

Ionic mechanism of electrical alternans

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Received 12 July 2001; accepted in final form 26 September 2001

Fox, Jeffrey J., Jennifer L. McHarg, and Robert F. Gilmour, Jr. Ionic mechanism of electrical alternans. *Am J Physiol Heart Circ Physiol* 282: H516–H530, 2002. First published October 4, 2001; 10.1152/ajpheart.00612.2001.—Although alternans of action potential duration (APD) is a robust feature of the rapidly paced canine ventricle, currently available ionic models of cardiac myocytes do not recreate this phenomenon. To address this problem, we developed a new ionic model using formulations of currents based on previous models and recent experimental data. Compared with existing models, the inward rectifier K⁺ current (I_{K1}) was decreased at depolarized potentials, the maximum conductance and rectification of the rapid component of the delayed rectifier K⁺ current (I_{Kr}) were increased, and I_{Kr} activation kinetics were slowed. The slow component of the delayed rectifier K⁺ current (I_{Ks}) was increased in magnitude and activation shifted to less positive voltages, and the L-type Ca²⁺ current (I_{Ca}) was modified to produce a smaller, more rapidly inactivating current. Finally, a simplified form of intracellular calcium dynamics was adopted. In this model, APD alternans occurred at cycle lengths = 150–210 ms, with a maximum alternans amplitude of 39 ms. APD alternans was suppressed by decreasing I_{Ca} magnitude or calcium-induced inactivation and by increasing the magnitude of I_{K1} , I_{Kr} , or I_{Ks} . These results establish an ionic basis for APD alternans, which should facilitate the development of pharmacological approaches to eliminating alternans.

action potential duration restitution; calcium current; potassium currents

THE DURATION of the cardiac action potential is determined in large part by the preceding diastolic interval. This relationship between action potential duration and diastolic interval, known as the action potential duration restitution relation, is an important determinant of cardiac dynamics (17). In particular, if the slope of the restitution relation is ≥ 1 , an alternation of action potential duration, or electrical alternans, commonly develops during high-frequency pacing (2, 8).

It has been suggested that rate-dependent electrical alternans may be a precursor to the development of ventricular arrhythmias, particularly ventricular fibrillation (VF) (6, 10, 19, 22). In support of this idea, several recent experiments (5, 11, 23) have shown that when the slope of the restitution relation is ≥ 1 , rapid pacing induces both alternans and fibrillation in isolated ventricles. If the slope of the restitution relation

is reduced to <1 , neither electrical alternans nor fibrillation occurs (5, 11, 12, 23). Unfortunately, the interventions used to date to suppress alternans and fibrillation [high-dose calcium channel blockers (23), hyperkalemia (12), and bretylium (5)] have limited clinical utility. More effective means of suppressing alternans need to be identified, a process that would be facilitated by a more complete understanding of the ionic basis for alternans.

One approach to determining the ionic basis for alternans is to use a computer model, several of which have been developed. For example, Luo and Rudy (15, 16), using data obtained primarily from guinea pig myocytes, developed a comprehensive ionic model (LR1) that subsequently was updated (LRd) to include formulations for the rapid and slow components of the delayed rectifier K⁺ current (I_{Kr} and I_{Ks} , respectively). Recently, Winslow et al. (26) modified the LRd model using data for ionic currents obtained from canine ventricular myocytes (CVM) and a formulation for calcium dynamics developed originally in guinea pig myocardial cells (9). An alternative formulation for calcium dynamics has been proposed by Chudin et al. (1) in their modification of the LR1 model.

Each of the models described above has limitations with respect to the study of the ionic basis for electrical alternans. The Winslow and LRd models do not produce sustained alternans at rapid pacing rates, whereas the Chudin model, which does generate electrical alternans, lacks formulations for repolarizing K⁺ currents likely to contribute importantly to alternans [I_{Kr} , I_{Ks} , and the transient outward K⁺ current (I_{to})].

Given that a complete ionic model that generates electrical alternans is not currently available, we set out to develop such a model, guided by the results obtained from our experimental studies in the canine ventricle (11, 23). Our initial objectives were to develop an ionic model of the CVM that exhibits stable electrical alternans and to use the model to identify the ionic currents responsible for alternans. Once the relevant ionic currents were identified, we then manipulated these currents to eliminate alternans. Our expectation is that the same ionic manipulations that suppress alternans in the ionic model will suppress fibrillation

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in vivo, in which case the results of the present study may suggest novel approaches to the prevention of VF.

Glossary

α_h	Voltage-dependent h gate parameter	\bar{I}_{Ca}	Maximal I_{Ca}
α_j	Voltage-dependent j gate parameter	I_{Cab}	Ca^{2+} background current
α_m	Voltage-dependent m gate parameter	$I_{Ca\text{half}}$	\bar{I}_{Ca} level that reduces P_{CaK} by one-half
αX_{to}	Voltage-dependent X_{to} gate parameter	I_{CaK}	K^+ current through the L-type Ca^{2+} channel
β_h	Voltage-dependent h gate parameter	I_{K1}	Inward rectifier K^+ current
β_i	Myoplasmic buffering factor	I_{Kp}	Plateau K^+ current
β_j	Voltage-dependent j gate parameter	I_{Kr}	Rapid component of the delayed rectifier K^+ current
β_m	Voltage-dependent m gate parameter	I_{Ks}	Slow component of the delayed rectifier K^+ current
β_{SR}	Sarcoplasmic reticulum buffering factor	I_{Na}	Na^+ current
βX_{to}	Voltage-dependent X_{to} gate parameter	I_{Nab}	Na^+ background current
γ	Sarcoplasmic reticulum Ca^{2+} -dependent J_{rel} factor	I_{NaCa}	Na^+/Ca^{2+} exchange current
η	Controls voltage dependence of I_{NaCa}	I_{NaK}	Na^+K^+ pump current
σ	Extracellular Na^+ I_{NaK} factor	\bar{I}_{NaK}	Maximal I_{NaK}
τ_d	I_{Ca} activation time constant	I_{pCa}	Sarcolemmal Ca^{2+} pump current
τ_f	I_{Ca} inactivation time constant	I_{pCa}	Maximal I_{pCa}
$\tau_{f_{Ca}}$	Ca^{2+} -dependent I_{Ca} inactivation time constant	I_{stim}	Stimulus current
τ_{Kr}	I_{Kr} activation time constant	I_{to}	Transient outward K^+ current
τ_{Ks}	I_{Ks} activation time constant	j	Slow I_{Na} inactivation gate
A_{cap}	Capacitive membrane area	J_{leak}	Leakage Ca^{2+} flux from the sarcoplasmic reticulum
APD	Action potential duration	J_{rel}	Release Ca^{2+} flux from the sarcoplasmic reticulum
BCL	Basic cycle length	J_{up}	Uptake Ca^{2+} flux to the sarcoplasmic reticulum
C_{sc}	Specific membrane capacity	JSR	Junctional sarcoplasmic reticulum
ΔCa_{max}	Maximum change in Ca^{2+}	k_{NaCa}	Scaling factor for I_{NaCa}
ΔCa_{min}	Minimum change in Ca^{2+}	k_{sat}	I_{NaCa} saturation factor for I_{NaCa}
$[Ca^{2+}]_i$	Intracellular Ca^{2+} concentration	K_1^∞	Steady-state I_{K1} activation
$[Ca^{2+}]_o$	Extracellular Ca^{2+} concentration	K_{Kp}	I_{Kp} activation
$[Ca^{2+}]_{SR}$	Sarcoplasmic reticulum Ca^{2+} concentration	K_m^{CMDN}	Ca^{2+} half-saturation constant for calmodulin
[CMDN] _{tot}	Total calmodulin concentration	K_m^{CSQN}	Ca^{2+} half-saturation constant for calsequestrin
[CSQN] _{tot}	Total calsequestrin concentration	K_{mCa}	Ca^{2+} half-saturation constant for I_{NaCa}
CVM	Canine ventricular myocyte	$K_{mf_{Ca}}$	Ca^{2+} half-saturation constant for f_{Ca}
d	I_{Ca} activation gate	K_{mK1}	K^+ half-saturation constant for I_{K1}
d^∞	Steady-state I_{Ca} activation	K_{mKo}	K^+ half-saturation constant for I_{NaK}
DI	Diastolic interval	K_{mNa}	Na^+ half-saturation constant for I_{NaCa}
E_{Ca}	Ca^{2+} equilibrium potential	K_{mNai}	Na^+ half-saturation constant for I_{NaK}
E_K	K^+ equilibrium potential	K_{mpCa}	Half-saturation constant for I_{pCa}
E_{Ks}	I_{Ks} equilibrium potential	K_{mup}	Ca^{2+} half-saturation constant for J_{up}
E_{Na}	Na^+ equilibrium potential	$[K^+]_i$	Intracellular K^+ concentration
f	I_{Ca} inactivation gate	$[K^+]_o$	Extracellular K^+ concentration
f^∞	Steady-state I_{Ca} inactivation	LR1	Luo and Rudy model
f_{Ca}^∞	Steady-state Ca^{2+} -dependent I_{Ca} inactivation	LRd	Updated Luo and Rudy model
f_{Ca}	Ca^{2+} -dependent I_{Ca} inactivation gate	m	I_{Na} activation gate
f_{NaK}	Voltage-dependent I_{NaK} factor	$[Na^+]_i$	Intracellular Na^+ concentration
F	Faraday constant	$[Na^+]_o$	Extracellular Na^+ concentration
\bar{G}_{Cab}	Peak I_{Cab} conductance	NSR	Nonjunctional sarcoplasmic reticulum
\bar{G}_{K1}	Peak I_{K1} conductance	\bar{P}_{Ca}	L-type Ca^{2+} channel permeability to Ca^{2+}
\bar{G}_{Kp}	Peak I_{Kp} conductance	\bar{P}_{CaK}	L-type Ca^{2+} channel permeability to K^+
\bar{G}_{Kr}	Peak I_{Kr} conductance	\bar{P}_{leak}	Ca^{2+} leakage permeability between the sarcoplasmic reticulum and the myoplasm
\bar{G}_{Ks}	Peak I_{Ks} conductance	\bar{P}_{rel}	Ca^{2+} maximal release permeability from the sarcoplasmic reticulum
\bar{G}_{Na}	Peak I_{Na} conductance	R	Ideal gas constant
\bar{G}_{to}	Peak I_{to} conductance		
h	Fast I_{Na} inactivation gate		
I_{Ca}	L-type Ca^{2+} channel current		

