

## TABLE OF INFORMATION

Rest mass of the electron

$$m_e = 9.11 \times 10^{-31} \text{ kilogram} = 9.11 \times 10^{-28} \text{ gram}$$

Magnitude of the electron charge

$$e = 1.60 \times 10^{-19} \text{ coulomb} = 4.80 \times 10^{-10} \text{ statcoulomb (esu)}$$

Avogadro's number

$$N_A = 6.02 \times 10^{23} \text{ per mole}$$

Universal gas constant

$$R = 8.31 \text{ joules/(mole} \cdot \text{K)}$$

Boltzmann's constant

$$k = 1.38 \times 10^{-23} \text{ joule/K} = 1.38 \times 10^{-16} \text{ erg/K}$$

Speed of light

$$c = 3.00 \times 10^8 \text{ m/s} = 3.00 \times 10^{10} \text{ cm/s}$$

Planck's constant

$$h = 6.63 \times 10^{-34} \text{ joule} \cdot \text{second} = 4.14 \times 10^{-15} \text{ eV} \cdot \text{second}$$

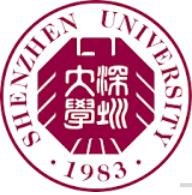
$$\hbar = h/2\pi$$

Vacuum permittivity

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ coulomb}^2/(\text{newton} \cdot \text{meter}^2)$$

Vacuum permeability

$$\mu_0 = 4\pi \times 10^{-7} \text{ weber}/(\text{ampere} \cdot \text{meter})$$

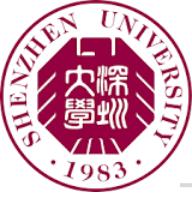


# 在科学家座谈会上的讲话

## (2020年9月11日)

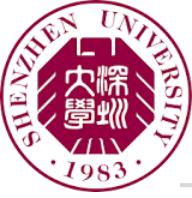
### 习近平

现在，我国经济社会发展和民生改善比过去任何时候都更加需要科学技术解决方案，都更加需要增强创新这个第一动力。同时，在激烈的国际竞争面前，在单边主义、保护主义上升的大背景下，我们必须走出适合国情的创新路子，特别是要把原始创新能力提升摆在更加突出的位置，努力实现更多“从0到1”的突破。希望广大科学家和科技工作者肩负起历史责任，坚持面向世界科技前沿、面向经济主战场、面向国家重大需求、面向人民生命健康，不断向科学技术广度和深度进军。



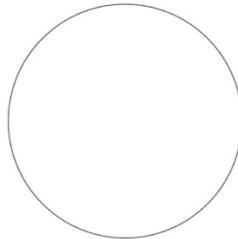
# How people in science see each other



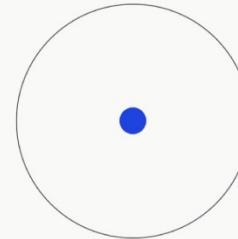


# The Illustrated Guide to a Ph.D by Matt Might

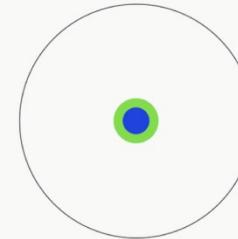
Imagine a circle that contains all of human knowledge:



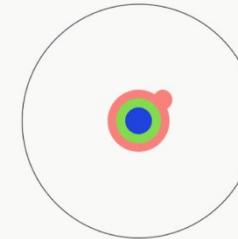
By the time you finish elementary school, you know a little:



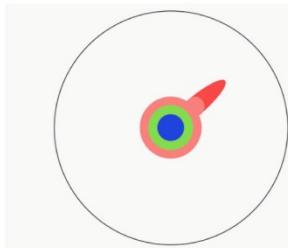
By the time you finish high school, you know a bit more:



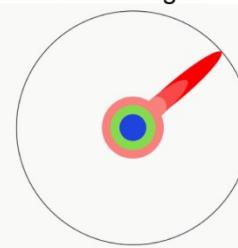
With a bachelor's degree, you gain a specialty:



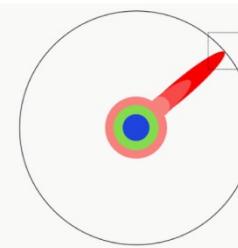
A master's degree deepens that specialty:



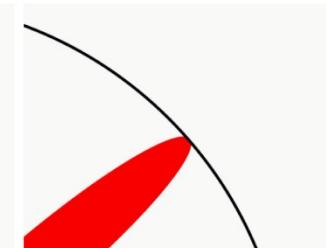
Reading research papers takes you to the edge of human knowledge:



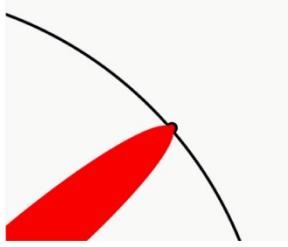
Once you're at the boundary, you focus:



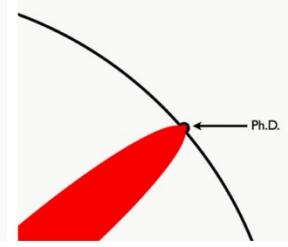
You push at the boundary for a few years:



Until one day, the boundary gives way:



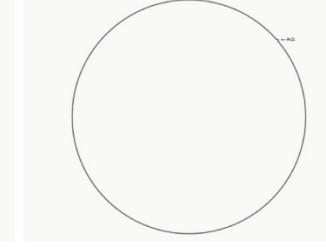
And, that dent you've made is called a Ph.D.:



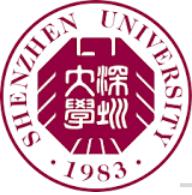
Of course, the world looks different to you now:

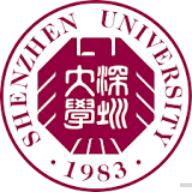


So, don't forget the bigger picture:



Keep pushing.

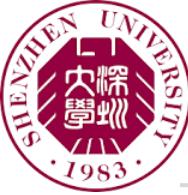




吾生也有涯，而知也无涯。以有涯随无涯，殆已！ —庄子

学而不思则罔，思而不学则殆。

— Confucius



## Reference books

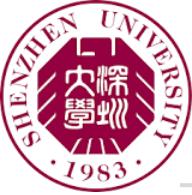
**Modern Atomic & Nuclear Physics, Fujia Yang and J. H. Hamilton, World Scientific Publishing Co., 2010**

原子物理学（第四版），杨福家，高等教育出版社，2008

**Introduction to Quantum Mechanics (2<sup>nd</sup> Edition), David J. Griffiths, 机械工业出版社 (reprint Edition)**

量子力学 卷I 曾谨言，科学出版社

量子物理（新概念物理教程），赵凯华 罗蔚茵 高等教育出版社



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## Chapter 1

### The Configuration of the Atom: Rutherford Model

## Chapter 2

### Introduction of Quantum Concepts and the Bohr Model

## Chapter 3

### Introductory Quantum Mechanics: Concepts and the Schrödinger Equation

## Chapter 4

### Fine Structure in Atomic Spectra: Electron Spin

## Chapter 5

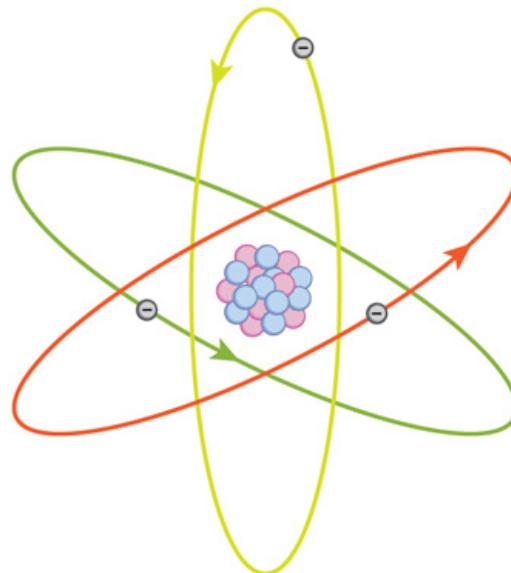
### Multi-Electron Atoms: The Pauli Exclusion Principle

## Chapter 6

### X-rays

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## Chapter 1 The Configuration of the Atom: Rutherford Model



atomic planetary model  
Rutherford, 1911

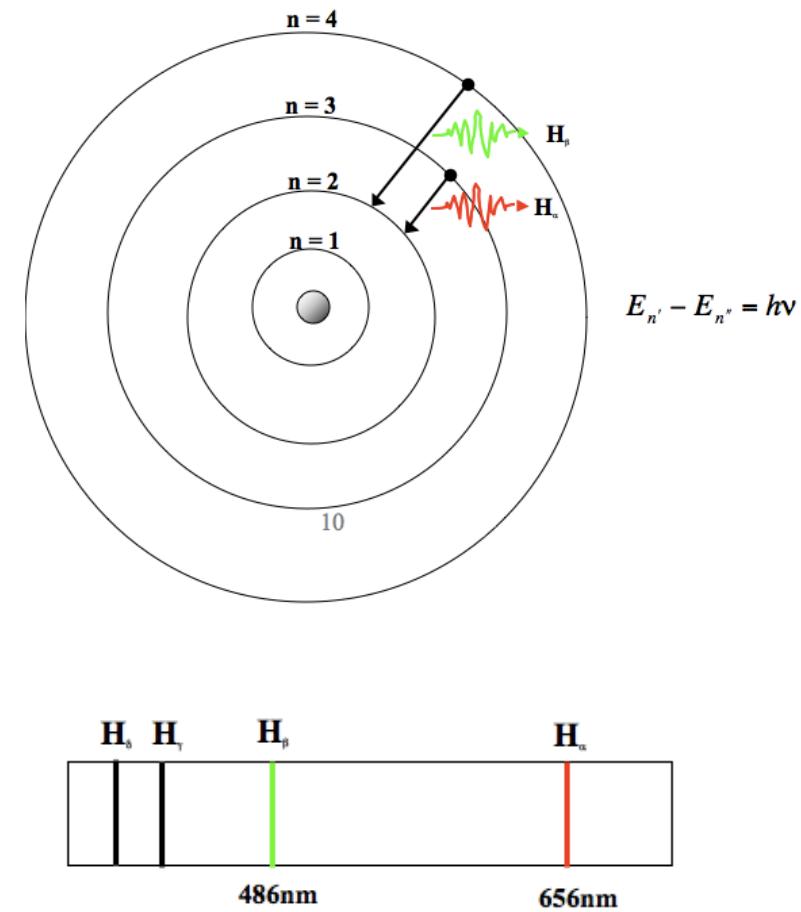
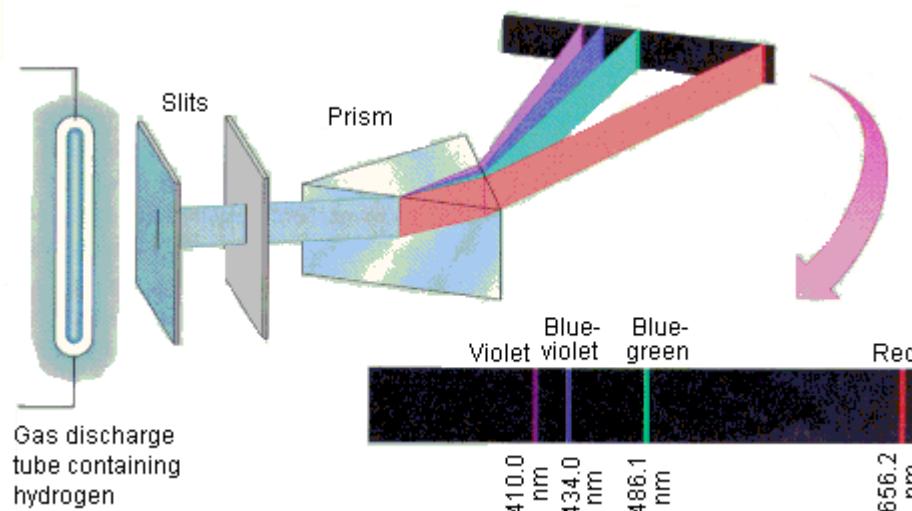


