
AlphaNet: Improved Training of Supernet with Alpha-Divergence

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Abstract

Weight-sharing neural architecture search (NAS) is an effective technique for automating efficient neural architecture design. Weight-sharing NAS builds a supernet that assembles all the architectures as its sub-networks and jointly trains the supernet with the sub-networks. The success of weight-sharing NAS heavily relies on distilling the knowledge of the supernet to the sub-networks. However, we find that the widely used distillation divergence, i.e., KL divergence, may lead to student sub-networks that overestimate or under-estimate the uncertainty of the teacher supernet, leading to inferior performance of the sub-networks. In this work, we propose to improve the supernet training with a more generalized α -divergence. By adaptively selecting the α -divergence, we simultaneously prevent the over-estimation or under-estimation of the uncertainty of the teacher model. We apply the proposed α -divergence based supernet training to both slimmable neural networks and weight-sharing NAS, and demonstrate significant improvements. Specifically, our discovered model family, AlphaNet, outperforms prior-art models on a wide range of FLOPs regimes, including BigNAS, Once-for-All networks, and AttentiveNAS. We achieve ImageNet top-1 accuracy of 80.0% with only 444M FLOPs. Our code and pretrained models are available at <https://github.com/facebookresearch/AlphaNet>.

1. Introduction

Designing accurate and computationally efficient neural network architectures is an important but challenging task.

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Neural architecture search (NAS) automates the neural network design by exploring an enormous architecture space and achieves state-of-the-art (SOTA) performance on various applications including image classification (Zoph & Le, 2017; Zoph et al., 2018), object detection (Ghiasi et al., 2019), semantic segmentation (Zhang et al., 2019) and natural language processing (Wang et al., 2020b).

Conventional NAS approaches can be prohibitively expensive as hundreds of candidate architectures need to be trained from scratch and evaluated (e.g., Tan et al., 2019; Zoph et al., 2018). The supernet based approach has recently emerged to be a promising approach for efficient NAS. A supernet assembles all candidate architectures into a weight sharing network with each architecture corresponding to one sub-network. By training the sub-networks simultaneously with the supernet, different architectures can directly inherit the weights from the supernet for evaluation and deployment, which eliminates the huge cost of training or fine-tuning each architecture individually.

Though promising, simultaneously optimizing all sub-networks with weight-sharing is highly challenging for the supernet training (e.g., Yu et al., 2020; Cai et al., 2019a). To stabilize the supernet training and improve the performance of sub-networks, one widely used approach is in-place knowledge distillation (KD) (Yu & Huang, 2019). In-place KD leverages the soft labels predicted by the largest sub-network in the supernet to supervise all the other sub-networks. By distilling the knowledge of the teacher model, the performance of the sub-networks can be improved significantly (Yu & Huang, 2019; Yu et al., 2020).

Standard knowledge distillation uses KL divergence to measure the discrepancy between the teacher and student networks. However, KL divergence penalizes the student model much more when it fails to cover one or more local modes of the teacher model (Murphy, 2012). Hence, the student model tends to over-estimate the uncertainty of the teacher model and suffers from inaccurate approximation of the most important mode, i.e., the correct prediction of the teacher model.

To further enhance the supernet training, we propose to replace the KL divergence with a more generalized α -divergence (Amari, 1985; Minka et al., 2005). Specifically, by adaptively controlling α in the proposed diver-

gence metric, we can penalize both the under-estimation and over-estimation of the teacher model uncertainty to encourage a more accurate approximation for the student models. While directly optimizing the proposed adaptive α -divergence may suffer from a high variance of the gradients, we further propose a simple technique to clip the gradients of our adaptive α -divergence to stabilize the training process. We show the clipped gradients still define a valid divergence metric implicitly and hence, yielding a proper optimization objective for KD.

We empirically verify the proposed adaptive α -divergence in two notable applications of supernets - slimmable networks (Yu & Huang, 2019) and weight-sharing NAS (Yu et al., 2020; Wang et al., 2020a) on ImageNet. For weight-sharing NAS, we train a supernet containing both small (200M FLOPs) and large (2G FLOPs) sub-networks following Wang et al. (2020a). With the proposed adaptive α -divergence, we are able to train high-quality sub-networks, called AlphaNets, that surpass all prior state-of-the-art models in the range of 200 to 800 MFLOPs, like EfficientNets (Tan & Le, 2019), OFANets (Cai et al., 2019a), and BigNas (Yu et al., 2020). Specifically, AlphaNet-A4 achieves 80.0% accuracy with only 444M FLOPs.

2. Background

Training high-quality supernets is fundamental for weight-sharing NAS but non-trivial (Benyahia et al., 2019). Recently, in-place KD is shown to be an effective mechanism that significantly improves the supernet performance (Yu & Huang, 2019; Yu et al., 2020).

To formalize the supernet training and in-place KD, consider a supernet with trainable parameter θ . Let \mathcal{A} denote the collection of all sub-networks contained in the supernet. The goal of training a supernet is to learn θ such that all the sub-networks in \mathcal{A} can be optimized simultaneously to achieve good accuracy.

