Ch.9: Object-oriented programming

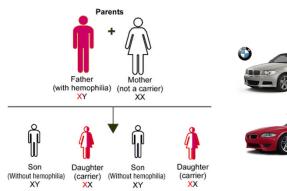
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Inheritance

Inheritance



Children

class Convertible {
// Key (private)
// Speed: 155 (miles / hour)
// Weight 1600 kg
// Engine: 3.2 L. S54 inline-6
}
class Roadster extends Convertible {
// Speed: 165 (miles / hour)
// Weight 1399 kg
}

The chapter title *Object-oriented programming* (OO) may mean two different things

- Programming with classes (better: object-based programming)
- Programming with class hierarchies (class families)

New concept: collect classes in families (hierarchies)

What is a class hierarchy?

- A family of closely related classes
- A key concept is inheritance: child classes can inherit attributes and methods from parent class(es) - this saves much typing and code duplication

As usual, we shall learn through examples!

OO is a Norwegian invention by Ole-Johan Dahl and Kristen Nygaard in the 1960s - one of the most important inventions in computer science, because OO is used in all big computer systems today!

Warning: OO is difficult and takes time to master

- Let ideas mature with time
- Study many examples
- OO is less important in Python than in C++, Java and C#, so the benefits of OO are less obvious in Python
- Our examples here on OO employ numerical methods for $\int_a^b f(x)dx$, f'(x), u'=f(u,t) make sure you understand the simplest of these numerical methods before you study the combination of OO and numerics
- Our goal: write general, reusable modules with lots of methods for numerical computing of $\int_a^b f(x)dx$, f'(x), u'=f(u,t)

A class for straight lines

Problem:

Make a class for evaluating lines $y = c_0 + c_1 x$

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```
Code:
 class Line:
     def __init__(self, c0, c1):
         self.c0, self.c1 = c0, c1
     def __call__(self, x):
         return self.c0 + self.c1*x
     def table(self, L, R, n):
         """Return a table with n points for L <= x <= R."""
         for x in linspace(L, R, n):
             y = self(x)
             s += \frac{12g}{12g}n' (x, y)
         return s
```

Problem:

Make a class for evaluating parabolas $y = c_0 + c_1 x + c_2 x^2$

```
Code:
    class Parabola:
        def __init__(self, c0, c1, c2):
            self.c0, self.c1, self.c2 = c0, c1, c2

    def __call__(self, x):
            return self.c2*x**2 + self.c1*x + self.c0

    def table(self, L, R, n):
        """Return a table with n points for L <= x <= R."""
        s = ''
        for x in linspace(L, R, n):</pre>
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Observation

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Code
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Observati<u>on:</u>

return s

Class Parabola as a subclass of Line; principles

- Parabola code = Line code + a little extra with the c_2 term
- Can we utilize class Line code in class Parabola?
- This is what inheritance is about!

Writing

```
class Parabola(Line)
pass
```

makes Parabola inherit all methods and attributes from Line, so Parabola has attributes cO and c1 and three methods

- Line is a superclass, Parabola is a subclass
 (parent class, base class; child class, derived class)
- Class Parabola must add code to Line's constructor (an extra c2 attribute), __call__ (an extra term), but table can be used unaltered
- The principle is to reuse as much code in Line as possible and avoid duplicating code

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- The principle is to reuse as much code in Line as possible and avoid duplicating code

A subclass method can call a superclass method in this way:
superclass_name.method(self, arg1, arg2, ...)