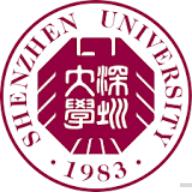
USA Atomic Energy Commission  
1946-1975

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## Chapter 2 Introduction of Quantum Concepts and the Bohr Model

### Spectrum of Atomic Hydrogen





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## Chapter 3

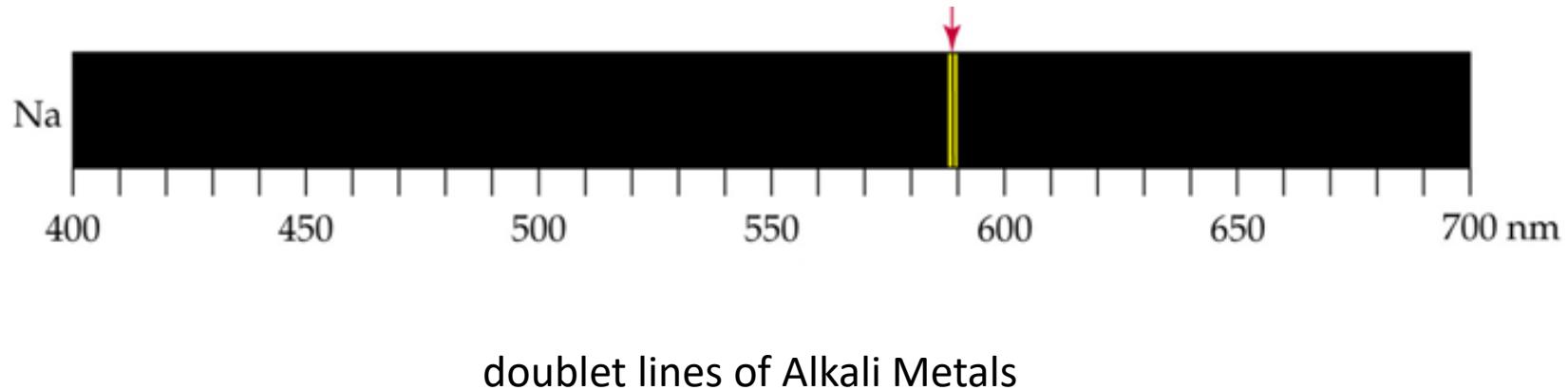
### Introductory Quantum Mechanics: Concepts and the Schrödinger Equation

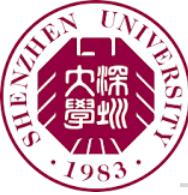
## Schrödinger equation

$$i\hbar \frac{\partial}{\partial t} \Psi(\mathbf{r}, t) = \hat{H}\Psi(\mathbf{r}, t)$$

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## Chapter 4 Fine Structure in Atomic Spectra: Electron Spin





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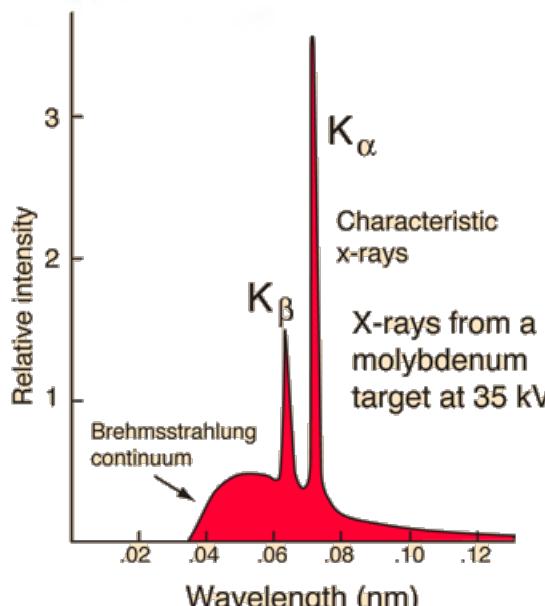
## Chapter 5 Multi-Electron Atoms: The Pauli Exclusion Principle

Mendeleev (1869)

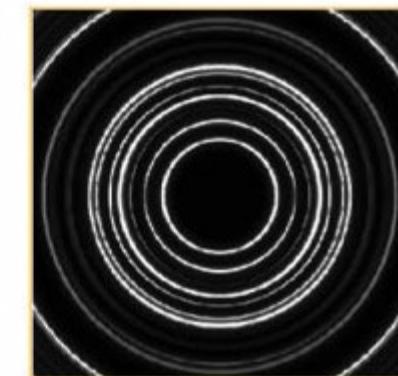
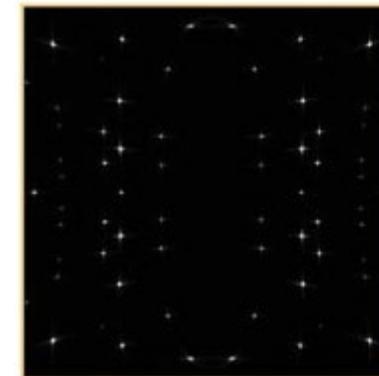
Periodic Table of the Elements																	
1 <b>H</b> Hydrogen 1.008	2 <b>He</b> Helium 4.003	3 <b>Li</b> Lithium 6.941	4 <b>Be</b> Beryllium 9.012	5 <b>B</b> Boron 10.811	6 <b>C</b> Carbon 12.011	7 <b>N</b> Nitrogen 14.007	8 <b>O</b> Oxygen 15.999	9 <b>F</b> Fluorine 18.998	10 <b>Ne</b> Neon 20.180	11 <b>Na</b> Sodium 22.990	12 <b>Mg</b> Magnesium 24.305	13 <b>Al</b> Aluminum 26.987	14 <b>Si</b> Silicon 28.086	15 <b>P</b> Phosphorus 30.974	16 <b>S</b> Sulfur 32.066	17 <b>Cl</b> Chlorine 35.453	18 <b>Ar</b> Argon 39.948
19 <b>K</b> Potassium 39.098	20 <b>Ca</b> Calcium 40.078	21 <b>Sc</b> Scandium 44.956	22 <b>Ti</b> Titanium 47.867	23 <b>V</b> Vanadium 50.942	24 <b>Cr</b> Chromium 51.996	25 <b>Mn</b> Manganese 54.938	26 <b>Fe</b> Iron 55.845	27 <b>Co</b> Cobalt 58.933	28 <b>Ni</b> Nickel 58.693	29 <b>Cu</b> Copper 63.546	30 <b>Zn</b> Zinc 65.38	31 <b>Ga</b> Gallium 69.723	32 <b>Ge</b> Germanium 72.631	33 <b>As</b> Arsenic 74.922	34 <b>Se</b> Selenium 78.972	35 <b>Br</b> Bromine 79.904	36 <b>Kr</b> Krypton 84.798
37 <b>Rb</b> Rubidium 85.468	38 <b>Sr</b> Strontium 87.62	39 <b>Y</b> Yttrium 88.906	40 <b>Zr</b> Zirconium 91.224	41 <b>Nb</b> Niobium 92.906	42 <b>Mo</b> Molybdenum 95.95	43 <b>Tc</b> Technetium 98.907	44 <b>Ru</b> Ruthenium 101.07	45 <b>Rh</b> Rhodium 102.906	46 <b>Pd</b> Palladium 106.42	47 <b>Ag</b> Silver 107.868	48 <b>Cd</b> Cadmium 112.411	49 <b>In</b> Indium 114.818	50 <b>Sn</b> Tin 118.711	51 <b>Sb</b> Antimony 121.760	52 <b>Te</b> Tellurium 127.6	53 <b>I</b> Iodine 126.904	54 <b>Xe</b> Xenon 131.294
55 <b>Cs</b> Cesium 132.905	56 <b>Ba</b> Barium 137.328	57-71 <b>Hf</b> Hafnium 178.49	72 <b>Ta</b> Tantalum 180.948	73 <b>W</b> Tungsten 183.84	74 <b>Re</b> Rhenium 186.207	75 <b>Os</b> Osmium 190.23	76 <b>Ir</b> Iridium 192.217	77 <b>Pt</b> Platinum 195.085	78 <b>Au</b> Gold 196.967	79 <b>Hg</b> Mercury 200.592	80 <b>Tl</b> Thallium 204.393	81 <b>Pb</b> Lead 207.2	82 <b>Bi</b> Bismuth 209.990	83 <b>Po</b> Polonium [208.982]	84 <b>At</b> Astatine 209.887	85 <b>Rn</b> Radon 222.018	
87 <b>Fr</b> Francium 223.020	88 <b>Ra</b> Radium 226.025	89-103 <b>Rf</b> Rutherfordium [261]	104 <b>Rf</b> Rutherfordium [261]	105 <b>Db</b> Dubnium [262]	106 <b>Sg</b> Seaborgium [266]	107 <b>Bh</b> Bohrium [264]	108 <b>Hs</b> Hassium [269]	109 <b>Mt</b> Methylmercury [268]	110 <b>Ds</b> Darmstadtium [269]	111 <b>Rg</b> Roentgenium [272]	112 <b>Cn</b> Copernicium [277]	113 <b>Nh</b> Nhium unknown	114 <b>Fl</b> Flerovium [289]	115 <b>Mc</b> Moscovium unknown	116 <b>Lv</b> Livermorium [298]	117 <b>Ts</b> Tennessee unknown	118 <b>Og</b> Oganesson unknown
57 <b>La</b> Lanthanum 138.905	58 <b>Ce</b> Cerium 140.116	59 <b>Pr</b> Praseodymium 140.908	60 <b>Nd</b> Neodymium 144.242	61 <b>Pm</b> Promethium 144.913	62 <b>Sm</b> Samarium 150.36	63 <b>Eu</b> Europium 151.964	64 <b>Gd</b> Gadolinium 157.25	65 <b>Tb</b> Terbium 158.925	66 <b>Dy</b> Dysprosium 162.500	67 <b>Ho</b> Holmium 164.930	68 <b>Er</b> Erbium 167.259	69 <b>Tm</b> Thulium 168.934	70 <b>Yb</b> Ytterbium 173.055	71 <b>Lu</b> Lutetium 174.967			
89 <b>Ac</b> Actinium 227.028	90 <b>Th</b> Thorium 232.038	91 <b>Pa</b> Protactinium 231.036	92 <b>U</b> Uranium 238.029	93 <b>Np</b> Neptunium 237.048	94 <b>Pu</b> Plutonium 244.064	95 <b>Am</b> Americium 243.061	96 <b>Cm</b> Curium 247.070	97 <b>Bk</b> Berkelium 247.070	98 <b>Cf</b> Californium 251.080	99 <b>Es</b> Einsteinium [254]	100 <b>Fm</b> Fermium 257.095	101 <b>Md</b> Mendelevium 258.1	102 <b>No</b> Nobelium 259.101	103 <b>Lr</b> Lawrencium [262]			
Alkali Metal		Alkaline Earth		Transition Metal		Basic Metal		Semimetal		Nonmetal		Halogen		Noble Gas		Lanthanide	

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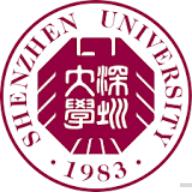
## Chapter 6 X-rays



X-ray emission spectrum



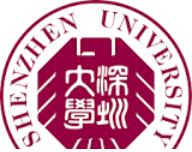
X-ray Diffraction (XRD)



# Grading Policy

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**Homework (30%)**  
**Attendance (10%)**  
**Final Exam (60%)**