SR	Sarcoplasmic reticulum
t	Time
T	Temperature
V	Voltage
ΔV_{\max}	Maximum change in voltage
ΔV_{\min}	Minimum change in voltage
V_{myo}	Myoplasmic volume
V_{SR}	Sarcoplasmic reticulum volume
V_{up}	Maximal Ca^{2+} uptake to the sarcoplasmic reticulum
VF	Ventricular fibrillation
X_{Kr}	I_{Kr} activation gate
X_{Kr}^{∞}	Steady-state I_{Kr} activation
X_{Ks}	I_{Ks} activation gate
X_{Ks}^{∞}	Steady-state I_{Ks} activation
X_{to}	I_{to} activation gate
Y_{to}	I_{to} inactivation gate

MATERIALS AND METHODS

To study the ionic mechanism of electrical alternans in canine myocytes, we constructed a CVM model using appropriate formulations of ionic currents from the LRD, Winslow, and Chudin models, altered as necessary to fit experimental voltage-clamp data from CVM. It has been well established that cellular electrical properties in the canine ventricle vary, both between right and left ventricles and within a given ventricle, according to whether a cell resides in the epicardium, endocardium, or midmyocardium (13, 14). Because the Winslow model is the only existing ionic model based on the electrical properties of the canine ventricle, we elected to use that model as the basis for the CVM model. Consequently, the CVM model, like its predecessor, recreates the midmyocardial or M cell action potential. Further alterations of various currents, including I_{Ks} , I_{to} and I_{NaCa} , would be required to model the electrical activity of canine endocardial and epicardial myocytes (13, 29).

The CVM model contains the following ionic current formulations

$$\frac{dV}{dt} = -(I_{\text{stim}} + I_{\text{Na}} + I_{\text{Kl}} + I_{\text{Kr}} + I_{\text{Ks}} + I_{\text{to}} + I_{\text{Kp}} + I_{\text{NaK}} + I_{\text{NaCa}} + I_{\text{Nab}} + I_{\text{Cab}} + I_{\text{pCa}} + I_{\text{Ca}} + I_{\text{CaK}})$$

Stimulus current. I_{stim} used to drive the model was a square wave pulse consisting of $-80 \mu\text{A}/\mu\text{F}$ of current for 1 ms.

Sodium current. I_{Na} was the same as that used in the Winslow model (26) except that the discontinuities in the h and j gate formulations were removed.

$$\begin{aligned} I_{\text{Na}} &= \bar{G}_{\text{Na}} m^3 h j (V - E_{\text{Na}}) & \alpha_m &= 0.32 \frac{V + 47.13}{1 - e^{-0.1(V + 47.13)}} \\ \frac{dm}{dt} &= \alpha_m (1 - m) - \beta_m m & \beta_m &= 0.08 e^{-V/11} \\ \frac{dh}{dt} &= \alpha_h (1 - h) - \beta_h h & \alpha_h &= 0.135 e^{(V+80)/-6.8} \\ \frac{dj}{dt} &= \alpha_j (1 - j) - \beta_j j & \beta_h &= \frac{7.5}{1 + e^{-0.1(V+11)}} \\ E_{\text{Na}} &= \frac{RT}{F} \ln \left(\frac{[\text{Na}^+]_o}{[\text{Na}^+]_i} \right) & \alpha_j &= \frac{0.175 e^{(V+100)/-2.3}}{1 + e^{0.15(V+79)}} \\ & & \beta_j &= \frac{0.3}{1 + e^{-0.1(V+32)}} \end{aligned}$$

Inward rectifier K^+ current. I_{Kl} was formulated to agree with data from Freeman et al. (4). These data indicate a smaller outward current at depolarized potentials than is seen in the Winslow model

$$I_{\text{Kl}} = \bar{G}_{\text{Kl}} K_1^{\infty} \frac{[\text{K}^+]_o}{[\text{K}^+]_o + K_{m\text{Kl}}} (V - E_{\text{K}})$$

$$K_1^{\infty} = \frac{1}{2 + e^{1.62F/(RT)(V - E_{\text{K}})}}$$

$$E_{\text{K}} = \frac{RT}{F} \ln \left(\frac{[\text{K}^+]_o}{[\text{K}^+]_i} \right)$$

Rapid component of the delayed rectifier K^+ current. I_{Kr} was fit to the data from Gintant (7). In particular, we reproduced the voltage-clamp experiment used to generate Fig. 2 in his paper. The Winslow formulation of the current was altered to increase rectification, slow kinetics at depolarized potentials, and increase maximum conductance

$$I_{\text{Kr}} = \bar{G}_{\text{Kr}} R(V) X_{\text{Kr}} \sqrt{\frac{[\text{K}^+]_o}{4}} (V - E_{\text{K}})$$

$$\frac{dX_{\text{Kr}}}{dt} = \frac{X_{\text{Kr}}^{\infty} - X_{\text{Kr}}}{\tau_{\text{Kr}}}$$

$$R(V) = \frac{1}{1 + 2.5 e^{0.1(V+28)}}$$

$$\tau_{\text{Kr}} = 43 + \frac{1}{e^{-5.495 + 0.1691V} + e^{-7.677 - 0.0128V}}$$

$$X_{\text{Kr}}^{\infty} = \frac{1}{1 + e^{-2.182 - 0.1819V}}$$

Slow component of the delayed rectifier K^+ current. I_{Ks} was fit to data from Varro et al. (25), specifically the results shown in Fig. 2 of their paper. The Winslow model was altered to increase the magnitude of the current and shift activation to less positive voltages

$$I_{\text{Ks}} = \bar{G}_{\text{Ks}} X_{\text{Ks}}^2 (V - E_{\text{Ks}})$$

$$E_{\text{Ks}} = \frac{RT}{F} \ln \left(\frac{[\text{K}^+]_o + 0.01833[\text{Na}^+]_o}{[\text{K}^+]_i + 0.01833[\text{Na}^+]_i} \right)$$

$$\frac{dX_{\text{Ks}}}{dt} = \frac{X_{\text{Ks}}^{\infty} - X_{\text{Ks}}}{\tau_{\text{Ks}}}$$

$$X_{\text{Ks}}^{\infty} = \frac{1}{1 + e^{(V-16)/-13.6}}$$

$$\tau_{\text{Ks}} = \frac{1}{\frac{0.0000719(V-10)}{1 - e^{-0.148(V-10)}} + \frac{0.000131(V-10)}{e^{0.0687(V-10)} - 1}}$$

Transient outward K^+ current. I_{to} in the model was the same as that in the Winslow model

$$I_{\text{to}} = \bar{G}_{\text{to}} X_{\text{to}} Y_{\text{to}} (V - E_{\text{K}})$$

$$\alpha_{X_{\text{to}}} = 0.04516 e^{0.03577V}$$

$$\beta_{X_{\text{to}}} = 0.0989 e^{-0.06237V}$$

$$\alpha_{Y_{\text{to}}} = \frac{0.005415 e^{(V+33.5)/-5}}{1 + 0.051335 e^{(V+33.5)/-5}}$$

$$\beta_{Y_{\text{to}}} = \frac{0.005415 e^{(V+33.5)/5}}{1 + 0.051335 e^{(V+33.5)/5}}$$

$$\begin{aligned} \frac{dX_{\text{to}}}{dt} &= \alpha_{X_{\text{to}}} (1 - X_{\text{to}}) - \beta_{X_{\text{to}}} X_{\text{to}} \\ \frac{dY_{\text{to}}}{dt} &= \alpha_{Y_{\text{to}}} (1 - Y_{\text{to}}) - \beta_{Y_{\text{to}}} Y_{\text{to}} \end{aligned}$$