Class Parabola as a subclass of Line:
class Parabola(Line):
 def __init__(self, c0, c1, c2):
 Line.__init__(self, c0, c1) # Line stores c0, c1
 self.c2 = c2

def __call__(self, x):
 return Line.__call__(self, x) + self.c2*x**2

- Class Parabola just adds code to the already existing code in class Line no duplication of storing c0 and c1, and computing c_0+c_1x
- Class Parabola also has a table method it is inherited
- __init__ and __call__ are overridden or redefined in the subclass

A subclass method can call a superclass method in this way:

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superclass_name.method(self, arg1, arg2, ...)
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- Class Parabola also has a table method it is inherited
- __init__ and __call__ are overridden or redefined in the subclass

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class Line:
    def init (self. c0. c1):
        self.c0. self.c1 = c0. c1
    def __call__(self, x):
        return self.c0 + self.c1*x
    def table(self, L, R, n):
        """Return a table with n points for L <= x <= R."""
        s = ''
        for x in linspace(L, R, n):
            y = self(x)
             s += \frac{12g}{12g} \frac{12g}{n}, \frac{1}{2g} \frac{1}{n}
        return s
class Parabola(Line):
    def __init__(self, c0, c1, c2):
        Line.__init__(self, c0, c1) # Line stores c0, c1
        self.c2 = c2
    def call (self. x):
        return Line. call (self. x) + self.c2*x**2
p = Parabola(1, -2, 2)
print p(2.5)
```

(Visualize execution)

We can check class type and class relations with isinstance(obj, type) and issubclass(subclassname, superclassname)

```
>>> from Line_Parabola import Line, Parabola
>>> 1 = Line(-1, 1)
>>> isinstance(1, Line)
True
>>> isinstance(1, Parabola)
False
>>> p = Parabola(-1, 0, 10)
>>> isinstance(p, Parabola)
True
>>> isinstance(p, Line)
True
>>> issubclass(Parabola, Line)
True
>>> issubclass(Line, Parabola)
False
>>> p.__class__ == Parabola
True
>>> p.__class__.__name__ # string version of the class name
'Parabola'
```

Recall the class for numerical differentiation from Ch. 7

$$f'(x) \approx \frac{f(x+h) - f(x)}{h}$$

```
class Derivative:
    def __init__(self, f, h=1E-5):
       self.f = f
       self.h = float(h)
    def __call__(self, x):
       f, h = self.f, self.h # make short forms
       return (f(x+h) - f(x))/h
def f(x):
   return exp(-x)*cos(tanh(x))
from math import exp, cos, tanh
dfdx = Derivative(f)
print dfdx(2.0)
```

There are numerous formulas numerical differentiation

$$f'(x) = \frac{f(x+h) - f(x)}{h} + \mathcal{O}(h)$$

$$f'(x) = \frac{f(x) - f(x-h)}{h} + \mathcal{O}(h)$$

$$f'(x) = \frac{f(x+h) - f(x-h)}{2h} + \mathcal{O}(h^2)$$

$$f'(x) = \frac{4}{3} \frac{f(x+h) - f(x-h)}{2h} - \frac{1}{3} \frac{f(x+2h) - f(x-2h)}{4h} + \mathcal{O}(h^4)$$

$$f'(x) = \frac{3}{2} \frac{f(x+h) - f(x-h)}{2h} - \frac{3}{5} \frac{f(x+2h) - f(x-2h)}{4h} + \frac{1}{10} \frac{f(x+3h) - f(x-3h)}{6h} + \mathcal{O}(h^6)$$

$$f'(x) = \frac{1}{h} \left(-\frac{1}{6} f(x+2h) + f(x+h) - \frac{1}{2} f(x) - \frac{1}{3} f(x-h) \right) + \mathcal{O}(h^3)$$

How can we make a module that offers all these formulas?

