Movers

Theory of Computation, Spring 2024

Luca Di Bello, Agnese Zamboni, Dimitrios Pagonis, Georgy Batyrev ${\rm May}\ 21,\ 2024$

Contents

1	Pro	blem Description	2	
2	Mathematical representation			
	2.1	Input Parameters	3	
	2.2	Sets / Domains	3	
	2.3	Variables	3	
		2.3.1 Variables describing the state of the system	3	
		2.3.2 Variables describing the actions of the movers	3	
	2.4	Constraints	3	
		2.4.1 Action Definition	3	
		2.4.2 Initial and Final Constraints	4	
		2.4.3 Other Constraints	4	
3	System Design 7			
	3.1	Frontend - User Interface	7	
	3.2	Backend - APIs and Solver	8	
4	Hov	w to Get Started	10	
	4.1	Requirements	10	
	4.2	Step 1: Clone the repository	10	
	4.3	Step 2: Install Python requirements	10	
	4.4	Step 3: Run the backend	10	
5	Eva	aluation	11	

1 Problem Description

In the movers satisfiability problem, a moving company is tasked with relocating all furniture from a building with multiple floors. The objective is to move all furniture to the ground floor within a given time frame (maximum number of time steps). For this task, the company has a team of movers of size m, and each mover is identified with a unique name, and can move up or down one floor at a time.

The building has n floors, each identified by a unique integer number. The building contains a set of furniture F = f1, f2, ..., fn to be moved. Each piece of furniture is located within the floors of the building, and there could be more than one piece of furniture on the same floor. The movers are initially located on the ground floor of the building, and they must move all furniture to the ground floor within a given time frame. By the end of the time frame, all movers and all furniture must be located on the ground floor in order to solve the problem.

When a mover is on the same floor as a piece of furniture, and decides to carry it, the mover and the furniture in question are moved together to the floor below.

2 Mathematical representation

2.1 Input Parameters

- 1. $m \in \mathbb{N}^+$: number of movers
- 2. $n \in \mathbb{N}^+$: number of floors
- 3. $t_{max} \in \mathbb{N}^+$: maximum number of steps to solve the problem

2.2 Sets / Domains

- $M = \{m_1, m_2, ..., m_m\}$: set of movers
- $L = \{l_1, l_2, ..., l_n\}$: set of floors ("levels") in the building
- $F = \{f_1, f_2, ..., f_k\}$: set of forniture items
- $T = \{t_1, t_2, ..., t_{max}\}$: set of timestamps from 1 to t_{max}

2.3 Variables

2.3.1 Variables describing the state of the system

- $atFloor(m, l, t) \in \{0, 1\}$, True if mover m is at floor l at time t
- $atFloorForniture(f, l, t) \in \{0, 1\}$, True if forniture f is at floor l at time t

2.3.2 Variables describing the actions of the movers

- $ascend(m,t) \in \{0,1\}$, True if mover m is ascending at time t
- $descend(m,t) \in \{0,1\}$, True if mover m is descending at time t
- $carry(m, f, t) \in \{0, 1\}$, True if mover m is carrying forniture f at time t

2.4 Constraints

2.4.1 Action Definition

This section describes how the actions of the movers alter the state of the system.

1. ascend(m,t): a mover can move up one floor at a time (except when at the last floor)

$$l < n-1 \land atFloor(m,l,t) \land ascend(m,t) \implies atFloor(m,l+1,t+1)$$

 \forall mover $m \in M$, floor $l \in L$, time $t \in T$

2. descend(m,t): a mover can move down one floor at a time (except when at the ground floor)

$$l > 0 \land atFloor(m, l, t) \land descend(m, t) \implies atFloor(m, l - 1, t + 1)$$

 \forall mover $m \in M$, floor $l \in L$, time $t \in T$

3. carry(m, f, t): a mover can carry a piece of forniture if it is at the same floor as the mover. At the next time step, the mover and the forniture will be at the floor below (except when at the ground floor):

$$l > 0 \land atFloor(m, l, t) \land atFloorForniture(f, l, t) \land carry(m, f, t) \implies atFloor(m, l - 1, t + 1) \land atFloorForniture(f, l - 1, t + 1)$$