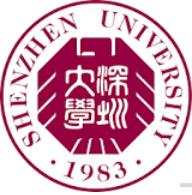


## 深圳大学期末考试试卷分析表

2018-2019学年第一学期

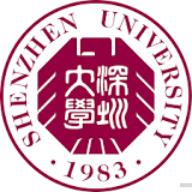
第1页，共1页

课程编号	6400370002		课程名称	量子力学（1）																		
课序号	01		课程类别	专业选修课																		
课程学分	4		考核表样式	期末考试(有附加题)																		
考试方式	闭卷		主讲教师	李武																		
实考人数	19																					
期末基本题得分情况	93~100:	1人, 占总数:	5.26%	<table border="1"><thead><tr><th>Score Range</th><th>Percentage (%)</th></tr></thead><tbody><tr><td>93~100</td><td>5.26%</td></tr><tr><td>85~92</td><td>36.84%</td></tr><tr><td>80~84</td><td>21.05%</td></tr><tr><td>75~79</td><td>5.26%</td></tr><tr><td>70~74</td><td>5.26%</td></tr><tr><td>65~69</td><td>5.26%</td></tr><tr><td>60~64</td><td>10.53%</td></tr><tr><td>0~59</td><td>10.53%</td></tr></tbody></table>	Score Range	Percentage (%)	93~100	5.26%	85~92	36.84%	80~84	21.05%	75~79	5.26%	70~74	5.26%	65~69	5.26%	60~64	10.53%	0~59	10.53%
	Score Range	Percentage (%)																				
	93~100	5.26%																				
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	70~74	5.26%																				
	65~69	5.26%																				
	60~64	10.53%																				
	0~59	10.53%																				
85~92:	7人, 占总数:	36.84%																				
80~84:	4人, 占总数:	21.05%																				
75~79:	1人, 占总数:	5.26%																				
70~74:	1人, 占总数:	5.26%																				
65~69:	1人, 占总数:	5.26%																				
60~64:	2人, 占总数:	10.53%																				
0~59:	2人, 占总数:	10.53%																				
最高分:	93	最低分:	15																			
平均分:	75.63	标准差:	18.28																			
附加题有效得分: 2人, 占总数: 10.53%																						



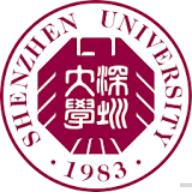
## A sample Exam Question

二. (10 points) When alpha particles are directed onto atoms in a thin foil, some make very close collisions with the nuclei of the atoms and are scattered at large angles. If an alpha particle with an initial kinetic energy of 5MeV happens to be scattered through an angle of 180 degree, what is its distance of the closest approach to the scattering nucleus?(Assume that the metal foil is made of silver, with  $Z=50$ .  $m_{\text{Ag}}=107.9\text{u}$ ,  $m_{\alpha}=4.0\text{u}$ )

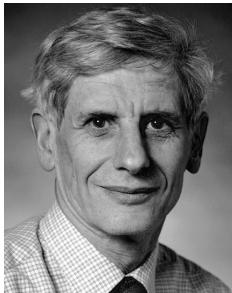


群名称: IAS2020量子力学(I)  
群号: 579464568

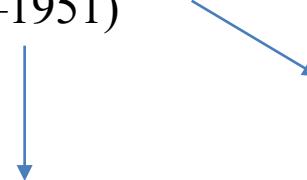
**Office hours:**  
**4-6pm,**  
**Wednesday,**  
**Office 341**



# Academic Family Tree



Arnold Sommerfeld  
(1868–1951)



Werner Heisenberg (1901-1976)  
**(Nobel Prize 1932)**



Hans Bethe (1906-2005)  
**(Nobel Prize 1967)**



Rudolf Peierls(1907–1995)



David J. Thouless, (1934-2019)  
**(Nobel Prize 2016)**



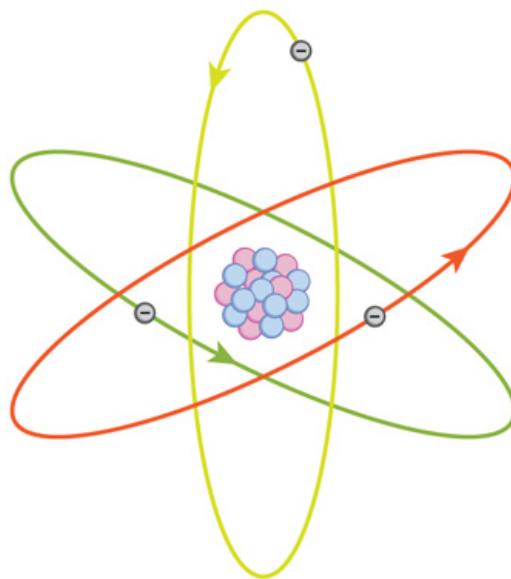
李武(SZU)

牛谦(UT Austin)

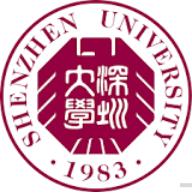
吴飙(PKU)

# Chapter 1

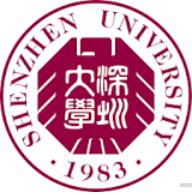
## The Configuration of the Atom: Rutherford Model



atomic planetary model  
Rutherford, 1911



## Lecture 02 Background



# 3 discoveries in the late 19th century

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X-ray (Rontgen, 1895)

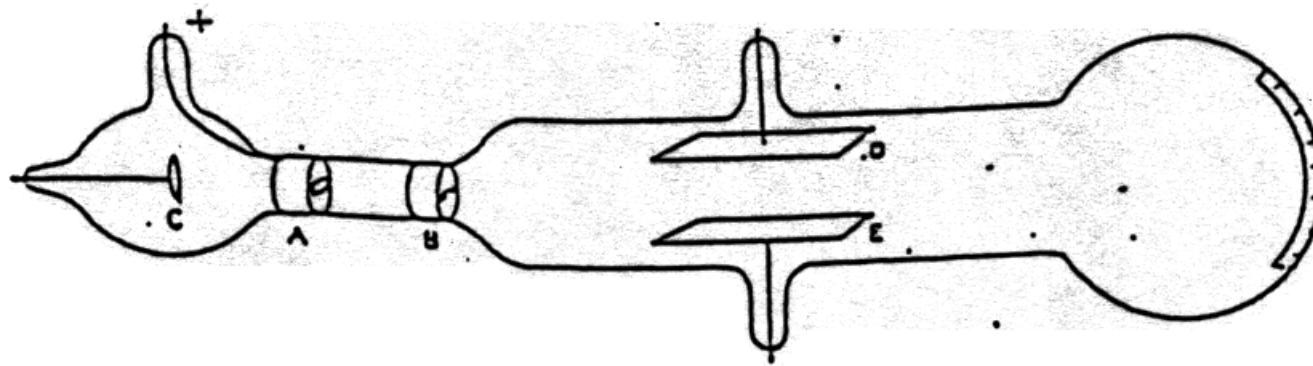
**Radioactivity (Becquerel, 1896)      beginning of nuclear physics**

Electron (Joseph J. Thomson, 1897)

# Electron Discovery Experiment

In 1874 G. J. Stoney introduced the concept “*fundamental unit quantity of electricity*”, and proposed the term “*electron*” in 1891.

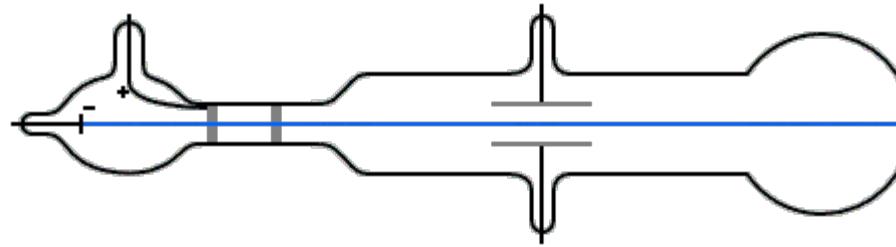
In 1897, Thomson discovered and identified electron in Crookes tube (discharge tube)



Cathode rays were emitted from the cathode C, passed through slits A (the anode) and B (grounded), then through the electric field generated between plates D and E, finally impacting the surface at the far end.

# Electron Discovery Experiment

Cathode rays could be deflected electrically => Cathode rays are negatively charged.

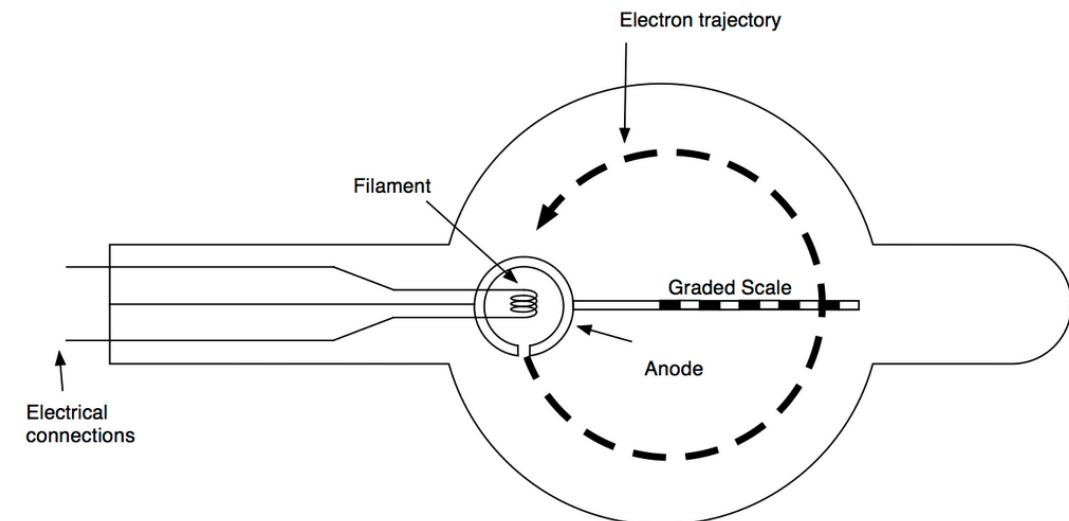
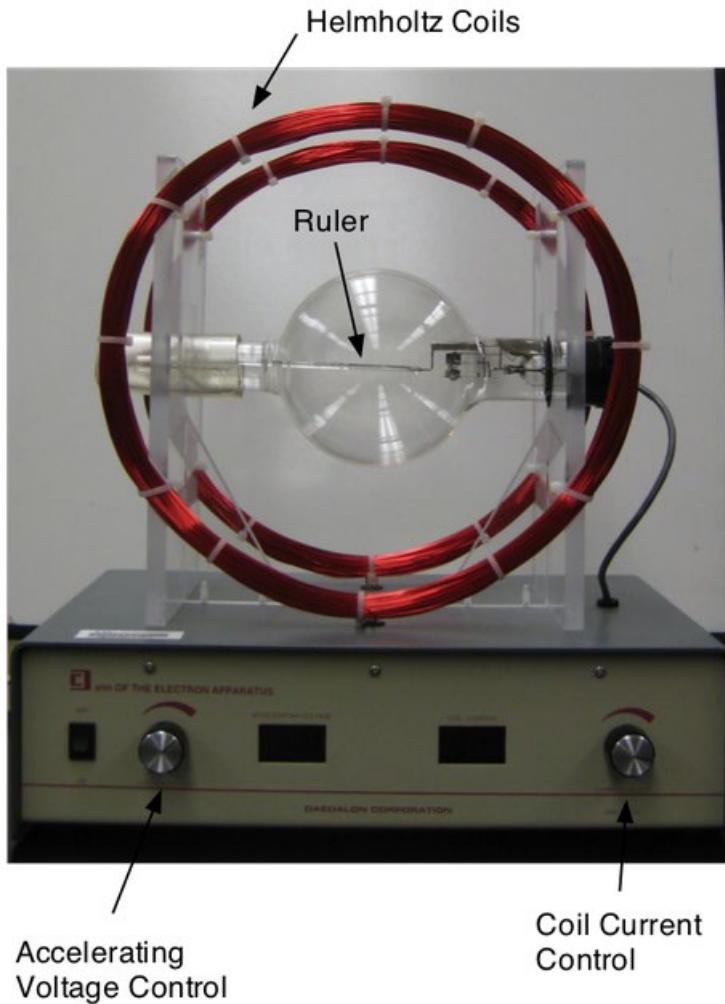


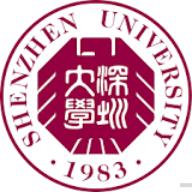
If further applying magnetic field  $H$  normal to screen,

$$v = E/H$$

# Electron Discovery Experiment

In the absence of electrical field and presence of magnetic field, the particles will travel along a circular arc.





