- Escape direction does not matter for some fish prey
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Abstract

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Predator-prey interactions in fish are commonly studied with an interest in determining whether prey adopt an optimal strategy to evade predators. However, it is not clear under what circumstances an optimal strategy aids a prey's survival. Here we examine the theoretical consequences of deviation from optimal strategy for predators that approach at different speeds. With a focus on the minimum distance between predator and prey, we simulated these interactions with numerical and analytical mathematics and compared our predictions with measurements in zebrafish (Danio rerio). We found that differences in escape direction had only a small effect on the minimum distance when predators were more than an order of magnitude faster than the prev. Furthermore, differences in direction had no effect on performance for a broad range of escape angles when the prey were faster than the predator, which is the case for zebrafish. Therefore, the escape angle either has no optimum or has a minor effect on predator-prey interactions in many situations where the predator is either slower or much faster than the prey. Optimal strategy is therefore most meaningful when prey are approached by a predator of intermediate speed. It remains to be seen whether prey behave optimally in this domain or whether optimal responses serve to enhance survivorship.

1 Introduction

Biologists have long-appreciated the importance of predation in the ecology and evolution of prey species. This subject is extensive enough to fill the pages of books with the fascinating diversity of strategies that prey use to avoid encounters with predators (e.g. Ruxton et al., 2004) or to defend themselves when discovered (e.g. Emlen, 2014; Evans and Schmidt, 1990). In contrast, our understanding for how prey evade capture by locomotion is relatively rudimentary. Although biomechanical studies commonly speculate on the importance of locomotor performance to survival, relatively few have tested what aspects of locomotion are most meaningful in these interactions. Studies that have explored this subject (reviewed by Domenici and Blagburn, 2011) underscore the common-sense notion that the direction of an escape matters to a prey's survival. This idea is formalized by pursuit models that aim to determine the optimal direction of an escape response. The present study examined such a model (Weihs and Webb, 1984) to consider the strategic consequences of deviating from optimal strategy in piscivorous interactions. We compare the predictions of this model to experimental results in zebrafish (Danio rerio) (Stewart et al., 2014) and offer new interpretations of theory on prey strategy. Pursuit models are an area of game theory that offers a basis for examining locomotor 38

behavior in strategic terms. There is recent interest in revisiting these models (e.g. Howland, 1974; Weihs and Webb, 1984) with experimental studies that consider the behavior of both predators and prey. This includes work on running vertebrates (e.g. Wilson et al., 2013), birds (e.g. Hedenström and Rosén, 2001; Kullberg et al., 1998) and bats (e.g. Ghose et al., 2006) in flight, running insects (Domenici et al., 2008), flying insects (e.g. Combes et al.,

2012), and swimming zooplankton (e.g. Arnott et al., 1999; Heuch et al., 2007) and fishes

(e.g. Domenici et al., 2000). These efforts offer the potential to reveal how sensory and motor

systems govern the outcome of predator—prey interactions.

A piscivorous interaction offers some advantages as a model for examining the sensorymotor basis of predator evasion. In many cases, this interaction can be easily studied in a
laboratory. Under artificial conditions, predatory fishes attempt to feed on prey and prey
initiate a 'fast-start' escape response (Fig. 1). Both players operate with motion that is
largely two-dimensional and therefore relatively simple to measure and describe. Zebrafish
exhibit both predator evasion and predatory behavior in the lab (Stewart et al., 2013) and
this species offers a growing wealth of understanding in physiology and neuroscience (e.g.
McLean and Fetcho, 2011; Briggs, 2002) that may be leveraged for mechanistic insight on
predator—prey interactions. In addition, fish offer one of the few biological pursuit systems
that have been mathematically modeled (Weihs and Webb, 1984). This model offers specific
predictions of swimming trajectories that may be tested with kinematic measurements.

Deviation from optimal strategy has commonly been interpreted as a strategic adaptation.

The protean hypothesis suggests that prey which are unpredictable should have an advantage in predator evasion over predictable prey (Humphries and Driver, 1970). This idea may apply to the erratic motion of an individual or to predators that learn or adapt to the behavior of a population of prey that exhibits variable motion. The 'fast start' escape response of fish generates a turn and acceleration of the body in a particular direction and therefore would appear to correspond to the latter category (Weihs, 1973), although a sequence of fast starts could offer the opportunity for erratic motion. Nonetheless, a potential trade-off exists for the direction of a fast start between optimal displacement away from an advancing predator

and the benefit of being unpredictable.

