



What is an outlier?

An outlier is a data point in a dataset that is distinct from all other observation

A data point that lies outside the overall distribution of the dataset



- What is the reason for outlier to exist in data set?
- 1-variability in the data
- 2-an experimental measurement error



- What are the impacts of having outlier in a dataset?
- 1-It causes various problems during our statistical analysis
- 2-it may cause a significant impact on the mean and standard diviations

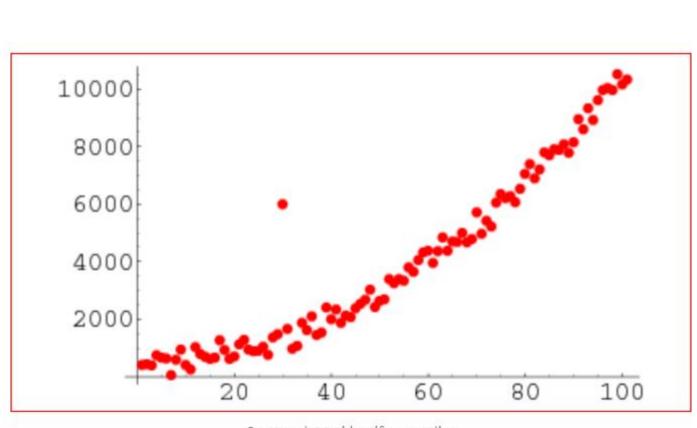


- Various ways of finding the outlier:
- 1-Scatter Plot
- 2-Z-score
- 3-Box plot



Scatter Plot:

We can see the scatter plot and it shows us if a data point lies outside the overall distribution of the dataset



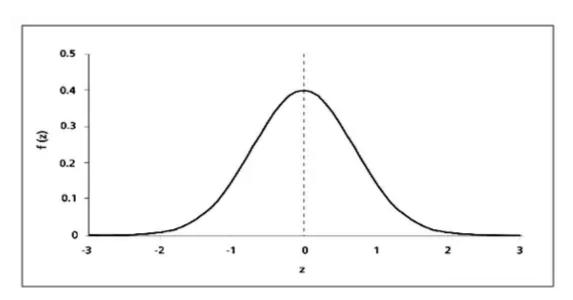
Scatter plot to identify an outlier

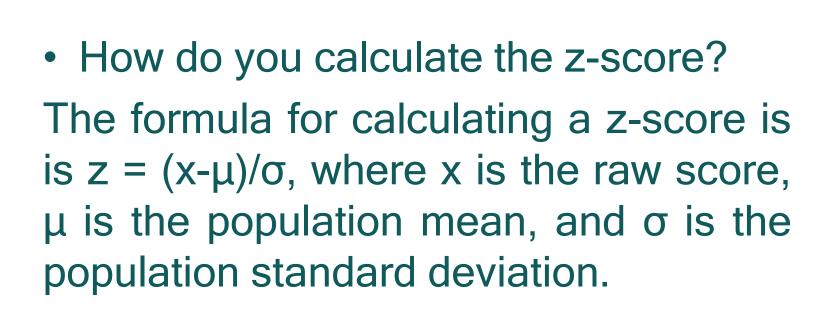


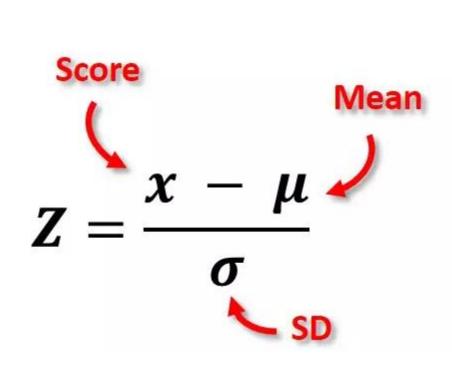
Z-Score:

A z-score describes the position of a raw score in terms of its distance from the mean, when measured in standard deviation units

• The z-score is positive if the value lies above the mean, and negative if it lies below the mean.









- The value of the z-score tells you how many standard deviations you are away from the mean.
- 1-If a z-score is equal to 0, it is on the mean.
- 2-A positive z-score indicates the raw score is higher than the mean average. For example.
- 3-A negative z-score reveals the raw score is below the mean average.

Exercise:

The grades on a history midterm at Almond have a mean of $\mu=85$ and a standard deviation of $\sigma=2$.

Michael scored 86 on the exam.

Find the z-score for Michael's exam grade.

$$z = \frac{\text{his grade} - \text{mean grade}}{\text{standard deviation}}$$

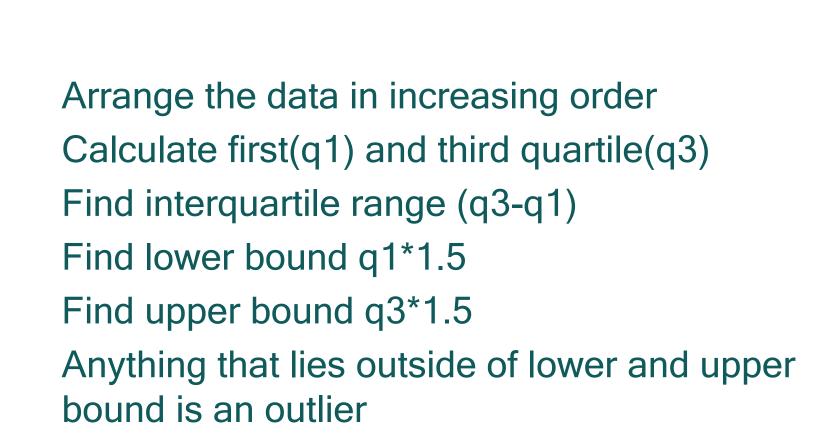
$$z = \frac{86 - 85}{2}$$

$$z = \frac{1}{2} = 0.5$$



Using IQR:

IQR tells how spread the middle values are. It can be used to tell when a value is too far from the middle.



Exercise:

Find the outliers, if any, for the following data set:

10.2, 14.1, 14.4. 14.4, 14.4, 14.5,

14.5, 14.6, 14.7, 14.7, 14.7, 14.9,

15.1, 15.9, 16.4

10.2, 14.1, 14.4. 14.4, 14.4, 14.5, 14.5, 14.6, 14.7, 14.7, 14.7, 14.9, 15.1, 15.9, 16.4

To find out if there are any outliers, I first have to find the IQR. There are fifteen data points, so the median will be at the eighth position:

$$(15+1) \div 2 = 8$$

Then $Q_2 = 14.6$.

There are seven data points on either side of the median. The two halves are:

10.2, 14.1, 14.4. 14.4, 14.4, 14.5, 14.5

...and:

14.7, 14.7, 14.7, 14.9, 15.1, 15.9, 16.4



 Q_1 is the fourth value in the list, being the middle value of the first half of the list; and Q_3 is the twelfth value, being th middle value of the second half of the list:

$$Q_1 = 14.4$$

$$Q_3 = 14.9$$

Then the IQR is given by:

$$IQR = 14.9 - 14.4 = 0.5$$

Outliers will be any points below $Q_1 - 1.5 \times IQR = 14.4 - 0.75 = 13.65$ or above $Q_3 + 1.5 \times IQR = 14.9 + 0.75 = 15.65$.

Then the outliers are at:

10.2, 15.9, and 16.4