The supernet training process with the in-place KD is illustrated in Figure 1. At each training step, given a mini-batch of data, the supernet as well as several sub-networks are sampled. While the supernet is trained with the real labels, all the sampled sub-networks are supervised with the soft labels predicted by the supernet. Then, the gradients from all the sampled networks are aggregated before the supernet parameters are updated. More formally, at the training step t , the supernet parameters θ are updated by

$$\theta_t \leftarrow \theta_{t-1} + \epsilon g(\theta_{t-1}),$$

where ϵ is the step size, and

$$g(\theta_{t-1}) = \nabla_\theta \left(\mathcal{L}_D(\theta) + \gamma \mathbb{E}_s \mathcal{L}_{KD}([\theta, s]; \theta_{t-1}) \right) \Big|_{\theta=\theta_{t-1}}. \quad (1)$$

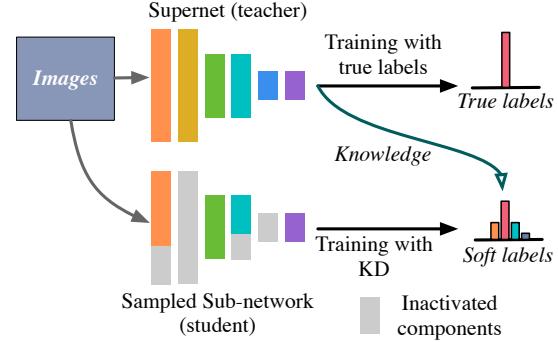


Figure 1. An illustration of training supernets with KD. Sub-networks are part of the supernet with weight-sharing.

Here, $\mathcal{L}_D(\theta)$ is the standard cross entropy loss of the supernet on a training dataset \mathcal{D} , γ is the weight coefficient, and $\mathcal{L}_{KD}([\theta, s]; \theta_t)$ is the KD loss for distilling the supernet into a randomly sampled sub-network s , for which KL divergence has been widely used (e.g., Yu et al., 2020).

Let $p(x; \theta)$ and $q(x; \theta, s)$ denote the output probability of the supernet and the sub-network s given input x , then, we have

$$\mathcal{L}_{KD}([\theta, s], \theta_t) = \mathbb{E}_{x \sim \mathcal{D}} [\text{KL}(p(x; \theta_t) || q(x; \theta, s))], \quad (2)$$

where $\text{KL}(p || q) = \mathbb{E}_p [\log(p/q)]$. Note that the gradient on $p(x; \theta_t)$ in the KD loss is stopped as (2) indicated. For notation simplicity, we denote p as our teacher model and q (or q_θ) as student models in the following.

Additionally, note that the way KD is used in the supernet training is different from the standard settings such as Hinton et al. (e.g., 2015), where the teacher network is pre-trained and fixed.

3. Supernet training with α -divergence

In this section, we analyze the limitations of using KL divergence in KD and propose to replace KL divergence with a more generalized α -divergence. We study the impact of different choices of α values in the proposed divergence metric and further propose an adaptive algorithm to select α values during the supernet training. Meanwhile, we also show that while directly optimizing α -divergence is challenging due to large gradient variances, a simple clipping strategy on α -divergence can be very effective to stabilize the training.

3.1. Classic KL based KD and its limitations

KL divergence has been widely used to measure the discrepancy in output probabilities between the teacher and student models in KD. One main drawback with KL di-

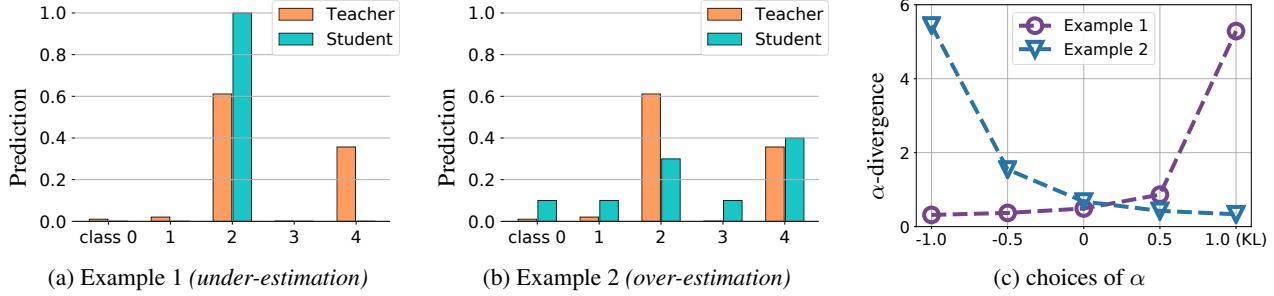


Figure 2. (a) *Example 1 - uncertainty under-estimation*. The student network under-estimates the uncertainty of the teacher model and misses important local modes of the teacher model. (b) *Example 2 - Uncertainty over-estimation*. In this case, the student network over-estimates the uncertainty of the teacher model and misclassifies the most dominant mode of the teacher model. (c) plots the corresponding α -divergences between the student model and the teacher model for Examples 1 and 2. Note that KL divergence is a special case of α -divergences with $\alpha = 1$. We refer to the uncertainty as the entropy of predictions after the Softmax layer of the network.

vergence is that it cannot sufficiently penalize the student model when it over-estimates the uncertainty of the teach model. Let p and q denote the output probability of the teacher and student models, respectively. The KL divergence between the teacher and student models is calculated by $\text{KL}(p||q) = \mathbb{E}_p[\log(p/q)]$. When $p > 0$, to ensure $\text{KL}(p||q)$ remains finite, we must have $q > 0$. This is the so-called *zero avoiding* property of KL. In contrast, when $p = 0$, $q > 0$ does not get penalized. For example, as shown in Figure 2 (b) and (c), even though the student model over-estimates the uncertainty of the teacher model and predicts the wrong class ("class 4"), the KL divergence is still small.

The aforementioned *over-estimation* in Example 2 would be penalized at a larger magnitude when using other types of divergences, e.g., reverse KL divergence $\text{KL}(q||p)$. For reverse KL divergence, $\text{KL}(q||p) = \mathbb{E}_q[\log(q/p)]$ is infinite if $p = 0$ and $q > 0$. Hence if $p = 0$ we must ensure $q = 0$, this is known as the *zero forcing* property (Murphy, 2012). Therefore, minimizing reverse KL divergence encourages the student model q to avoid low probability modes of p while focusing on the modes with high probabilities, and thus, may *under-estimate* the uncertainty of the teacher model, as shown in Example 1 in Figure 2.