Plateau K^+ current. I_{Kp} was the same as that in the Winslow model

$$I_{Kp} = \bar{G}_{Kp} K_{Kp} (V - E_K)$$

$$K_{Kp} = \frac{1}{1 + e^{(7.488 - V)/5.98}}$$

Na^+ - K^+ pump current. I_{NaK} was the same as that in the LRd model

$$I_{NaK} = \bar{I}_{NaK} f_{NaK} \frac{1}{1 + \left(\frac{K_{mNa}}{[Na^+]_i} \right)^{1.5}} \frac{[K^+]_o}{[K^+]_o + K_{mKo}}$$

$$f_{NaK} = \frac{1}{1 + 0.1245e^{-0.1VF/(RT)} + 0.0365\sigma e^{-VF/(RT)}}$$

$$\sigma = 1/7 (e^{[Na^+]_o/67.3} - 1)$$

Na^+ / Ca^{2+} exchange current, sarcolemmal pump current, and Ca^{2+} and Na^+ background currents. I_{NaCa} , I_{pCa} , I_{Ca} , and I_{Na} were the same as those in the Winslow model

$$I_{NaCa} = \bar{G}_{NaCa} (V - E_{NaCa})$$

$$I_{pCa} = \bar{I}_{pCa} \frac{[Ca^{2+}]_i}{K_{mCa} + [Ca^{2+}]_i}$$

$$I_{Ca} = \bar{G}_{Ca} (V - E_{Ca})$$

$$E_{Ca} = \frac{RT}{2F} \ln \left(\frac{[Ca^{2+}]_o}{[Ca^{2+}]_i} \right)$$

L -type Ca^{2+} channel current. I_{Ca} in the model was a modified version of that found in the LRd model. A time-dependent, enhanced Ca^{2+} -induced inactivation was used, as well as a decrease in the current magnitude. These changes produced a smaller, more rapidly inactivating Ca^{2+} current, in agreement with experimental observations by A. C. Zygmunt (personal communication)

$$I_{Ca} = \bar{I}_{Ca} f_{Ca}$$

$$f_{Ca} = \frac{1}{1 + e^{(V+12.5)/5}}$$

$$\bar{I}_{Ca} = \frac{\bar{P}_{Ca}}{C_{sc}} \frac{4VF^2}{RT} \frac{[Ca^{2+}]_i e^{2VF/(RT)}}{e^{2VF/(RT)} - 1}$$

$$\tau_f = 30 + \frac{200}{1 + e^{(V+20)/9.5}}$$

$$\frac{df}{dt} = \frac{f^\infty - f}{\tau_f}$$

$$d^\infty = \frac{1}{1 + e^{(V+10)/-6.24}}$$

$$\frac{dd}{dt} = \frac{d^\infty - d}{\tau_d}$$

$$\tau_d = \frac{1}{0.25e^{-0.01V} + \frac{0.07e^{-0.05(V+40)}}{1 + e^{0.05(V+40)}}}$$

$$\frac{df_{Ca}}{dt} = \frac{f_{Ca}^\infty - f_{Ca}}{\tau_{f_{Ca}}}$$

$$f_{Ca}^\infty = \frac{1}{1 + \left(\frac{[Ca^{2+}]_i}{K_{mf_{Ca}}} \right)^3}$$

$$\tau_{f_{Ca}} = 30$$

K^+ current through the L -type Ca^{2+} channel. I_{CaK} was also a modified version of the LRd formulation

$$I_{CaK} = \frac{\bar{P}_{CaK}}{C_{sc}} \frac{f_{df_{Ca}}}{1 + \frac{\bar{I}_{Ca}}{I_{CaHalf}}} \frac{1,000VF^2}{RT} \frac{[K^+]_i e^{VF/(RT)} - [K^+]_o}{e^{VF/(RT)} - 1}$$

Calcium handling. A modified form of the intracellular calcium dynamics from Chudin et al. (1) was used. We included buffering from calmodulin in the cytoplasm and calsequestrin in the SR, omitted spontaneous release of calcium from the SR, and combined the concentrations of calcium in the JSR and NSR into a single variable

$$\frac{d[Ca^{2+}]_i}{dt} = \beta_i \left(J_{rel} + J_{leak} - J_{up} - \frac{A_{Cap} C_{sc}}{2FV_{myo}} \right)$$

$$\beta_i = \left(1 + \frac{[CMDN]_{tot} K_m^{CMDN}}{(K_m^{CMDN} + [Ca^{2+}]_i)^2} \right)^{-1}$$

$$J_{rel} = \bar{P}_{rel} f_{df_{Ca}} \frac{\gamma [Ca^{2+}]_{SR} - [Ca^{2+}]_i}{1 + 1.65e^{V/20}}$$

$$\gamma = \frac{1}{1 + \left(\frac{2,000}{[Ca^{2+}]_{SR}} \right)^3}$$

$$J_{up} = \frac{V_{up}}{1 + \left(\frac{K_{mup}}{[Ca^{2+}]_i} \right)^2}$$

$$J_{leak} = \bar{P}_{leak} ([Ca^{2+}]_{SR} - [Ca^{2+}]_i)$$

$$\frac{d[Ca^{2+}]_{SR}}{dt} = \beta_{SR} (J_{up} - J_{leak} - J_{rel}) \frac{V_{myo}}{V_{SR}}$$

$$\beta_{SR} = \left(1 + \frac{[CSQN]_{tot} K_m^{CSQN}}{(K_m^{CSQN} + [Ca^{2+}]_{SR})^2} \right)^{-1}$$

Numerical methods. The equations listed above were solved using parameter values and initial conditions found in Table 1. The simulations were run on Macintosh G3 and G4 computers using a program written in C. The numerical integration scheme was similar to that used in Luo and Rudy (15, 16) and in Rush and Larsen (24). Briefly, the time steps of integration were made small enough so that the changes in voltage and in calcium concentrations remained below maximum values, ΔV_{max} and ΔCa_{max} . If the changes in voltage and calcium concentration were below a minimum value (ΔV_{min} and ΔCa_{min}), the time step was increased. By keeping the changes in voltage small, we could solve the linear gate variable equations exactly during each time step. We used the following values: $\Delta V_{max} = 0.8$ mV, $\Delta V_{min} = 0.2$ mV, $\Delta Ca_{max} = 1.067 \times 10^{-2}$ μ M, and $\Delta Ca_{min} = 2.67 \times 10^{-3}$ μ M. (See Refs. 15, 16, and 24 for more details.) The other time-dependent variables in the model were solved using the adaptive fourth-order Runge-Kutta method (21). The errors were normalized as described in Jafri et al. (9). We used a maximum error of 1×10^{-6} , a minimum time step of 0.005 ms, and a maximum time step of 0.5 ms. During the stimulus, the step size was fixed at 0.005 ms.

To further increase computational speed, lookup tables were used to avoid repeatedly calculating exponentials and other computationally expensive functions. The lookup tables were calculated once before each simulation for 15,000 values

Table 1. *Parameters and initial conditions*

	Values
<i>Parameters</i>	
\bar{G}_{Na} , mS/ μ F	12.8
\bar{G}_{K1} , mS/ μ F	2.8
\bar{G}_{Kr} , mS/ μ F	0.0136
\bar{G}_{Ks} , mS/ μ F	0.0245
\bar{G}_{Kp} , mS/ μ F	0.002216
\bar{G}_{to} , mS/ μ F	0.23815
\bar{G}_{NaB} , mS/ μ F	0.0031
\bar{G}_{CaB} , mS/ μ F	0.0003842
\bar{P}_{Ca} , cm/ms	0.0000226
\bar{P}_{CaK} , cm/ms	5.79×10^{-7}
\bar{P}_{rel} , ms $^{-1}$	6
\bar{P}_{leak} , ms $^{-1}$	0.000001
\bar{I}_{NaK} , μ A/ μ F	0.693
\bar{I}_{CaHalf} , μ A/ μ F	-0.265
\bar{I}_{pCa} , μ A/ μ F	0.05
R , J/mol K	8.314
T , Kelvins	310
F , coulomb/mol K	96.5
A_{cap} , cm 2	1.534×10^{-4}
C_{sc} , μ F/cm 2	1
η	0.35
k_{sat}	0.2
k_{NaCa} , μ A/ μ F	1,500
K_{mfCa} , μ M	0.18
K_{mK1} , mM	13
K_{mNa} , mM	87.5
K_{mCa} , μ M	1,380
K_{mNaI} , mM	10
K_{mKo} , mM	1.5
K_{mpCa} , μ M	0.05
K_{mup} , μ M	0.32
$[CMDN]_{tot}$, μ M	10
$[CSQN]_{tot}$, μ M	10,000
K_{mCMDN} , μ M	2
K_{mCSQN} , μ M	600
V_{up} , μ M/ms	0.1
V_{myo} , μ l	25.84×10^{-6}
V_{SR} , μ l	2×10^{-6}
$[Na^+]_i$, mM	10
$[K^+]_i$, mM	149.4
$[Na^+]_o$, mM	138
$[K^+]_o$, mM	4
$[Ca^{2+}]_o$, μ M	2,000
<i>Initial Conditions</i>	
t , ms	0.0
V , mV	-94.7
$[Ca^{2+}]_i$, μ mol	0.0472
$[Ca^{2+}]_{SR}$, μ mol	320
f	0.983
d	0.0001
m	2.4676×10^{-4}
h	0.99869
j	0.99887
f_{Ca}	0.942
X_{Kr}	0.229
X_{Ks}	0.0001
X_{to}	3.742×10^{-5}
Y_{to}	1

See *Glossary* for abbreviations.

of voltages ranging from -100 to +100 mV. Values of voltages lying between the indexes of the lookup table were calculated using linear interpolation. To check that these numerical techniques did not affect the accuracy of the simulation, simulations also were run using no lookup tables, with a maximum time step of 0.1 ms. The action potential

durations throughout a pacedown from a pacing cycle length of 400 ms to a cycle length of 90 ms differed by <1% between the two simulations.