 \forall mover $m \in M$, forniture $f \in F$, floor $l \in L$, time $t \in T$

2.4.2 Initial and Final Constraints

1. Initial constraint: movers start at the ground floor

$$atFloor(m_i, 0, 0)$$

 \forall mover $m \in M$

2. Final constraint: movers end at the ground floor

$$atFloor(m, 0, t_{max}) \wedge atFloorForniture(f, 0, t_{max})$$

 \forall mover $m \in M$, forniture $f \in F$

2.4.3 Other Constraints

- 1. Each mover is exactly at one floor at a time
 - Each mover is at least at one floor

$$\bigvee_{m \in M, l \in L, t \in T} atFloor(m, l, t)$$

• A mover cannot be at more than one floor

$$atFloor(m, l_1, t) \implies \neg atFloor(m, l_2, t)$$

 \forall mover $m \in M$, floors $l_1 \neq l_2 \in L$, time $t \in T$

- 2. Each forniture is exactly at one floor at a time
 - Each forniture is at least at one floor

$$\bigvee_{f \in F, l \in L, t \in T} atFloorForniture(f, l, t)$$

• A forniture cannot be at more than one floor

$$atFloorForniture(f, l_1, t) \implies \neg atFloorForniture(f, l_2, t)$$

 \forall forniture $f \in F$, floors $l_1 \neq l_2 \in L$, time $t \in T$

3. If a mover is not ascending, descending, or carrying it stays at the same floor

$$atFloor(m,l,t) \land \neg ascend(m,t) \land \neg descend(m,t) \land \bigwedge_{f \in F} \neg carry(m,f,t) \implies atFloor(m,l,t+1)$$

 \forall mover $m \in M$, floor $l \in L$, time $t \in T$

4. If a forniture is not being carried, it stays at the same floor

$$atFloorForniture(f,l,t) \land \bigwedge_{m \in M} \neg carry(m,f,t) \implies atFloorForniture(f,l,t+1)$$

 \forall forniture $f \in F$, floor $l \in L$, time $t \in T$

- 5. Each mover can do only one action at a time
 - $ascend(m,t) \implies \neg descend(m,t)$
 - $ascend(m,t) \implies \neg carry(m,f,t)$
 - $descend(m,t) \implies \neg ascend(m,t)$
 - $descend(m,t) \implies \neg carry(m,f,t)$
 - $carry(m, f, t) \implies \neg ascend(m, t)$
 - $carry(m, f, t) \implies \neg descend(m, t)$

 \forall mover $m \in M$, floor $l \in L$, forniture $f \in F$, time $t \in T$

6. Each mover can carry at most one piece of forniture

$$carry(m, f_1, t) \implies \neg carry(m, f_2, t)$$

 \forall mover $m \in M$, forniture $f_1 \neq f_2 \in F$, time $t \in T$

7. A piece of forniture can be carried by only one mover

$$carry(m_1, f, t) \implies \neg carry(m_2, f, t)$$

 \forall mover $m_1 \neq m_2 \in M$, forniture $f \in F$, time $t \in T$

8. Movers cannot ascend if they are at the top floor

$$atFloor(m, n-1, t) \implies \neg ascend(m, t)$$

 \forall mover $m \in M$, time $t \in T$

9. Movers cannot descend if they are at the ground floor

$$atFloor(m, 0, t) \implies \neg descend(m, t)$$

 \forall mover $m \in M$, time $t \in T$

10. A mover has to be on the same floor as an item in order to carry it

$$atFloor(m, l_1, t) \land atFloorForniture(f, l_2, t) \implies \neg carry(m, f, t)$$

 \forall mover $m \in M,$ floors $l_1 \neq l_2 \in L$, for niture $f \in F,$ time $t \in T$

11. A mover cannot carry an item which is at the ground floor

$$atFloorForniture(f, 0, t) \implies \neg carry(m, f, t)$$

 $\forall \text{ mover } m \in M \text{, for$ $niture } f \in F \text{, time } t \in T$

3 System Design

The system has been divided into a frontend and a backend. The frontend is responsible for receiving the problem instance from the user and sending it to the backend for processing. The backend will receive the problem data from a specialized API and will solve the problem using the z3-solver. The solution will be sent back to the frontend as a response.

In the following sections, the frontend and backend will be described in more detail.

3.1 Frontend - User Interface

The frontend of our system is built using Chakra UI, a simple, modular, and accessible component library that provides the building blocks needed to build React applications. Chakra UI ensures a consistent look and feel across the application and enhances the development experience with its extensive set of customizable components.

To facilitate interaction with the backend API, we have implemented a custom library. This library simplifies API calls and manages the communication between the frontend and backend, ensuring a seamless and efficient data exchange.

The user initiates the process by composing a form in the React-app. This form contains information about the problem setup, such as the number of movers, floors, maximum steps, and furniture details. Once the form is completed, the React-app sends an HTTP POST request to the backend solver service at the /solve endpoint. This request includes the data provided by the user. This form is used to validate user inputs before sending data to the backend. It ensures that the data received by the backend is correct and reduces the likelihood of errors, providing a smoother user experience.