Hence, a natural question is whether it is possible to generalize the KL divergence to simultaneously suppress both the under-estimation and over-estimation of the teacher model uncertainty during the supernet training.

3.2. KD with adaptive α -divergence

Our observations shown in Figure 2 motivate us to design a new KD objective that simultaneously penalize both over-estimation and under-estimation of the teacher model uncertainty. We first generalize the typical KL divergence with a more flexible α -divergence (Minka et al., 2005).

Consider $\alpha \in \mathbb{R} \setminus \{0, 1\}$, the α -divergence is defined as

$$D_\alpha(p || q) = \frac{1}{\alpha(\alpha - 1)} \sum_{i=1}^m q_i \left[\left(\frac{p_i}{q_i} \right)^\alpha - 1 \right], \quad (3)$$

where $q = [q_i]_{i=1}^m$ and $p = [p_i]_{i=1}^m$ are two discrete distributions on m categories. The α -divergence includes a large spectrum of classic divergence measures. In particular, the KL divergence $\text{KL}(p || q)$ is the limit of $D_\alpha(p || q)$ with $\alpha \rightarrow 1$ while the reverse KL divergence $\text{KL}(q || p)$ is the limit of $D_\alpha(p || q)$ with $\alpha \rightarrow 0$.

A key feature of α -divergence is that we can decide to focus on penalizing different types of discrepancies (under-estimation or over-estimation) by choosing different α values. For example, as shown in Figure 2 (c), when α is negative, $D_\alpha(p || q)$ is large when q is more widely spread than p (when q *over-estimates* the uncertainty in p), and is small when q is more concentrated than p (when q *under-estimates* the uncertainty in p). The trend is opposite when α is positive: under-estimation would be more heavily penalized than over-estimation.

To simultaneously alleviate the over-estimation and under-estimation problem when training the supernet, we consider a positive α_+ together with a negative α_- , and propose to use the maximum of $D_{\alpha_+}(p || q)$ and $D_{\alpha_-}(p || q)$ in the KD loss function:

$$D_{\alpha_+, \alpha_-}(p || q) = \max \left\{ \underbrace{D_{\alpha_-}(p || q)}_{\text{penalizing over-estimation}}, \underbrace{D_{\alpha_+}(p || q)}_{\text{penalizing under-estimation}} \right\}.$$

Our KL loss now changes from Eqn. (2) to

$$\mathcal{L}_{KD}([\theta, s], \theta_t) = \mathbb{E}_{x \sim \mathcal{D}} [D_{\alpha_+, \alpha_-}(p(x; \theta_t) || q(x; \theta, s))]. \quad (4)$$

We denote this KD strategy that always chooses the maximum of D_{α_-} and D_{α_+} to optimize as *Adaptive-KD*.

3.3. Stabilizing α -divergence KD

One would prefer to set both $|\alpha_+|$ and $|\alpha_-|$ to be large to ensure the student model is sufficiently penalized when it either under-estimates or over-estimates the uncertainty the teacher model. However, directly optimizing the α -divergence with large $|\alpha|$ is often challenging in practice. Consider the gradient of α -divergence:

$$\nabla_{\theta} D_{\alpha}(p \parallel q_{\theta}) = -\frac{1}{\alpha} \mathbb{E}_{q_{\theta}} \left[\left(\frac{p}{q_{\theta}} \right)^{\alpha} \nabla_{\theta} \log q_{\theta} \right].$$

If $|\alpha|$ is large, then the powered term $(p/q_{\theta})^{\alpha}$ can be quite significant and cause the training process to be unstable. To enhance the training stability, we clamp the maximum value of $(p/q_{\theta})^{\alpha}$ to be β , and obtain

$$\tilde{\nabla}_{\theta} D_{\alpha}(p \parallel q_{\theta}) \stackrel{\text{def}}{=} -\frac{1}{\alpha} \mathbb{E}_{q_{\theta}} \left[\text{Clip}_{\beta} \left(\frac{p}{q_{\theta}} \right)^{\alpha} \nabla_{\theta} \log q_{\theta} \right], \quad (5)$$

where $\text{Clip}_{\beta}(t) = \min(t, \beta)$.

Eqn. (5) is a simple yet effective heuristic approximation of $\nabla_{\theta} D_{\alpha}(p \parallel q_{\theta})$. It is important to note that Eqn. (5) equals the *exact* gradient of a special f divergence between p and q_{θ} . Hence, our updates still amount to minimizing a valid divergence. Note that the clipping function $\text{Clip}_{\beta}(\cdot)$ is only partially differentiable. So naively clipping on $(p/q_{\theta})^{\alpha}$ in Eqn. (3) may stop gradients back-propagating from the density ratio terms, hence yielding gradients that are not from a valid divergence.

To show that we still optimize a valid divergence with Eqn. (5), note that, for a convex function $f: [0, +\infty) \rightarrow \mathbb{R}$, the f -divergence between p and q_{θ} is defined as

$$D_f(p \parallel q_{\theta}) = \mathbb{E}_{q_{\theta}} \left[f \left(\frac{p}{q_{\theta}} \right) - f(1) \right]. \quad (6)$$

Its gradient w.r.t. θ is

$$\nabla_{\theta} D_f(p \parallel q_{\theta}) = -\mathbb{E}_{q_{\theta}} \left[\rho_f \left(\frac{p}{q_{\theta}} \right) \nabla_{\theta} \log q_{\theta} \right],$$

where $\rho_f(t) = f'(t)t - f(t)$ (Wang et al. (2018)). Note that α -divergence is a special case of f -divergence when $f(t) = t^{\alpha}/(\alpha(\alpha-1))$.