# Electron Discovery Experiment

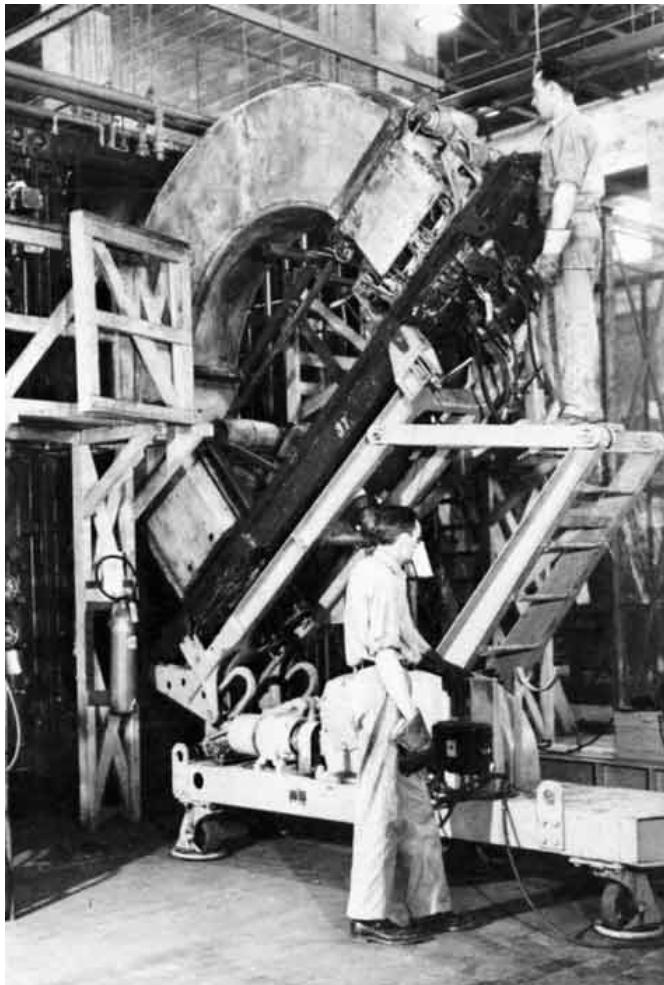
---

In 1890, A. Shuster observed a much larger charge-to-mass ratio for the cathode ray than that of  $H^+$  (referred to as *proton* in 1920 by Rutherford).

In 1897, W. Kaufman obtained much more accurate charge-to-mass ratio than J. Thomson did, and also discovered the velocity dependence of mass of the electron.

# Mass Spectrometry

principle: mass to charge ratio

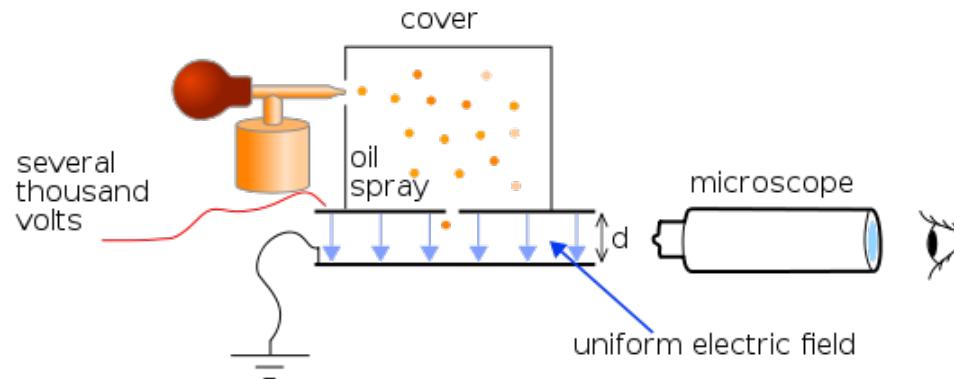


Calutron mass spectrometers were used in the Manhattan Project for uranium enrichment.



Inductively coupled plasma mass spectrometry

# Charge and Mass of the Electron



The drag force from Stokes's law

$$F_d = 6\pi r\eta v_1$$

and the effective weight

$$\mathbf{w} = \frac{4\pi}{3}r^3(\rho - \rho_{air})\mathbf{g}$$

should cancel out, suggesting

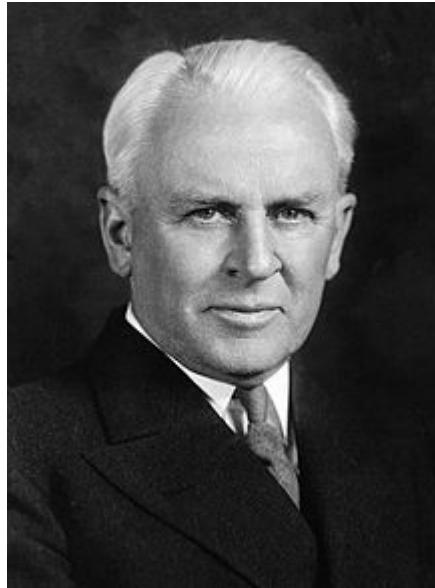
$$r^2 = \frac{9\eta v_1}{2g(\rho - \rho_{air})}.$$

Turn on an electric field  $\mathbf{E}$ , so that a new upwards terminal velocity is reached. Then

$$q\mathbf{E} - \mathbf{w} = 6\pi\eta(\mathbf{r} \cdot \mathbf{v}_2) = \left| \frac{\mathbf{v}_2}{\mathbf{v}_1} \right| \mathbf{w}.$$

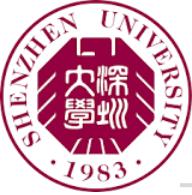
# Charge and Mass of the Electron

1910, Robert A. Millikan, Oil-drop experiment  
Nobel prize in 1923



(1868-1953)

Student: Chung-Yao Chao (赵忠尧), anomalously high scattering cross-section of Gamma rays (1930).



# Charge and Mass of the Electron

Electron charge reported by Robert A. Millikan:

$$e=1.59 \times 10^{-19} \text{ C},$$

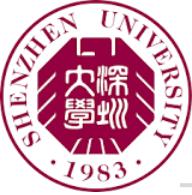
Which is 1% less than the modern value:

$$e=1.60217662 \times 10^{-19} \text{ C}.$$

Further from measured mass-to-charge ratio, one can obtain the **rest mass energy**

$$m_e = 9.10938215(45) \times 10^{-31} \text{ kg}$$

**approximately  $0.51 \text{ MeV}/c^2$**

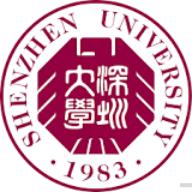


# Other things we learn from oil-drop experiments

**Quote from Richard Feynman:**

We have learned a lot from experience about how to handle some of the ways we fool ourselves. One example: Millikan measured the charge on an electron by an experiment with falling oil drops, and got an answer which we now know not to be quite right. It's a little bit off because he had the incorrect value for the viscosity of air. It's interesting to look at the history of measurements of the charge of an electron, after Millikan. If you plot them as a function of time, you find that one is a little bit bigger than Millikan's, and the next one's a little bit bigger than that, and the next one's a little bit bigger than that, until finally they settle down to a number which is higher.

Why didn't they discover the new number was higher right away? It's a thing that scientists are ashamed of—this history—because it's apparent that people did things like this: When they got a number that was too high above Millikan's, they thought something must be wrong—and they would look for and find a reason why something might be wrong. When they got a number close to Millikan's value they didn't look so hard. And so they eliminated the numbers that were too far off, and did other things like that...



# Other properties of the Electron

## LETTER

Nature, 473, 493 (2011) doi:10.1038/nature10104

### Improved measurement of the shape of the electron

J. J. Hudson<sup>1</sup>, D. M. Kara<sup>1</sup>, I. J. Smallman<sup>1</sup>, B. E. Sauer<sup>1</sup>, M. R. Tarbutt<sup>1</sup> & E. A. Hinds<sup>1</sup>

作者：邱徵文 来源：澎湃新闻 发布时间：2016/9/2 13:38:54

选择字号：小 中 大

#### Shape:

perfect sphere  
radius smaller than  $1E-17$  cm (C.C. Ting).

丁肇中：过去四十多年，我一直在找电子的半径

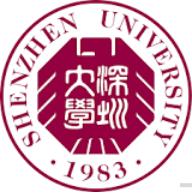
#### Spin

magnetic moment  
spin-orbit interaction



丁肇中  
诺贝尔物理学奖得主  
著名华裔物理学家

现在宇宙已经140多亿年了



# Avogadro constant

In 1811, A. Avogadro first proposed that the volume of a gas is proportional to the number of atoms or molecules regardless of the nature of the gas.

In 1909 Jean Perrin (Nobel laureate in 1926) proposed naming the constant in honor of Avogadro.

The earliest accurate method was based on **Coulometry**

$$N_A = \frac{F}{e}$$

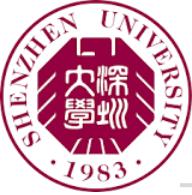
where F is Faraday constant (1833).

$k_B$  introduced by  
Planck (1900-1901)  
in *law of black  
body radiation*

It also links the gas constant R and Boltzmann constant:

$$R = k_B N_A$$

X-ray crystal density (XRCD) methods: the ratio of the molar volume  $V_m$  to the atomic volume  $V_{\text{atom}}$   
International Avogadro Coordination



## (Further reading) Estimation of Avogadro constant

Loschmidt constant (number density in the ideal gas)

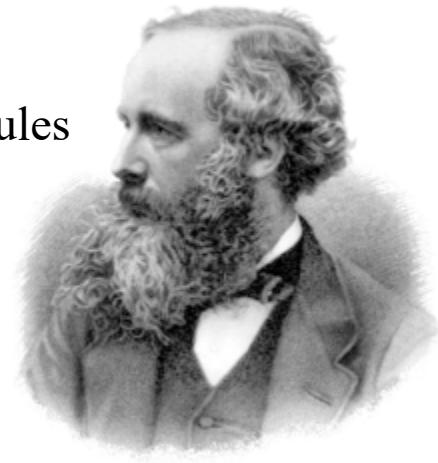
$$n_0 = \frac{p_0 N_A}{R T_0} \quad \text{connection with } N_A$$

It can be estimated from the mean free path and diameter of molecules

$$\ell = \frac{3}{4 n_0 \pi d^2} \quad \text{Kinetic theory}$$

Its modern value  $n_0 = 2.686\ 7805 \times 10^{25} \text{ m}^{-3}$

Loschmidt's estimate  $n_0 = 1.81 \times 10^{24} \text{ m}^{-3}$

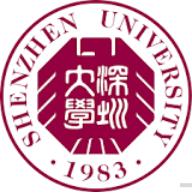


James Clerk Maxwell  
(1831–1879)

The diameter can be further related to the *condensation coefficient*

$$d = 8 \frac{V_l}{V_g} \ell$$

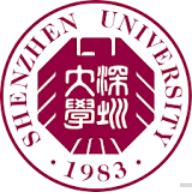
$$\text{yielding } n_0 = \left( \frac{V_g}{V_l} \right)^2 \frac{3}{256 \pi \ell^3}$$