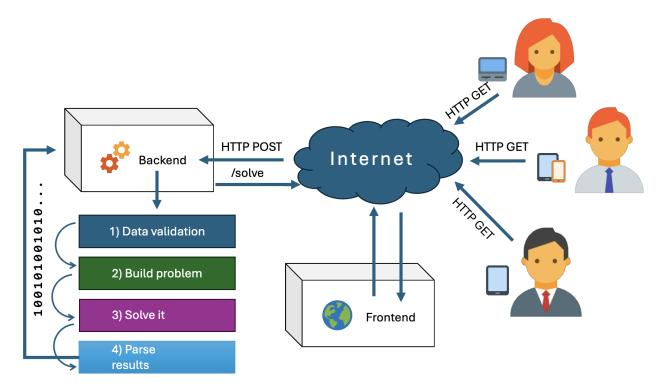


Figure 1: Diagram of the User Interface

3.2 Backend - APIs and Solver

The backend, as previously mentioned, is responsible for receiving the problem instance from the frontend and solving it using the z3-solver. The backend exposes a single endpoint /solve which receives a JSON object containing the problem instance and returns a JSON object with the solution.

This is the structure of a call to the /solve endpoint on the backend started on the local machine:

```
curl -X POST -H "Content-Type: application/json" \
     --data '{"max_t": 10, "furniture": [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]}' \
     http://localhost:5000/solve?m=2&n=5&max_t=10
```

The sequence diagram in Figure 2 illustrates the interaction between a user, the React-app frontend via Custom API, and the backend solver service in a Movers SAT problem-solving application.

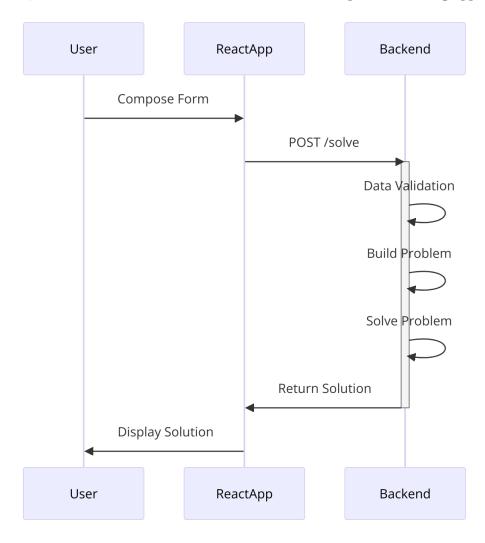


Figure 2: Sequence Diagram

Below is a step-by-step explanation of the process:

1. Backend Solver Service:

• Upon receiving the request, the backend solver service is activated and begins processing the request.

- Data Validation: The backend performs data validation to ensure that the input parameters (number of movers, floors, maximum steps, and furniture details) are valid and correctly formatted.
- **Problem Building**: After successful validation, the backend constructs the problem by defining the necessary constraints and setup required to solve the Movers SAT problem.
- **Problem Solving**: The backend then runs the solver to compute the solution to the problem. This involves calculating the optimal steps and actions needed to move the furniture as specified.

2. Response to React-app:

• Once the problem is solved, the backend sends the solution back to the React-app. This response includes the computed steps and actions for the movers and furniture.

3. Display Solution:

• The React-app receives the solution and displays it to the user. The user can now see the detailed steps and actions taken to solve the Movers SAT problem.

This diagram captures the entire workflow from user input to solution display, highlighting the key interactions and processes involved in solving the Movers SAT problem using the React-app and backend solver service.

4 How to Get Started

This guide will help you to install the tool and run your first network.

4.1 Requirements

- Python 3.6 or higher
- pip (Python package manager) or conda (Anaconda package manager)

4.2 Step 1: Clone the repository

You can clone the repository using git:

```
# With SSH
git clone git@github.com:lucadibello/movers-sat-problem.git && cd movers-sat-problem
# With HTTPS
git clone https://github.com/lucadibello/movers-sat-problem.git && cd movers-sat-
    problem
```

4.3 Step 2: Install Python requirements

To install the required Python packages, you can either use pip (to install the packages globally) or use conda (preferred method) to create a virtual environment and install the packages locally.

Option A: Using conda

```
# Create virtual environment + install packages
conda env create --file=environment.yml
# Activate the virtual environment
conda activate movers
```

Option B: Using pip

```
# Install the required packages
pip install -r requirements.txt
```

4.4 Step 3: Run the backend

```
# Start the backend in production mode
cd ./src/backend && make start
  or, if you want to start the backend in development mode (with fast refresh):
# Start the backend in development mode
cd ./src/backend && make dev
```

5 Evaluation

First of all, we needed to thoroughly understand the problem at hand. To achieve this, we organized a comprehensive discussion involving all team members. This discussion aimed to elucidate the various aspects of the problem, ensuring that everyone had a clear and vivid understanding of the issue. We explored different perspectives, asked clarifying questions, and shared relevant insights, all of which contributed to a more profound and collective grasp of the problem's intricacies. Then we divided into smaller groups so that we could work on frontend and backend at the same time.

General Problems:

1. We encountered some difficulty in identifying all the edge cases of the problem due to the lack of clarity in certain descriptions.

2.

Frontend Problems:

1. Due to our initial unfamiliarity with the React library, we required a considerable amount of time to learn how to utilize it effectively to achieve the desired results.

Backend Problems:

1.