Proposition 3.1. *There exists a convex function $f: (0, +\infty) \rightarrow \mathbb{R}$, such that $\tilde{\nabla}_{\theta} D_{\alpha}(p \parallel q_{\theta})$ in (5) is the exact gradient of $D_f(p \parallel q_{\theta})$, that is, $\tilde{\nabla}_{\theta} D_{\alpha}(p \parallel q_{\theta}) = \nabla_{\theta} D_f(p \parallel q_{\theta})$.*

Proof. Let $\rho_*(t) = \frac{1}{\alpha} \text{Clip}_{\beta}(t)^{\alpha}$. We just need to find a f such that

$$\rho_f(t) = f'(t)t - f(t) = \rho_*(t).$$

Algorithm 1 Training supernets with α -divergence

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- 1: **Input:** Adaptive α -divergence range given by α_- and α_+ , a clipping factor β , a supernet with parameter θ , and a search space \mathcal{A} .
 - 2: **while** not converging **do**
 - 3: Sample a mini-batch of data B .
 - 4: Train the supernet with true labels from B
 - 5: Draw k subnetworks $\{s_1, \dots, s_k\}$ from \mathcal{A} ; train sub-networks to mimic the supernet on the mini-batch data B with the KD loss defined in Eqn. (4) using clipped gradients in Eqn. (5).
 - 6: **end while**
-

Taking derivation on both sides, we get $f''(t)t = \rho'_*(t)$. This gives $f''(t) = \rho'_*(t)/t$ and hence $f(t) = \int \rho'_*(t)/tdt$, where $\int \int$ denotes second-order antiderivative (or indefinite integral). Because $\rho_*(t)$ is non-decreasing, we have $\rho'_*(t)/t \geq 0$ for $t > 0$, and hence f is convex on $(0, +\infty)$. \square

In practice, we apply Eqn. (5) to the α -divergence used in Eqn. (4). By clipping the value of importance weights, what we optimize is still a divergence metric but is more friendly to gradient-based optimization.

4. Experiments

We apply our *Adaptive-KD* to improve notable supernet-based applications, including slimmable neural networks (Yu & Huang, 2019) and weight-sharing NAS (e.g., Cai et al., 2019a; Yu et al., 2020; Wang et al., 2020a). We provide an overview of our algorithm for training the supernet in Algorithm 1.

Adaptive-KD settings In our algorithm, α_- and α_+ control the magnitude of penalizing on *over-estimation* and *under-estimation*, respectively. And, β controls the range of density ratios between the teacher model and the student model. We find our method performs robustly w.r.t. a wide range of choices of α_- , α_+ and β , yielding consistent improvements over the KL based KD baseline. Throughout the experimental section, we set $\alpha_- = -1$, $\alpha_+ = 1$ and $\beta = 5.0$ as default for our method. We provide detailed ablation studies on these hyper-parameters in section 4.4.

4.1. Slimmable Neural Networks

Slimmable neural networks (Yu et al., 2018; Yu & Huang, 2019) are examples of supernets that support a wide range of channel width configurations. The search space \mathcal{A} of slimmable networks contains networks with different width and all the other architecture configurations (e.g. depth, convolution type, kernel size) are the same. This way,

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Model	Method	0.25×	0.3×	0.35×	0.4×	0.45×	0.5×	0.55×	0.6×	0.65×	0.7×	0.75×
MbV1	w/o KD	53.9	55.3	57.1	59.1	61.1	62.9	64.0	65.8	66.9	67.9	68.8
	w/ KL-KD	56.4	57.8	59.5	61.0	63.0	64.4	65.5	67.1	68.3	69.1	69.8
	w/ Adaptive-KD (ours)	56.4	57.9	59.7	61.7	63.4	65.0	66.2	67.7	68.8	69.5	70.1
MbV2	w/o KD	-	-	61.9	62.8	63.7	64.5	65.1	67.2	67.7	68.3	69.0
	w/ KL-KD	-	-	63.2	64.4	65.1	66.0	66.5	68.4	69.2	69.5	70.1
	w/ Adaptive-KD (ours)	-	-	63.7	64.6	65.6	66.3	66.9	68.7	69.3	69.9	70.5

Table 1. Top-1 validation accuracy on ImageNet for Slimmable MobileNetV1 networks (denoted by MbV1) and Slimmable MobileNetV2 networks (denoted by MbV2) trained with different KD strategies.

Model	Method	0.25×	0.3×	0.35×	0.4×	0.45×	0.5×	0.55×	0.6×	0.65×	0.7×	0.75×
MbV1	w/ KL-KD (T=0.5)	55.1	56.0	57.6	59.1	61.4	62.5	64.0	65.6	66.9	67.9	68.7
	T=2.0	55.4	57.0	58.8	60.7	62.6	64.1	65.3	66.6	67.9	68.7	69.5
	T=4.0	48.7	50.7	53.1	55.9	58.8	60.9	62.7	64.6	66.0	67.4	68.3
MbV2	w/ KL-KD (T=0.5)	-	-	61.7	62.9	63.8	64.6	65.0	67.4	68.4	68.8	69.8
	T=2.0	-	-	62.6	63.9	64.8	65.6	66.4	68.1	68.6	69.1	70.0
	T=4.0	-	-	59.3	60.9	62.2	63.1	64.0	66.3	67.1	67.7	68.8

Table 2. Comparison to KL based KD with different temperature (T). We report top-1 validation accuracy on ImageNet for slimmable MobileNetV1 and MobileNetV2 networks, denoted by MbV1 and MbV2, respectively.

slimmable networks allow different devices or applications to adaptively adjust the model width on the fly according to on-device resource constraints to achieve the optimal accuracy vs. energy efficiency trade-off.

Settings We closely follow the training recipe provided in Yu & Huang (2019), and use slimmable MobileNetV1 (Howard et al., 2017) and slimmable MobileNetV2 (Sandler et al., 2018) as our testbed. Specifically, we train slimmable MobileNetV1 to support arbitrary dynamic width in the range of [0.25, 1.0], and train slimmable MobileNetV2 to support dynamic widths of [0.35, 1.0].