Restitution relations were generated using the procedure described in Koller et al. (11), where action potential duration was expressed as a function of the preceding diastolic interval. The magnitude of action potential duration alternans was defined as the difference in action potential duration between two consecutive action potentials. Action potential duration was measured to 95% of repolarization.

RESULTS

Action potential and ionic currents. Figure 1 illustrates the action potentials, ionic currents, and Ca^{2+} transients generated by the CVM model at a pacing cycle length of 400 ms. The action potential (Fig. 1A) was characterized by the familiar spike-and-dome morphology of canine midmyocardial cells. I_{Ca} (Fig. 1B) was of smaller magnitude and inactivated more rapidly than I_{Ca} in previous models, in agreement with the recent experimental observations of A. C. Zygmunt (private communication). The time course and magnitude of $[Ca^{2+}]_i$ (Fig. 1D) was similar to experimental results reported previously (1, 26), indicating that the simplified calcium handling in the CVM model generated realistic Ca^{2+} transients.

As shown in Fig. 1F, I_{Kr} increased significantly toward the end of plateau, in good agreement with the data from Gintant (7). In contrast, I_{Ks} was too small to contribute significantly to repolarization at this cycle length (Fig. 1G, note the current scale compared with Fig. 1F), primarily because of its very slow recovery from deactivation (25).

Electrical alternans. The CVM model generated electrical alternans at physiologically relevant pacing cycle lengths. Figure 2 shows the action potential and selected plateau currents at a cycle length of 180 ms, where the CVM model produced stable alternans of large magnitude. Note that I_{Ca} , f_{Ca} , and the Ca^{2+} transient were significantly different between the long and short action potentials, whereas peak I_{Kr} and peak inward I_{NaCa} were not. I_{Ks} varied in magnitude between the long and short action potentials, but the peak current magnitude remained small.

Figure 3 shows the relationship between action potential duration and the pacing cycle length over the range of cycle lengths that produced electrical alternans (400–90 ms; Fig. 3A) and over a wider range of cycle lengths (8,000–90 ms; Fig. 3C). Action potentials generated at several different pacing cycle lengths are shown in Fig. 3D. The model generated electrical alternans over a wide range of pacing cycle lengths, in association with a region of the restitution relation having a slope equal to 1 (Fig. 3B). At cycle lengths <150 ms, alternans was absent. The initial increase in alternans magnitude as the pacing cycle length was shortened, followed by a subsequent decrease in alternans magnitude with a further shortening of the cycle length, is in good agreement with experimental data (11).

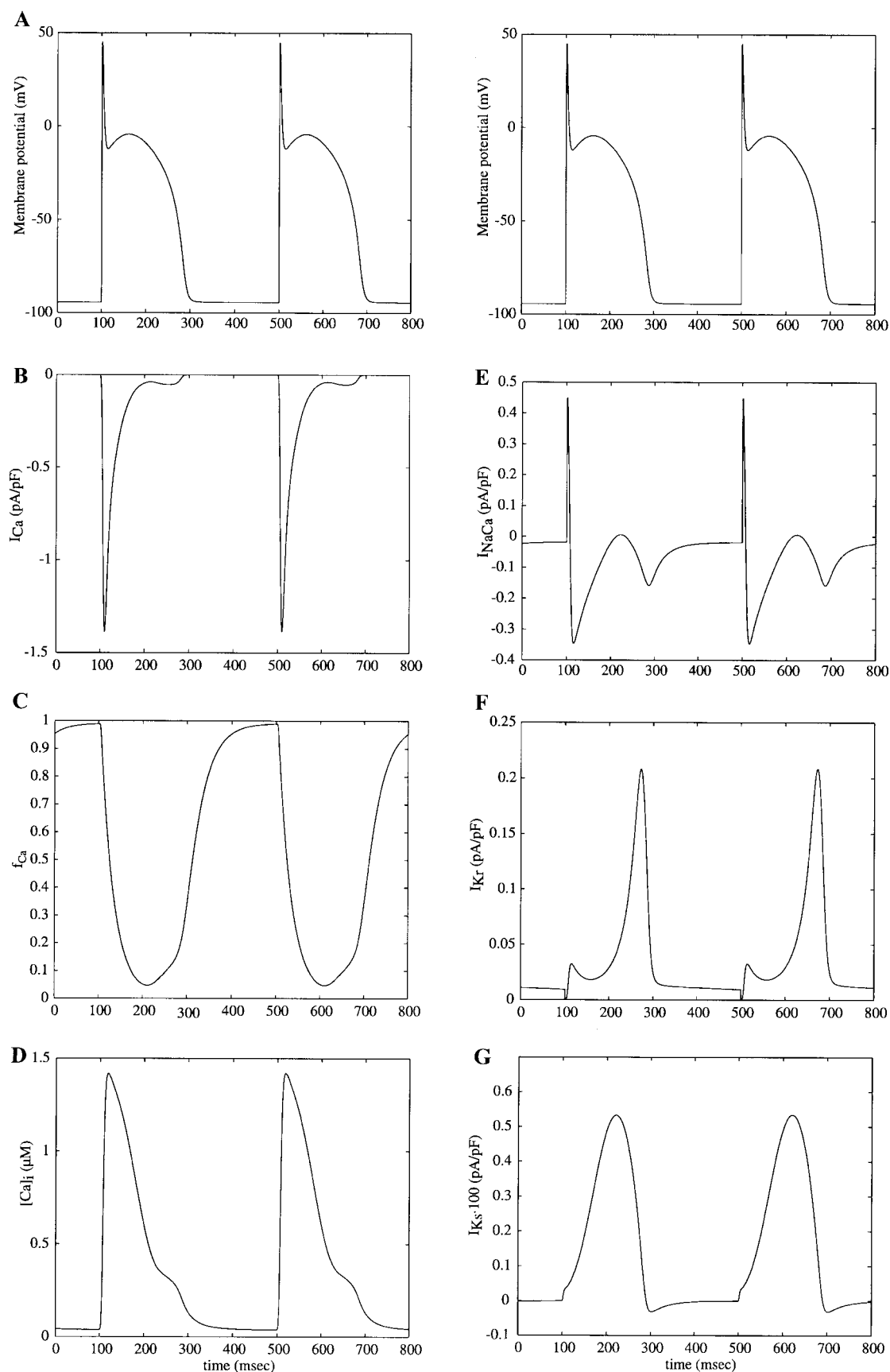


Fig. 1. Action potentials, ionic currents, and Ca^{2+} transients generated by the CVM model after 50 beats at a cycle length of 400 ms. A: action potentials; B: I_{Ca} ; C: f_{Ca} ; D: $[Ca^{2+}]_i$; E: I_{NaCa} ; F: I_{Kr} ; G: I_{Ks} . See Glossary for abbreviations.

