MBL-Exercises

```
EXERCISE @ex:myLabel
```

```
% All of the following "attributes" are optional.
% Attributes MUST be listed before code and text
% The curent exercise can only be solved, if dependent
% exercises have been passed before
REQUIREMENT=ex:myEx1,ex:myEx2
% forbid shuffling of single/multiple choice answers
ORDER=static
                            % default is shuffle
% display (short!) single/multiple choice answers horizontally
CHOICE ALIGNMENT=horizontal % default is vertical
% forbid student to reanswer exercise
DISABLE RETRY=true % default is false
% Limited time to solve the question [seconds].
TIME=4
                             % default is -1 := not timed
% total score weighting for this exercise. Default score per
% answer is 1. The sum of scores of all answers is weighted
% to the attribute given here.
SCORES=4
                             % default is 1
% generates random variables and calculates the solution.
CODE
   let u = true
   let f(x) = x^2 + c % f(x) = x^2 + 4
   let g(x) = x^2 + term(c) % g(x) = x^2 + 1 + 3
   let h(x) = 2x + 5x % h(x) = 2x + 5x

let y(x) = opt(h) % y(x) = 7x (opt := optimize)
   let w(x) = sin(2x) + 3x
   Multiple Choice:
[x] correct answer
```

- [] incorrect answer
- % Dynamic answers. Only the name of a variable can be given % here. Calculations must be done in part CODE.
- [:d] correct iff \$a > b\$ is true
- [:u] correct answer, given per variable

```
Single Choice:
(x) correct answer
( ) incorrect answer
% Asks "1 + 3 = [ ]" and provides a keyboard with
% integer numbers.
$a+b=$ <mark>#c</mark>
% Asks "\int (x^2+4) dx = [ ] +C (CER)" and provides a
% keyboard for terms.
% The student answer is <u>first</u> differentiated w.r.t.
% variable x, and then it is evaluated, i.e. compared to
% variable f.
% Asks "Garfield is a _ _ _ .".
% The keyboard only shows letters \{a,c,t\} in shuffled order.
Garfield is a #"cat".
% Per default, gap answers give a hint on the number of
% characters needed. Also the keyboard is restricted to the
% letters that occur in the solution.
% Use the following attributes to change that behavior.
Garfield is a #"cat", HIDE_LENGTH, SHOW_ALL_LETTERS.
% Asks "Order the numbers ascendingly: [3] [2] [4] [1]"
% A correct answer is rewarded with 3 scores.
% \rightarrow \text{multiple attributes can be combined with "," as separator}
Order the numbers ascendingly: #v,ARRANGE,SCORE=3
% Asks "The 3x3 identity matrix is [ ]".
% Per default, the student only needs to give the elements
% of the solution matrix. If attributes ROWS and/or
% COLS are set to dynamic, then the student also
% needs to find the matrix dimensions.
The 3x3 identity matrix is #I,ROWS=dynamic,COLS=dynamic
```

```
% Asks "(\sqrt{-1})^2 = [ ]". Since variable s is integral (-1), the
% default keyboard would only contain numeral keys.
% To "confuse" students, a keyboard with key "i" would be
% nice. Attribute KEYBOARD sets an existing or custom
% keyboard.
$term(s)=$ #s,KEYBOARD=myKeyboardName
% Asks "1 + 3 = [A][B][C]..." and provides one correct
% and (n-1) incorrect answers (e.g. \{2,5,6,\underline{4},1\} for CHOICES=5)
$a+b=$ #c,CHOICES=5
% Asks "f(x) = \sin(2x) + 3x, f'(x) = [ ]" and shows (e.g.)
% tokens [+] [*] [\sin(2x)] [3] [2] [\cos(2x)] [4] [1]
% that must be selected to build the solution term,
% here: "f'(x)=2*\sin(2*x)+3".
% Tokens are automatically derived from the solution term.
% The constant 1.5 is the factor of automatically generated
% tokens (based on the number of essential tokens). If this
% number is equal to 1, then each generated token is useful
% for the solution.
% Additional tokens (for student confusion) can be provided by
% adding +"MY TOKEN 1"+"MY TOKEN 2".... Tokens are in SMPL
% math format.
f''(x)=w, f'(x)=$ \#wd, TOKENS=1.5+"pi"
```

Keyboard definition

% keyboards must currently be inserted manually into the app code. KEYBOARD myKeyboardName

```
% Keys are separated by one or more spaces.
% A "submatrix" where each of the elements is the same
% is rendered as large key (e.g. "sqrt(" in the example spans
% two columns).
% Special key "!B" is the backspace key.
% Special key "!E" is the enter key.
789 +
                  !B
456 *
                  !B
1 2 3 ^(
           )
0 i pi sqrt( sqrt( !E
```

^{1 &}lt;a href="https://github.com/mathebuddy/mathebuddy/blob/main/app/lib/keyboard">https://github.com/mathebuddy/mathebuddy/blob/main/app/lib/keyboard layouts.dart

GAME Codename "Event"

(refer to slides in Sciebo)

EVENT % level name

#####

EXERCISE % level contains n≥1 exercises

TIME=5

•••

EXERCISE

...

GAME Codename: "Tetris" (... it's not Tetris)

Answers (or term-tokens) are falling down from top to bottom

→ the student must move them left or right (or keep middle)
in limited time

→ speed accelerates...

Example

		rt falling token rrently falling token
$f(x) = 3x^2$ f'(x) = 6	$f(x) = \sin(x)$ $f'(x) =$	f(x) = cos(x) $f'(x) =$

TETRIS % level name ######

EXERCISE % level contains exactly 1 exercise

 $\mbox{\%}$ shown columns (maybe two columns are the limit on

% smartphones with small displays...??)