We adopt the sandwich rule sampling proposed in Yu & Huang (2019) for training. At each training iteration, we sample the largest sub-network with the largest channel width, the smallest sub-network with the smallest channel width and two random sub-networks to accumulate the gradients. We train the supernet with ground truth labels and train all subsampled sub-networks with KD following (1). For our baseline KD strategy, we set the KD coefficient γ to be the number of sub-networks sampled, i.e., $\gamma = 3$, as default following Yu & Huang (2019). To evaluate the effectiveness of our method, we simply replace the baseline KL-based KD loss used in Yu & Huang (2019) with our adaptive KD loss in (4).

Additionally, we train all models for 360 epochs using SGD optimizer with momentum as 0.9, weight decay as 10^{-5} and dropout as 0.2. We use cosine learning rate decay, with an initial learning rate of 0.8, and batch size of 2048 on 16 GPUs. Following Yu & Huang (2019), we evaluate on Im-

ageNet (Deng et al., 2009). We note that the baseline models trained with our hyper-parameter settings outperform those reported in Yu & Huang (2019).

Results We summarize our results in Table 1. We report the top-1 accuracy on the ImageNet. Here, *w/o KD* denotes the training strategy that excludes the effect of KD. All such sub-networks are trained with ground truth labels via cross entropy.

As we can see from Table 1, both baseline KL based KD (denoted as *w/ KL-KD*) and our *adaptive KD* (denoted as *w/ Adaptive-KD*) yield significant performance improvements compared to *w/o KD*. Our results confirm the importance of KD for training Slimmable networks. Meanwhile, our Adaptive-KD further improves on KL based KD for all the channel width configurations evaluated for both Slimmable MobileNetV1 (denoted by MbV1) and Slimmable MobileNetV2 (denoted by MbV2).

Comparison to KD with different temperature coefficients As discussed in Hinton et al. (2015), for standard KL based KD, one can soften (or sharpen) the probabilities of the teacher and the student model by applying a temperature in their softmax layers. The best distillation performance might be achieved with a different temperature other than the normally used temperature of 1.

To ensure a fair comparison, we further evaluate the baseline KL based KD under different temperature (T) settings following the approach in Hinton et al. (2015). We refer the reader to Appendix C for detailed discussion on this topic.

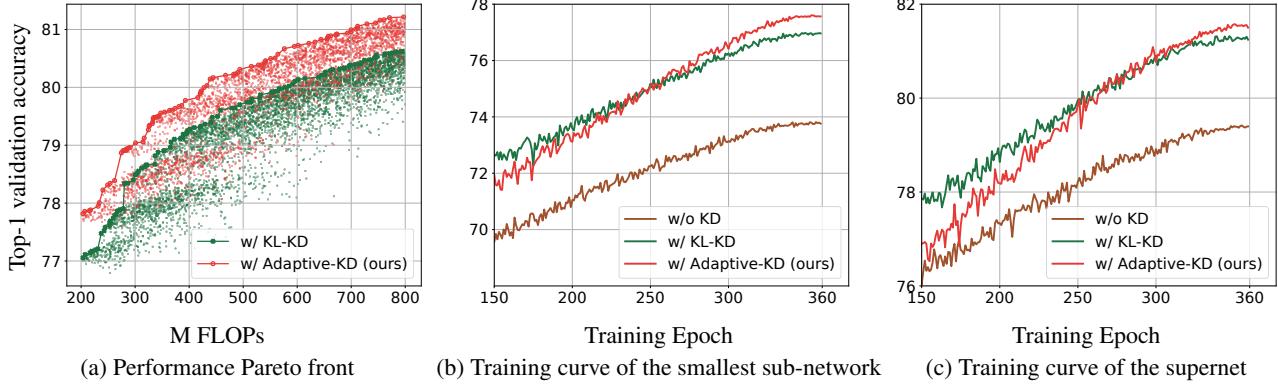


Figure 3. (a) Comparison of Pareto-set performance of the supernet trained via KL based KD and our adaptive KD, respectively. Each dot represents a sub-network evaluated during the evolutionary search step. (b-c) Training curves of the smallest sub-network and the largest sub-network (i.e., the supernet).

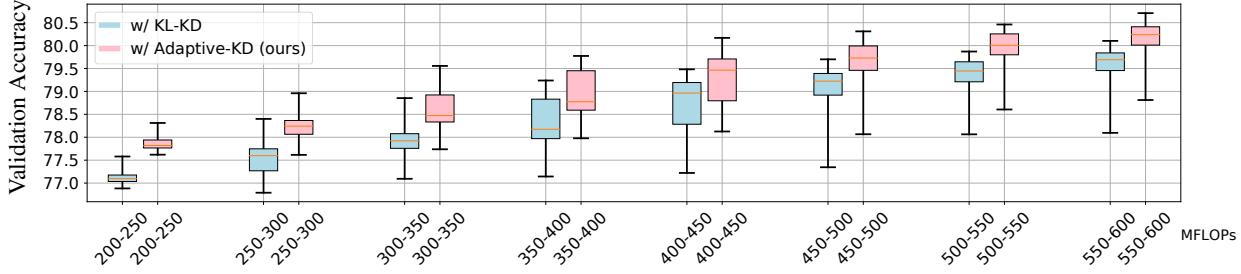


Figure 4. Top-1 accuracy on ImageNet from weight-sharing NAS with KL-based KD and adaptive-KD. Each box plot shows the performance of sampled sub-networks within each FLOPs regime. From bottom to top, each horizontal bar represents the minimum accuracy, the first quartile, the median, the third quartile and the maximum accuracy, respectively.

