

A* Search Algorithm

Topic-1: Graph Representation

- Adjacency Matrix
- Adjacency List

Topic-2: Type of Searching Techniques

- Uninformed Searching
 - BFS, DFS, etc.
 - Cons: Time Consuming & Complexity
- Informed Searching
 - A*, Heuristic DFS, Best First Search, etc.
 - Pros: Provides quick solution & less Complexity

Topic-3: Heuristic Function & Heuristic Value

Topic-4: Admissibility

- Underestimation
- Overestimation

A given heuristic function $h(n)$ is **admissible** if it never **overestimates** the real distance between n and the goal node.

Therefore, for every node n the following formula applies:

$$h(n) \leq h^*(n)$$

Topic-5: Consistency

A given heuristic function $h(n)$ is **consistent** if the estimate is always less than or equal to the estimated distance between the goal n and any given neighbor, plus the estimated cost of reaching that neighbor:

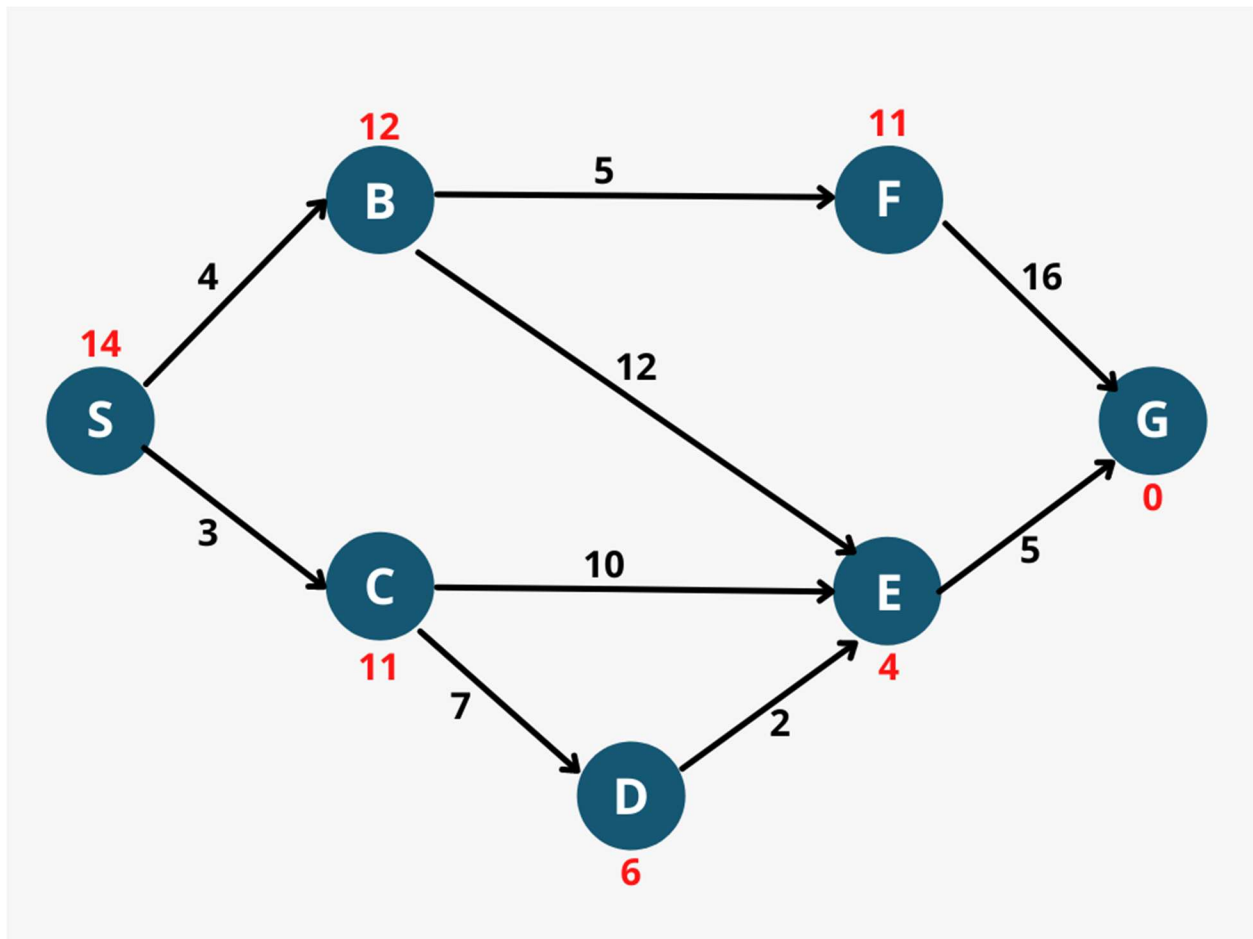
$$c(n, m) + h(m) \geq h(n)$$

Topic-6: A* Search Algorithm

A* is based on using heuristic methods to achieve **optimality** and **completeness**, and is a variant of the **best-first algorithm**.

When a search algorithm has the property of optimality, **it means it is guaranteed to find the best possible solution**, in our case the shortest path to the finish state. When a search algorithm has the property of completeness, **it means that if a solution to a given problem exists, the algorithm is guaranteed to find it**.

A* Search Algorithm



Initialize a min priority queue **Q** ordered based on $f(n) = (g(n) + h(n))$

$g \leftarrow 0$

$h \leftarrow \text{euclidean_distance}(\text{start_node}, \text{goal_node})$

$f \leftarrow g(n) + h(n)$

create **start_state**(start_node, g(n), f(n), parent=None)

insert **start_state** to **Q**

while **Q** not empty:

curr_state \leftarrow extract_min(**Q**)

 if **curr_state.node** is the goalnode then

print solution path and cost and **return**

 for each node **M** adjacent to node **curr_state.node**:

$g(n) \leftarrow \text{curr_state.g}(n) + \text{edge_cost}(\text{curr_state.node}, M)$

$h(n) \leftarrow \text{euclidean_distance}(M, \text{goal_node})$

$f(n) \leftarrow g(n) + h(n)$

 create **new_state**(M, g, f, parent=curr_state)

 Insert **new_state** to **Q**

A* Search Algorithm

Sample Input:

```
7 9 (no_of_vertices no_of_edges)
0 1 4 (starting_vertex_of_an_edge ending_vertex_of_an_edge weight_of_the_edge)
0 2 3
1 4 12
1 5 5
2 3 7
2 4 10
3 4 2
4 6 5
5 6 16
14 12 11 6 4 11 0
```

Sample Output:

Path: 0 --> 2 --> 3 --> 4 --> 6

Total Actual Cost: 17

References:

<https://stackabuse.com/basic-ai-concepts-a-search-algorithm/>

<https://www.pythonpool.com/a-star-algorithm-python/>

Tutorials:

https://www.youtube.com/watch?v=vP5TkF0xJgI&ab_channel=GeeksforGeeks

https://www.youtube.com/watch?v=tvAh0JZF2YE&ab_channel=GateSmashers