**) still perform strongly. In fact, our variant FastCUT does not use the identity loss. However, reducing number of layers (last) or using external patches (ext) hurts performance.

(mAP), pixel-wise accuracy (pixAcc), and average class accuracy (classAcc). See Appendix C for more evaluation details.

Comparison to baselines. In Table 1, we show quantitative measures of our and Figure 3, we compare our method to baselines. We present two settings of our method in Eqn. 5: CUT with the identity loss ($\lambda_X = \lambda_Y = 1$), and FastCUT without it ($\lambda_X = 10, \lambda_Y = 0$). On image quality metrics across datasets, our methods outperform baselines. We show qualitative results in Figure 3 and additional results in Appendix A. In addition, our Cityscapes semantic segmentation scores are higher, suggesting that our method is able to find correspondences between output and input.

Speed and memory. Since our model is one-sided, our method is memory-efficient and fast. For example, our method with the identity loss was 40% faster and 31% more memory-efficient than CycleGAN at training time, using the same architectures as CycleGAN (Table 1). Furthermore, our faster variant FastCUT is 63% faster and 53% lighter, while achieving superior metrics to CycleGAN. Table 1 contains the speed and memory usage of each method measured on NVIDIA GTX 1080Ti, and shows that FastCUT achieves competitive FIDs and segmentation scores with a lower time and memory requirement. Therefore, our method can serve as a practical, lighter alternative in scenarios, when an image translation model is jointly trained with other components [26,57].

4.2 Ablation study and analysis

We find that in the image synthesis setting, similarly to the unsupervised learning setting [22,21,7], implementation choices for contrastive loss are important. Here, try various settings and ablations of our method, summarized in Figure 4. By default, we use the ResNet-based generator used in CycleGAN [81], with patchNCE using (a) negatives sampled from the input image, (b) multiple layers of the

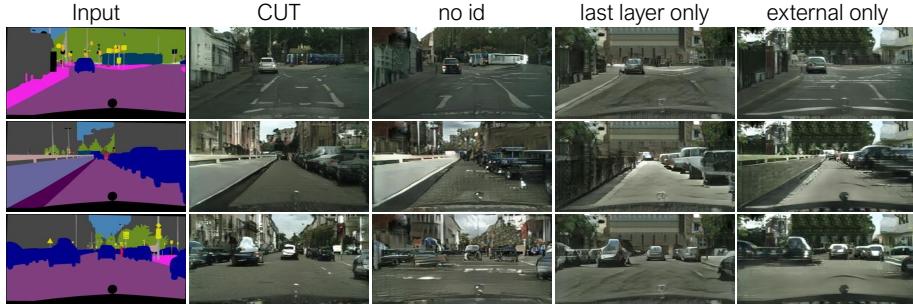


Fig. 5: **Qualitative ablation results** of our full method (CUT) are shown: *without* the identity loss $\mathcal{L}_{\text{PatchNCE}}(G, H, Y)$ on domain Y (**no id**), using only one layer of the encoder (**last layer only**), and using external instead of internal negatives (**external only**). The ablations cause noticeable drop in quality, including repeated building or vegetation textures when using only external negatives or the last layer output.

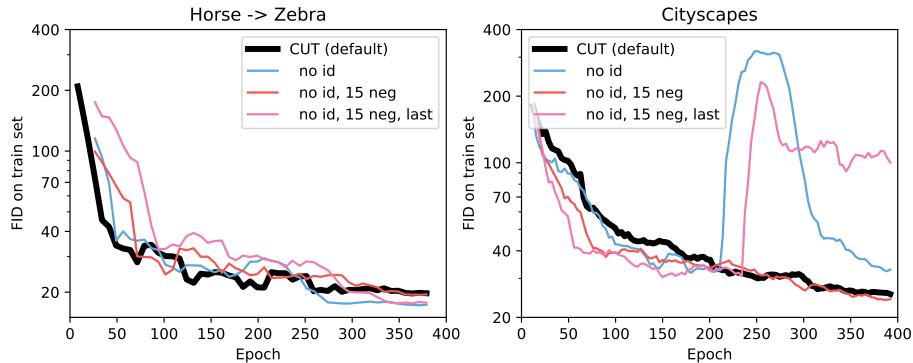


Fig. 6: **Identity loss $\mathcal{L}_{\text{PatchNCE}}(G, H, Y)$ on domain Y adds stability.** This regularizer encourages an image from the output domain Y to be unchanged by the generator. Using it (shown in **bold, black** curves), we observe better stability in comparison to other variants. On the left, our variant without the regularizer, **no id**, achieves better FID. However, we see higher variance in the training curve. On the right, training without the regularizer can lead to collapse.

encoder, and (c) a PatchNCE loss $\mathcal{L}_{\text{PatchNCE}}(G, H, Y)$ on domain Y . In Figure 4, we show results using several variants and ablations, taken after training for 400 epochs. We show qualitative examples in Figure 5.

