

# Atelier

# LATEX

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Quadratic Function

matematika.pl

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## Objectives

Objectives for today:

Introducing specific vocabulary.

- Quick revision of quadratic function.

- Factorising Quadratics.

- Proving Vieta's formulas.

- Carrying out gained knowledge by working out some word problems.

## Factorising a Quadratic

Factorising a quadratic means putting it into two brackets, and is useful if you're trying to draw a graph of a quadratic solve a quadratic equation. It's pretty easy if  $a = 1$  (in  $ax^2 + bx + c$  form), but can be a real pain otherwise.

In order to factorise a quadratic, you should follow steps outlined below:

- Rearrange the equation into the standard  $ax^2 + bx + c$  form.

- Write down two brackets:  $(x \quad)(x \quad)$
- Find two numbers that multiply to give 'c' and add or subtract to give 'b' (ignoring signs).
- Put the numbers in brackets and check their signs.

## Factorising

1. Factorise  $x^2 - x - 12$ .

2. Solve  $x^2 - 8 = 2x$  by factorising.

## Myth of Delta $\Delta$

It is commonly believed that in order to work out roots of a quadratic function you need to use the quadratic formula. However this is untrue since factorising in many cases is even better than simply counting  $\Delta$ .

## Example of Factorisation

Solve  $x^2 + 4x - 21 = 0$  by factorising.

$$x^2 + 4x - 21 = (x \quad)(x \quad)$$

1 and 21 multiply to give -21. 1 and 21 subtract to give 22 and 20. 3 and 7 multiply to give 21 and 4. 3 and 7 subtract to give -4 and -21.

$$x^2 + 4x + 21 = (x + 7)(x + 3)$$

In solving the equation:  $(x + 7)(x + 3) = 0$  we get  $x = -7$ ,  $x = -3$

## Proof of Vieta's Formulas

Let's prove that:

$$x_1 + x_2 = -\frac{b}{a}$$

When  $\Delta$  is positive we have two roots:  $x_1 = \frac{-b - \sqrt{\Delta}}{2a}$ ,  $x_2 = \frac{-b + \sqrt{\Delta}}{2a}$

Substituting for  $x_1$  and  $x_2$  respectively, we receive:

$$\begin{aligned} x_1 + x_2 &= \frac{-b - \sqrt{\Delta}}{2a} + \frac{-b + \sqrt{\Delta}}{2a} = \frac{-b - \sqrt{\Delta} - b + \sqrt{\Delta}}{2a} = \frac{-2b}{2a} = -\frac{b}{a} \end{aligned}$$

The same we could do with another root, which is going to be your task in next section.

## Some Necessary and Useful Vocabulary

- (n.) sign  $\rightarrow +$  or  $-$
- (n.) equation  $\rightarrow$  something  $= 0$
- (n.) factor  $\rightarrow$  two multiplied factors give result
- (v.) factorise  $\rightarrow$  putting into brackets
- (n.) coefficient  $\rightarrow$  a constant number i.e.  $a$ ,  $b$ ,  $c$  in a pattern  $ax^2 + bx + c$
- (n.) quadratic function  $\rightarrow f(x) = ax^2 + bx + c$
- (n.) root  $\rightarrow$  sth or solution of equation
- (n.) formula = pattern

