

TEXTURE, RESIDUAL STRESS AND STRUCTURAL ANALYSIS OF THIN FILMS USING A COMBINED X-RAY ANALYSIS

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Rietveld Texture Analysis (RiT)

- **Goals:**

- *Obtain structure, microstructure, texture and residual stresses of thin films and multilayer by one step methodology*
- *The analysis should not be limited by phase overlapping, strong texture or complex structures*

- **How? -> Rietveld based analysis or full pattern fitting**

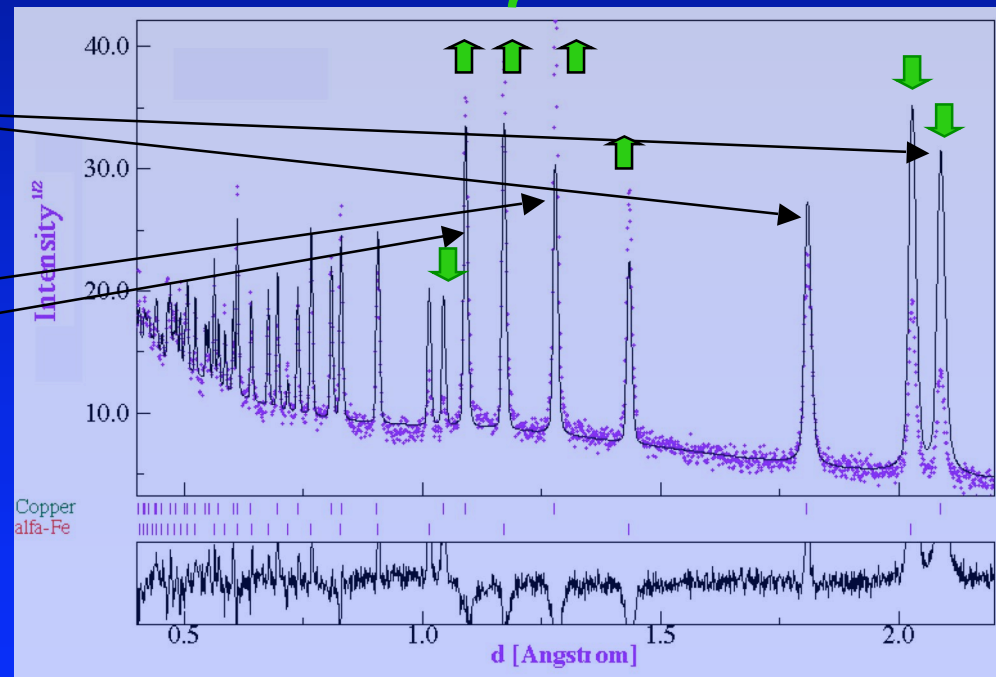
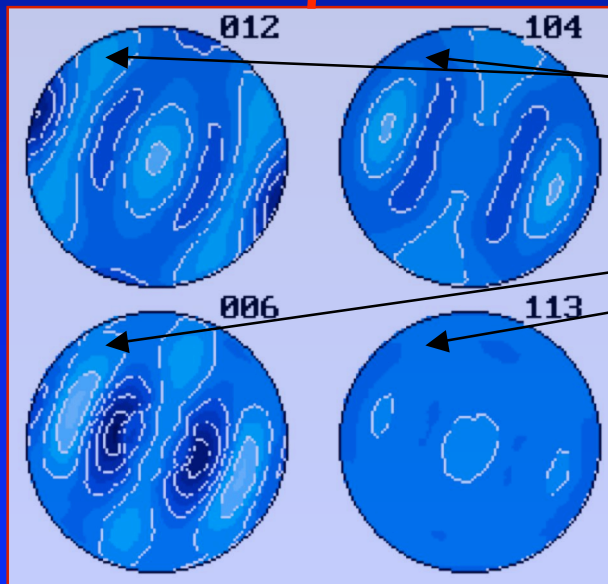
- *The Rietveld method is a powerful fitting method of the diffraction pattern to refine the crystal structure.*
- *We select and develop some particular methodologies for the analyses.*
- *We incorporate in a Rietveld package all these methodologies from microstructure to texture, residual stress and reflectivity.*
- *We build a machine to collect several full XRD spectra at different tilting position of the sample and reflectivity pattern.*
- *The final program is Maud, developed inside the ESQUI European project*

Texture from Spectra

Orientation Distribution Function (ODF)

From pole figures

From spectra



How it works (RiT)

The equation:

$$I_i^{calc}(\chi, \phi) = \sum_{n=1}^{Nphases} S_n \sum_k L_k |F_{k;n}|^2 S(2\theta_i - 2\theta_{k;n}) P_{k;n}(\chi, \phi) A + bkg_i$$

Harmonic:

$$P_k(\chi, \phi) = \sum_{l=0}^{\infty} \frac{1}{2l+1} \sum_{n=-l}^l k_l^n(\chi, \phi) \sum_{m=-l}^l C_l^{mn} k_n^{*m}(\Theta_k \phi_k)$$

$$f(g) = \sum_{l=0}^{\infty} \sum_{m,n=-l}^l C_l^{mn} T_l^{mn}(g)$$

- C_l^{mn} are additional parameters to be refined
- Data (reflections, number of spectra) sufficient to cover the ODF
- **Pro:**
 - Easy implementation
 - Very elegant, completely integrated in the Rietveld
 - Fast, low memory consumption to store the ODF.
- **Cons:**
 - No automatic positive condition (ODF > 0)
 - Not for sharp textures
 - Low symmetries -> too many coefficients to refine (where are the advantages?)
 - Memory hog for refinement.
 - No ghost correction.

How it works (RiT)

- **WIMV**

- *Discrete method. ODF space is divided in regular cells (ex. 5x5x5 degrees) and the function value is stored for each cell.*
- *Numerical integration:*
- *For each refinement iteration:*
 - *P_k extracted (Le Bail method)*
 - *ODF computed (WIMV)*
 - *P_k recalculated*
 - *Fitting of the spectra*
- *Advantages:*
 - *ODF > 0, always*
 - *Ok for sharp textures and low symmetries*
- *Disadvantages:*
 - *Less elegant (require extraction and interpolation to a regular grid)*
 - *Tricky to implement*
 - *Slower in the Rietveld (high symmetries)*

$$P_k(\chi, \phi) = \int_{\varphi} f(g, \varphi) d\varphi$$

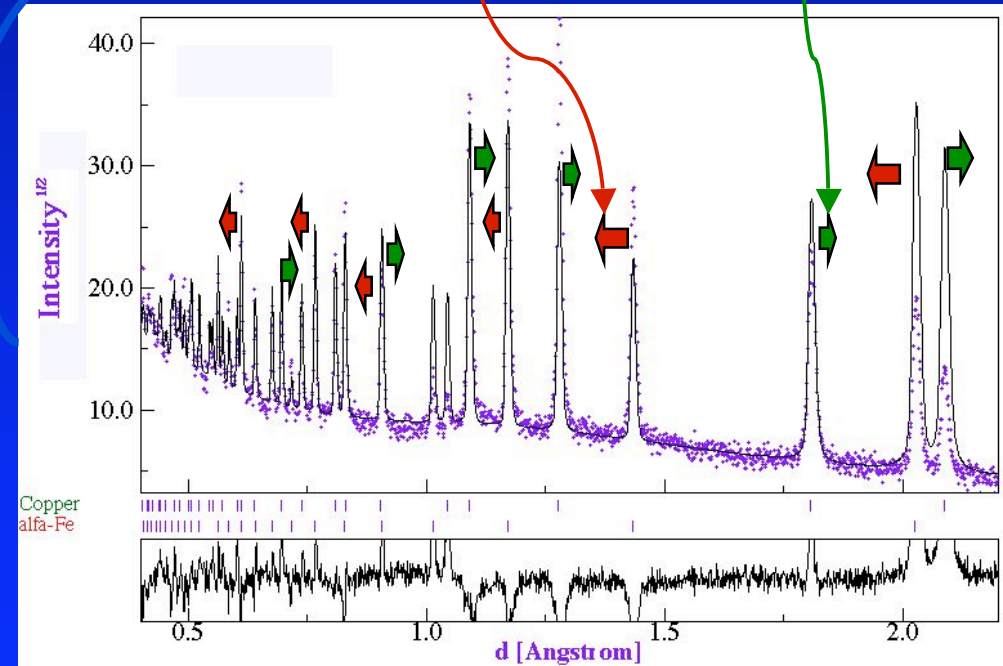
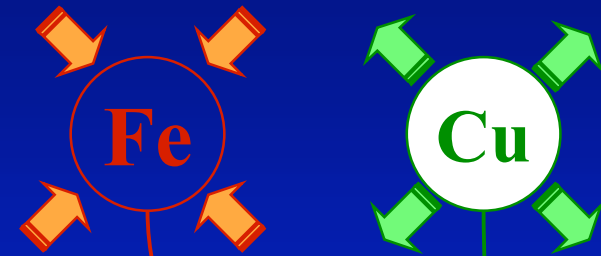
Residual Stresses and Rietveld

- Macro elastic strain tensor (I kind)
- Crystal anisotropic strains (II kind)

C

Macro and micro stresses

Applied macro stresses



Methodology implementation

Maud program:

■ Rietveld based analysis software:

- Crystal structure
- Microstructure
- Quantitative phase analysis
- Layered sample model

■ Texture:

- WIMV
- E-WIMV (modified)
- Harmonic

■ Residual Stresses

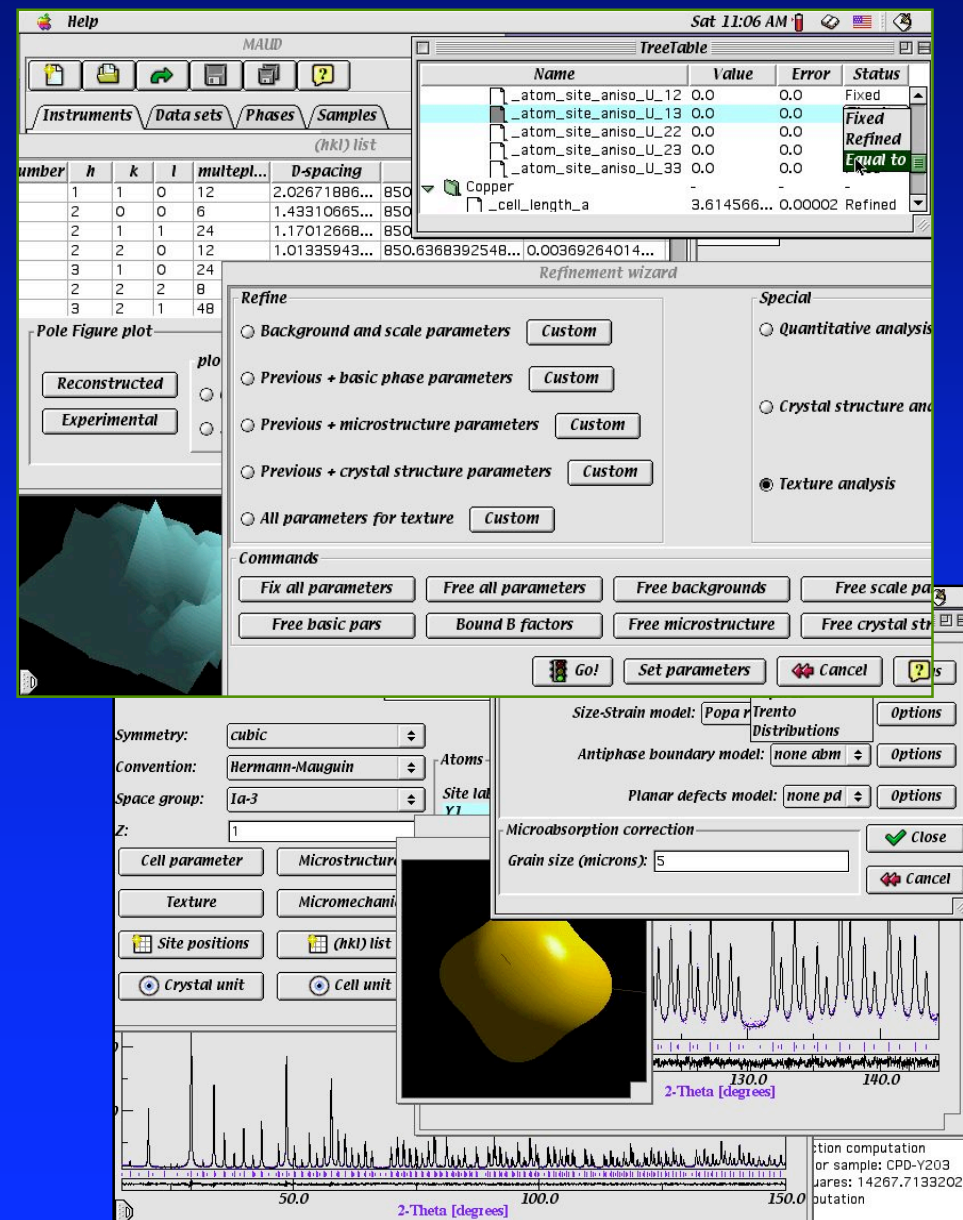
- No texture: triaxial tensor
- With texture: Reuss, Voigt, Geometrical mean