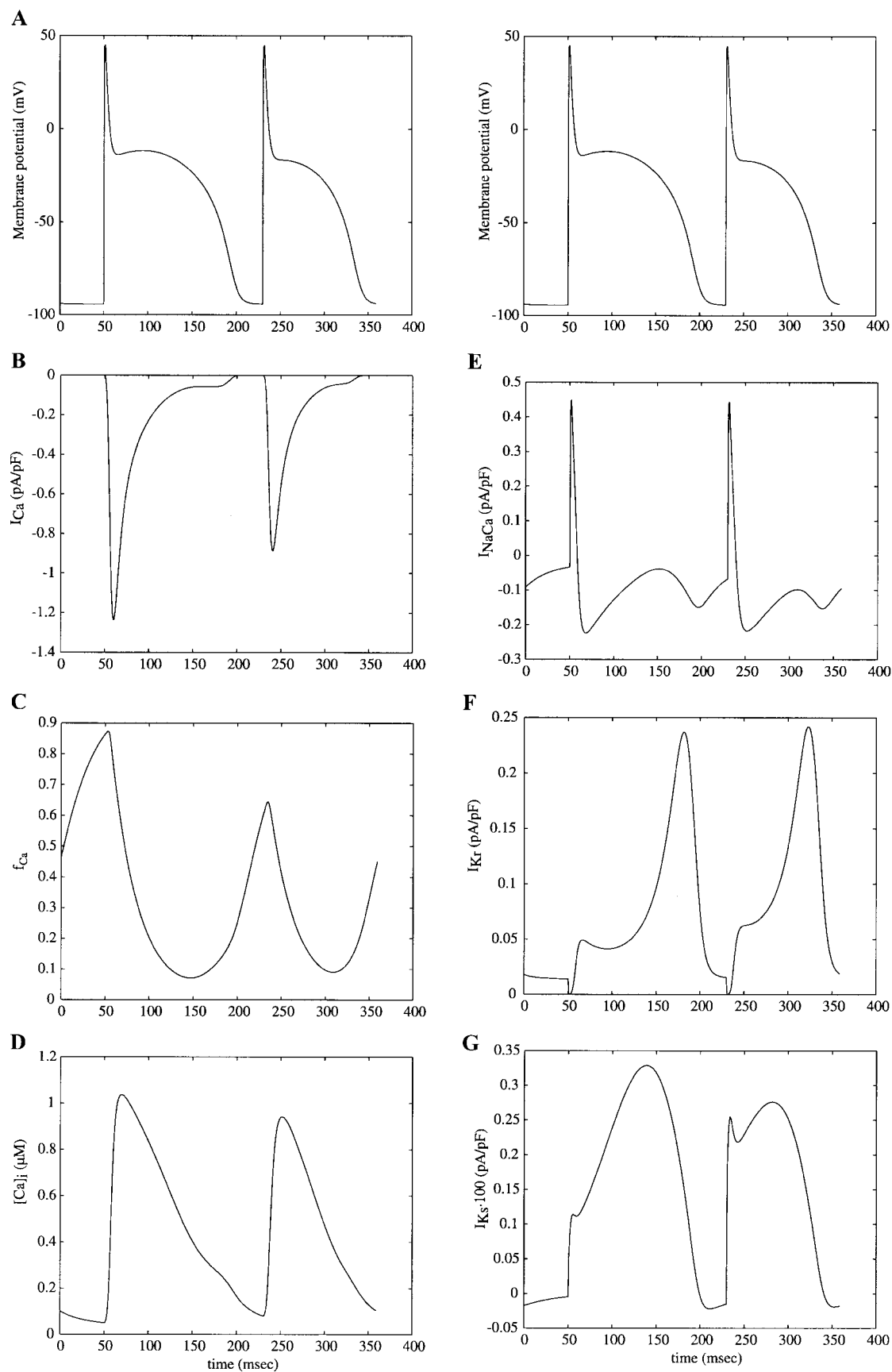


Fig. 2. Action potentials, ionic currents, and Ca^{2+} transients generated by the CVM model after 50 beats at a cycle length of 180 ms. A: action potentials; B: I_{Ca} ; C: f_{Ca} ; D: $[Ca^{2+}]_i$; E: I_{NaCa} ; F: I_{Kr} ; G: I_{Ks} .

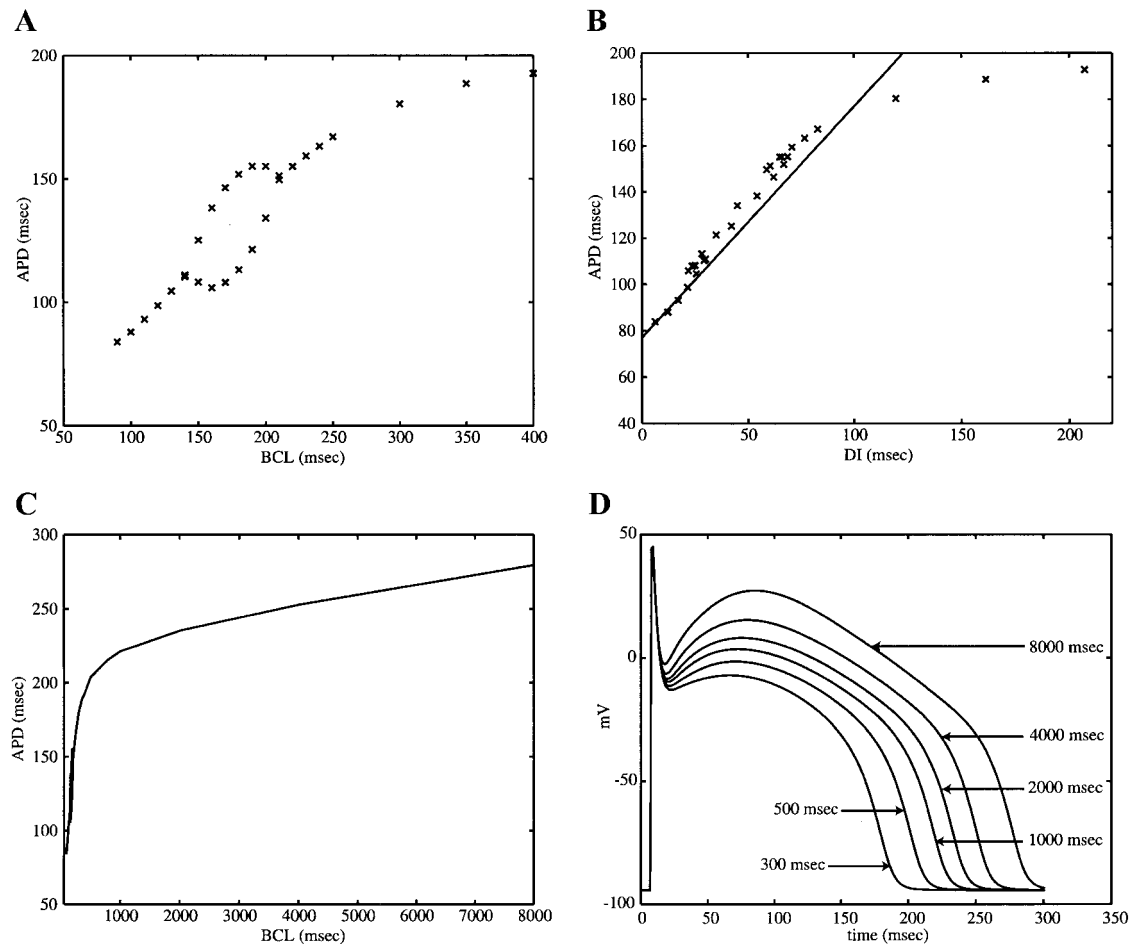


Fig. 3. Action potentials generated by the CVM model at pacing cycle lengths of 8,000–90 ms. Two-to-one block occurred at a cycle length of 80 ms. **A:** action potential duration (APD) plotted as a function of the basic cycle length (BCL) of pacing over a BCL range of 90–400 ms. **B:** APD restitution, where APD is plotted as a function of the diastolic interval (DI) for DI < 210 ms. The solid line has a slope of 1. Note that alternans occurred where the slope of the restitution relation was ≥ 1 . **C:** APD as a function of BCL over a BCL range of 90–8,000 ms. **D:** examples of action potentials at BCL = 300, 500, 1,000, 2,000, 4,000, and 8,000 ms. Over this range of BCL, resting membrane potential = -94 mV, action potential amplitude = 139 mV, overshoot = 45 mV, and maximum $dV/dt = 278$ – 280 V/s. See *Glossary* for abbreviations.

Role of plateau Na^+ and Ca^{2+} currents in alternans. The large difference in I_{Ca} between the long and short action potentials shown in Fig. 2 suggests that I_{Ca} contributes significantly to the development of alternans. Experiments using calcium channel blockers also have indicated that I_{Ca} may mediate alternans (23). To simulate the effects of a generic calcium channel blocker in the model, we decreased the magnitude of I_{Ca} by 20%. Figure 4 shows the action potential and plateau currents in the decreased I_{Ca} model at a pacing cycle length of 180 ms. No alternans of I_{Ca} or action potential duration occurred at this or any other pacing cycle length. As expected, the restitution relation lacked a region of slope equal to 1 (Fig. 5A).

The elimination of alternans in the reduced I_{Ca} model was mediated primarily by alterations of calcium-induced inactivation of I_{Ca} and the resultant changes in action potential duration (Fig. 6A). After a long diastolic interval, calcium-induced inactivation

recovered to a nearly maximal value, which resulted in a large I_{Ca} during the next action potential and a correspondingly long action potential duration. Because of the long action potential duration, the next diastolic interval was shortened. Consequently, the calcium-induced inactivation gate did not recover fully by the time the next stimulus was applied. The subsequent I_{Ca} was smaller, causing a shorter action potential duration. A long diastolic interval followed the short action potential duration, and the cycle repeated.

When I_{Ca} was diminished, the action potential duration was shortened, resulting in a prolongation of diastolic interval (Fig. 6B). The longer diastolic interval allowed for complete recovery of f_{Ca} . Consequently, I_{Ca} was constant for each action potential, although reduced in magnitude.

According to the scenario described above, not only should a reduction of I_{Ca} decrease alternans magnitude, but an increase in I_{Ca} should increase alternans