In particular, we test a number of temperatures - 0.5, 2 and 4. We summarize our results in Table 2. We find all these settings to systematically perform worse than the simple KD strategy without temperature scaling, i.e., $T = 1$. Additionally, the models trained via our method yield the best performance.

4.2. Weight-sharing NAS

We apply our *Adaptive-KD* to improve the training of the supernet for weight-sharing NAS (Cai et al., 2019a; Yu et al., 2020; Wang et al., 2020a). Please see Appendix A for a brief introduction on weight-sharing NAS. Note that one main procedure of weight-sharing NAS is to simultaneously train all sub-networks specified in the search space to convergence. Similar to training Slimmable neural networks, this is often achieved by enforcing all sub-networks to learn from the supernet with KL based KD, (e.g., Yu et al., 2020).

Training. Our training recipe follows Wang et al. (2020a) except we use uniform sampling for simplicity. We pursue minimum code modifications to ablate the effective-

ness of our KD strategy. We evaluate on the ImageNet dataset (Deng et al., 2009). All training details and the search space we used are discussed in Appendix B.

We use the update rule defined in (1) to train the supernet. Following Wang et al. (2020a) and Yu et al. (2020), at each iteration, we train the supernet with ground truth labels and simultaneously we train the smallest sub-network and two random sub-networks with KD. In this way, a total of 4 networks are trained at each iteration.

Evaluation We compare the accuracy vs. FLOPs Pareto formed by the supernet learned by different KD strategies. To estimate the performance Pareto, we proceed as follows: 1) we first randomly sample 512 sub-networks from the supernet and estimate their accuracy on the ImageNet validation set; 2) we apply crossover and random mutation on the best performing 128 sub-networks following Wang et al. (2020a). We fix both the crossover size and mutation size to be 128, yielding 256 new sub-networks. We then evaluate the performance of these sub-networks; 3) We repeat the second step 20 times. The total number of sub-networks thus evaluated is 5,376.

	A0 (203M)	A1(279M)	A2(317M)	A3(357M)	A4(444M)	A5 (491M)	A6 (709M)
w/o KD	73.8	75.4	75.6	76.0	76.8	77.1	77.9
w/ KL-KD	77.0	78.2	78.5	78.8	79.3	79.6	80.1
w/ Symmetric KL-KD	77.0	78.4	78.5	78.7	79.3	79.5	79.9
w/ KL-KD + Attentive Sampling [†]	77.3	78.4	78.8	79.1	79.8	80.1	80.7
w/ Adaptive-KD (ours - AlphaNet)	77.8	78.9	79.1	79.4	80.0	80.3	80.8

Table 3. Performance on the discovered networks in Wang et al. (2020a). Each (#M) denotes the FLOPs of the corresponding model. [†] uses additional attentive sampling (Wang et al., 2020a) for training the supernet. We denote our models as AlphaNet models. Here symmetric KL refers to a combination of the KL and the reverse KL divergence, i.e., $KL(q \parallel p) + KL(p \parallel q)$.

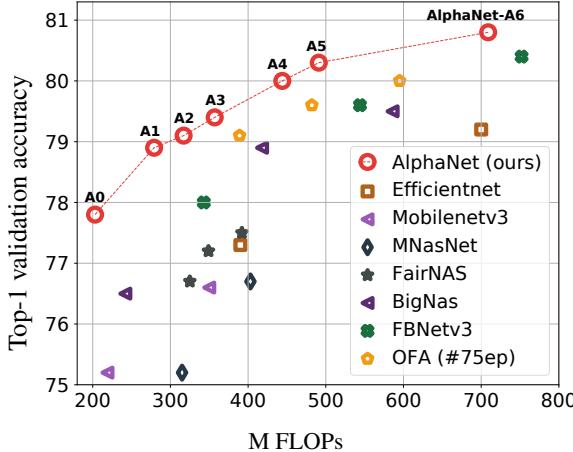


Figure 5. Comparison with prior art NAS approaches on ImageNet. #75ep denotes the models are further finetuned for 75 epochs with weights inherited from the corresponding supernet.

Results As we can see from Figure 3(a), *Adaptive-KD* achieves a significantly better Pareto frontier compared to the KL-based KD baseline (denoted as *w/ KL-KD*) and the simple training strategy without KD (denoted as *w/o KD*). Figures 3(b) and (c) plot the convergence curve of the smallest sub-network and the supernet, respectively. Our method adaptively optimizes a more difficult KD loss between the supernet and the sub-networks, yielding slightly slower convergence in the early stage of the training but better performance towards the end of the training.

In Figure 4, we group sub-networks according to their FLOPs and visualize five statistics for each group of sub-networks, including the minimum, the first quantile, the median, the third quantile and the maximum accuracy. Our method learns significantly better sub-networks in a quantitative way.

Improvement on SOTA As we use the same search space as in Wang et al. (2020a), we further evaluate the discovered AttentiveNAS models (from A0 to A6) with the supernet weights learned by our adaptive KD. We refer to our models as AlphaNet models.

Dataset	Eff-B0	Alp-A0	Eff-B1	Alp-A6
Oxford Flowers	97.2	97.7	97.8	98.7
Oxford-IIIT Pets	91.2	91.5	92.4	92.9
Food-101	87.6	88.3	89.0	89.6
Stanford Cars	91.0	91.5	92.2	92.6
FGVC Aircraft	88.1	88.5	88.7	89.1

Table 4. Comparison of transfer learning accuracy. ‘Eff’ and ‘Alp’ denotes EfficientNet and AlphaNet, respectively. All the networks are pretrained on ImageNet and then finetuned on transfer learning datasets. EfficientNet-B0 and B1 has a model size of 390 MFLOPs and 700 MFLOPs, respectively. AlphaNet-A0 and A6 use 203 MFLOPs and 709 MFLOPs, respectively.