■ Reflectivity

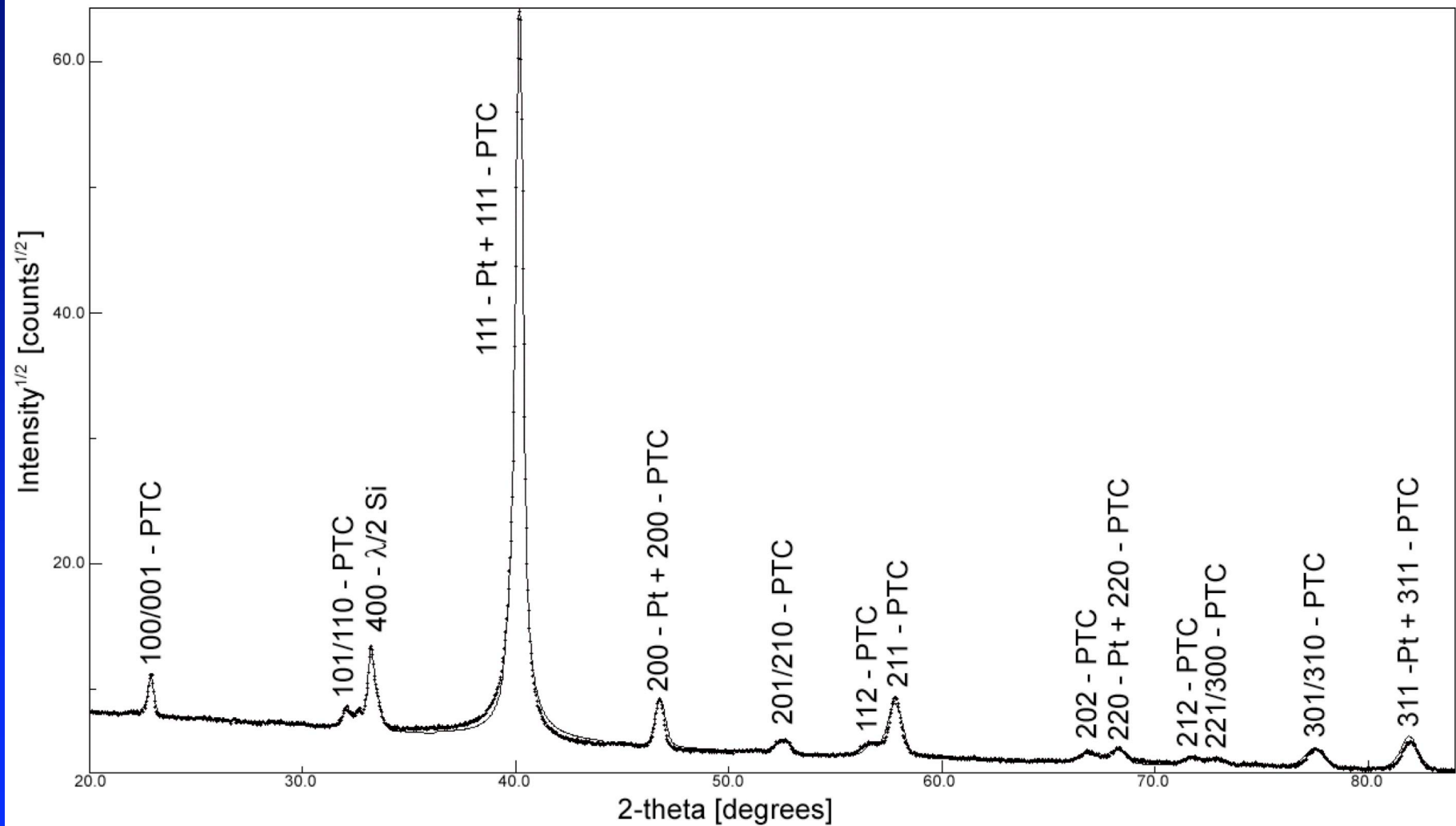
- Matrix method
- DWBA LS fit (electron density profile)
- Genetic algorithm

■ <http://www.ing.unitn.it/~luttero/maud>

■ Supported by: ESQUI European project

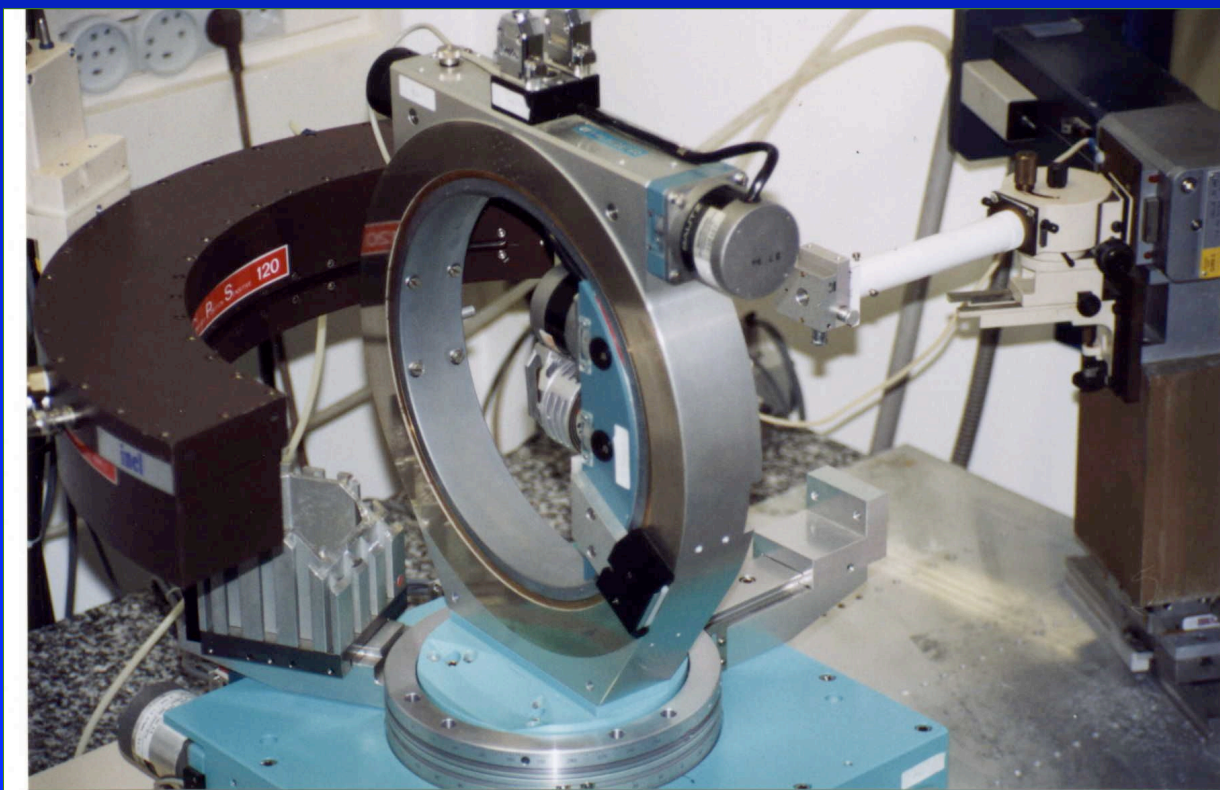


PTC film: the overlapping problem



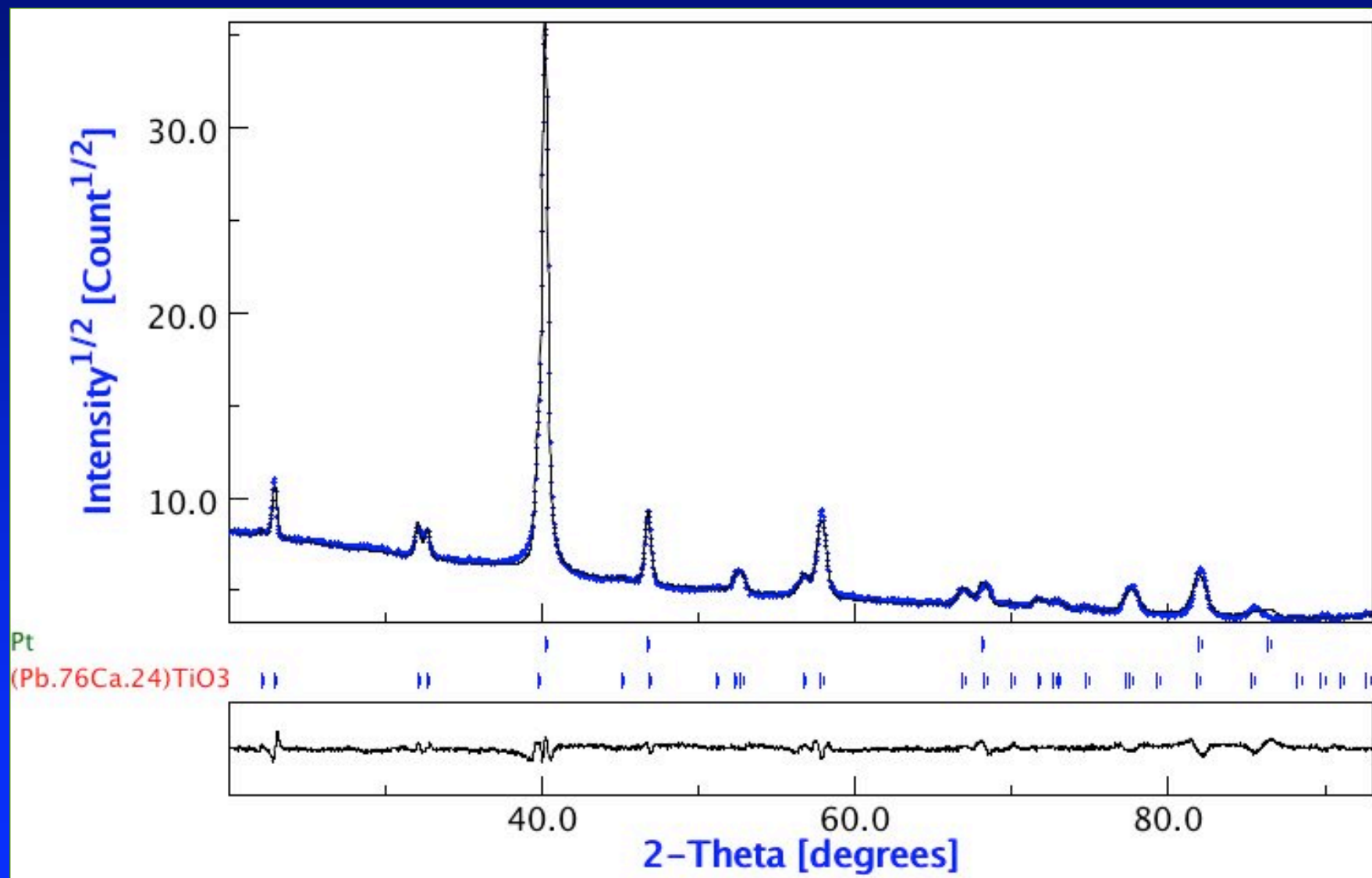
PTC film: the measurement

- *Substrate: $\text{TiO}_2/\text{SiO}_2/\text{Si}(100)$*
- *400 nm of $\text{Pb}_{0.76}\text{Ca}_{0.24}\text{TiO}_3$ (PTC) film deposited by spin coating of a sol-gel solution (CSIC Madrid).*
- *50 nm of Pt buffer layer.*
- *Instrument: 120 degs curved position sensitive detector on a closed eulerian cradle, graphite primary monochromator (LPEC - Le Mans, France)*
- *Collected full spectra on a 5x5 degs grid in chi and phi. From 0 to 355 in phi and up to 50 deg in chi.*



The LPEC, Le Mans instrument

PTC and Pt phase separation



PTC film: harmonic texture model

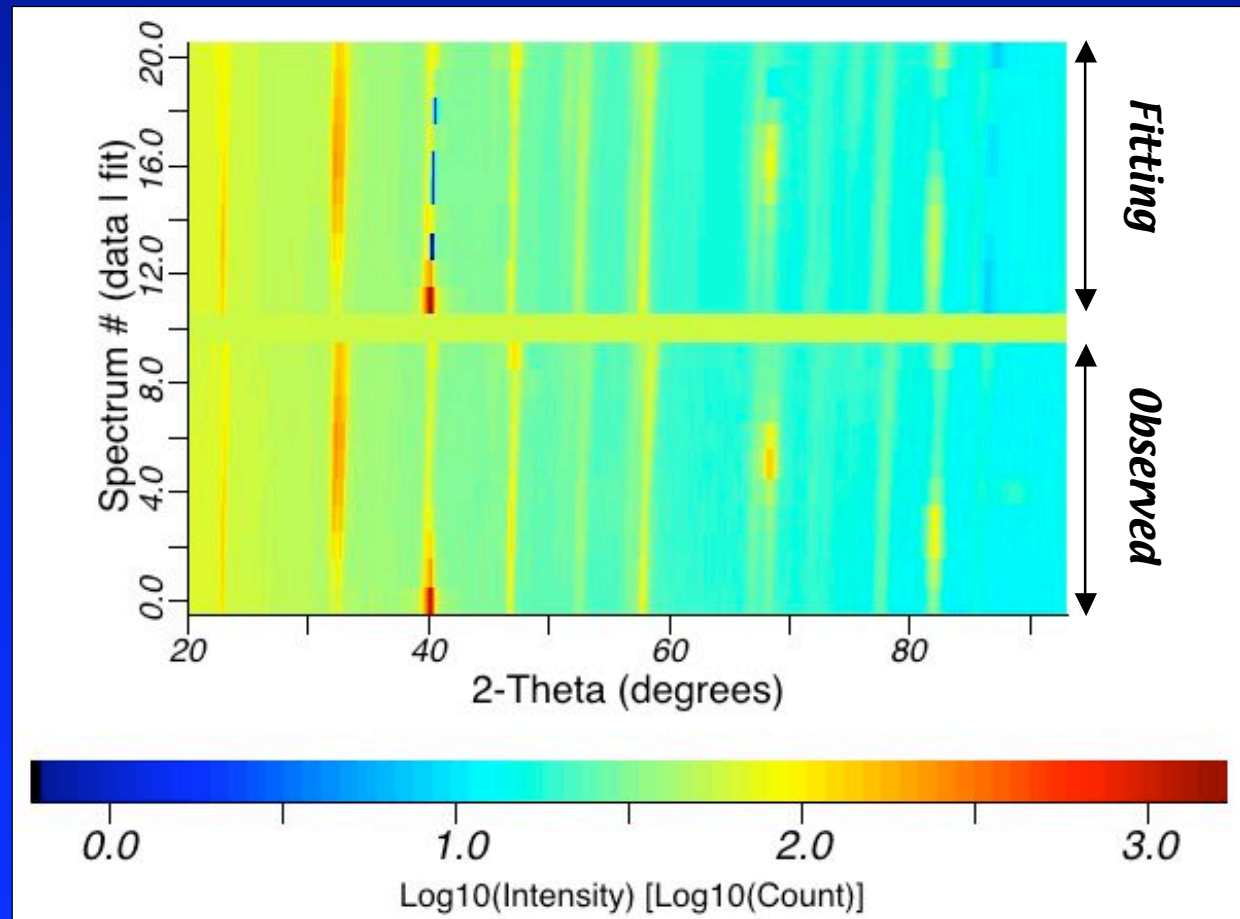
Triclinic sample symmetry: 1245 parameters only for PTC ($L_{\max} = 22$)