# Size of the Atom

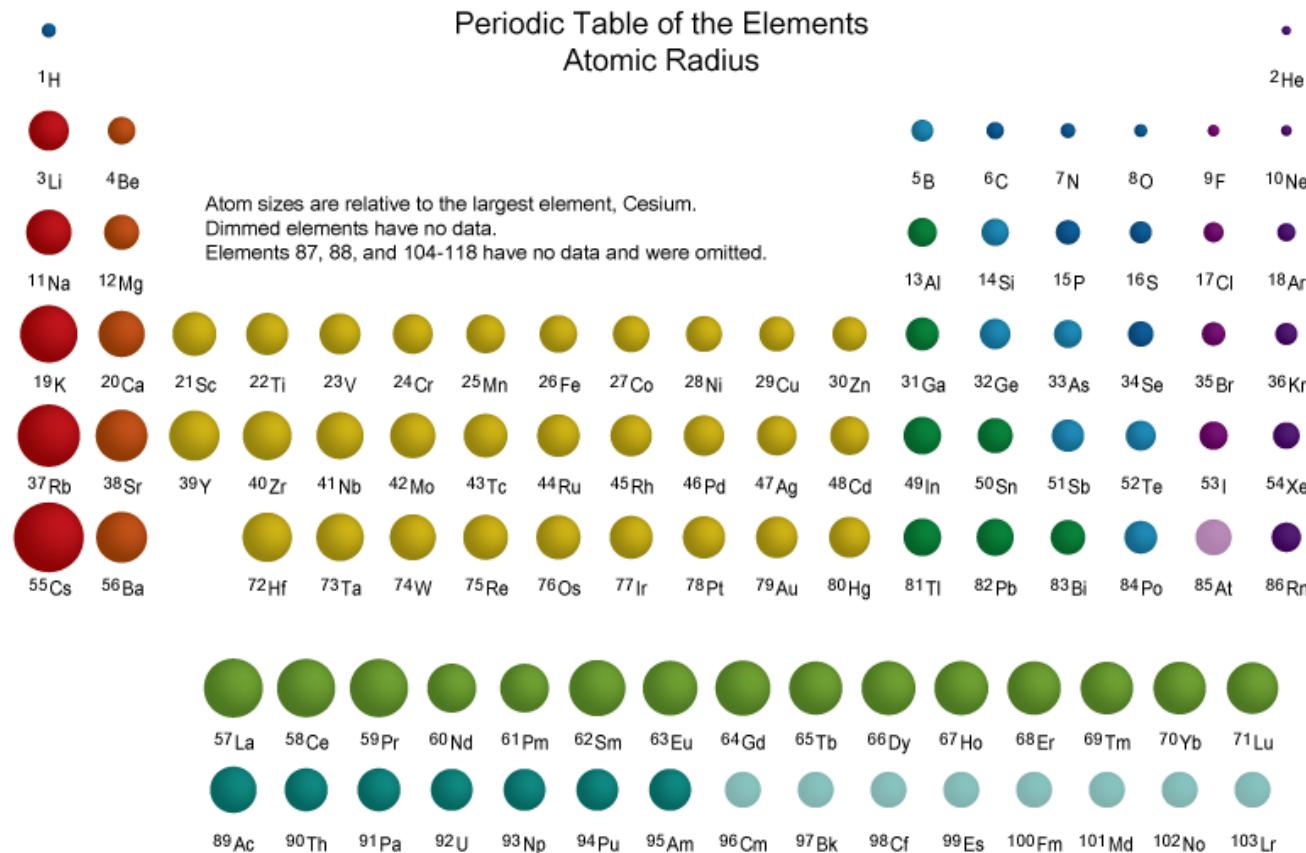
For an arbitrary atom  ${}^A X$ , the atomic radius  $r$  of  $X$  can be estimated as

$$\frac{4}{3} \pi r^3 N_A = \frac{A}{\rho}$$



# Size of the Atom

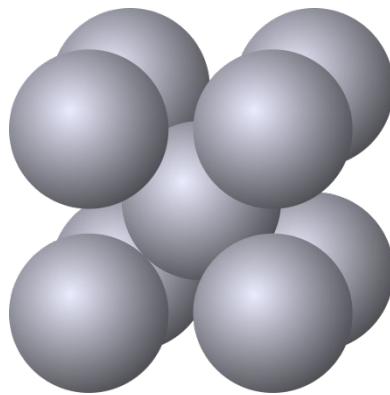
Atomic size: few angstroms



©2014 Todd Helmenstine  
sciencenotes.org

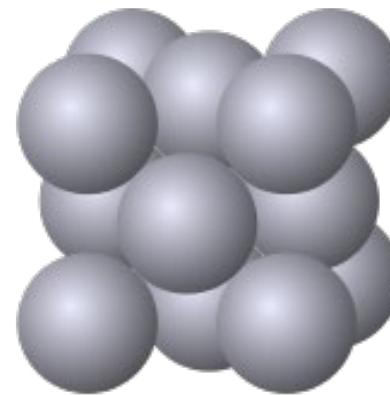
# (Further Reading) Size of the Atom

body centered cubic  
(BCC)



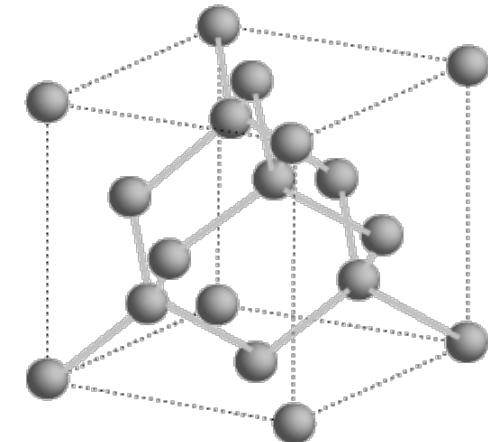
lithium

face centered cubic  
(FCC)



aluminum, lead, copper

diamond cubic



diamond, silicon

	atomic packing factor
simple cubic	0.524
bcc	0.680
<b>fcc</b>	0.740
diamond cubic	0.34

The **largest** packing factor

$$\frac{\pi}{3\sqrt{2}} \simeq 0.74048.$$

# Plum pudding model (Thomson)

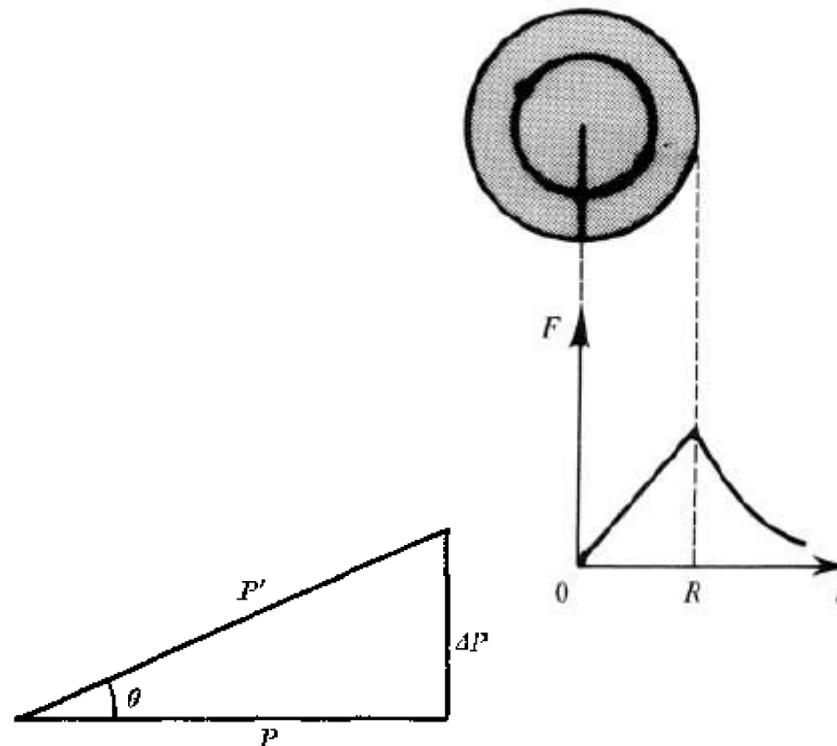


图 2.2 散射引起的动量变化

The positive charge in an atom was uniformly distributed in the spherical atom, and the electrons were embedded.

To explain the periodic table of elements, Thomson further assumed the electrons were distributed in rings.

**contribution from positive charges**

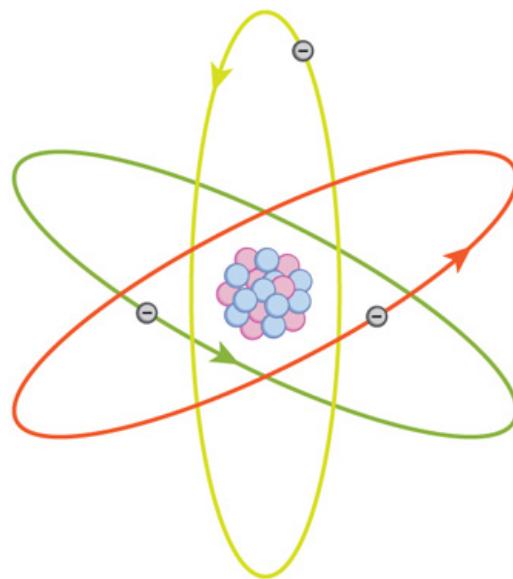
$$\frac{\Delta p}{p} = \frac{F 2R/v}{m_\alpha v} = \frac{2Ze^2/R}{\frac{1}{2}m_\alpha v^2} \simeq \frac{2Z \times 1.44 \text{ fm} \cdot \text{MeV}/1\text{\AA}}{E_\alpha(\text{MeV})}$$

$$\simeq 3 \times 10^{-5} \frac{Z}{E_\alpha} \text{ radian}$$

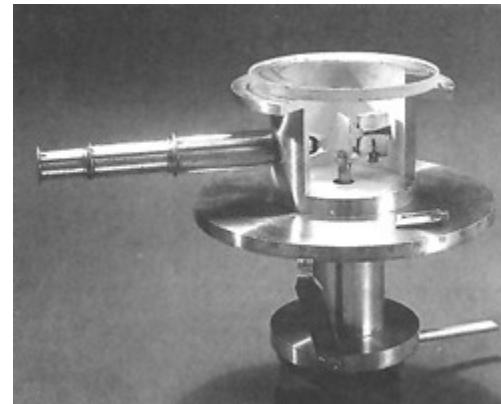
**negligible contribution from electrons**

$$\frac{\Delta p}{p} \simeq \frac{m_e}{m_\alpha} \sim \frac{1}{8000} \sim 10^{-4}$$