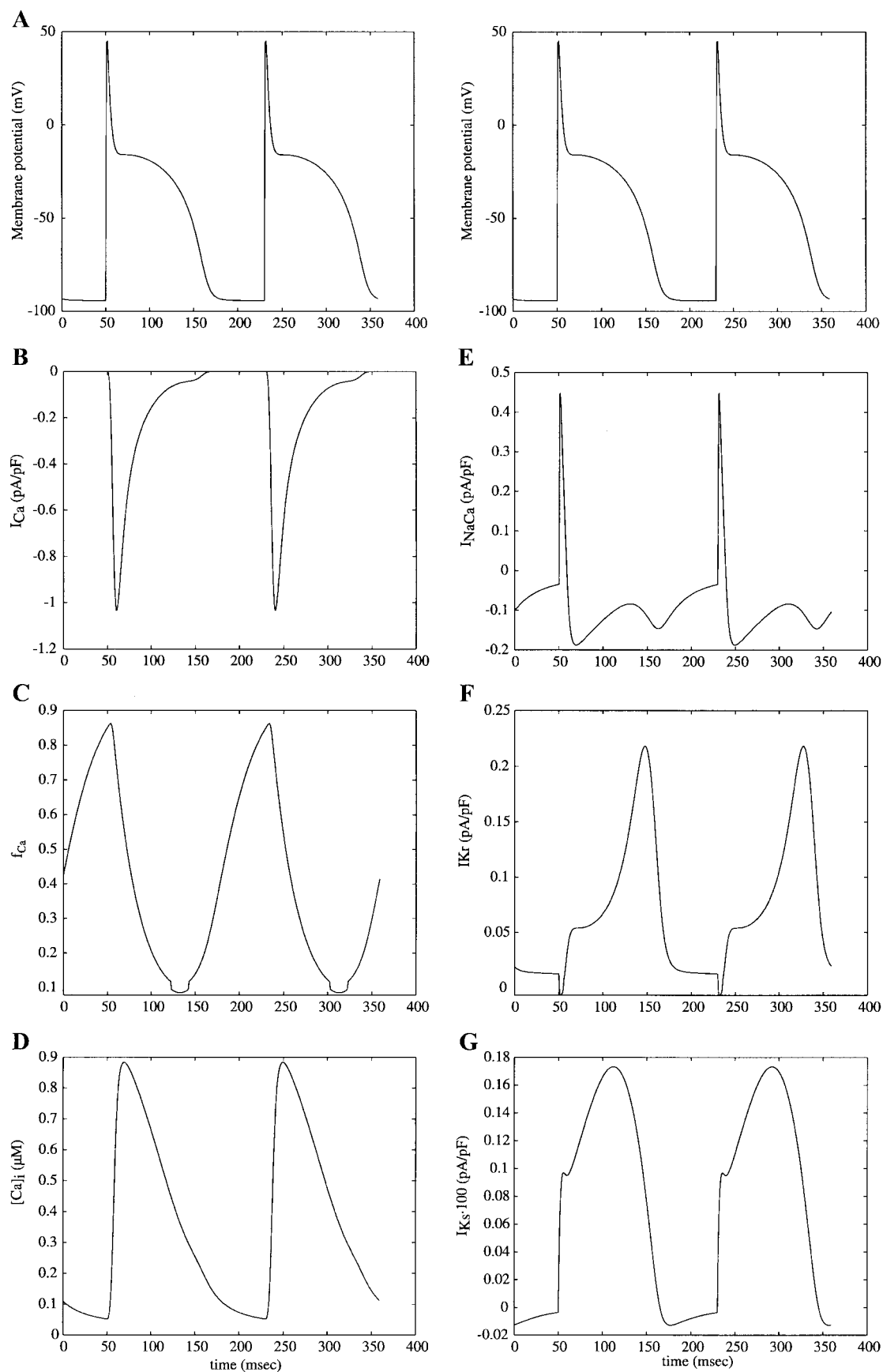


Fig. 4. Action potentials, ionic currents, and Ca^{2+} transients generated by the reduced I_{Ca} CVM model at a pacing cycle length of 180 ms. A: action potentials; B: I_{Ca} ; C: f_{Ca} ; D: $[Ca^{2+}]_i$; E: I_{NaCa} ; F: I_{Kr} ; G: I_{Ks} .

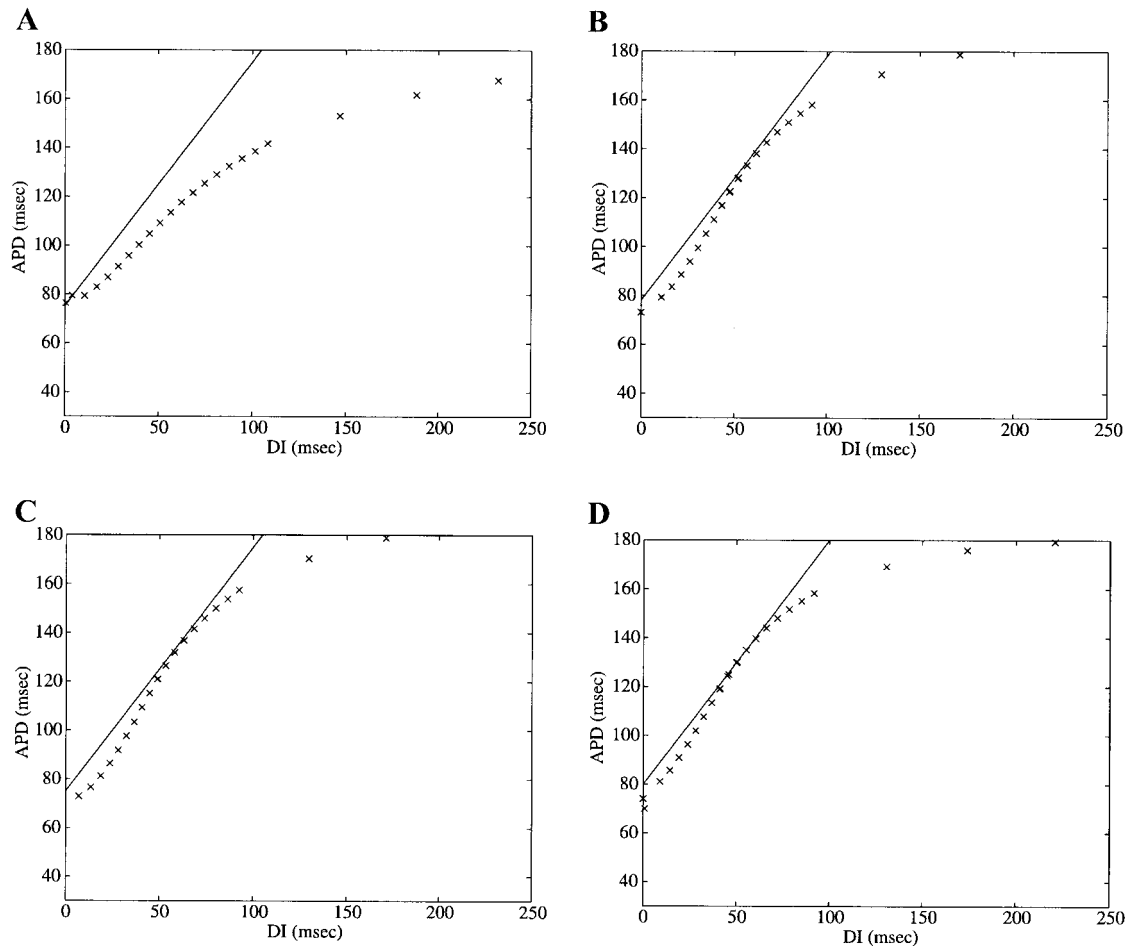


Fig. 5. Relationship between APD and DI in the CVM model after reducing \bar{P}_{Ca} by 20% (A), increasing \bar{G}_{K1} by 7% (B), increasing \bar{G}_{Kr} by 62% (C), and increasing \bar{G}_{Ks} by 14.3-fold (D). The solid line has a slope of 1. See Glossary for abbreviations.

magnitude. To test this hypothesis, the magnitude of I_{Ca} was varied, and the resultant magnitude of action potential duration alternans was measured. As shown in Fig. 7, alternans magnitude was proportional to the magnitude of I_{Ca} . In addition, alternans magnitude could be altered predictably by varying the time constant for calcium-induced inactivation ($\tau_{f_{Ca}}$), where decreasing $\tau_{f_{Ca}}$ eliminated alternans of I_{Ca} and action potential duration, secondary to a reduction in the magnitude of I_{Ca} , and increasing $\tau_{f_{Ca}}$ had the opposite effects.

The magnitude of action potential duration alternans also could be altered by changing the magnitude of I_{Na} and I_{NaCa} (Fig. 7). As I_{Na} was increased (by increasing \bar{G}_{Na}), alternans magnitude decreased. Conversely, alternans magnitude was increased after a reduction of I_{Na} . Both increases and decreases of I_{NaCa} , secondary to alterations of k_{NaCa} , reduced the magnitude of action potential duration alternans.

Role of repolarizing K^+ currents in alternans. The effects of altering I_{to} , I_{Kp} , I_{K1} , I_{Kr} , and I_{Ks} on alternans also were determined (Fig. 7). The magnitude of each of the currents was increased individually until alternans no longer occurred during pacing at any cycle length.

Elimination of alternans occurred after increasing I_{to} by $\geq 10\%$, I_{K1} by $\geq 7\%$, or I_{Kr} by $\geq 62\%$. A substantially greater increase in the magnitude of I_{Ks} or I_{Kp} was required to eliminate alternans. Decreasing the magnitude each of the K^+ currents increased the magnitude of action potential duration alternans with the exception of I_{to} , where decreasing the magnitude of the current decreased the alternans magnitude.

Increasing I_{K1} , I_{Kr} , or I_{Ks} reduced action potential duration from a control value of 220 ms to 211, 211 and 197 ms, respectively, at a pacing cycle length of 1,000 ms. Despite the reduction in action potential duration, the magnitudes of I_{Ca} and the Ca^{2+} transient were minimally affected, both at short pacing cycle lengths (compare Figs. 2 and 8) and at a cycle length of 1,000 ms: peak I_{Ca} magnitudes for control and elevated I_{K1} , I_{Kr} , and I_{Ks} were -1.57 , -1.57 , -1.57 , and -1.58 pA/pF, respectively, and peak $[Ca^{2+}]_i$ magnitudes were 2.15, 2.10, 2.12, and 2.04 μM , respectively.