```
It's easy:
 class Forward1:
     def __init__(self, f, h=1E-5):
         self.f = f
         self.h = float(h)
     def __call__(self, x):
         f, h = self.f, self.h
         return (f(x+h) - f(x))/h
 class Backward1:
     def __init__(self, f, h=1E-5):
         self.f = f
         self.h = float(h)
     def __call__(self, x):
         f, h = self.f, self.h
         return (f(x) - f(x-h))/h
 class Central2:
     # same constructor
     # put relevant formula in __call__
```

What is the problem with this type of code?

All the constructors are identical so we duplicate a lot of code.

- A general OO idea: place code common to many classes in a superclass and inherit that code
- Here: inhert constructor from superclass,
 let subclasses for different differentiation formulas implement
 their version of __call__

Class hierarchy for numerical differentiation

Superclass:

```
class Diff:
    def __init__(self, f, h=1E-5):
        self.f = f
        self.h = float(h)
```

Subclass for simple 1st-order forward formula:

```
class Forward1(Diff):
    def __call__(self, x):
        f, h = self.f, self.h
        return (f(x+h) - f(x))/h
```

Subclass for 4-th order central formula:

Use of the differentiation classes

```
Interactive example: f(x) = \sin x, compute f'(x) for x = \pi

>>> from Diff import *
>>> from math import sin
>>> mycos = Central4(sin)
>>> # compute \sin^*(pi):
>>> mycos(pi)
-1.000000082740371

Central4(sin) calls inherited constructor in superclass, while mycos(pi) calls __call__ in the subclass Central4
```

```
class Diff:
    def __init__(self, f, h=1E-5):
        self.f = f
        self.h = float(h)

class Forward1(Diff):
    def __call__(self, x):
        f, h = self.f, self.h
        return (f(x+h) - f(x))/h
```

dfdx = Diff(lambda x: x**2)

print dfdx(0.5)

(Visualize execution)

A flexible main program for numerical differentiation

Suppose we want to differentiate function expressions from the command line:

```
Terminal> python df.py 'exp(sin(x))' Central 2 3.1 -1.04155573055

Terminal> python df.py 'f(x)' difftype difforder x f'(x)
```

With eval and the Diff class hierarchy this main program can be realized in a few lines (many lines in C# and Java!):

```
import sys
from Diff import *
from math import *
from scitools.StringFunction import StringFunction

f = StringFunction(sys.argv[1])
difftype = sys.argv[2]
difforder = sys.argv[3]
classname = difftype + difforder
df = eval(classname + '(f)')
x = float(sys.argv[4])
print df(x)
```

Investigating numerical approximation errors

- We can empirically investigate the accuracy of our family of 6 numerical differentiation formulas
- Sample function: $f(x) = \exp(-10x)$
- See the book for a little program that computes the errors:

Observations:

- Halving h from row to row reduces the errors by a factor of 2, 4 and 16, i.e, the errors go like h, h^2 , and h^4
- Central4 has really superior accuracy compared with Forward1

Alternative implementations (in the book)

- Pure Python functions
 downside: more arguments to transfer, cannot apply formulas
 twice to get 2nd-order derivatives etc.
- Functional programming gives the same flexibility as the OO solution
- One class and one common math formula applies math notation instead of programming techniques to generalize code

These techniques are beyond scope in the course, but place OO into a bigger perspective. Might better clarify what OO is - for some.

Formulas for numerical integration

There are numerous formulas for numerical integration and all of them can be put into a common notation:

$$\int_a^b f(x)dx \approx \sum_{i=0}^{n-1} w_i f(x_i)$$

 w_i : weights, x_i : points (specific to a certain formula)

The Trapezoidal rule has h=(b-a)/(n-1) and

$$x_i = a + ih$$
, $w_0 = w_{n-1} = \frac{h}{2}$, $w_i = h$ $(i \neq 0, n-1)$

The Midpoint rule has h = (b - a)/n and

$$x_i = a + \frac{h}{2} + ih, \quad w_i = h$$

More formulas

Simpson's rule has

$$x_i = a + ih$$
, $h = \frac{b - a}{n - 1}$
 $w_0 = w_{n-1} = \frac{h}{6}$
 $w_i = \frac{h}{3}$ for i even, $w_i = \frac{2h}{3}$ for i odd

Other rules have more complicated formulas for w_i and x_i

Why should these formulas be implemented in a class hierarchy?

- A numerical integration formula can be implemented as a class: a, b and n are attributes and an integrate method evaluates the formula
- All such classes are quite similar: the evaluation of $\sum_j w_j f(x_j)$ is the same, only the definition of the points and weights differ among the classes
- Recall: code duplication is a bad thing!
- The general OO idea: place code common to many classes in a superclass and inherit that code
- ullet Here we put $\sum_i w_j f(x_j)$ in a superclass (method integrate)
- Subclasses extend the superclass with code specific to a math formula, i.e., w; and x; in a class method construct_rule

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The superclass for integration