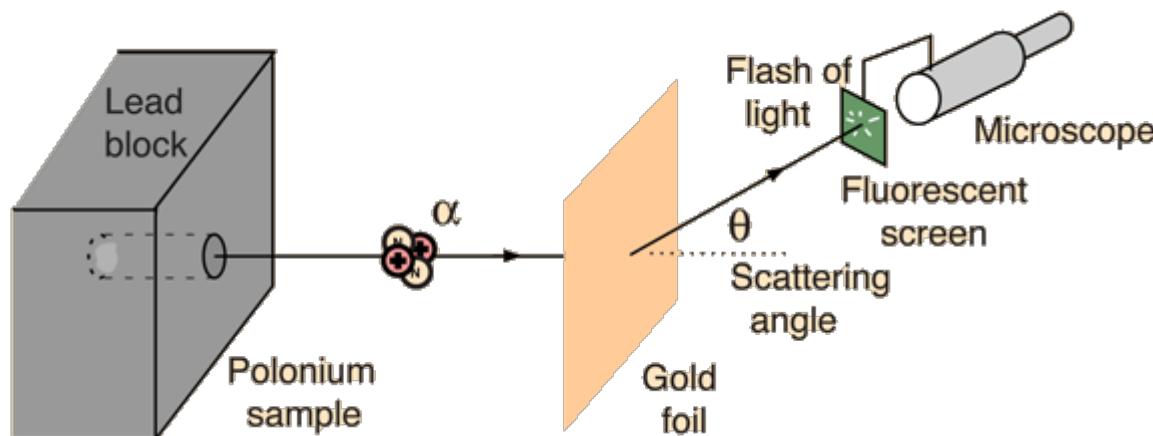
## Lecture 03 Rutherford Model



atomic planetary model  
Rutherford, 1911



## Geiger–Marsden experiment (1908-1913)

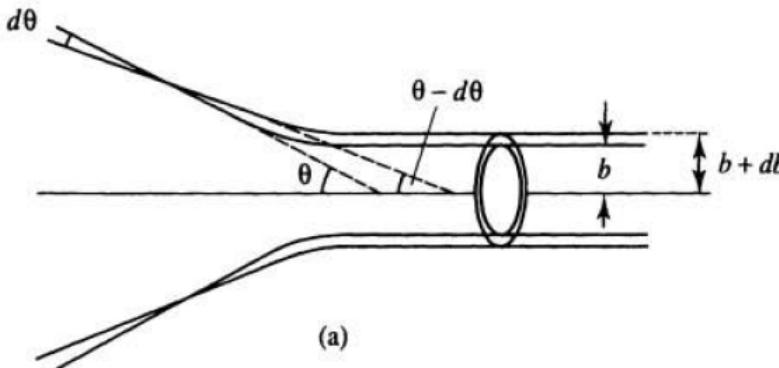


# differential (scattering) cross-section

## differential (scattering) cross-section

$$\frac{d\sigma}{d\Omega} = \frac{1}{j_i} \left( \frac{dn}{d\Omega} \right)$$

单位时间有 $dn$ 个粒子沿 $(\theta, \varphi)$ 方向的立体角 $d\Omega$ 出射

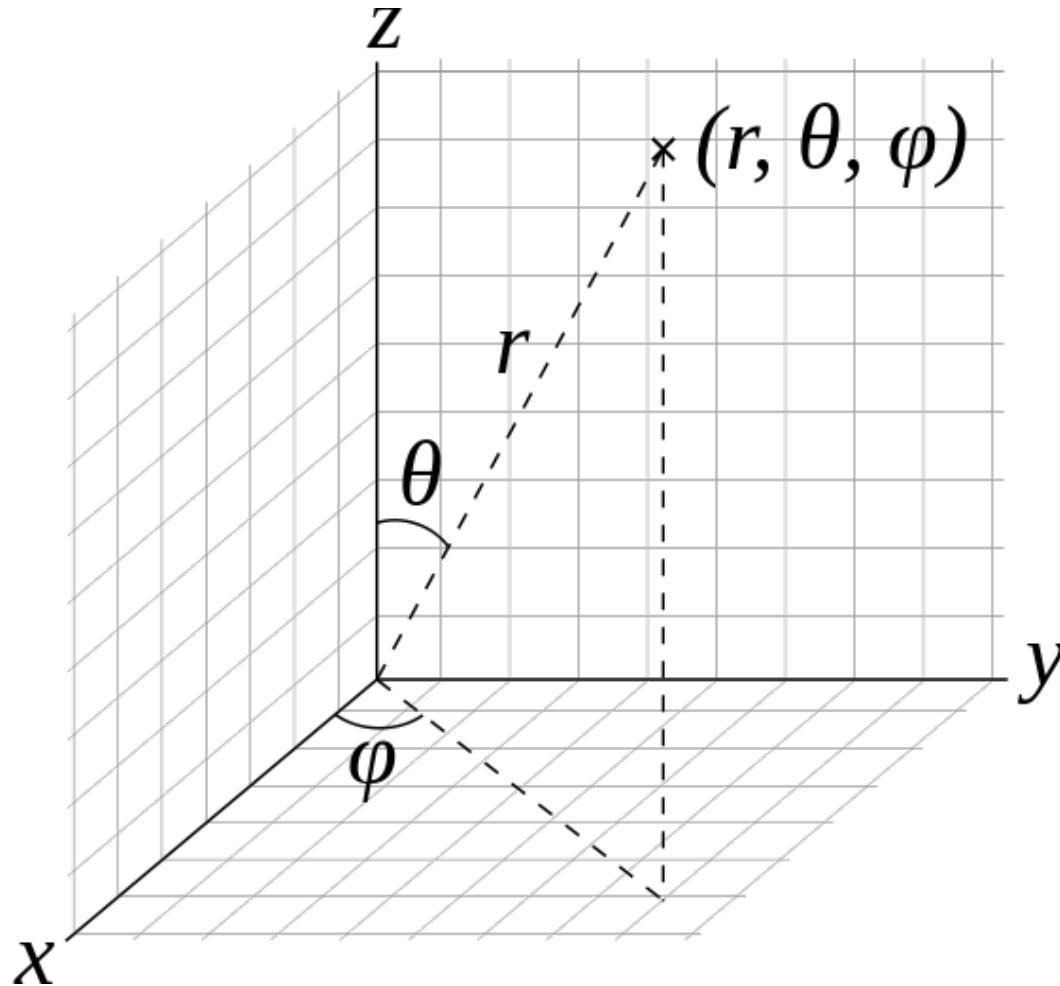


$j_i$ : 粒子入射密度 (单位时间穿过单位面积的粒子数)

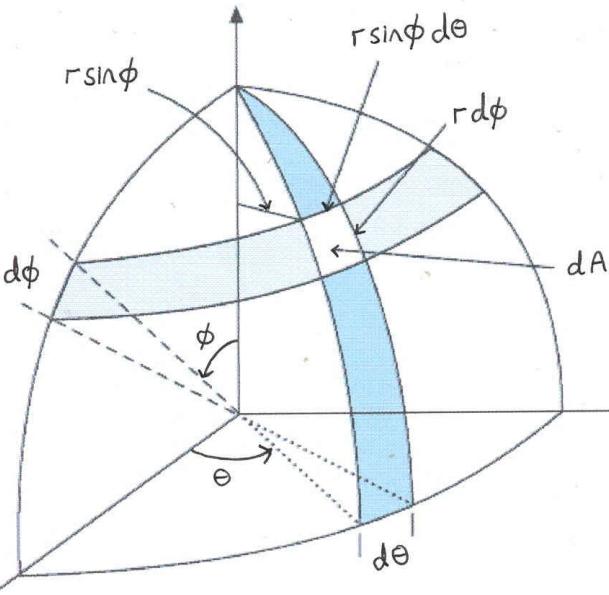
$$d\Omega = \sin\theta d\theta d\varphi$$

$$\frac{d\sigma}{d\Omega} = \left| \frac{b db}{\sin\theta d\theta} \right|$$

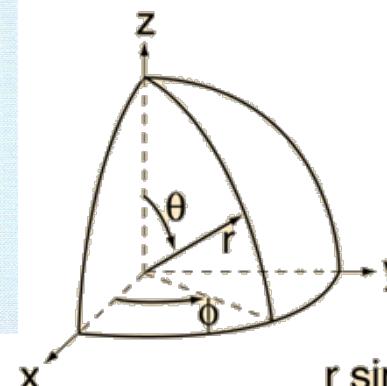
# Spherical Coordinate System



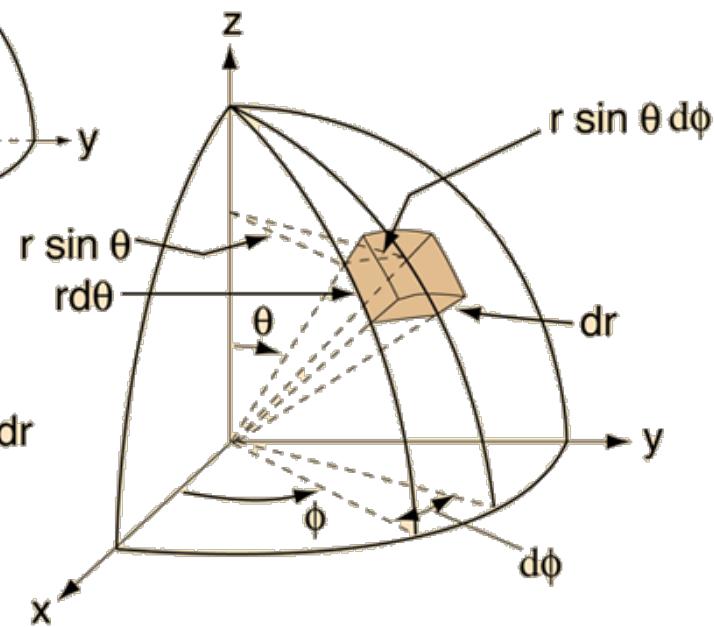
Spherical coordinates  $(r, \theta, \varphi)$  as commonly used in physics: radial distance  $r$ , polar angle (极角)  $\theta$  and azimuthal angle (方位角)  $\varphi$ .

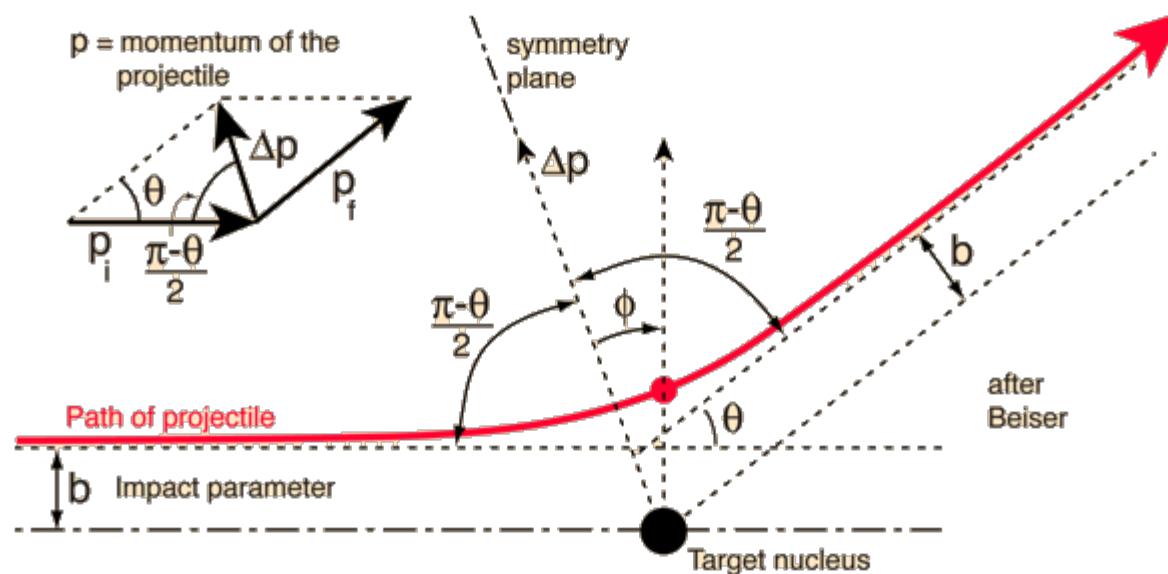


$$dA = r^2 \sin \theta d\theta d\phi$$



Volume element  
 $dV = r^2 \sin \theta d\theta d\phi dr$





### Coulomb scattering formula

$$b = \frac{a}{2} \cot \frac{\theta}{2} \quad \text{with} \quad a \equiv \frac{Z_1 Z_2 e^2}{E}$$

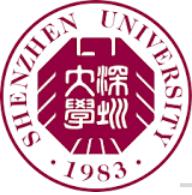
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**Impact parameter,  $b$  (fm)**

10  
100  
1000

**Angle of scattering,  $\theta$  (deg)**

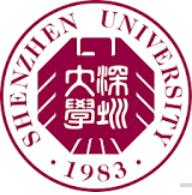
112  
16.9  
1.7



# Scattering Cross Section

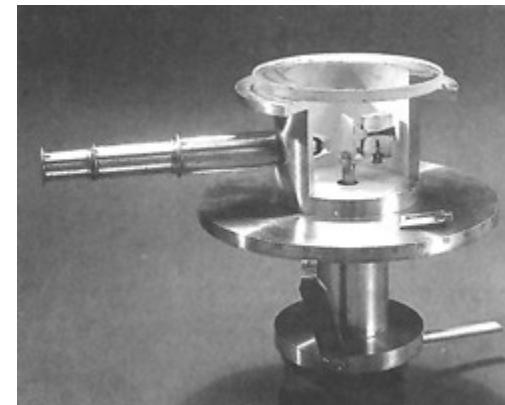
Rutherford's Formula

$$\frac{d\sigma}{d\Omega} = \left( \frac{Z_1 Z_2 e^2}{8\pi\epsilon_0 m v_0^2} \right)^2 \csc^4 \left( \frac{\Theta}{2} \right)$$