Internal negatives are more effective than external. By default, we sample negatives from *within* the same image (internal negatives). We also try adding negatives from other images, using a momentum encoder [21]. However, the external negatives, either as addition (**int and ext**) or replacement of internal negatives (**ext only**), hurts performance. In Figure 5, we see a loss of quality, such as repeated texture in the Cityscapes dataset, indicating that sampling negatives from the same image serves as a stronger signal for preserving content.

Importance of using multiple layers of encoder. Our method uses multiple layers of the encoder, every four layers from pixels to the 16th layer. This

is consistent with the standard use of ℓ_1 +VGG loss, which uses layers from the pixel level up to a deep convolutional layer. On the other hand, many contrastive learning-based unsupervised learning papers map the whole image into a single representation. To emulate this, we try only using the last layer of the encoder (`1last`), and try a variant using external negatives only (`ext only`, `1last`). Performance is drastically reduced in both cases. In unsupervised representation learning, the input images are fixed. For our application, the loss is being used as a signal for synthesizing an image. As such, this indicates that the dense supervision provided by using multiple layers of the encoder is important when performing image synthesis.

$\mathcal{L}_{\text{PatchNCE}}(G, H, Y)$ regularizer stabilizes training. Given an image from the output domain $\mathbf{y} \in \mathcal{Y}$, this regularizer encourages the generator to leave the image unchanged with our patch-based contrastive loss. We also experiment with a variant without this regularizer, `no id`. As shown in Figure 4, removing the regularizer improves results for the horse→zebra task, but decreases performance on Cityscapes. We further investigate by showing the training curves in Figure 6, across 400 epochs. In the Cityscapes results, the training can collapse without the regularizer (although it can recover). We observe that although the final FID is sometimes better without, the training is more stable with the regularizer.

Visualizing learned similarity by encoder G_{enc} To further understand why our encoder network G_{enc} has learned to perform horse→ zebra task, we study the output space of the 1st residual block for both horse and zebra features. As shown in Figure 7. Given an input and output image, we compute the distance between a query patch’s feature vector \mathbf{v} (highlighted as red or blue dot) to feature vectors \mathbf{v}^- of all the patches in the input using $\exp(\mathbf{v} \cdot \mathbf{v}^- / \tau)$ (Eqn. 2). Additionally, we perform a PCA dimension reduction on feature vectors from both horse and zebra patches. In (d) and (e), we show the top three principal components, which looks similar before and after translation. This indicates that our encoder is able to bring the corresponding patches from two domains into a similar location in the feature embedding space.

Additional applications. Figure 8 shows additional results: Parisian street → Burano’s brightly painted houses and Russian Blue cat → Grumpy cat.

4.3 High-resolution single image translation

Finally, we conduct experiments in the single image setting, where both the source and target domain only have one image each. Here, we transfer a Claude Monet’s painting to a natural photograph. Recent methods [58,59] have explored training unconditional models on a single image. Bearing the additional challenge of respecting the structure of the input image, conditional image synthesis using only one image has not been explored by previous image-to-image translation methods. Our painting → photo task is also different from neural style transfer [17,31] (photo → painting) and photo style transfer [44,74] (photo → photo).

Since the whole image (at HD resolution) cannot fit on a commercial GPU, at each iteration we train on 16 random crops of size 128×128. We also randomly

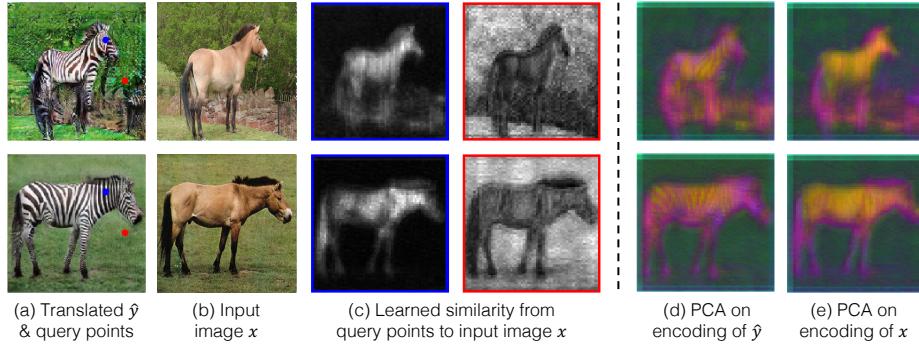


Fig. 7: **Visualizing the learned similarity by G_{enc} .** Given query points (blue or red) on an output image (a) and input (b), we visualize the learned similarity to patches on the input image by computing $\exp(\mathbf{v} \cdot \mathbf{v}^- / \tau)$ in (c). Here \mathbf{v} is the query patch in the output and \mathbf{v}^- denotes patches from the input. This suggests that our encoder may learn cross-domain correspondences implicitly. In (d) and (e), we visualize the top 3 PCA components of the shared embedding.