```
class Integrator:
    def __init__(self, a, b, n):
        self.a, self.b, self.n = a, b, n
        self.points, self.weights = self.construct_method()
    def construct method(self):
        raise NotImplementedError('no rule in class %s' % \
                                  self.__class__._name__)
    def integrate(self, f):
        for i in range(len(self.weights)):
            s += self.weights[i] *f(self.points[i])
        return s
    def vectorized_integrate(self, f):
        # f must be vectorized for this to work
        return dot(self.weights, f(self.points))
```

A subclass: the Trapezoidal rule

```
class Trapezoidal(Integrator):
    def construct_method(self):
        h = (self.b - self.a)/float(self.n - 1)
        x = linspace(self.a, self.b, self.n)
        w = zeros(len(x))
        w[1:-1] += h
        w[0] = h/2;      w[-1] = h/2
        return x, w
```

Another subclass: Simpson's rule

- Simpson's rule is more tricky to implement because of different formulas for odd and even points
- Don't bother with the details of w_i and x_i in Simpson's rule now focus on the class design!

```
class Simpson(Integrator):
    def construct_method(self):
        if self.n % 2 != 1:
            print 'n=%d must be odd, 1 is added' % self.n
            self.n += 1
        <code for computing x and w>
            return x, w
```

About the program flow

return x*x

```
Let us integrate \int_0^2 x^2 dx using 101 points:
def f(x):
```

```
method = Simpson(0, 2, 101)
print method.integrate(f)
```

Important:

- method = Simpson(...): this invokes the superclass constructor, which calls construct_method in class Simpson
- method.integrate(f) invokes the inherited integrate method, defined in class Integrator

```
class Integrator:
    def __init__(self, a, b, n):
        self.a, self.b, self.n = a, b, n
        self.points, self.weights = self.construct_method()
    def construct_method(self):
        raise NotImplementedError('no rule in class %s' % \
                                   self.__class__._name__)
    def integrate(self, f):
        s = \bar{0}
        for i in range(len(self.weights)):
            s += self.weights[i] *f(self.points[i])
        return s
class Trapezoidal(Integrator):
    def construct method(self):
        h = (self.b - self.a)/float(self.n - 1)
        x = linspace(self.a, self.b, self.n)
        w = zeros(len(x))
        w[1:-1] += h
        w[0] = h/2; w[-1] = h/2
        return x. w
def f(x):
   return x*x
method = Trapezoidal (0, 2, 101)
print method.integrate(f)
```

Applications of the family of integration classes

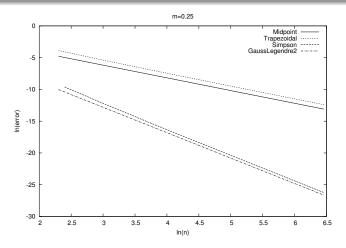
We can empirically test out the accuracy of different integration methods Midpoint, Trapezoidal, Simpson, GaussLegendre2, ... applied to, e.g.,

$$\int\limits_0^1 \left(1+\frac{1}{m}\right)t^{\frac{1}{m}}dt=1$$

- This integral is "difficult" numerically for m > 1.
- Key problem: the error in numerical integration formulas is of the form Cn^{-r} , mathematical theory can predict r (the "order"), but we can estimate r empirically too
- See the book for computational details
- Here we focus on the conclusions

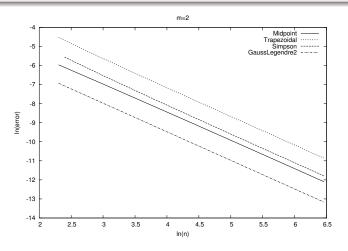
Convergence rates for m < 1 (easy case)

Simpson and Gauss-Legendre reduce the error faster than Midpoint and Trapezoidal (plot has ln(error) versus ln n)



Convergence rates for m > 1 (problematic case)

Simpson and Gauss-Legendre, which are theoretically "smarter" than Midpoint and Trapezoidal do not show superior behavior!



Summary of object-orientation principles

- A subclass inherits everything from the superclass
- When to use a subclass/superclass?
 - if code common to several classes can be placed in a superclass
 - if the problem has a natural child-parent concept
- The program flow jumps between super- and sub-classes
- It takes time to master when and how to use OO
- Study examples!

Recall the class hierarchy for differentiation

Mathematical principles:

Collection of difference formulas for f'(x). For example,

$$f'(x) \approx \frac{f(x+h) - f(x-h)}{2h}$$

Superclass Diff contains common code (constructor), subclasses implement various difference formulas.

Implementation example (superclass and one subclass)

