

- 2 (a) Let  $F$  and  $G$  be two non-empty proper subsets of  $\mathbb{R}$  such that  $F$  is closed and  $G$  is open. If  $F \Delta G$  is both open and closed then show that  $F^c = G$ . [3]
- (b) Let  $(X, d)$  be a metric space. If  $x \in X$  then show that  $\{x\}$  is closed. [3]
- (c) Let  $G = \{x \in \mathbb{R} \setminus \mathbb{Q} : x \leq 0\}$  and  $F = \{x \in \mathbb{Q} : x \geq 0\}$ . Show that [3+6]
- (i)  $G$  is a  $G_\delta$  set.
- (ii)  $F \cup G$  is neither  $F_\sigma$  nor  $G_\delta$