O(n²) Sorting

Time Complexity of Sorting

- · a really bad, yet "correct" sorting algorithm:
 - · shuffle the array randomly
 - · check to see if it is in order
 - · if yes, done
 - · if not, repeat
- the probability of never generating the correct order is zero
- the time complexity is O(n!)

O(n2) Sorting

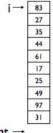
- O(n²) sorting algorithms take O(n) steps to place each of n elements into its correct position
- insertion sort
- bubble sort
- others

```
public class Array {
    private Comparable[] val;
    private int count;

    public Array (int max) {
        this.val = new Comparable[max];
        this.count = 0;
    }

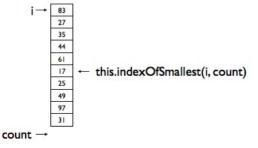
    public void swap (int i, int j) {
        Comparable temp = this.val[i];
        this.val[j] = this.val[j];
        this.val[j] = temp;
    }
...
...
}
```

Insertion Sort

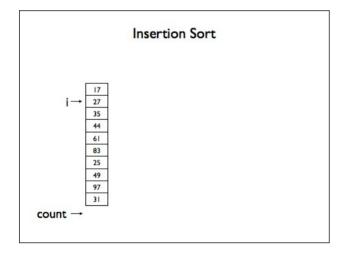


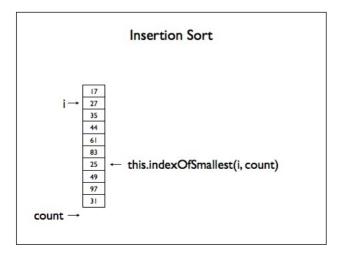
count →

Insertion Sort

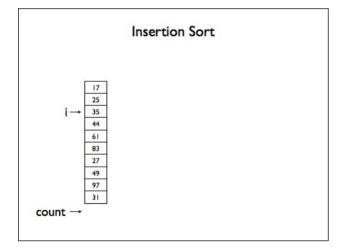


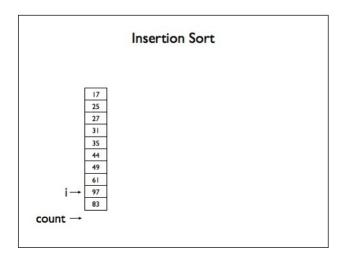
Insertion Sort $i \rightarrow \frac{17}{27}$ 35 44 61 83 25 49 97 31count \rightarrow

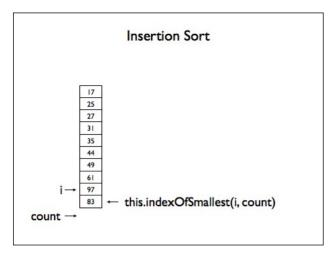


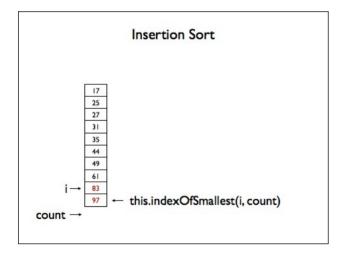


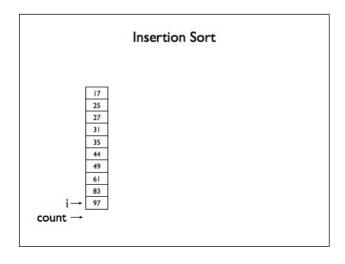
Insertion Sort $i \rightarrow \frac{17}{25}$ 35 44 61 83 27 49 97 31count \rightarrow





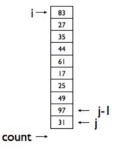






```
public class Array {
...
public void insertionSort () {
    for (int i = 0; i < this.count - 1; i++)
        this.swap(i,this.indexOfSmallest(i, this.count));
}

private int indexOfSmallest (int top, int out) {
    int small = top;
    for (int i = top + 1; i < out; i++)
        if (this.val[small].compareTo(this.val[i]) > 0)
        small = i;
    return small;
}
...
}
```



```
i → 83

27

35

44

61

17

25

49

31

97 ← j-1
```

Bubble Sort

Bubble Sort

Bubble Sort

Bubble Sort

25 j → 83

Bubble Sort

17

$$i \rightarrow \begin{array}{c} 17 \\ 25 \\ 27 \\ 31 \\ 83 \\ \hline 44 \\ 49 \\ 61 \\ 97 \end{array}$$

$$\downarrow j-1$$

$$\begin{array}{c|c}
 & 17 \\
 & 25 \\
 & 27 \\
 & 31 \\
 & 83 \\
 & 35 \\
 & 44 \\
 & 49 \\
 & 61 \\
 & 97 \\
 & \leftarrow j - 1
\end{array}$$
count

$$i \rightarrow \begin{array}{c} 17 \\ 25 \\ 27 \\ 31 \\ 83 \\ 44 \\ 49 \\ 61 \\ 97 \end{array} \leftarrow j-1$$

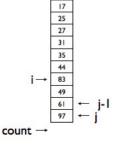
$$count \rightarrow$$

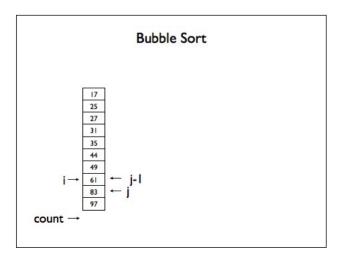
Bubble Sort

$$\begin{array}{c}
 & 17 \\
 & 25 \\
 & 27 \\
 & 31 \\
 & 35 \\
 & 83 \\
 & 44 \\
 & 49 \\
 & 61 \\
 & 97 \\

\end{array}$$

$$\leftarrow j-1$$
count \rightarrow





```
17
25
27
31
35
44
49
61
49
61
61
61
61
61
61
61
61
```