COLUMNS=3

f(x)=ff

f'(x) = #ffd, TOKENS

let ffd(x) = diff(ff)

% code instances; each instance must provide all referenced
% variables

CODE

```
let a/b = rand(2,7)
  let ff(x) = a x^b % "*" can be omitted :-)
  let ffd(x) = diff(ff)

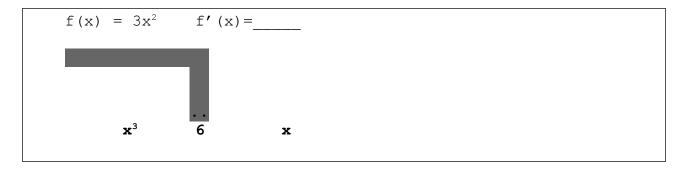
CODE
  let ff(x) = sin(x)
  let ffd(x) = diff(ff)

CODE
  let ff(x) = cos(x)
```

. . .

GAME Codename: "Snake"

The answer (or tokens) are randomly placed in a 2D-grid. A snake, that keeps moving into a direction until changed, must be controlled towards the next correct solution. If the solution is "eaten", the snake gets larger. Speed accelerates...



SMPL-Loops & Conditions

```
let x = 5
% execute block \{...\}, while x > 0 is true
while x > 0 {
  x = x - 1
}
% execute block once and repeat loop as long as x < 5 is true
do {
   x = x + 1
} while x < 5
let f = 1
% set (new) variable k to 1, 2, 3, 4, 5 and run the block each
% iteration
for k from 1 to 5 { % bounds can also be terms
   f = f * k
}
x = 4
let s = 0
               % s := sign(x)
if x > 0 {
   s = 1
} elif s < 0 { % elif := else if</pre>
   s = -1
} else {
  s = 0
               % redundant here, since s is already 0
}
```

MATH-RUNTIME:

OPERAND-TYPE EXAMPLE(s) boolean true, false -3, 4 int rational 4/7 3.14, -1.337 real irrational pi, e 4+5i complex vector [1,2,3+4i]matrix [[1,2],[3,4],[5,6]] (3x2 matrix) { 3, 4, 4/3 } set identifier **blub** "hello, world!" string

List of nullary functions (ups; dimensions are some kind of non-null-arity):

List of unary functions: TODO: acos, asin, ...

```
absolute value of x (int, vector, cmplx, ...)
abs(x)
                  argument of complex x
arg(x)
                  smallest integer that is \geq x
ceil(x)
                  number of columns of matrix x
cols(x)
                  conjugate complex number of x
conj(x)
                 cosine of x
cos(x)
                  determinant of matrix x
det(x)
                 exponential function of x
exp(x)
                  factorial of x
fac(x)
                  smallest integer xthat is \leq x
floor(x)
                  imaginary part of complex x
imag(x)
is_invertible(x) true, if mat x is invertible, otherwise false
is symmetric(x) true, if mat x is symmetrix, otherwise false
is zero(x)
                  true, if (value, vec, mat, ...) x is approx zero
                  number of elements of set or vector
len(x)
                  natural logarithm
ln(x)
                  maximum element of vector, matrix, set, ...
max(x)
min(x)
                minimum element of vector, matrix, setm, ...
                euclidean norm of vector x
norm(x)
opt(x)
                optimize term x (e.g. 2x+3x \rightarrow 5x)
               real part of complex x round to nearest integer
real(x)
round(x)
                 number of rows of a matrix
rows(x)
               shuffles the elements of a vector
shuffle(x)
                 sine
sin(x)
sqrt(x)
                 square root
tan(x)
                  tan
                  term of variable x (refer to exercise example)
term(x)
                transpose matrix x
transpose(x)
triu(x)
                  upper triangular part of matrix x
```

List of binary functions:

```
binomial(n,k)
complex(x,y)
col(a,k)
cross(x,y)
diff(f,x)
dot(x,y)
dot(x,y)
dot(x,y)
draws a random number in range [x,y]
binomial coefficient
returns a complex number x+y*i
gets column k (first is 0) from matrix a
cross(x,y)
cross product of vetors x and y
automatic differentiation of function f w.r.t
variable x
dot(x,y)
draws a random number in range [x,y]
```

SYNTHESIS OF TERM TOKENS:

```
example:
  input term t:
    2*\sin(2*x)+3 as tree: +(*(2,\sin(*(2,x))),3)
  number of output tokens N:
  output:
    \{+,*,2,\sin(2*x),3,\cos(2*x)\} (underlined := incorrect)
depth=0: \{+,2*\sin(2*x),3\} n=3 < N
depth=1: \{+,*,2,\sin(2*x),3\} n=5 < N
depth=2: \{+, *, 2, \sin(,), x, 3\} n=7 > N
→ choose smallest depth with n<N and fill remaining tokens with
  shuffling:
     change constants:
         new := old + randZ(-1,1) * rand(1,floor(value/2))
         keep positive;
     change sin ↔ cos ↔ exp
\rightarrow if N is not given, then choose depth=1, and all tokens are
needed for the solution TODO: handling of tokens that are used
twice or more in the solution
```

```
Algorithm:
Input:
t := the input term
N := the number of output tokens
Algorithm:
T := { t }
for each Ti in T:
Ti := set of operator(s) and operand(s) for Ti
Ti := shuffle(Ti)
T := T uu Ti
```

```
n := |T|
if n < N then depth++ and goto 2.
Output:
Т
Algorithm for shuffle(U):
Input:
    V := term
Algorithm:
Output:
 U
```