```
class Diff:
    def __init__(self, f, h=1E-5):
        self.f = f
        self.h = float(h)

class Central2(Diff):
    def __call__(self, x):
        f, h = self.f, self.h
        return (f(x+h) - f(x-h))/(2*h)
```

Recall the class hierarchy for integration (1)

Mathematical principles:

General integration formula for numerical integration:

$$\int_a^b f(x)dx \approx \sum_{j=0}^{n-1} w_j f(x_j)$$

Superclass Integrator contains common code (constructor, $\sum_{j} w_{i} f(x_{i})$), subclasses implement definition of w_{i} and x_{i} .

Recall the class hierarchy for integration (2)

```
Implementation example (superclass and one subclass):
  class Integrator:
     def __init__(self, a, b, n):
         self.a, self.b, self.n = a, b, n
         self.points, self.weights = self.construct_method()
     def integrate(self, f):
         s = 0
         for i in range(len(self.weights)):
             s += self.weights[i] *f(self.points[i])
         return s
  class Trapezoidal (Integrator):
     def construct_method(self):
         x = linspace(self.a, self.b, self.n)
         h = (self.b - self.a)/float(self.n - 1)
         w = zeros(len(x)) + h
         w[0] /= 2; w[-1] /= 2 # adjust end weights
         return x, w
```

A summarizing example: Generalized reading of input data

Write a table of $x \in [a, b]$ and f(x) to file:

```
outfile = open(filename, 'w')
from numpy import linspace
for x in linspace(a, b, n):
    outfile.write('%12g %12g\n' % (x, f(x)))
outfile.close()
```

We want flexible input:

Read a, b, n, filename and a formula for f from...

- the command line
- interactive commands like a=0, b=2, filename=mydat.dat
- questions and answers in the terminal window
- a graphical user interface
- a file of the form

```
a = 0
b = 2
filename = mydat.dat
```

Graphical user interface



First we write the application code

Desired usage:

```
from ReadInput import *
# define all input parameters as name-value pairs in a dict:
p = dict(formula='x+1', a=0, b=1, n=2, filename='tmp.dat')
# read from some input medium:
inp = ReadCommandLine(p)
# or
inp = PromptUser(p) # questions in the terminal window
# or
inp = ReadInputFile(p) # read file or interactive commands
# or
inp = GUI(p)
                     # read from a GUI
# load input data into separate variables (alphabetic order)
a, b, filename, formula, n = inp.get_all()
# qo!
```

About the implementation

- A superclass ReadInput stores the dict and provides methods for getting input into program variables (get, get_all)
- Subclasses read from different input sources
- ReadCommandLine, PromptUser, ReadInputFile, GUI
- See the book or ReadInput.py for implementation details
- For now the ideas and principles are more important than code details!