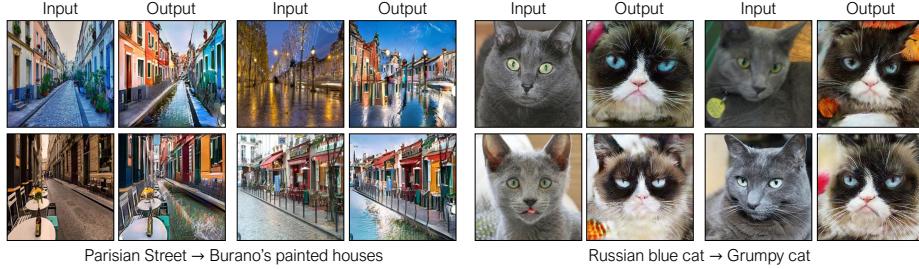


Fig. 8: **Additional applications** on Parisian street → Burano’s colored houses and Russian Blue cat → Grumpy cat.

scale the image to prevent overfitting. Furthermore, we observe that limiting the receptive field of the discriminator is important for preserving the structure of the input image, as otherwise the GAN loss will force the output image to be identical to the target image. Therefore, the crops are further split into 64×64 patches before passed to the discriminator. Lastly, we find that using gradient penalty [49,32] stabilizes optimization.

Figure 9 shows a qualitative comparison between our results and baseline methods including two neural style transfer methods (Gatys et al. [17] and STROTSS [35]), one leading photo style transfer method WCT² [74], and a CycleGAN baseline [81] that uses the ℓ_1 cycle-consistency loss instead of our contrastive loss at the patch level. The input paintings are high-res, ranging from 1k to 1.5k. Appendix B includes additional examples. We observe that Gatys et al. [17] fails to synthesize realistic textures. Existing photo style transfer methods such as WCT² can only modify the color of the input image. Our method outperforms CycleGAN and is comparable to a leading style transfer method [35], which is based on optimal transport and self-similarity. Interestingly, our method

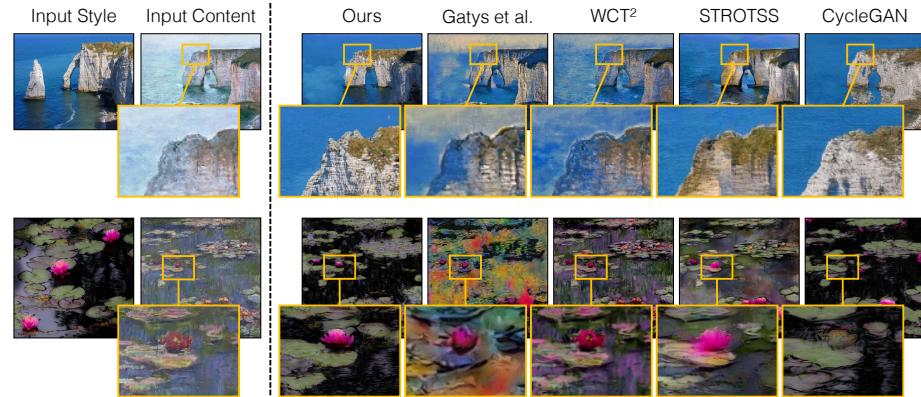


Fig. 9: **High-res painting to photo translation.** We transfer Claude Monet’s paintings to reference natural photographs. The training only requires a single image from each domain. We compare our results to recent style and photo transfer methods including Gatys et al. [17], WCT² [74], STROTSS [35], and patch-based CycleGAN [81]. Our method generates can reproduce the texture of the reference photo while retaining structure of input painting. Our generation is at 1k ~ 1.5k resolution.

is not originally designed for this application. This result suggests the intriguing connection between image-to-image translation and neural style transfer.

5 Conclusion

We propose a straightforward method for encouraging content preservation in unpaired image translation problems – by maximizing the mutual information between input and output with contrastive learning. The objective learns an embedding to bringing together corresponding patches in input and output, while pushing away noncorresponding “negative” patches. We study several important design choices. Interestingly, drawing negatives from *within* the image itself, rather than other images, provides a stronger signal. Our method learns a cross-domain similarity function and is the first image translation algorithm, to our knowledge, to not use any pre-defined similarity function (such as ℓ_1 or perceptual loss). As our method does not rely on cycle-consistency, it can enable one-sided image translation, with better quality than established baselines. In addition, our method can be used for *single-image* unpaired translation.

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