As we can see from Table 3, our Adaptive-KD significantly improves on classic KL based KD, yielding an average of 0.7% improvements in the top-1 accuracy from A0 to A6. We also compare with symmetric KL based KD (namely, $KL(p \parallel q) + KL(q \parallel p)$). The corresponding results are no better than those by using standard KL based KD training. This is probably because the two different KL terms produce conflicted gradients during training, which may therefore lead to inferior final performance. Additionally, our AlphaNet outperform all corresponding Attentive-NAS models (Wang et al., 2020a), which requires building Pareto-aware sampling distributions with additional computational overhead.

We further compare our AlphaNet against prior art NAS baselines, including EfficientNet (Tan & Le, 2019), FB-NetV3 (Dai et al., 2020), BigNAS (Yu et al., 2020), OFA (Cai et al., 2019a), MobileNetV3 (Howard et al., 2019), FairNAS (Chu et al., 2019) and MNasNet (Tan et al., 2019), in Figure 5. Our method outperforms all the baselines evaluated, establishing new SOTA accuracy vs. FLOPs trade-offs on ImageNet. For example, our model achieves 77.8% top-1 accuracy with only 203M FLOPs. Under similar FLOPs constraint, the corresponding top-1 accuracy is 75.2% with 219M FLOPs for MobileNetV3, 76.5% top-1 accuracy with 242M FLOPs for BigNAS. Compared to OFA, our model achieves the same 80.0% top-1 accuracy with 35% fewer FLOPs (444M v.s. 595M) and the same 79.1% top-1 accuracy with 26% fewer FLOPs (317M v.s. 400M).

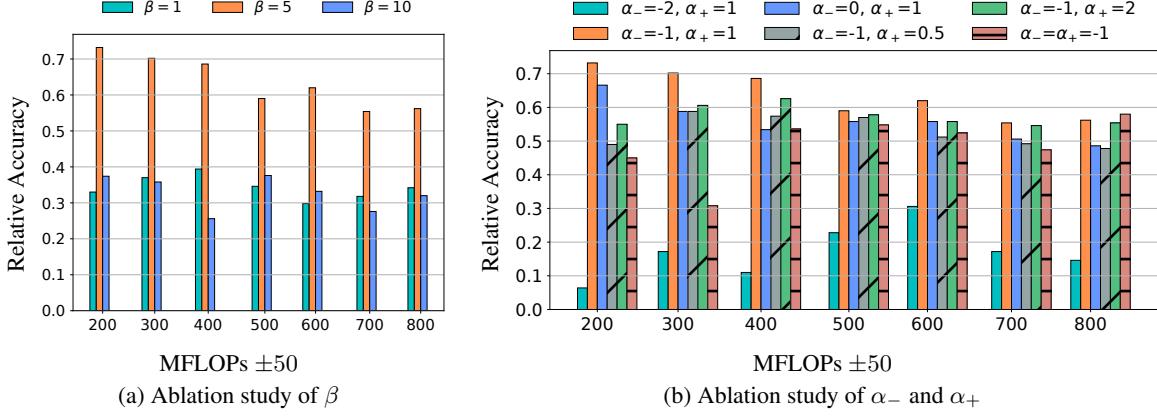


Figure 6. Relative accuracy compared to the results of KL based KD. Figure (a): we fix $\alpha_- = -1, \alpha_+ = 1$ and study the effect of our clipping factor β . Figure (b): we set $\beta = 5$ as default and study the impact of α_- and α_+ .

Model	w/o KD	w/ KL-KD (T=1)	T=2	T=4	Adaptive-KD (Ours)
MobileNetV3 0.75×	73.3	73.9	72.2	70.8	73.9
MobileNetV3 0.5×	69.6	69.8	65.4	63.6	70.0

Table 5. Comparison to KL based KD with fixed teacher models on ImageNet. Here T denotes the temperature used in classic KL based KD (see Appendix C). We use a MobileNetV3 1.0× as our teacher model, which yields 75.4% top-1 validation accuracy on ImageNet. All MobileNetV3 student models are trained for 360 epochs with cosine learning rate decay.

Teacher	MobileNetV1 1.0x		MobileNetV2 1.0x		RegNetY
Student	ShuffleNet 0.5x	ShuffleNet 1.0x	MobileNetV2 0.25x	MobileNetV2 0.5x	DeiT-tiny
w/ KL-KD (T=1)	60.3	69.3	54.4	65.3	74.6
Adaptive-KD (Ours)	61.1	69.5	55.0	65.7	75.2

Table 6. Additional KD results on ImageNet. Our MobileNet V1 and V2 teacher has a top-1 accuracy of 73.2% and 72.9%, respectively. All ShuffleNets (Ma et al., 2018) and MobileNetV2 models are trained for 120 epochs with standard random crop and resize data augmentation. For DeiT-tiny (Touvron et al., 2020), we exactly follow the settings of DeiT for training and use a RegNetY (Radosavovic et al., 2020) as the teacher model.

4.3. Transfer learning

Here we show that our AlphaNet models are not overfitted on ImageNet and the knowledge learned on ImageNet could be transferred to other datasets as well. Specifically, we take our AlphaNet-A0 and AlphaNet-A6 models pretrained on ImageNet and fine-tune them on a number of transfer learning benchmarks. We closely follow the training settings in EfficientNet (Tan & Le, 2019) and GPipe (Huang et al., 2018). We use SGD with momentum of 0.9, label smoothing of 0.1 and dropout of 0.5. All models are fine-tuned for 150 epochs with batch size of 64. Following Huang et al. (2018), we search the best learning rate and weight decay on a hold-out subset (20%) of the training data.