Increasing sample symmetry to orthorhombic: 181 parameters

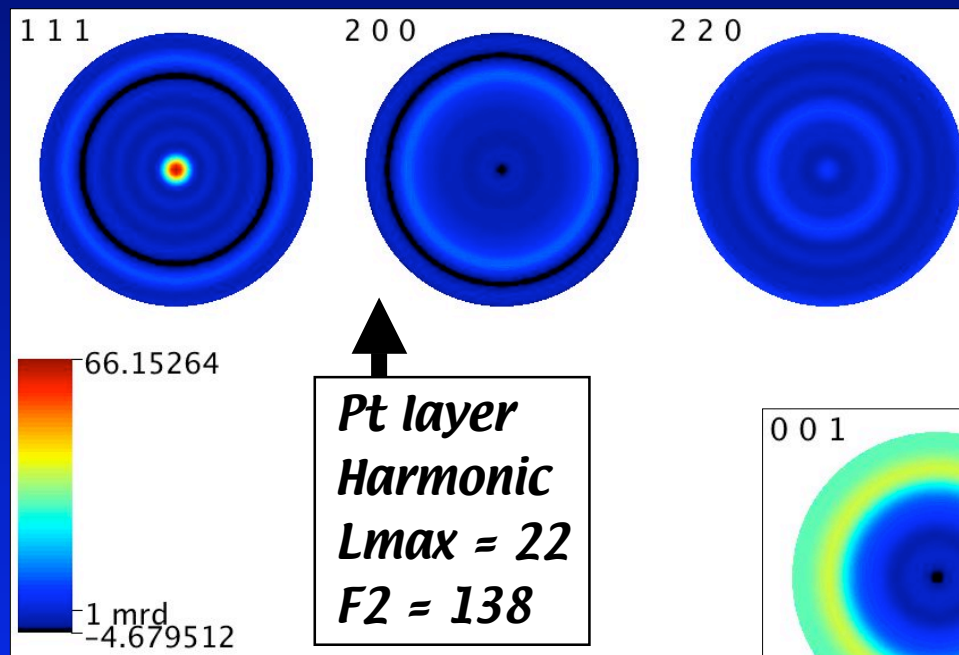
Reducing sample symmetry to fiber and L_{\max} to 16: 24 parameters

For Pt layer: fiber texture, $L_{\max} = 22 \rightarrow 15$ parameters

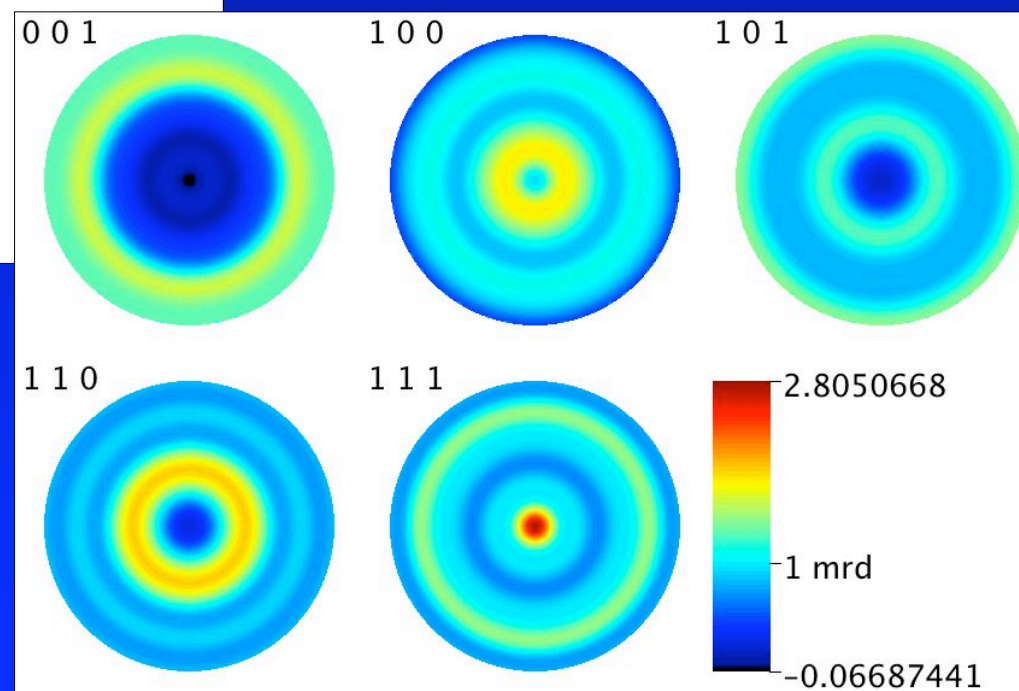
Rw (%) = 14.786048



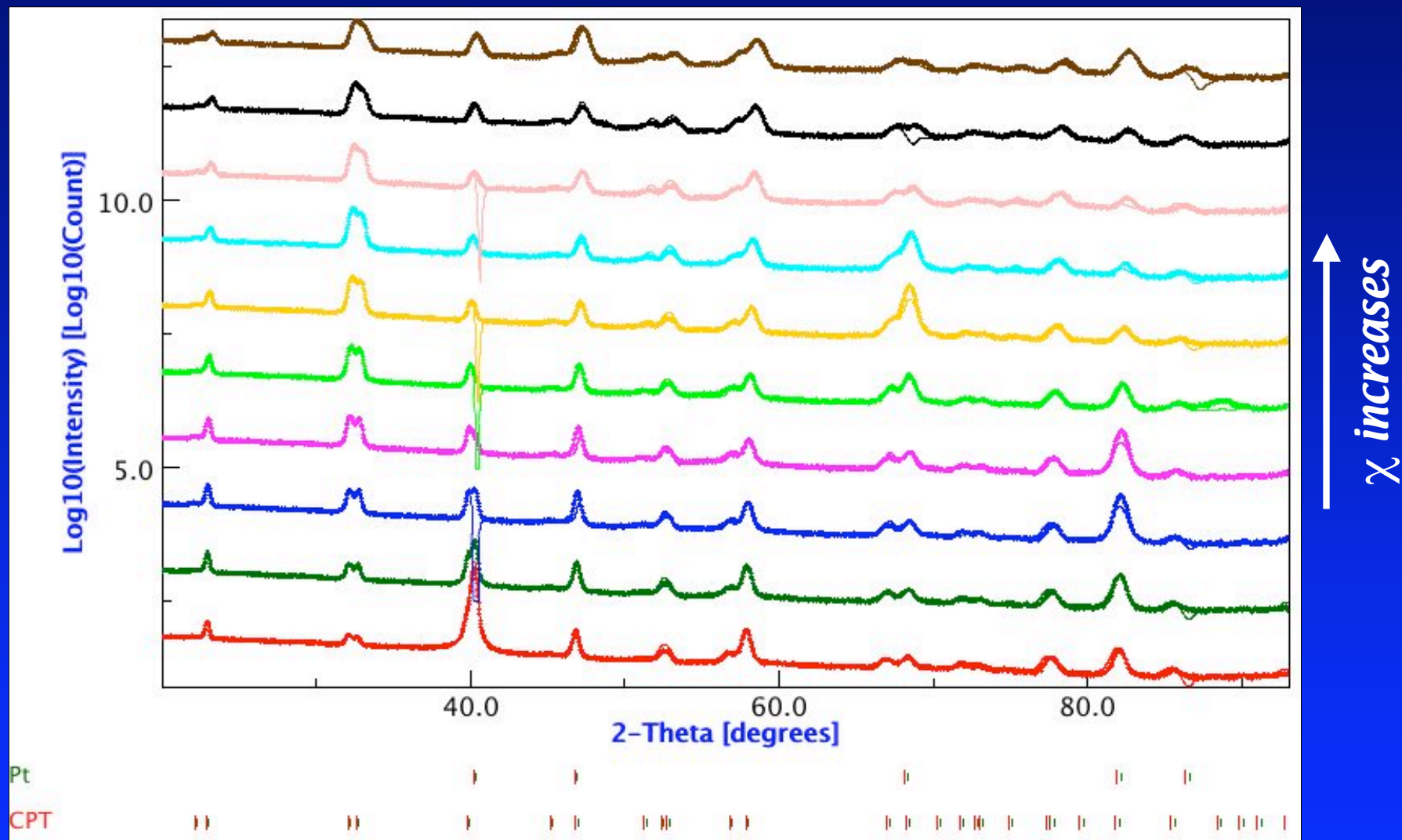
PTC film: harmonic reconstructed pole figures



CPT layer
Harmonic method
 $L_{max} = 16$
 $F2 = 1.55$



PTC film: harmonic fitting, the “Ghost” problem



PTC film fitting: WIMV

WIMV

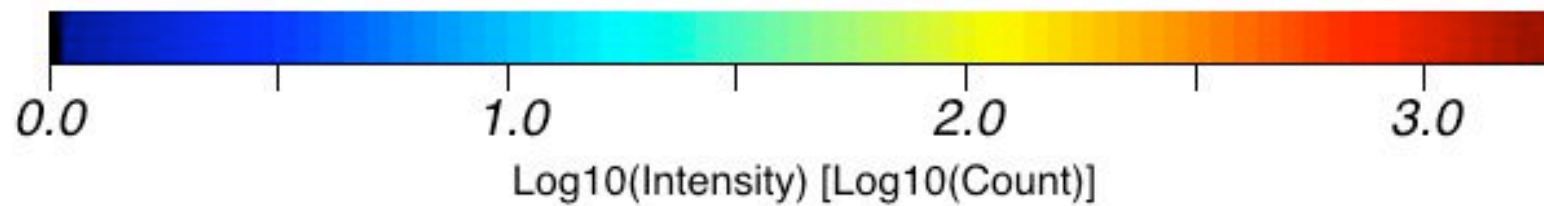
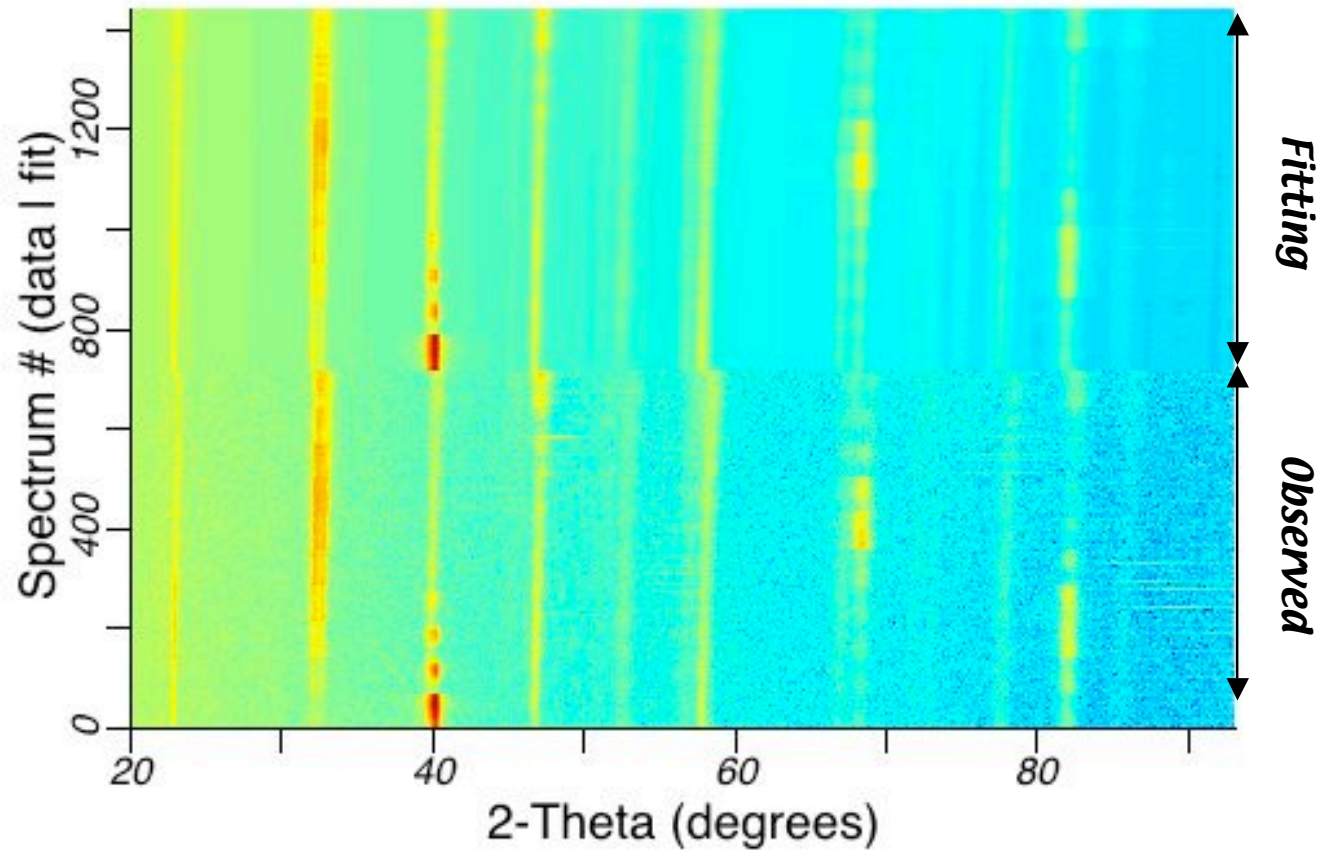
2 layers