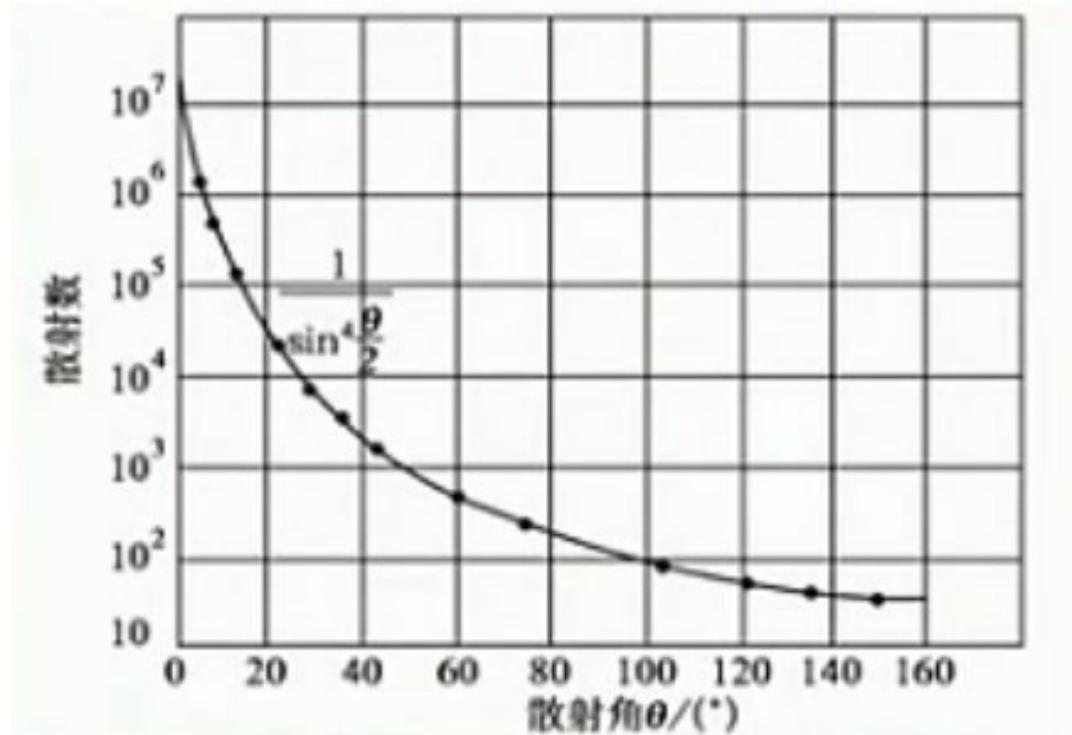
# Experimental Verification of Planetary Model

$$\frac{d\sigma}{d\Omega} = \left( \frac{Z_1 Z_2 e^2}{8\pi\epsilon_0 m v_0^2} \right)^2 \csc^4 \left( \frac{\Theta}{2} \right)$$

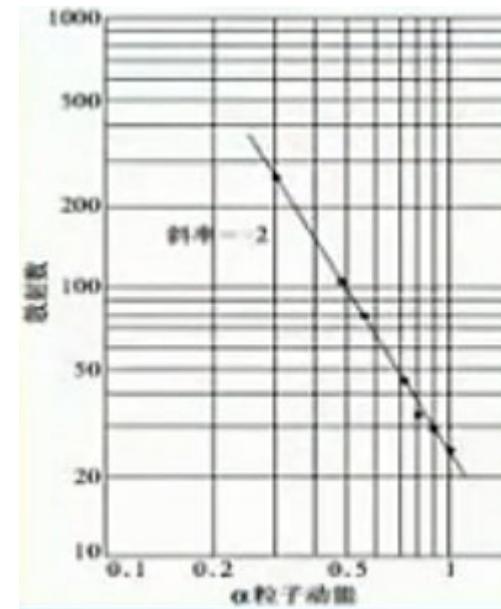


**Geiger–Marsden experiment (1908-1913)**

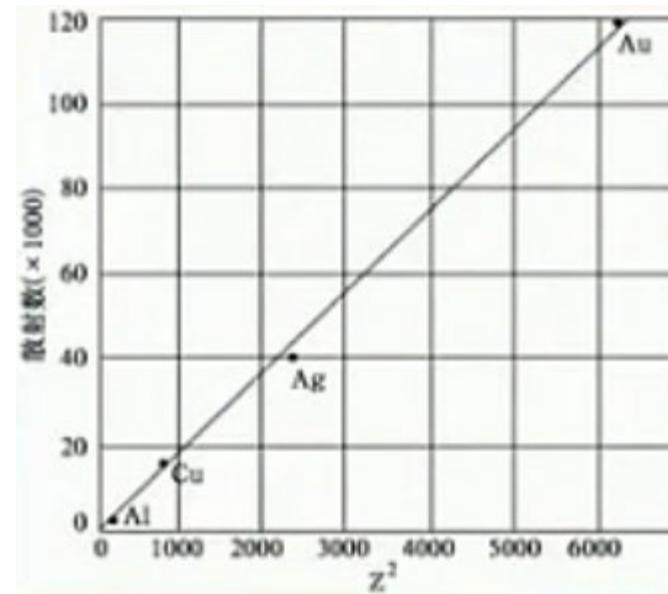
# Angle Dependence



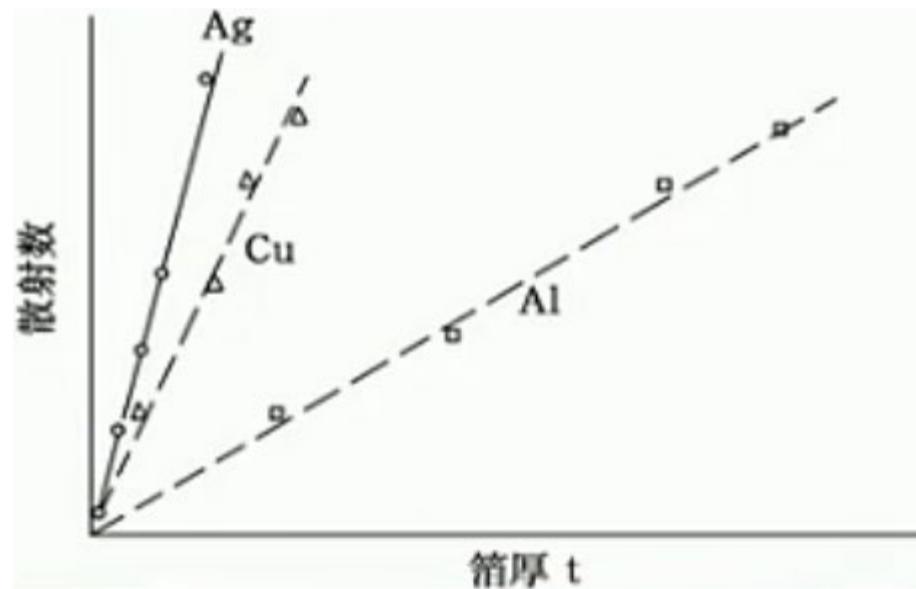
# Energy Dependence

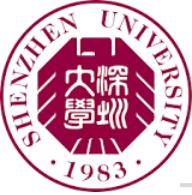


# Atomic Number Dependence



# Thickness Dependence





# Estimation of the Nuclear Radius

At **180°** scattering angle (**if Rutherford's formula still holds**)

$$\frac{1}{2}mv^2 = \frac{1}{4\pi\epsilon_0} \cdot \frac{q_1 q_2}{b}$$

$$b = \frac{1}{4\pi\epsilon_0} \cdot \frac{2q_1 q_2}{mv^2}$$

For an alpha particle:

$$m = 6.64424 \times 10^{-27} \text{ kg}$$

$$q_1 = 2 \times (1.6 \times 10^{-19}) \text{ C}$$

$$q_2 \text{ (for gold)} = 79 \times (1.6 \times 10^{-19}) \text{ C}$$

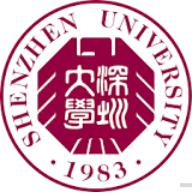
$$v \text{ (initial velocity)} = 2 \times 10^7 \text{ m/s}$$



8.28MeV

$b = 2.7 \times 10^{-14} \text{ m}$ . (The true radius is about  **$7.3 \times 10^{-15} \text{ m}$** .)

1 fm(**femtometre**) =  $1 \times 10^{-15} \text{ m}$       in nuclear physics



# Multiple Scattering Events

Gold foil:

nuclear radius:  $\sim 7$  fermis

atomic radius:  $\sim 0.13$  nm.

The geometrical cross section of the nucleus:  $\sim 154$  fm $^2$

The cross sectional area of the atom is then about  $3.45 \times 10^8$  times the area of the nucleus. The probability of an alpha particle hitting the nucleus would be  $\sim$  one in 345 million!

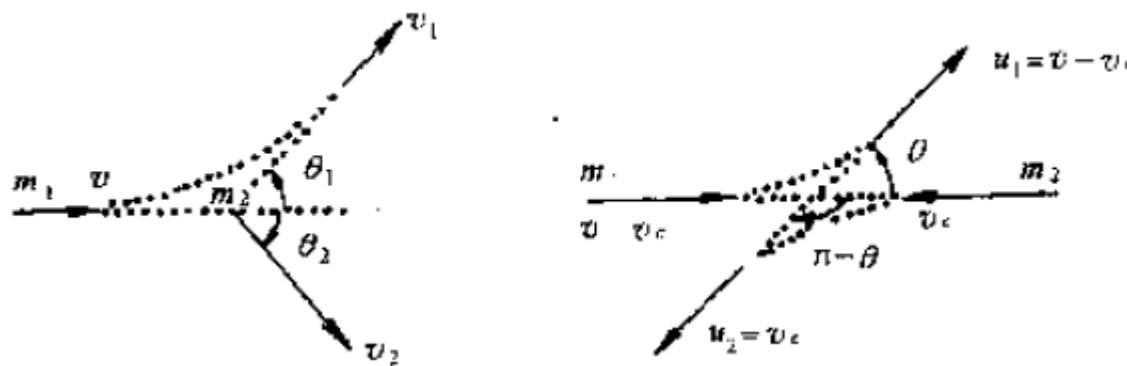
$3.45 \times 10^6$  layers of Gold (900 micrometers) is required to cover 1% of the area to have a 1% probability of a second scattering event.

The actual cross section for scattering above  $30^\circ$  is  $\sim 15730$  fm $^2$ , implying that the thickness is **9 micrometers**.

**1 micrometer** in Rutherford's experiment.

# Scattering Cross Section

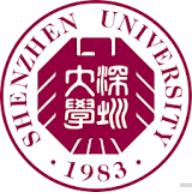
When the target nucleus cannot be regarded as fixed,