Transfer learning results We evaluated on five transfer learning benchmark datasets, including Oxford Flowers (Nilsback & Zisserman, 2008), Oxford Pets (Parkhi et al., 2012), Food-101 (Bossard et al., 2014), Stan-

ford Cars (Krause et al., 2013) and Aircraft (Maji et al., 2013). As we can see from Table 4, our AlphaNet-A0 and AlphaNet-A6 models lead to significant better transfer learning accuracy compared to those from EfficientNet-B0 and EfficientNet-B1 models.

4.4. Additional results

Robustness w.r.t. clipping factor β We follow the training and evaluation settings in section 4.2 and study the effect of β . In Figure 6 (a), we group sub-networks according to their FLOPs, and report the relative top-1 accuracy improvements of the maximum top-1 accuracy of each FLOPs group over the result from the KL based KD baseline. As shown in Figure 6(a), our algorithm is robust to the choice of β . Our algorithm works with a large range of β , from 1 to 10, yielding consistent improvements over the classic KL based KD baseline. And our default setting $\beta = 5$ achieves best performance on all FLOPs regimes evaluated.

Robustness w.r.t. α We ablate the impact of both α_- and α_+ under the same settings as in section 4.2. In this case, we fix $\beta = 5$. We present our findings in Figure 6(b).

Firstly, we test with $\alpha_- = -2, -1, 0$, with α_+ fixed as 1. With a more negative α (e.g., $\alpha_- = -2$), this defines a more difficult objective that brings optimization challenges. With a large α_- (e.g., $\alpha_- = 0$), the resulting KD loss is less discriminative regarding uncertainty over-estimation. Overall, $\alpha_- = -1$ achieves a good balance between optimization difficulty and over-estimation penalization, yielding the best performance. Secondly, we vary α_+ from 0.5 to 2, with α_- fixed as -1 . Similarly, we find that large α_+ (e.g., $\alpha_+ = 1$) yields the best performance. Lastly, we set both $\alpha_- = \alpha_+ = -1$. In this case, we still achieve better performance compared to the results of our KL based KD baseline, indicating the importance of penalizing over-estimation in training sub-networks. Also, our adaptive KD that regularizes on both over-estimation and under-estimation achieves better performance in general.

Improvement on single network training To further demonstrate the broader applicability of our method, we apply our Adaptive-KD to train a single neural network with a pretrained teacher model, as in conventional KD setup (See Appendix C).

Specifically, in Table 5, we use a MobileNetV3 $1.0\times$ (Howard et al., 2019) as our teacher model and train MobileNetV3 $0.5\times$ and $0.75\times$ as our student models. In Table 6, we provide additional comparisons for training ShuffleNets (Ma et al., 2018), MobileNetv2 models (Sandler et al., 2018) and more recent vision transformers (Touvron et al., 2020)¹ with a fixed temperature of 1.0.

We summarize the top-1 validation accuracy on ImageNet from the models trained with different KD strategies in both Table 5 and Table 6. The student models trained via our method yield the best accuracy.

5. Related work

Neural architecture search (NAS) NAS offers a powerful tool to automate the design of neural architectures for challenging machine learning tasks (e.g., Fang et al., 2020; Fu et al., 2021; Moons et al., 2020; Li et al., 2020; Peng et al., 2020). Early NAS solutions usually build upon black-box optimization, e.g. reinforcement learning (e.g., Zoph & Le, 2017), Bayesian optimisation (e.g., Kandasamy et al., 2018), evolutionary algorithms (e.g., Real et al., 2019). These methods find good networks but are extremely computationally expensive in practice.

More recent NAS approaches have adopted weight-sharing

(Pham et al., 2018) to improve search efficiency. Weight-sharing based approaches often frame NAS as a constrained optimization and solve with continuous relaxations (e.g., Liu et al., 2019; Cai et al., 2019b). However, these methods require to run NAS for each deployment consideration, e.g. a specific latency constraint for a particular mobile device, the total search cost grows linearly with the number of deployment considerations (Cai et al., 2019a).

To further alleviate the aforementioned limitations, one-shot supernet-based NAS (e.g., Cai et al., 2019a; Yu et al., 2020; Wang et al., 2020a) proposes to first jointly train all candidate sub-networks specified in the weight-sharing graph such that all sub-networks reach good performance at the end of training; then one can apply typical search algorithms, e.g., genetic search, to find a set of Pareto optimal networks for various deployment scenarios. Overall, one-shot supernet based methods provide a highly flexible and efficient NAS framework, yielding state-of-the-art empirical NAS performance on various challenging applications (e.g., Cai et al., 2019a; Wang et al., 2020b).

Knowledge Distillation Our knowledge distillation forces the student model to mimic the predictions of the teacher model. As shown in the literature, the features in intermediate layers of the teacher model can also be used as knowledge to supervise the training of the student model, notable examples include (Romero et al., 2014; Huang & Wang, 2017; Ahn et al., 2019; Jang et al., 2019; Passalis & Tefas, 2018; Li et al., 2019, e.g.). Furthermore, correlations between different training examples (e.g. similarity) learned by the teacher model also provide rich information, which could be distilled to the student model (Park et al., 2019; Yim et al., 2017). However, in our work, our KD involves training a large amount of sub-networks (students) with different architecture configurations, e.g., different network depth, channel width, etc. It is less clear on how to define a good matching in the latent feature space between the teacher supernet and student sub-networks in a consistent way. While our method offers a simple distillation mechanism that is easy to use in practice and in the meantime, leads to significant empirical improvements.

6. Conclusion

In this work, we propose a method to improve the training of supernets with α -divergence based knowledge distillation. By adaptively selecting an α -divergence to optimize, our method simultaneously penalizes *over-estimation* and *under-estimation* in KD. Applying our method for neural architecture search, the searched AlphaNet models establish the new state-of-the-art accuracy vs. FLOPs trade-offs on the ImageNet dataset.

¹<https://github.com/facebookresearch/deit>

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