2 phases

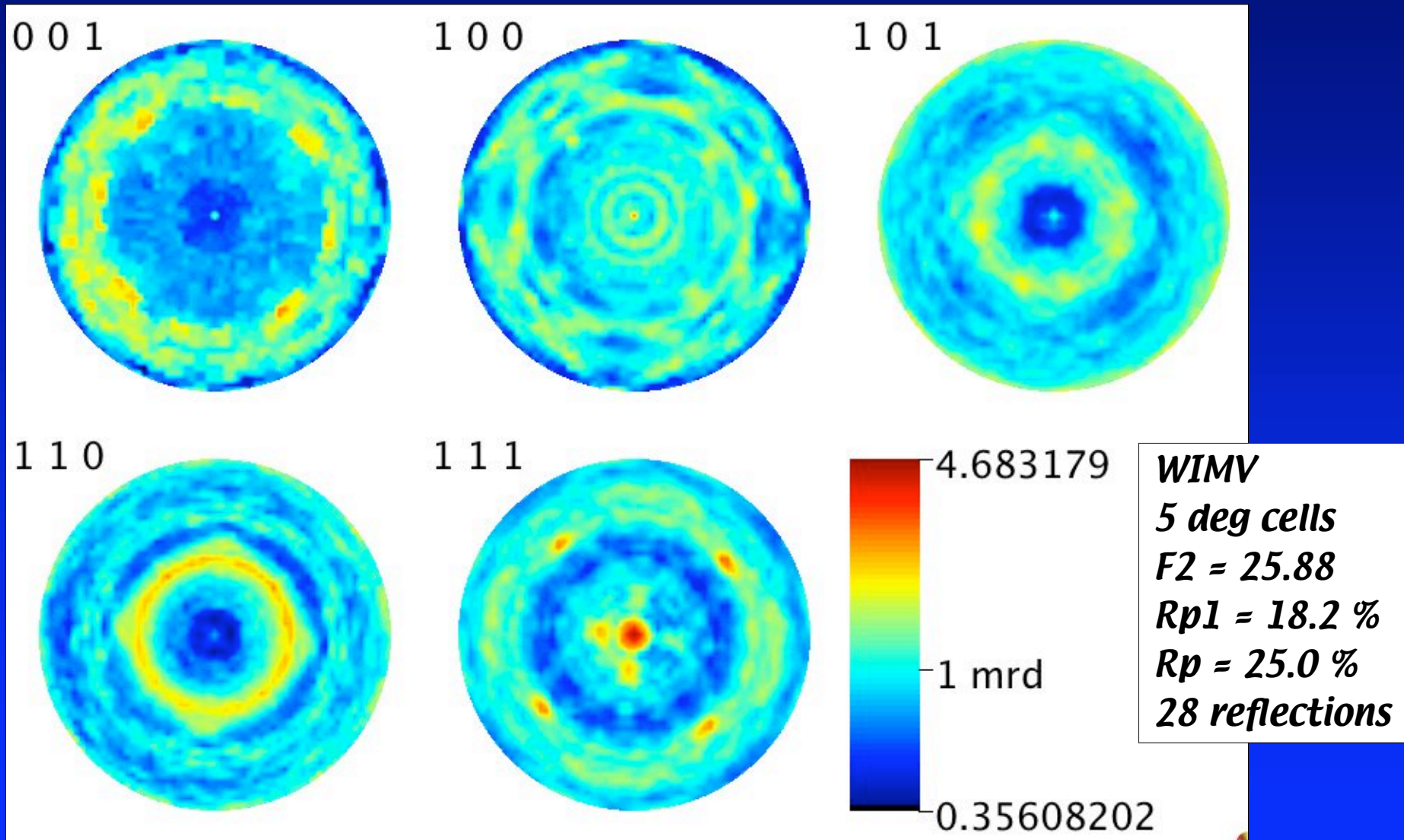
$R_w = 25.5\%$

$R = 42.6\%$

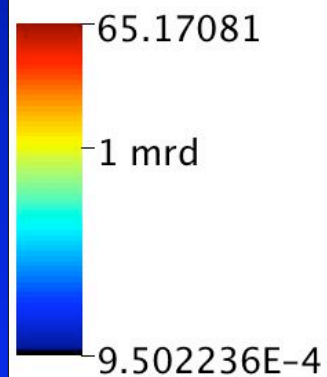
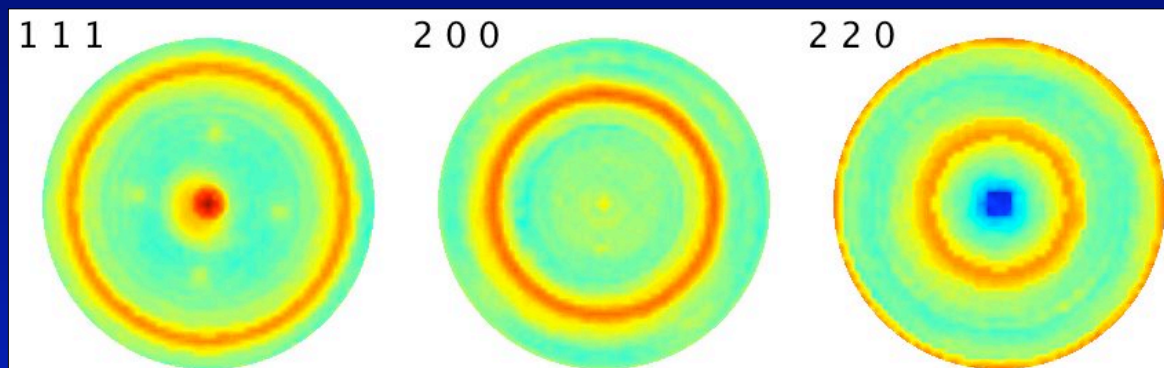
792 spectra



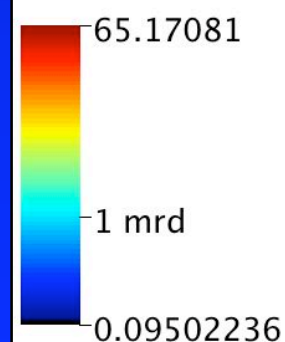
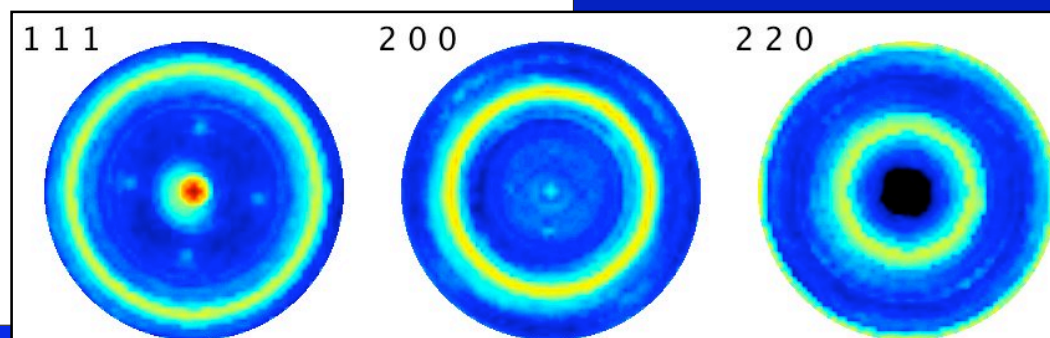
PTC film: CPT reconstructed pole figures, WIMV



PTC film: reconstructed Pt pole figures, WIMV



WIMV
5 deg cells
F2 = 2.13
Rp1 = 27.3 %
Rp = 28.6 %
5 reflections



Rescaled for comparison

E-WIMV

Modified WIMV algorithm for Rietveld Texture Analysis

Differences respect to WIMV:

- *ODF cell path computed for each measured point (no interpolation of pole figures on a regular grid)*
- *Different cell sizes available (Ex: 15, 10, 7.5, 5, 2.5, 1.25, 1.....) in degs.*
- *Tube projection computation (similar to the ADC method)*
- *Minimization engine more entropy like*

Problems:

- *Path computation is slow for low symmetries (high number of data)*

PTC film fitting: E-WIMV

E-WIMV

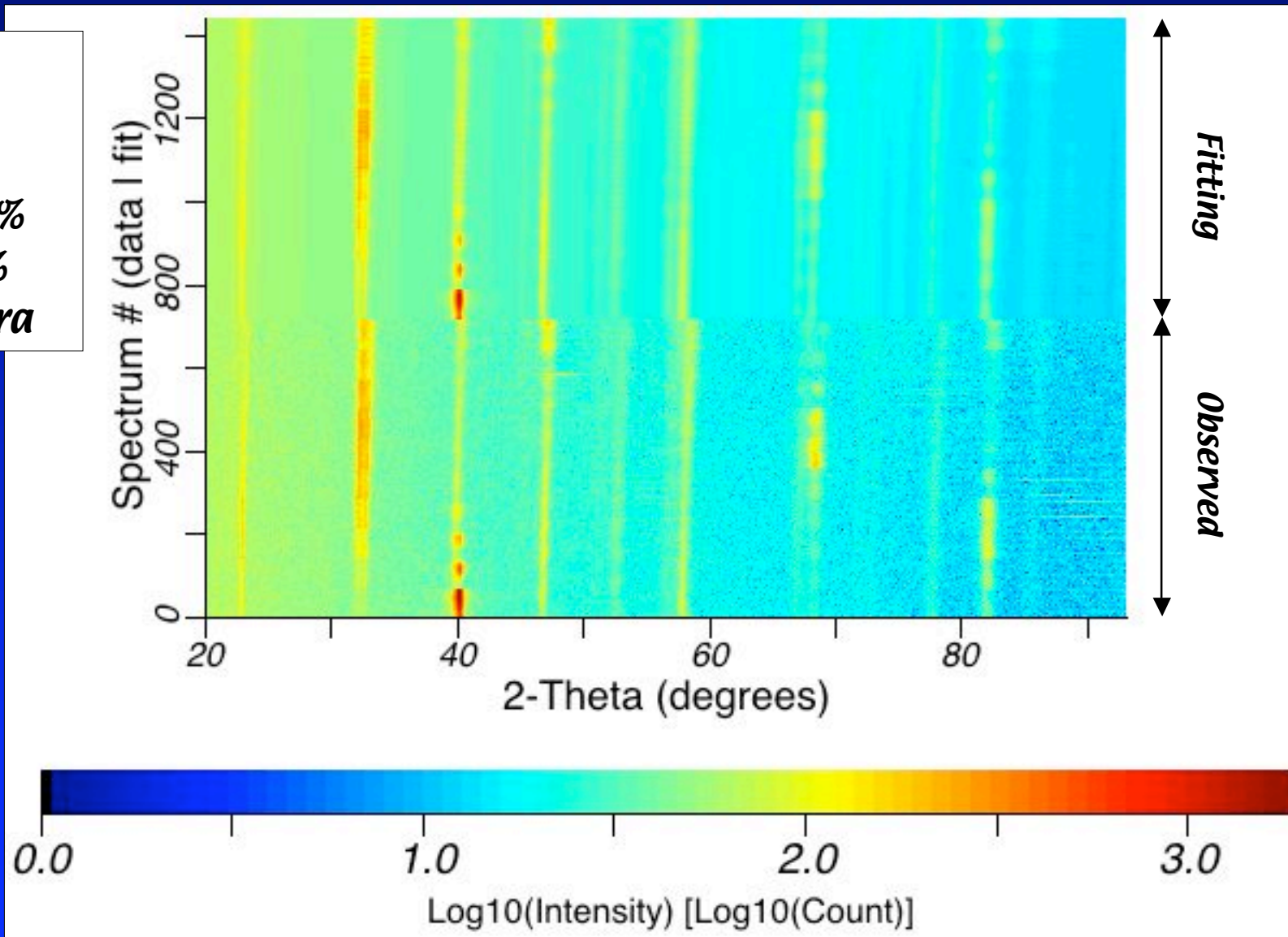
2 layers

2 phases

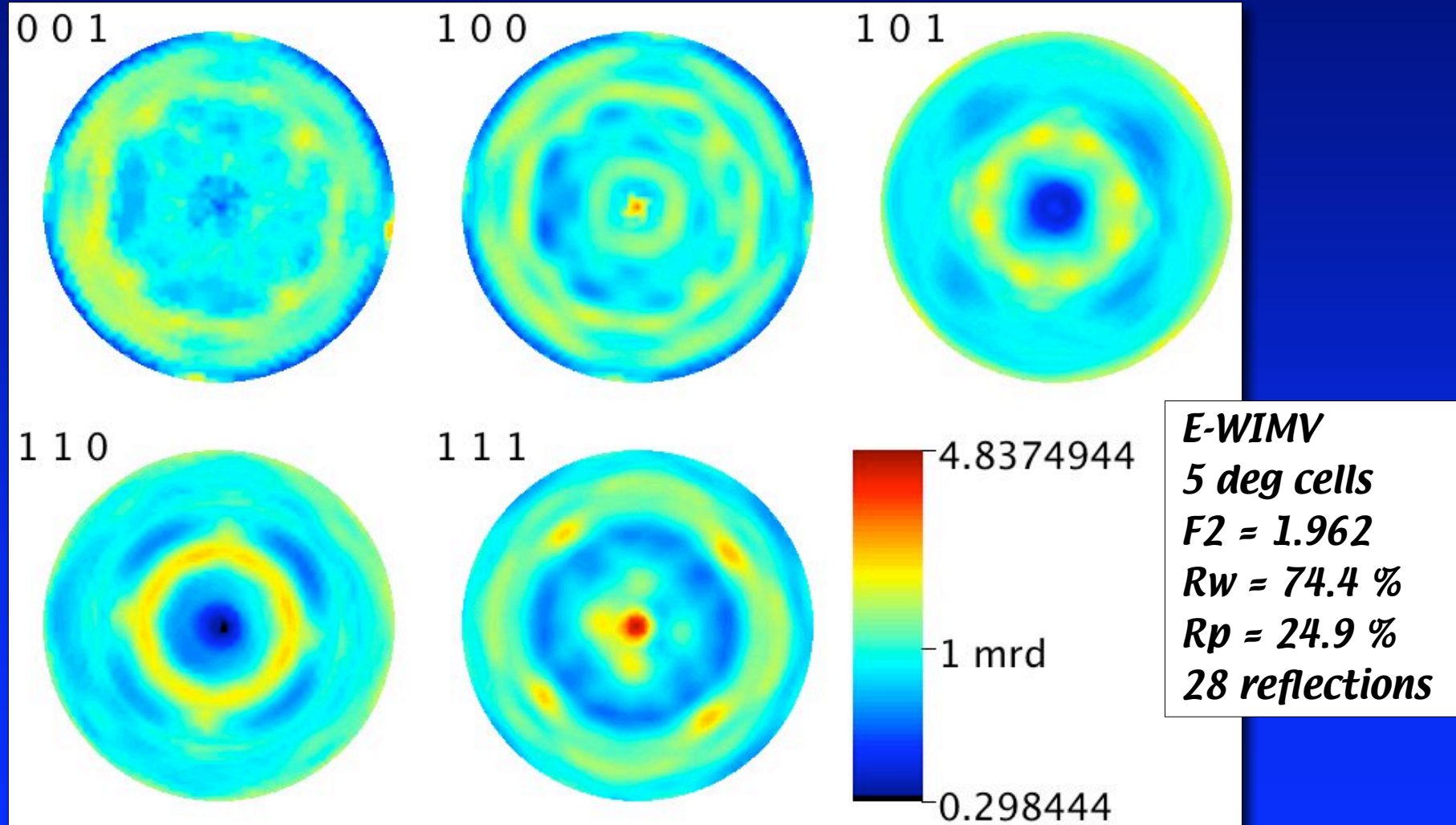
R_w = 21.7%

R = 40.0 %

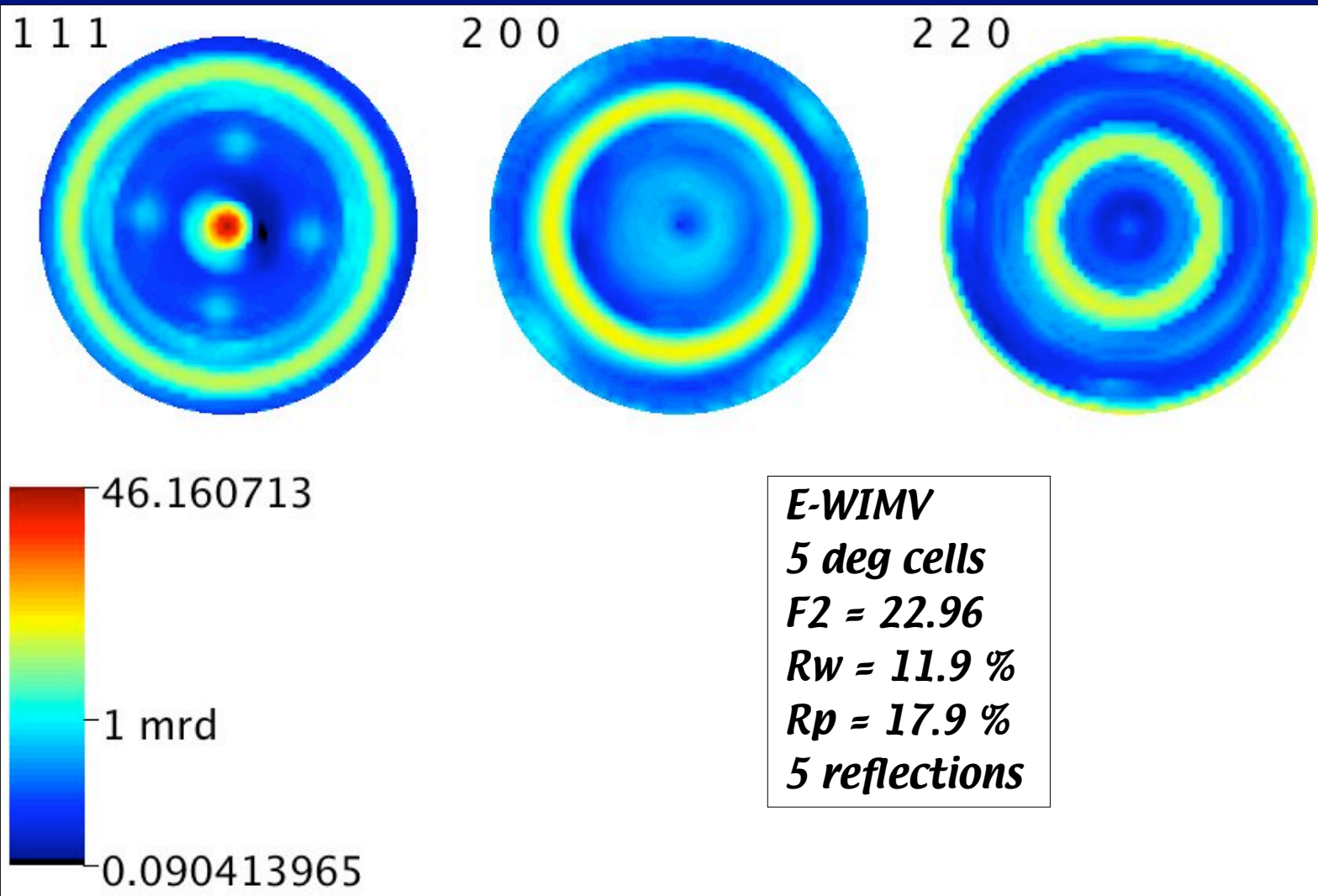
792 spectra



PTC film: PTC reconstructed pole figures



Pt buffer layer: reconstructed pole figures



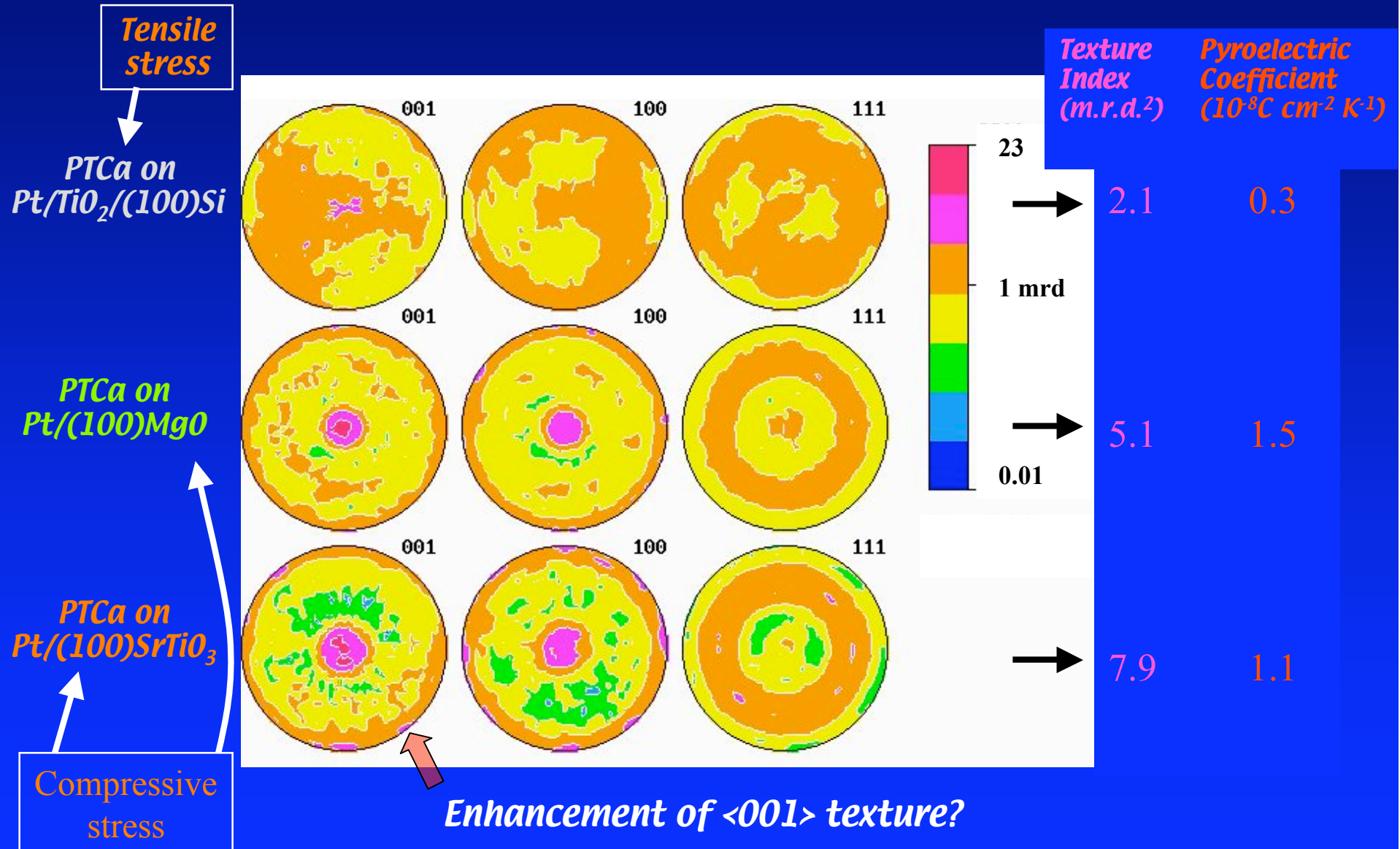
Results on the PTC film

Layer/Phase	Cell parameters (Å)	Cryst. Size (Å)	r.m.s. microstrain	Layer thickness (Å)
Pt	3.955(1)	462(4)	0.0032(1)	458(3)
PTC	a=3.945(1) c=4.080(1)	390(7)	0.0067(1)	4080(1)

PTC crystal structure

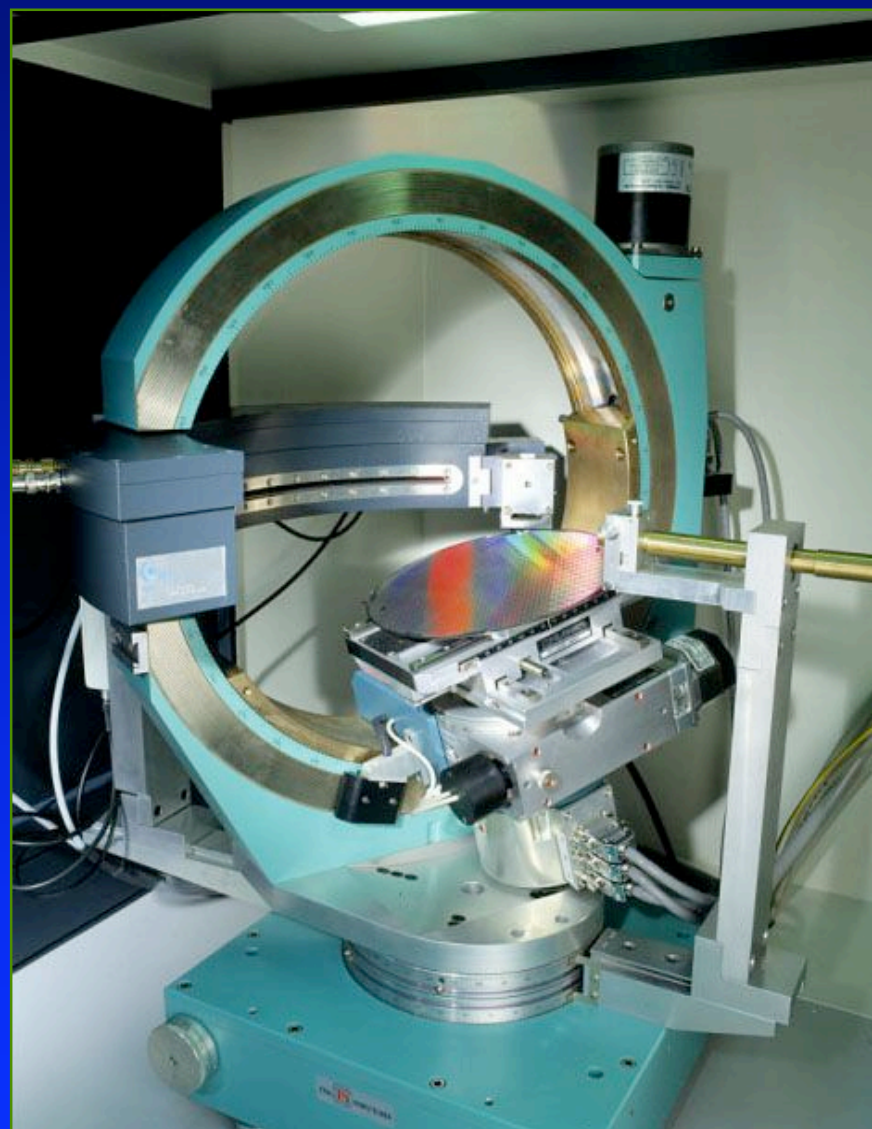
<i>Atom</i>	<i>Occupancy</i>	<i>x</i>	<i>y</i>	<i>z</i>
<i>Pb</i>	<i>0.76</i>	<i>0.0</i>	<i>0.0</i>	<i>0.0</i>
<i>Ca</i>	<i>0.24</i>	<i>0.0</i>	<i>0.0</i>	<i>0.0</i>
<i>Ti</i>	<i>1.0</i>	<i>0.5</i>	<i>0.5</i>	<i>0.477(2)</i>
<i>O1</i>	<i>1.0</i>	<i>0.5</i>	<i>0.5</i>	<i>0.060(2)</i>
<i>O2</i>	<i>1.0</i>	<i>0.0</i>	<i>0.5</i>	<i>0.631(1)</i>

