

```

1 //
2 // Taro and Jiro will play the following game against each other.
3 // Initially, they are given a sequence a = (a[1], a[2], ..., a[n])
4 // Until a becomes empty, the two players perform the following operation alternately,
5 // starting from Taro:
6 //   - Remove the element at the beginning or the end of a.
7 //   The player earns x points, where x is the removed element.
8 //
9 // Let X and Y be Taro's and Jiro's total score at the end of the game, respectively.
10 // Taro tries to maximize X-Y, while Jiro tries to minimize X-Y.
11 // Assuming that the two players play optimally, find the resulting value of X-Y.
12 //
13 // Time Complexity: O(N^2)
14 //
15
16 #include <bits/stdc++.h>
17 #define ll long long
18
19 using namespace std;
20
21 int main() {
22     int n;
23     cin >> n;
24
25     vector<ll> awards(n);
26     vector<vector<ll>> dp(n, vector<ll>(n, 0));
27     for (int i = 0; i < n; i++) {
28         cin >> awards[i];
29
30         // BASE CASE:
31         dp[i][i] = awards[i];
32     }
33
34     // interval starting and ending at position i = score is awards[i]
35     // solving for subintervals
36
37     /// - - - - -
38     ///   <====>
39     ///   <====>
40     ///   <====>
41
42     for (int size = 1; size < n; size++) { // size of interval
43         for (int start = 0; start < n - size; start++) { // starting position of interval
44             if (size % 2 == 0) { // Taro (max)
45                 // START - L
46                 // START+SIZE = R
47                 dp[start][start+size] =
48                     max(dp[start][start+size-1] + awards[start+size],
49                        dp[start+1][start+size] + awards[start]);
50             } else { // Jiro (min)
51                 dp[start][start+size] =
52                     min(dp[start][start+size-1] - awards[start+size],
53                        dp[start+1][start+size] - awards[start]);
54             }
55         }
56     }
57
58     // dp[0][n-1]
59     cout << (n % 2 == 0 ? -1LL : 1LL) * dp[0][n-1] << endl;
60     return 0;
61 }

```