10/11/22, 9:56 PM I\_Coins.cpp

```
1 | //
 2 //
        Let N be a positive odd number.
 3
        There are N coins, numbered 1,2,...,N. For each i (1 \le i \le N), when Coin i is tossed,
   //
        it comes up heads with probability p[i] and tails with probability 1-p[i] tails.
 4
   //
        Taro has tossed all the N coins. Find the probability of having more heads than tails.
   //
 6
   //
 7
    //
        Time Complexity: O(N^2)
 8
    //
 9
10
   #include <bits/stdc++.h>
11
12 using namespace std;
13
14
    int main() {
15
        int n;
16
        cin >> n;
17
18
        // everything in this problem
19
        // is with 1-based indexing
20
        // for simplicity
21
        vector<double> p(n+1);
        for (int i = 1; i \le n; i \leftrightarrow ) {
22
23
            cin >> p[i];
24
25
        vector<vector<double>> dp(n+1, vector<double>(n+1, 0));
26
27
        dp[1][0] = 1 - p[1];
28
        dp[1][1] = p[1];
29
30
        for (int i = 2; i ≤ n; i++) {
            for (int j = 0; j \le i; j \leftrightarrow) {
31
32
                 // dp[i][j] - the probability of
                                getting j heads out of
33
34
                 //
                                the coins to the i-th index
35
36
                 if (j > 0)
                     dp[i][j] += dp[i-1][j-1] * p[i];
37
38
                 dp[i][j] += dp[i-1][j] * (1 - p[i]);
39
            }
40
        }
41
42
        double ans = 0;
for (int i = n/2 + 1; i \leq n; i++) {
43
44
45
            ans += dp[n][i];
46
47
        cout << setprecision(16) << ans << endl;</pre>
48
49
        return 0;
50 }
```