Substrate influence on Residual Stress and Texture

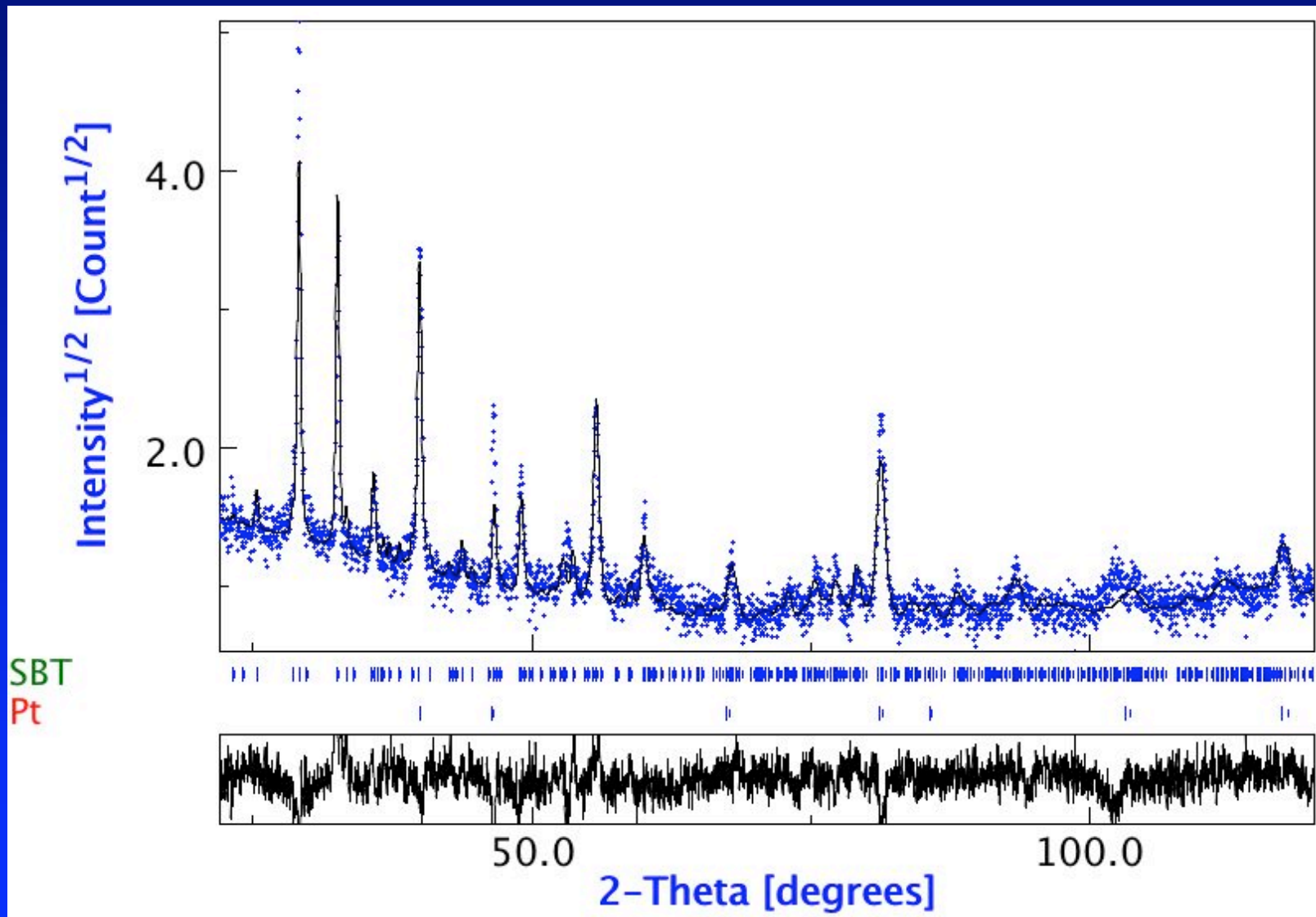


SBT film

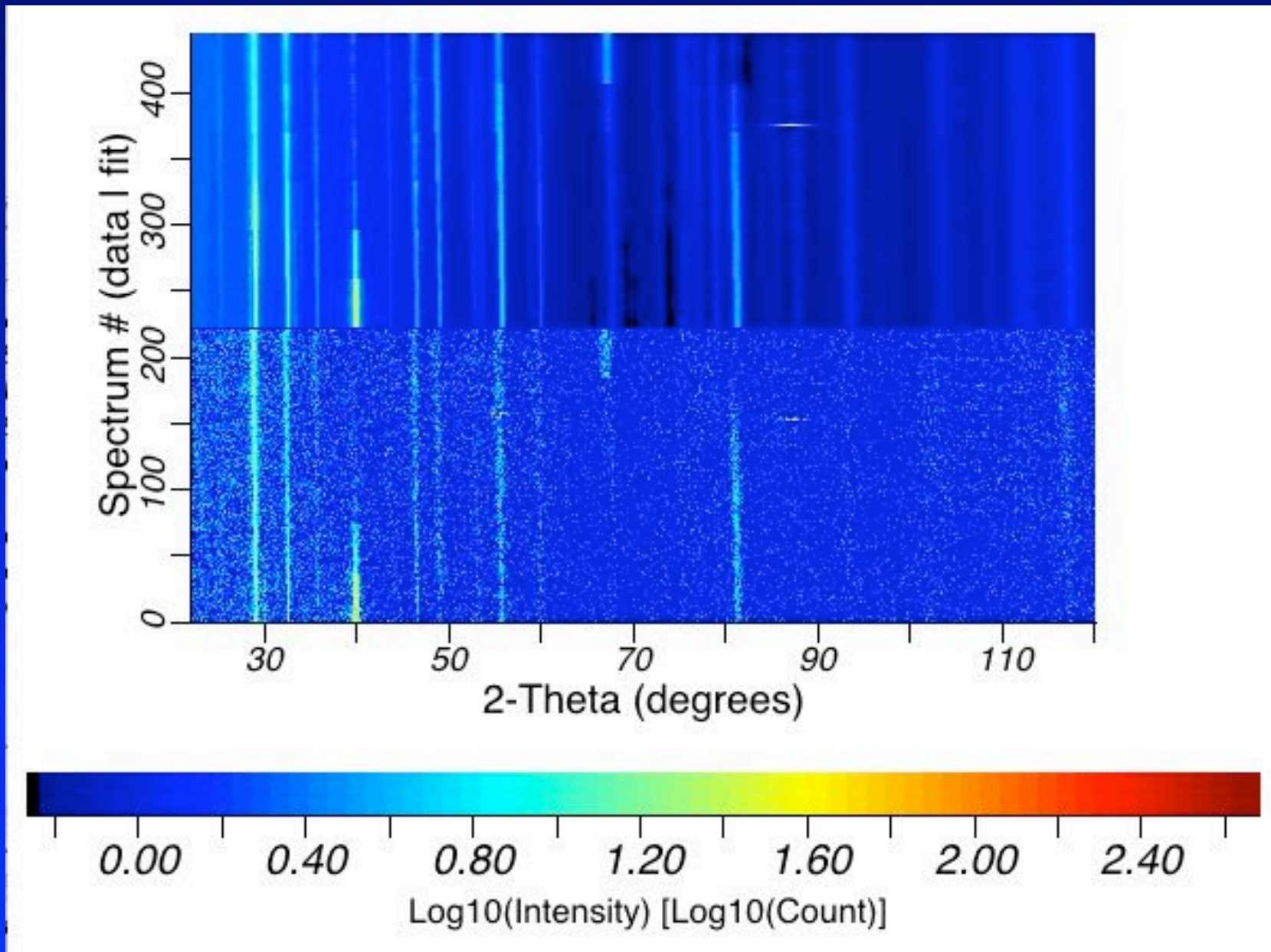
- *Si Wafer + 50 nm Pt buffer layer*
- *~ 300 nm of $(\text{Sr}_{0.82}\text{Bi}_{0.12})\text{Bi}_2\text{Ta}_2\text{O}_9$ - Orthorhombic A21am:-cba*
- *Spectra collection on the ESQUI diffractometer (right)*
- *120 degs position sensitive detector on an eulerian cradle; multilayer as a primary beam monochromator*
- *Spectra collected in chi from 0 to 45 degrees in step of 5 deg for chi and 0 to 180 in steps of 5 deg for phi*
- *Structure refined*