DISCUSSION

We developed an ionic model of the canine ventricular muscle cell that generates physiologically realistic

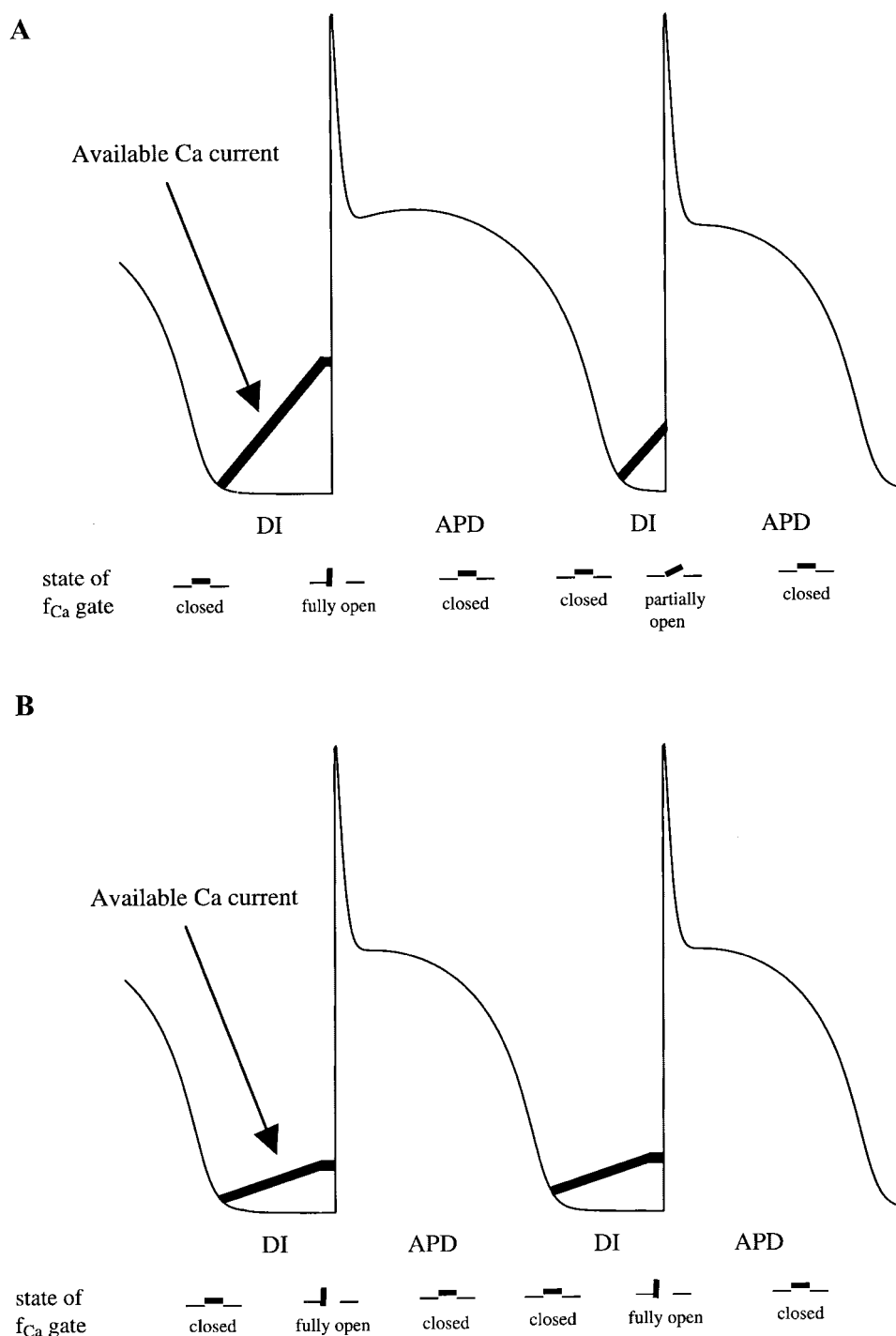


Fig. 6. Relationship among the kinetics of the calcium-induced inactivation gate (f_{Ca}), APD, DI, and the time course of I_{Ca} in the normal CVM model (A) and in the reduced I_{Ca} model (B) at a pacing cycle length of 180 ms. See text for discussion and *Glossary* for abbreviations.

action potential duration alternans characterized by a large magnitude and a wide range of pacing cycle lengths over which they appear. Action potential duration alternans was caused primarily by an alternans of I_{Ca} , where the latter resulted from the time-dependent behavior of the calcium-induced inactivation gate, f_{Ca} . Alternans was suppressed by reducing the magnitude

of I_{Ca} as well as by increasing the magnitude of selected repolarizing K^+ currents. Although the CVM model has some limitations, as discussed below, it is the first ionic model of the CVM that reproduces physiological alternans at rapid pacing rates. As such, it provides a useful simulation tool for studying the complicated interactions of cardiac membrane currents.

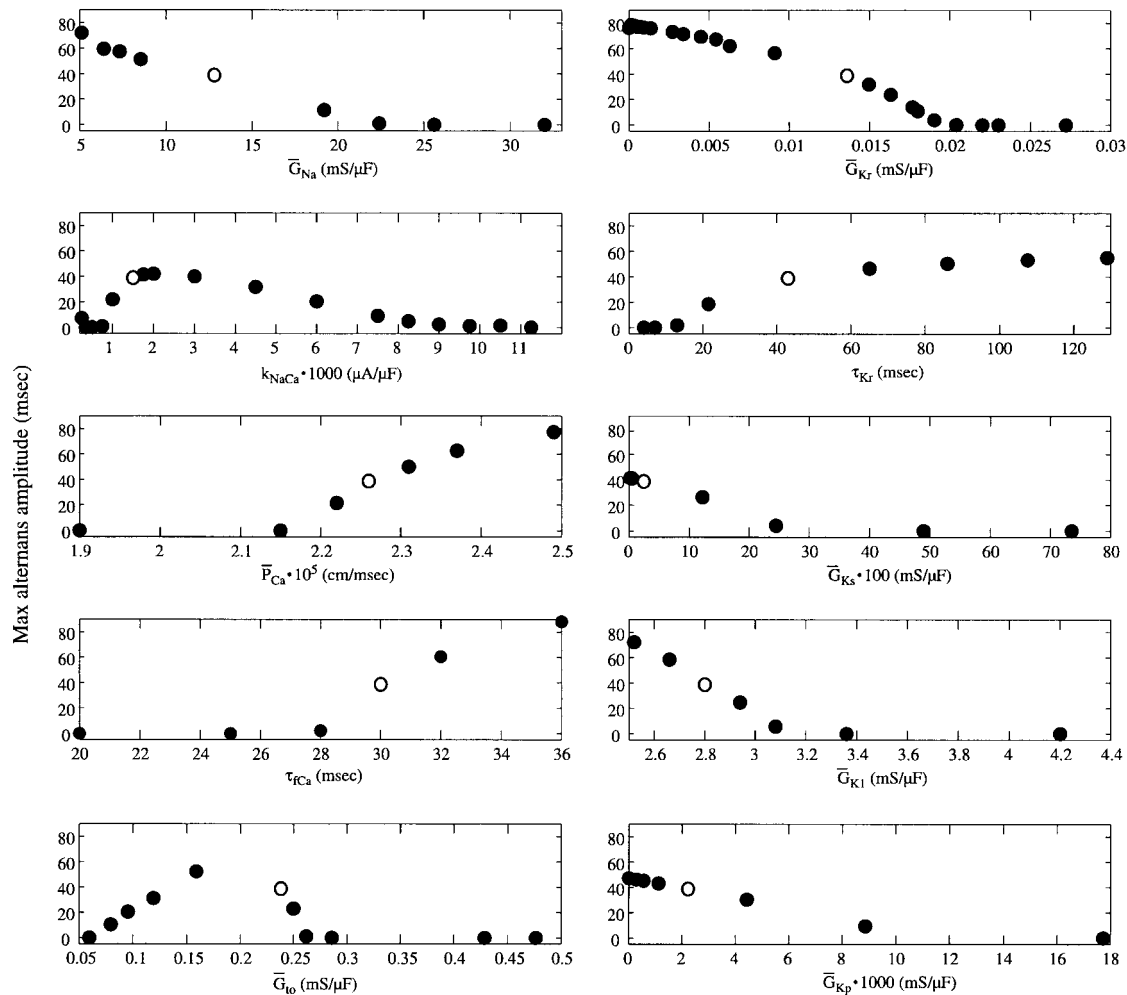


Fig. 7. Dose-response relationships between ionic current magnitude and alternans magnitude in the CVM model. Shown are the maximum magnitudes of APD alternans as a function of a particular model parameter. \circ , Control parameter value. *Left* (from *top to bottom*): maximum I_{Na} conductance, I_{NaCa} , maximum I_{Ca} permeability, time constant for f_{Ca} , and maximum conductance for I_{Io} . *Right* (from *top to bottom*): maximum conductance for I_{Kr} , time constant for I_{Kr} , maximum conductance for I_{Ks} , maximum conductance for I_{K1} , and maximum conductance for I_{Kp} . See *Glossary* for abbreviations.

Role of I_{Ca} in alternans. The development of action potential duration alternans required that 1) the duration of the action potential have a sensitive dependence on I_{Ca} and 2) the recovery of I_{Ca} have a sensitive dependence on diastolic interval. The first condition applied so long as there was a relative balance of repolarizing K^+ current and I_{Ca} during the action potential plateau. The second condition was manifest during pacing at short cycle lengths, where partial recovery of I_{Ca} after short diastolic intervals resulted in short action potential durations, followed by long diastolic intervals. Nearly complete recovery of I_{Ca} after long diastolic intervals produced action potentials with long durations, followed by short diastolic intervals. By this mechanism, a self-perpetuating sequence of long-short action potential durations was established. A similar mechanism likely contributed to action potential duration alternans in previously published ionic models (1, 22), although alternans of I_{Ca} was not specifically reported in those studies.