lab frame vs center of mass frame  
two-body  $\Rightarrow$  one-body

the reduced mass

$$\mu = \frac{mM}{m + M}$$

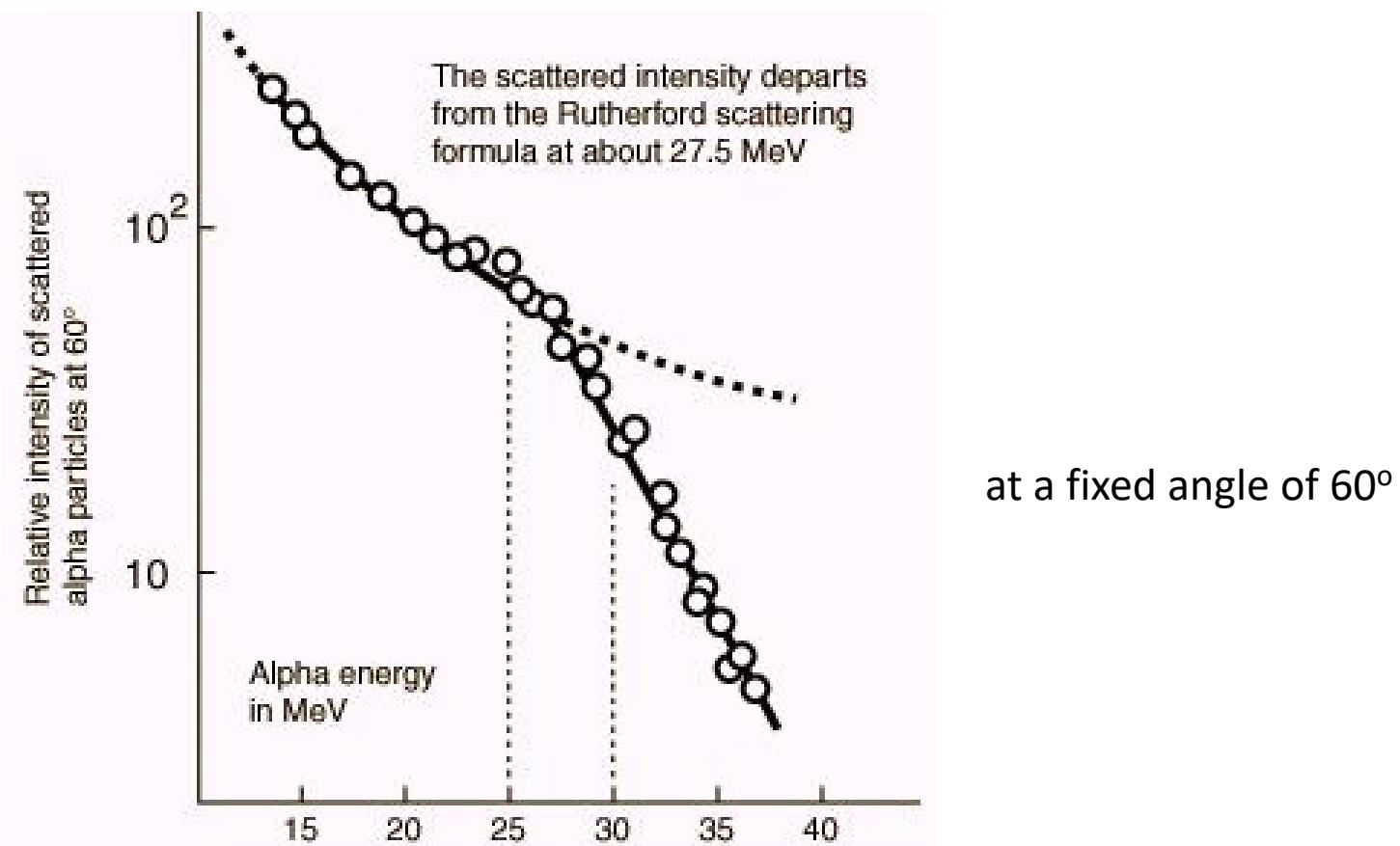


# Failure at small angles

$$\frac{d\sigma}{d\Omega} = \left( \frac{Z_1 Z_2 e^2}{8\pi\epsilon_0 m v_0^2} \right)^2 \csc^4 \left( \frac{\Theta}{2} \right)$$

**long range** nature of Coulomb potential  
**screened** Coulomb potential (electron)

# Deviation from Rutherford's Formula

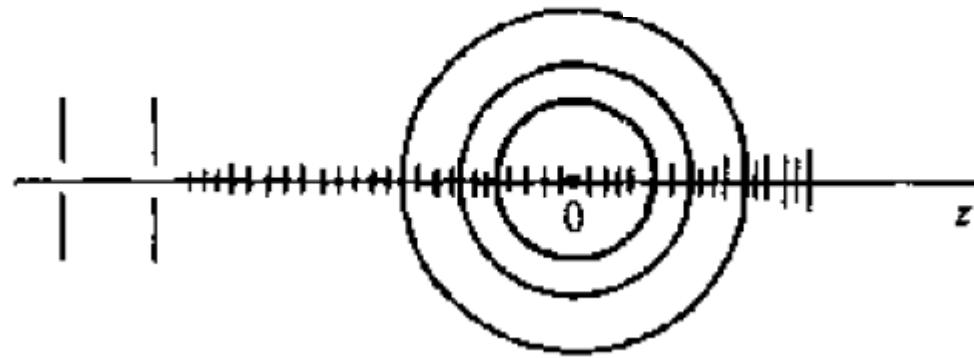


The relativistic correction has been obtained by N. F. Mott within the framework of QED

$$d\sigma(\theta, E)/d\Omega = [(Ze^2E)/(2|\mathbf{p}|^2c^2)]^2 \cdot \{[(1 - \beta^2 \sin^2(\theta/2))/\sin^4(\theta/2)]\} \text{ ----- (38d)}$$

where  $\mathbf{p}$  is the momentum of the incident particle,  $E = (m_0^2 c^4 + \mathbf{p}^2 c^2)^{1/2}$ , and  $\beta = |\mathbf{p}|c/E$ .

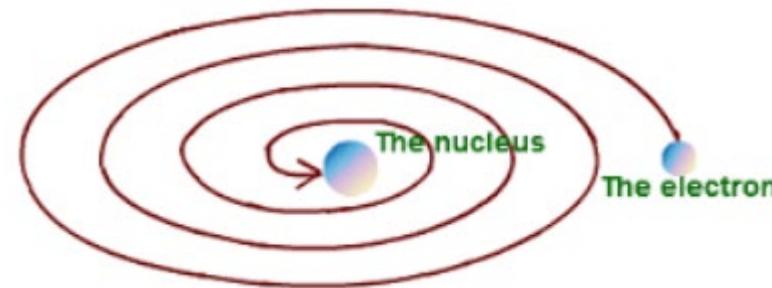
# Quantum Mechanical Description



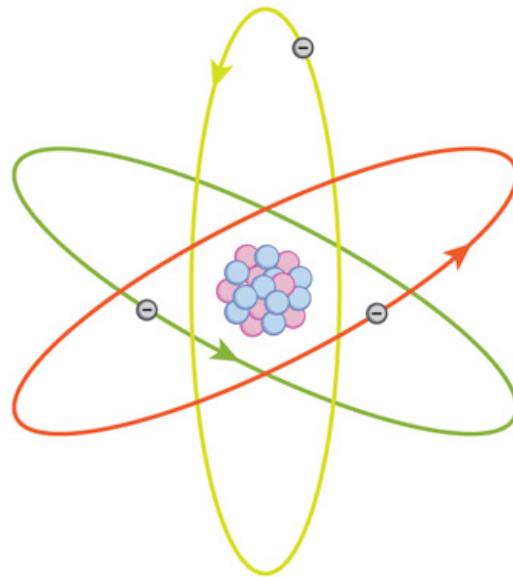
$$\psi \xrightarrow{r \rightarrow \infty} \exp[ikz] + f(\theta) \frac{\exp[ikr]}{r}$$

$$\frac{d\sigma}{d\Omega} = |f(\theta)|^2$$

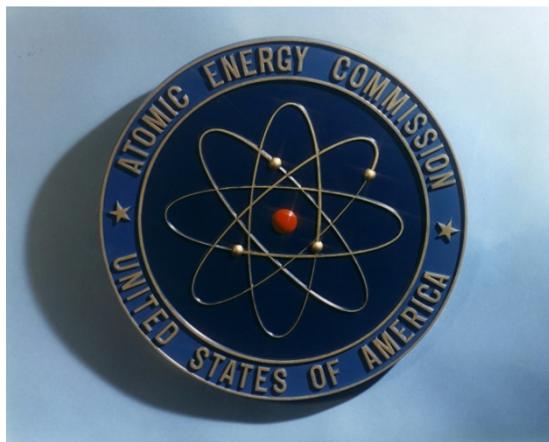
# Difficulties



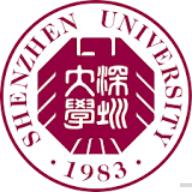
# Significances



atomic planetary model  
Rutherford, 1911



USA Atomic Energy Commission  
1946-1975



# Significances

The most beautiful experiments voted from *Physics World* (2002):

- (1) Young's double-slit experiment applied to the interference of single electrons;
- (2) Galileo's experiment on falling bodies (1600s);
- (3) Millikan's oil-drop experiment (1910s);
- (4) Newton's decomposition of sunlight with a prism (1665–1666);
- (5) Young's light-interference experiment (1801);
- (6) Cavendish's torsion-bar experiment (1798);
- (7) Eratosthenes's measurement of the Earth's circumference (3<sup>rd</sup> century BC);
- (8) Galileo's experiments with rolling balls down inclined planes (1600s);
- (9) Rutherford's discovery of the nucleus (1911);
- (10) Foucault's pendulum (1851).

# Scattering Spectroscopy

Rutherford back scattering spectrometry

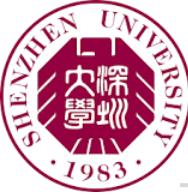
**principle: Z dependence of cross section**



Neutron backscattering spectroscopy

X-ray spectroscopy

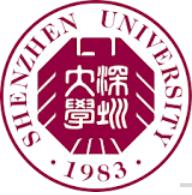
Electron spectroscopy



# Collider

Accelerator	Centre, city, country	First operation	accelerated particles	max energy per beam, GeV
VEPP-2000	INP, Novosibirsk, Russia	2006	e <sup>+</sup> e <sup>-</sup>	1.0
VEPP-4M	INP, Novosibirsk, Russia	1994	e <sup>+</sup> e <sup>-</sup>	6
BEPC II	IHEP, Beijing, China	2008	e <sup>+</sup> e <sup>-</sup>	3.7
DAFNE	Frascati, Italy	1999	e <sup>+</sup> e <sup>-</sup>	0.7
KEKB	KEK, Tsukuba, Japan	1999	e <sup>+</sup> e <sup>-</sup>	8.5 (e-), 4 (e+)
RHIC	BNL, United States	2000	pp, Au-Au, Cu-Cu, d-Au	100/n
LHC	CERN	2008	pp, Pb-Pb, p-Pb	6500 (planned 7000), 1580/n (planned 2760/n)





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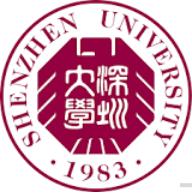
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cost: 20 billion \$



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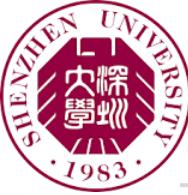
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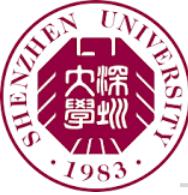
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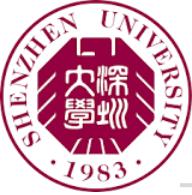
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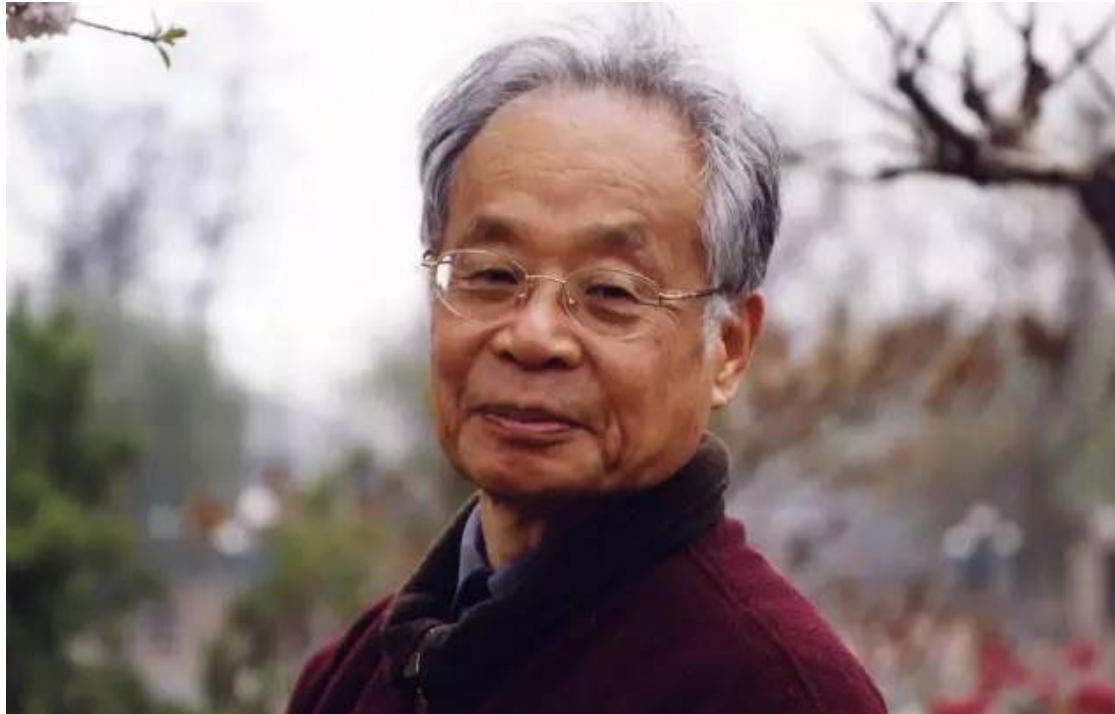
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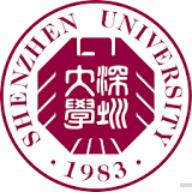


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