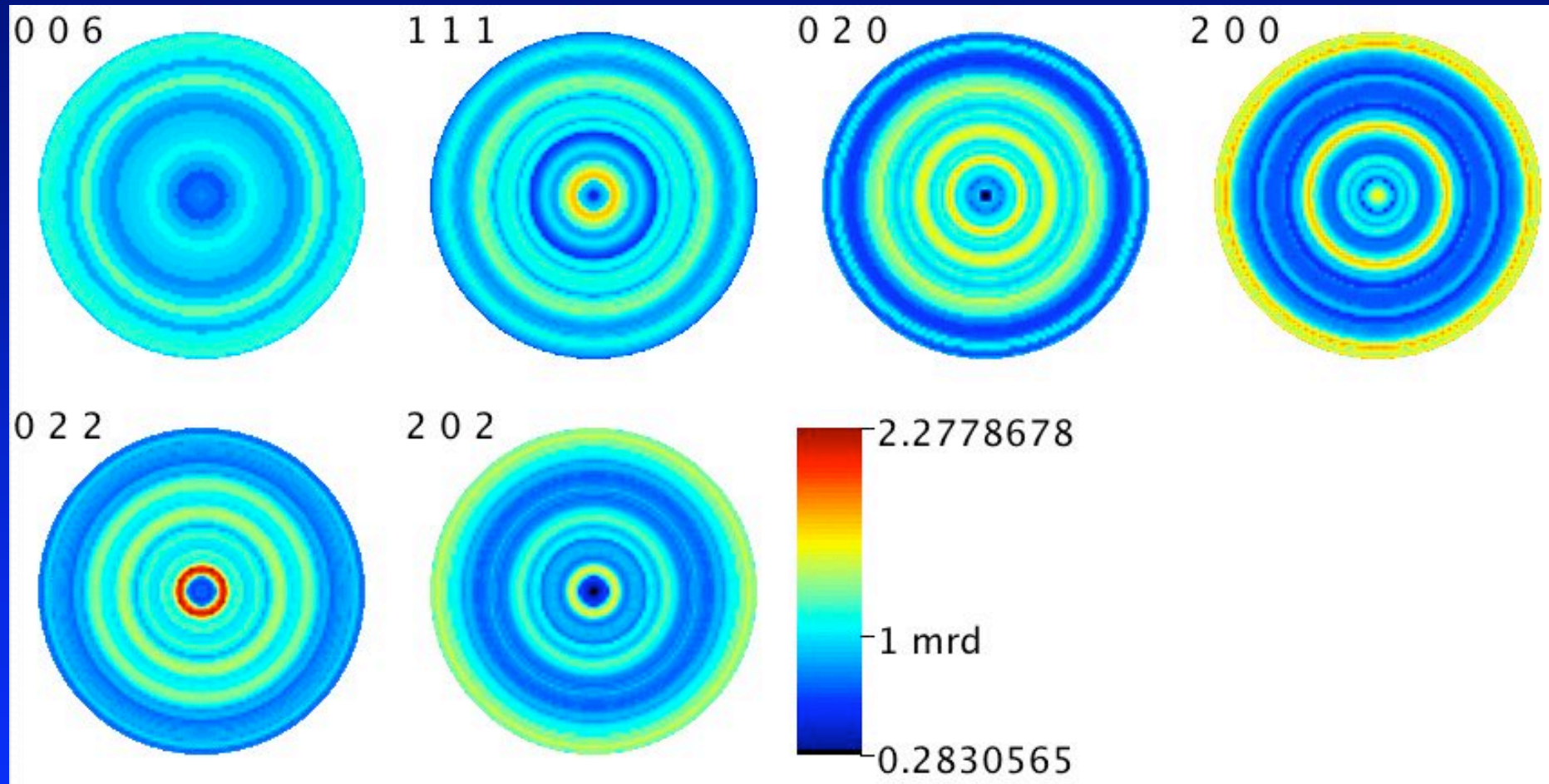
Rietveld Texture refinement



SBT thin film Rietveld fit



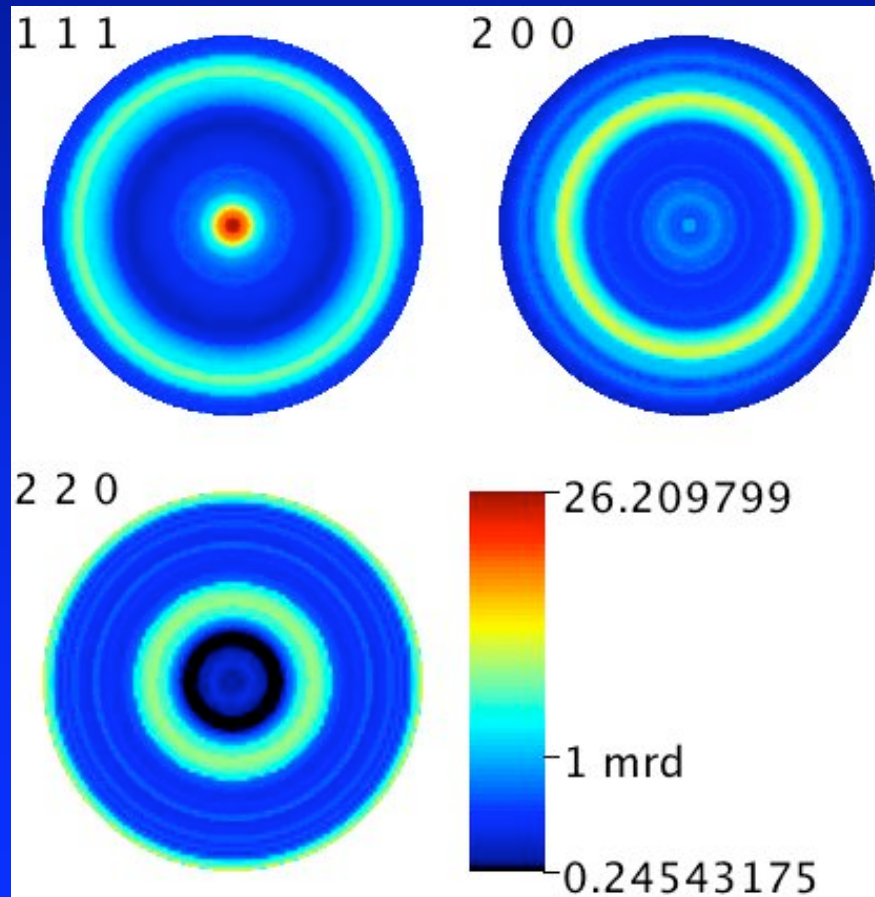
SBT pole figures reconstructed



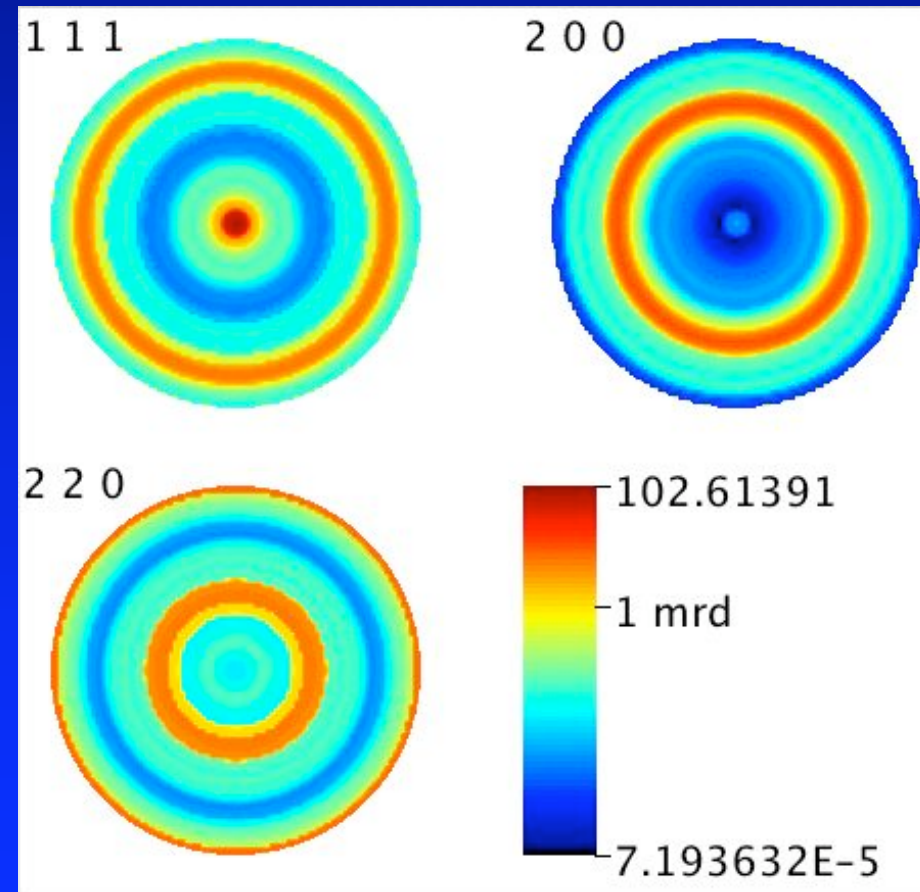
Pt texture too sharp for WIMV

Special texture methodology for Rietveld developed: Entropy based WIMV using tube projections. Interpolation of pole figures avoided.

WIMV



E-WIMV



SBT film microstructure and crystal structure

	<i>Cell parameters</i> (Å)	<i>Cryst. Size</i> (Å)	<i>Microstrain</i>	<i>Layer thickness</i> (Å)
<i>SBT</i>	$a \approx b = 5.5473(2)$ $c = 25.316(2)$	565(5)	0.0037(3)	3579(72)
<i>Pt</i>	3.9411(1)	317(4)	0.0029(2)	557(15)



Space group: A21am:-cba

*14 atomic position
parameters refined*

Extremely sharp Al film (ST microelectronics)

Aluminum film

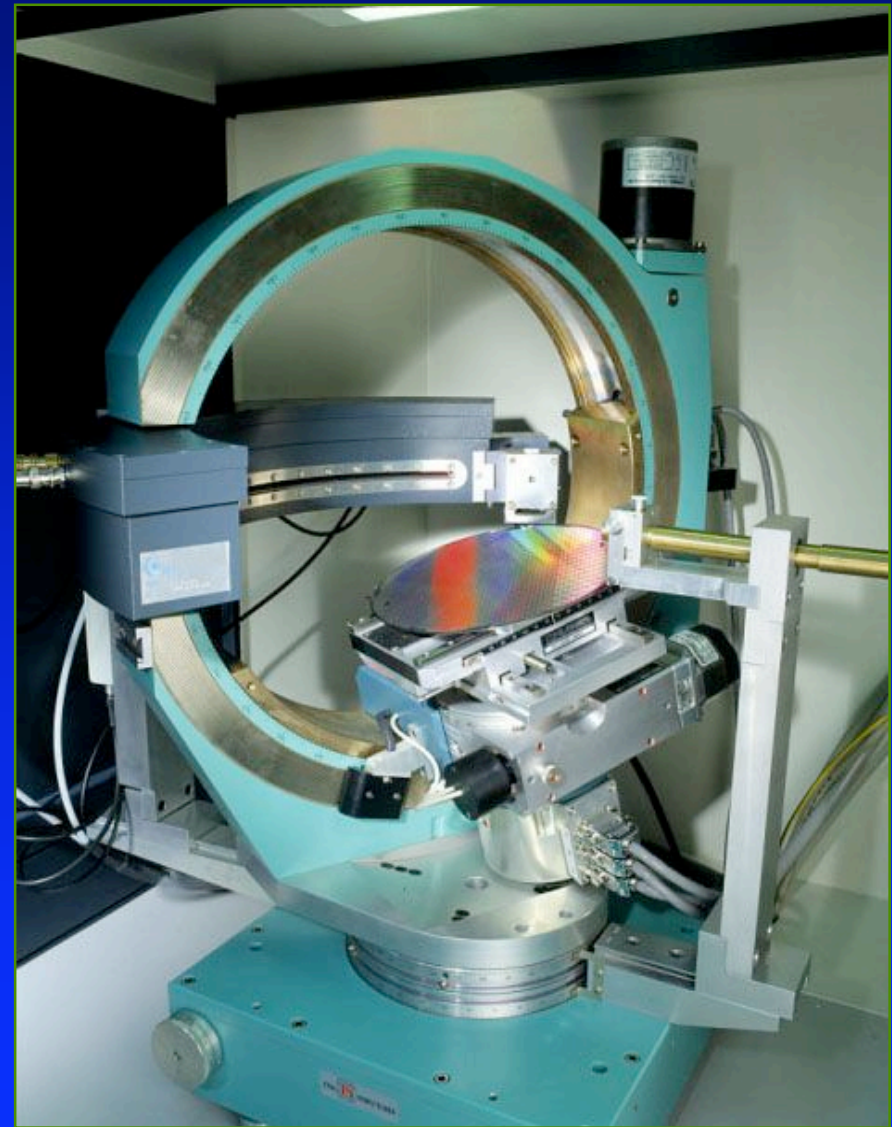
Si wafer substrate

*Spectra collection on the ESQUI
diffractometer (right)*

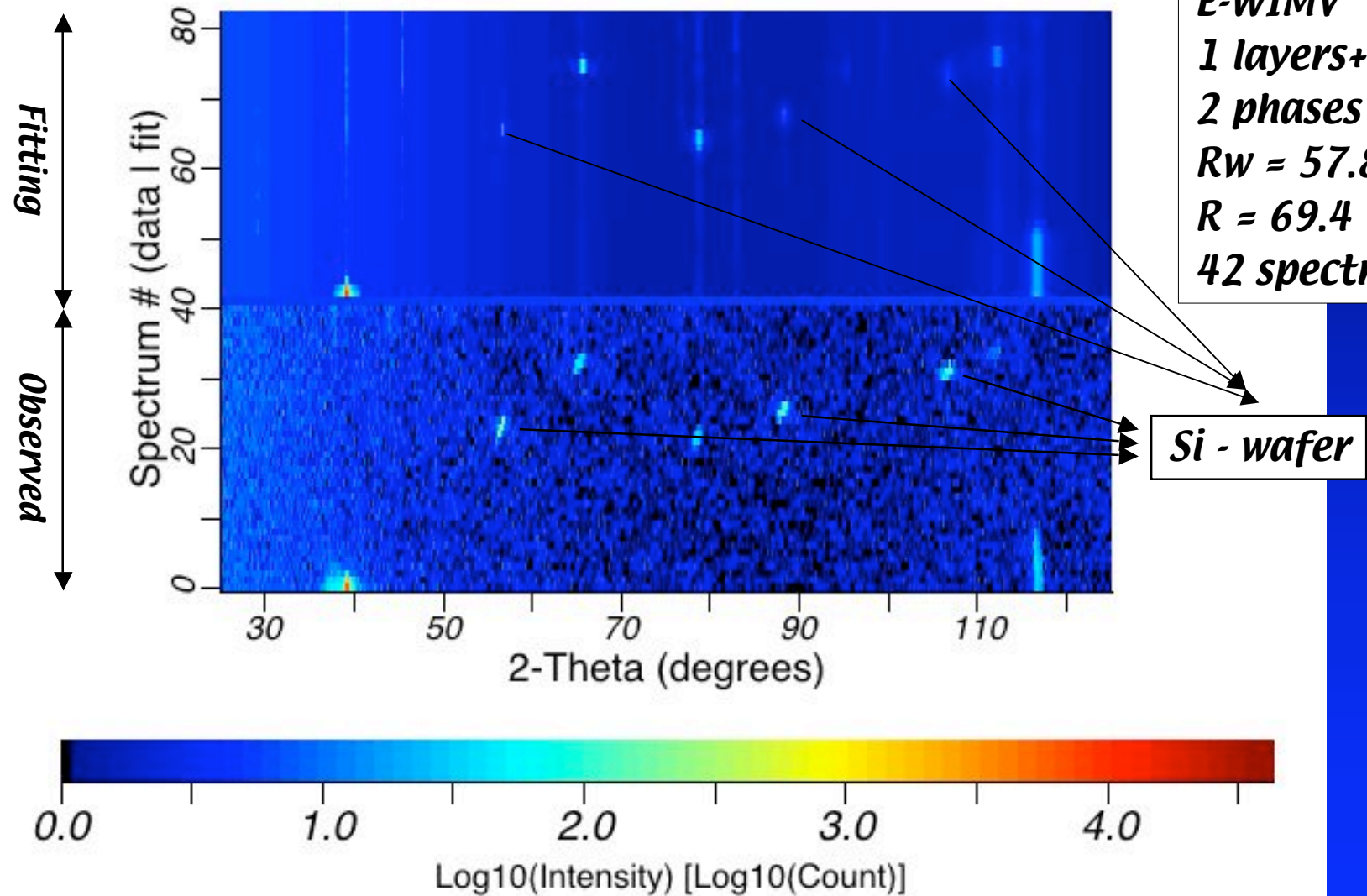
*120 degs position sensitive detector on
an eulerian cradle; multilayer as a
primary beam monochromator*

*Spectra collected in chi from 0 to 45
degrees in step of 1 deg turning
continuously the phi motor (fiber
texture)*