After the magnitude of I_{Ca} was reduced by decreasing \bar{P}_{Ca} or increasing calcium-induced inactivation, the balance of I_{Ca} and repolarizing K^+ currents was shifted in favor of the repolarizing currents, resulting in shorter action potential durations. The resultant longer diastolic intervals allowed for complete recovery of I_{Ca} , albeit to a lesser magnitude, during pacing at cycle lengths that induced alternans in the control model. At even shorter pacing cycle lengths, diastolic intervals were too short to allow full recovery of I_{Ca} . However, because of the reduced magnitude of I_{Ca} and rate-dependent accumulation of incompletely deactivated K^+ current, the dependence of action potential duration on I_{Ca} was minimized and action potential durations remained consistently short. A similar mechanism accounts for the attenuation of alternans in the control model at very short pacing cycle lengths (Fig. 3).

Role of repolarizing K^+ currents in alternans. Beat-to-beat alterations of I_{K1} , I_{Kr} , and I_{Ks} appeared to play

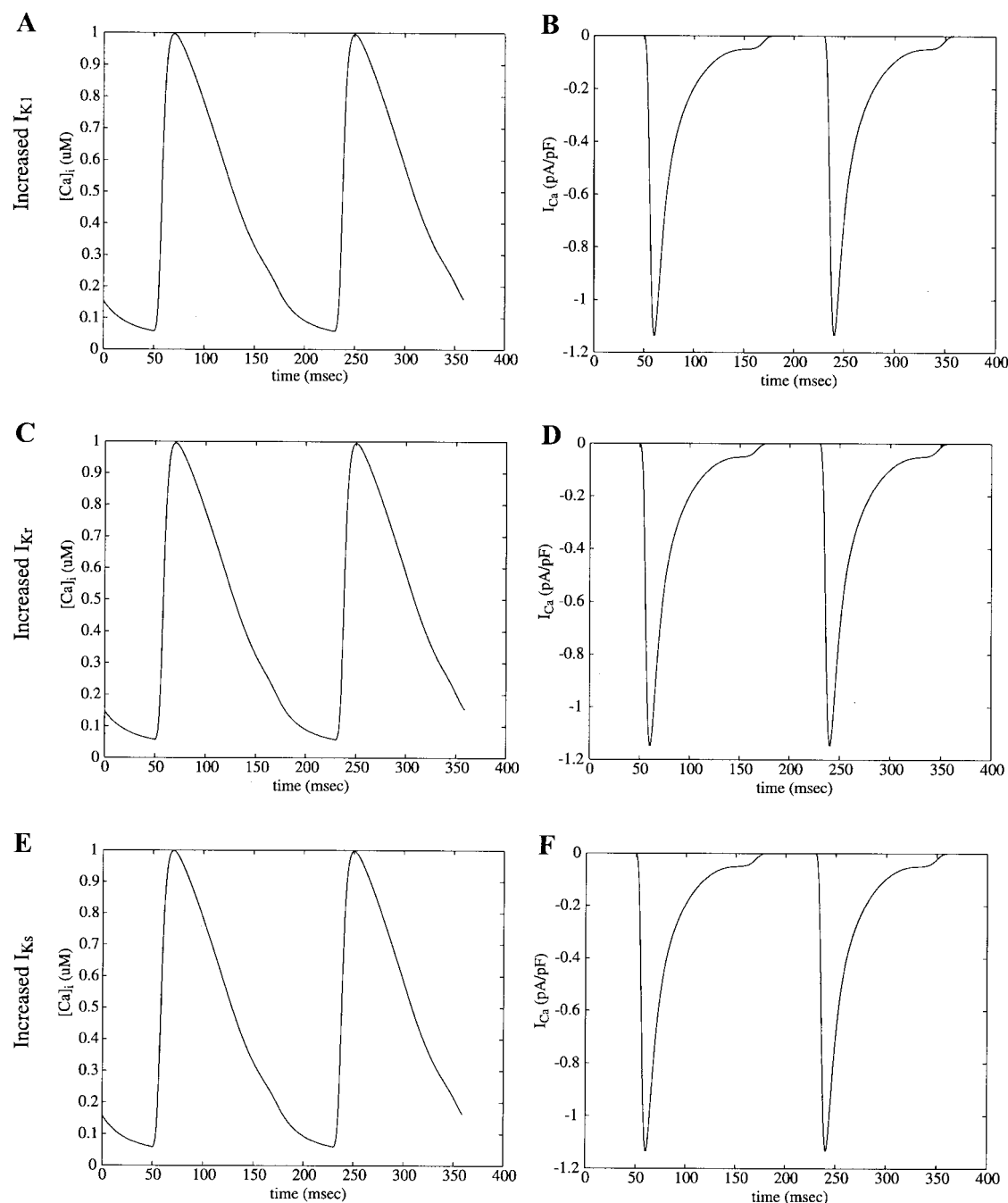


Fig. 8. $[Ca^{2+}]_i$ (left) and I_{Ca} (right) in the CVM model after increasing I_{K1} (A and B), I_{Kr} (C and D), or I_{Ks} (E and F). See Glossary for abbreviations.

a minor role in mediating alternans. As expected, I_{K1} , which has no time dependence, displayed no beat-to-beat variations in magnitude, whereas the beat-to-beat changes in I_{Ks} were too small to affect action potential duration appreciably at short pacing cycle lengths. Total I_{Kr} also alternated during alternans; however, peak I_{Kr} did not, suggesting that alternation of I_{Kr} resulted from alternans of action potential duration rather than vice versa.

Although the beat-to-beat variations of I_{K1} , I_{Kr} , and I_{Ks} did not contribute appreciably to alternans, increasing

any one of these currents sufficiently suppressed alternans. The mechanism for this effect was analogous to that described in *Role of I_{Ca} in alternans* for the suppressant effects of reducing I_{Ca} on alternans. With elevation of I_{K1} , I_{Kr} , or I_{Ks} , the balance of repolarizing K^+ currents and I_{Ca} during the action potential plateau was skewed, resulting in consistently short action potential durations. Consequently, the pattern of action potential duration and diastolic interval was similar to that shown in Fig. 6B except that I_{Ca} not only recovered fully but also achieved a larger magnitude.

Implications. Decreasing the magnitude of I_{Ca} , either experimentally (23) or in an ionic model (22), has been shown to eliminate alternans and to convert VF into a periodic rhythm. However, this approach clearly is not useful clinically because decreasing I_{Ca} decreases the Ca^{2+} transient, thereby reducing contractile force. With the use of the CVM model to explore other methods for eliminating alternans, we found that alternans was suppressed by increasing the magnitude of three repolarizing K^+ currents: I_{K1} , I_{Kr} , and I_{Ks} .

Given that increasing I_{K1} , I_{Kr} , and I_{Ks} decreased action potential duration, we determined whether such shortening truncated I_{Ca} , in which case increasing K^+ conductance might have the same clinical limitation as decreasing Ca^{2+} conductance. However, I_{Ca} was minimally affected both at short and at long pacing cycle lengths, as was the Ca^{2+} transient. Consequently, it is possible, at least in the CVM model, to increase K^+ conductance to the point of suppressing alternans without reducing contractility.

These simulation results suggest a novel strategy for treating ventricular tachyarrhythmias. Previous attempts at treatment of such arrhythmias with pharmacological agents have been largely unsuccessful. In particular, class III antiarrhythmic drugs, which are designed to block K^+ currents, have been shown to be proarrhythmic (20). The CVM simulations suggest that a new class of drugs designed to increase the magnitude of selected outward currents may be useful in preventing alternans and, therefore, in preventing the development of arrhythmias such as VF. It should be emphasized, however, that only those K^+ channel agonists that reduce the slope of the action potential duration restitution relation are expected to suppress VF. Drugs such as ATP-sensitive K^+ channel current agonists, which markedly increase outward K^+ current and shorten action potential duration, increase the slope of the restitution relation and, presumably by that mechanism, facilitate the induction of VF (27).

Limitations. While the CVM model successfully reproduces alternans, it has several limitations. First, the formulation of I_{Ca} is based solely on the qualitative characteristics of I_{Ca} . To improve the model, I_{Ca} should conform to the results of quantitative voltage-clamp experiments, where the latter ideally have been conducted under circumstances that preserve the native behavior of I_{Ca} during pacing at short cycle lengths (e.g., no buffering of $[Ca^{2+}]_i$ or washout of the intracellular space). Second, although the simplified calcium handling in the model reproduces physiological Ca^{2+} transients, it ignores several of the details of calcium release from the SR. Further work needs to be done to incorporate detailed calcium handling mechanisms such as those in the Winslow model (26). Third, the model does not include the late Na^+ current, which may contribute significantly to plateau duration (28). A formulation of this current that agrees with voltage-clamp experiments also needs to be included to complete the model. Finally, it has been shown that trans-

mural heterogeneity of the heart is caused by differences in I_{to} , I_{Ks} , I_{NaCa} , and the late Na^+ current in endocardial, midmyocardial, and epicardial canine heart cells (13, 14, 27, 29). We hope in the future to develop specific models for canine endocardium, midmyocardium, and epicardium cells that will take these differences into account.

These studies were supported by Integrative Graduate Education and Research Traineeship Program in Nonlinear Systems National Science Foundation Grant DGE-9870631, by National Heart, Lung, and Blood Institute Grant HL-84536, and by a grant-in-aid from the American Heart Association, New York State Affiliate.

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