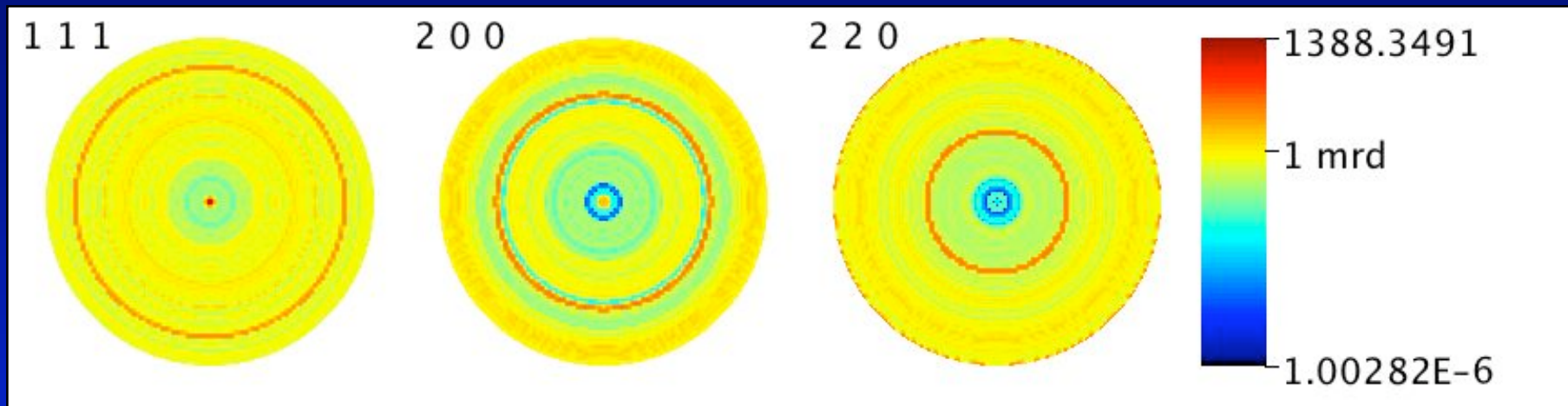
*E-WIMV used only; too sharp texture
even for WIMV*



Al film: fitting the spectra



Al film: Al reconstructed pole figures



E-WIMV

1 deg cells

$F2 = 1100.9$

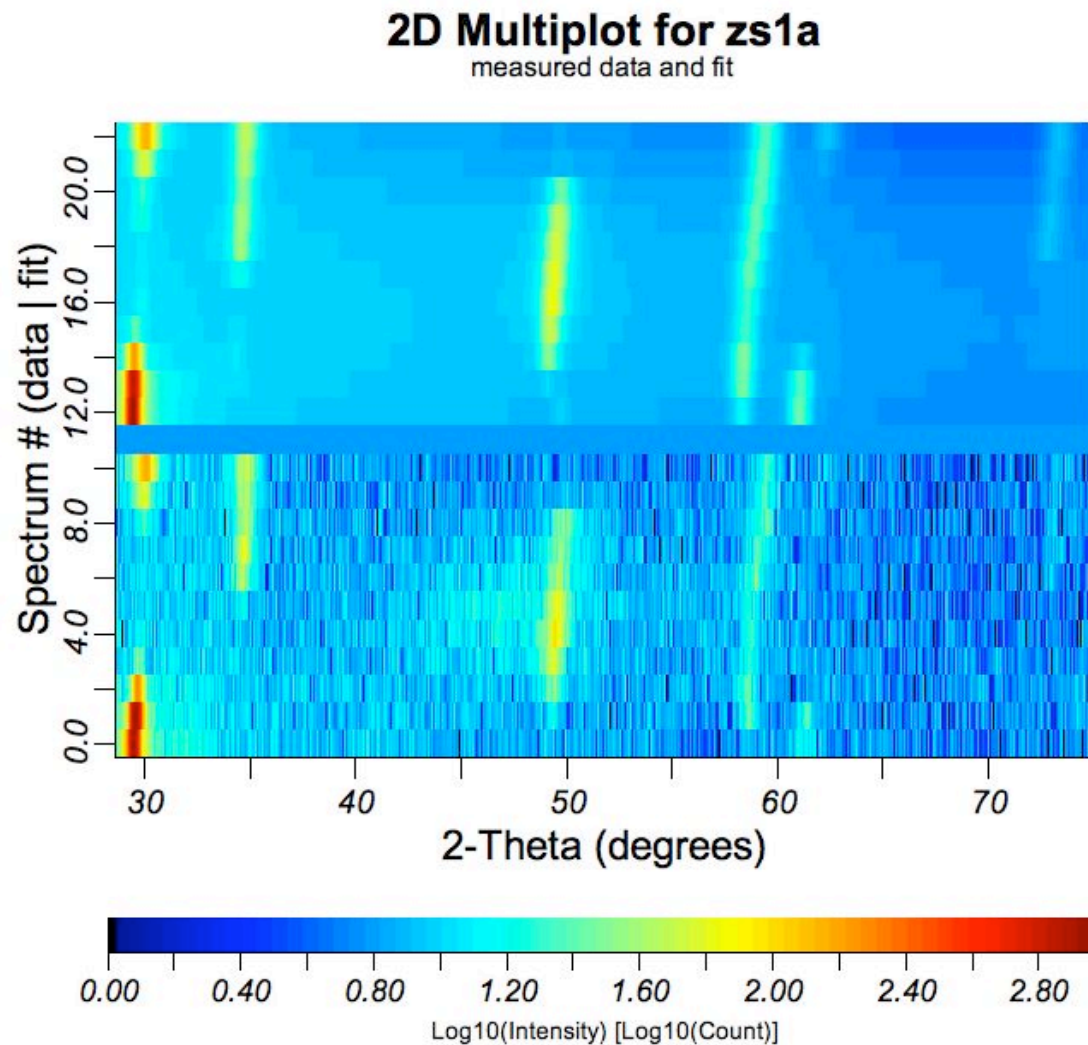
$Rw = 15.4 \%$

$Rp = 19.5 \%$

8 reflections

Cubic ZrO₂ thin film: stress-texture analysis

- *Measurement by Huber stress-texture goniometer (point detector)*
- *EWIMV for texture and Geometrical mean for stress (BulkPathGE0 method)*



ZrO_2 film: results

*Very high in plane residual stresses
(compression):*

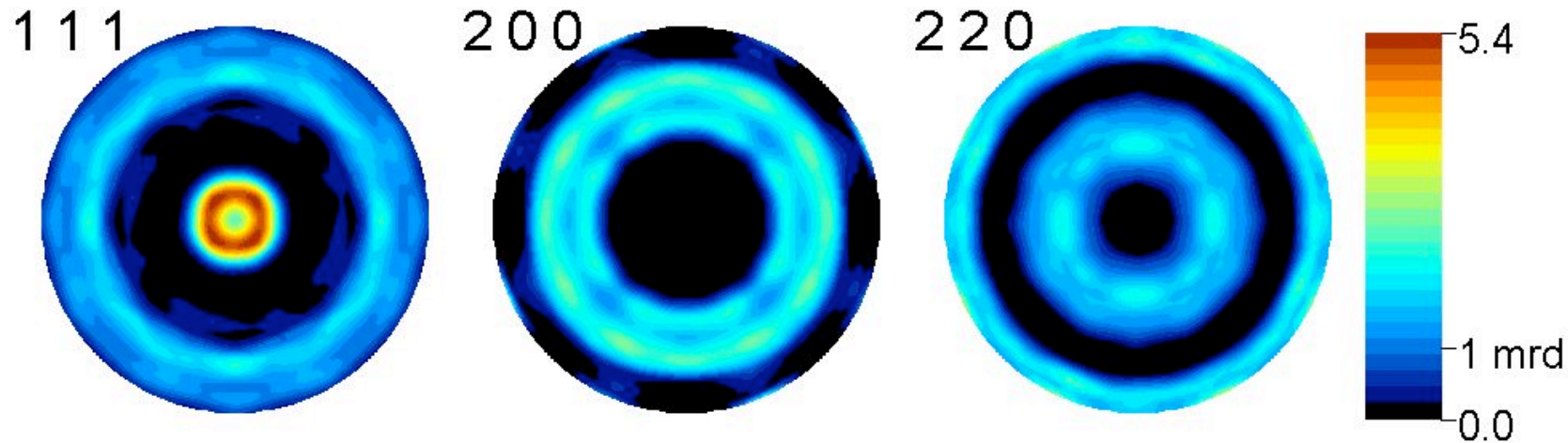
Reuss model: 3.6 GPa

Bulk Path GEO: 3.47(5) GPa

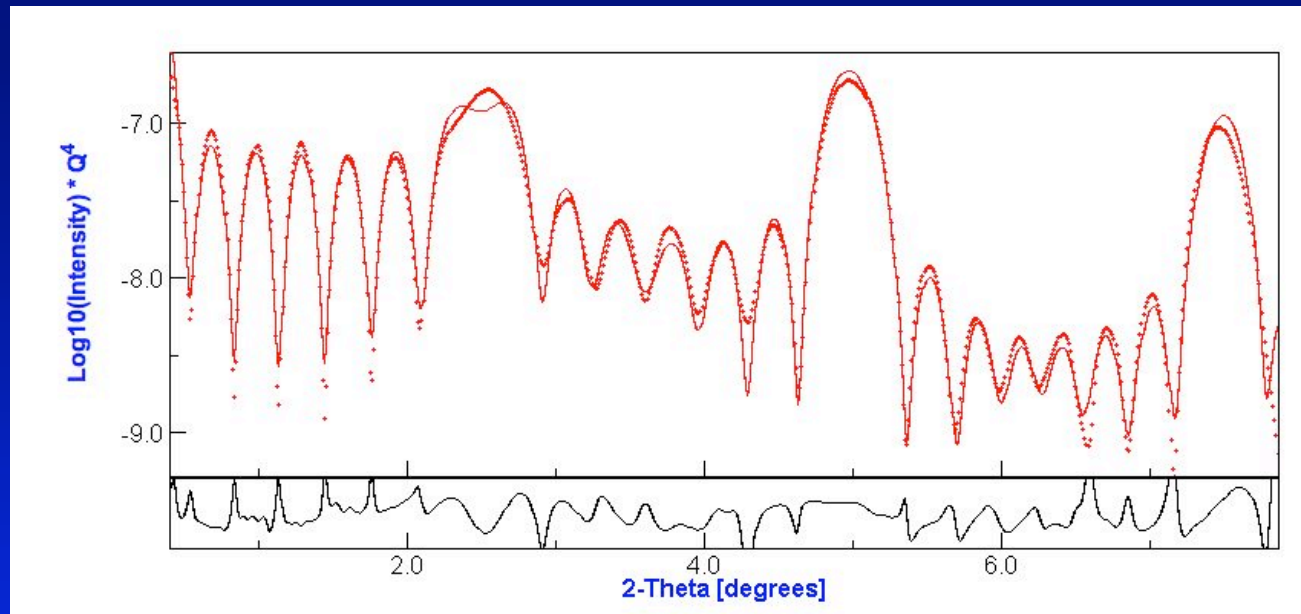
Curvature method: > 10 GPa !?

Thickness: 320 Nanometer

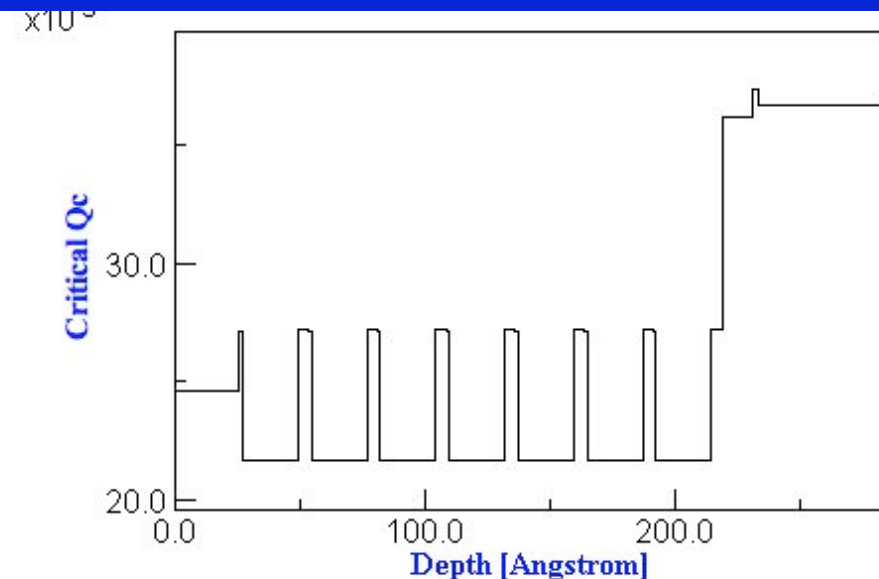
Reconstructed pole figures



Reflectivity for multilayer analysis



- *Langmuir-Blodgett film*
- *24 layers sequence*
- *Matrix method used for the analysis in Maud*
- *Film and data collected by A. Gibaud (LPEC, Le Mans)*



Conclusions

- *Combined analysis (Rietveld, microstructure, texture, residual stresses and reflectivity) is very powerful for thin film*
- *Extremely sharp textures requires the new E-WIMV method*
- *Bulk Path GEO confirms to be powerful for macro residual stresses*
- *We need to decrease the measurement time*
- *Severe overlapping is no more a problem*

The ESQUI European Project site:

<http://www.ing.unitn.it/~maud/esqui>

Future work (in progress)

- *Driving the experiment (ODF coverage etc.). Using Genetic Algorithms?*
- *Sharp textures -> continuous coverage -> 2D detectors -> 2D fitting?*
- *Ab initio structure solution. Problems:*
 - *Textured sample preparation*
 - *Data collection (fast, reliable, high resolution)*
- *Reflectivity: off specular computation (reciprocal map fitting)*