Interpretations of prey motion have generally not considered the effect of deviating from optimal strategy. For example, it is not clear whether an escape that is 5° or 50° from the optimum predicted by Weihs and Webb (1984) has a major or negligible effect on evasion success. If evasive performance is insensitive to differences in escape direction, then no trade-off exists between evasiveness and predictability. In short, it is unclear when optimal strategy matters. The present study therefore revisited the mathematics of the Weihs and Webb (1984) model to examine how deviation from optimal strategy affects prey evasion. We expanded this model and performed numerical simulations for comparison with experimental results. In this effort, we arrived at new interpretations of theory on prey evasion. In particular, we identified conditions where the escape direction is predicted to have little or no effect on the evasiveness of prey.

79 2 Optimal prey strategy

The Homicidal Chauffeur is the colorful title for a pursuit game that has been applied to a variety of systems, including predator-prey interactions (Isaacs, 1965). Pursuit games consider the trajectories of its players and thereby address the effects of directional decision—making to the outcome of an interaction. Weihs and Webb (1984) adopted the Homicidal Chauffeur to model the responses of a prey fish that encounters a predator fish. Here we offer a brief review of this model as a means to explain the basis for our expansion of the theory and our interpretations of prey strategy, though a more complete derivation is presented in the original study (Weihs and Webb, 1984).

The payoff is a quantity used in game models to define the beneficial or detrimental consequences of playing with a particular strategy (Webb, 2007). For pursuit models, the payoff is often defined as the minimum distance between predator and prey. This quantity reflects the condition where the predator has the best opportunity to capture the prey. The optimal strategy for an evasive prey is therefore defined as the escape angle that yields the greatest minimum distance (Weihs and Webb, 1984).

Predicting the distance between predator and prey requires relatively few parameters under some simplifying assumptions. In the rapid events of a predatory strike, it is reasonable to approximate the predator's motion as a constant speed, U. If one neglects the acceleration period of the fast start, then the prey's motion may be approximated with a constant speed, V, at an escape angle α , defined with respect to the heading of the predator (Fig. 1A). Under these conditions, the distance between predator and prey, D, may be calculated over time:

$$D^{2} = ((X_{0} - Ut) + Vt \cos \alpha)^{2} + (Vt \sin \alpha)^{2}, \tag{1}$$

where X_0 is the starting position of the prey.

The minimum distance, the payoff in this game, may be calculated from the distance equation. The first step is to calculate the time, t_{\min} , at which the minimum distance occurs. This may be found from the root of the first derivative of Eqn. 1 with respect to time, which yields the following solution:

$$t_{\min} = \frac{X_0}{V} \frac{K - \cos \alpha}{1 - 2K \cos \alpha + K^2},\tag{2}$$

where K indicates the speed of the predator relative to the prey (K = U/V). Weihs and
Webb observed that this equation yields negative values of time where K < 1 and is therefore

only useful when the predator is faster than the prey (Weihs and Webb, 1984). The minimum distance was consequently determined for K > 1 by solving for distance (Eqn. 1) at t_{\min} :

$$\overline{D}_{\min}^2 = \frac{D_{\min}^2}{X_0^2} = \frac{\sin^2 \alpha}{K^2 - 2K\cos \alpha + 1},\tag{3}$$

where \overline{D}_{\min} is the minimum distance normalized by the starting position of the prey.

Finally, the optimal strategy for the prey may be determined by finding the escape angle that yields the greatest minimum distance. This occurs where the derivative of Eqn. 3 with respect to α is equal to zero, which is explicitly described by the following equation:

$$0 = \frac{\partial \overline{D}_{\min}^2}{\partial \alpha} = \frac{2 \sin \alpha \cos \alpha (K^2 - 2K \cos \alpha + 1) - 2K \sin^3 \alpha}{(K^2 - 2K \cos \alpha + 1)^2}.$$
 (4)

Among the solutions that satisfy this equation, Weihs and Webb proposed that the following indicates the optimal strategy when the predator is faster than the prey (K > 1):

$$\alpha_{\text{opt}} = \pm \arccos K^{-1}. \tag{5}$$

We added the \pm symbol to this expression to indicate that prey are equally effective if escaping at an optimal angle toward the left $(\alpha > 0)$, or right $(\alpha < 0)$ of the predator's heading. For relatively fast prey $(K \le 1)$, Weihs and Webb suggested that the optimal solution consists of swimming directly away from the predator $(\alpha = 0)$ (Weihs and Webb, 1984). Therefore, for any predator speed, this model offers predictions for how a prey can direct its escape to maximize its chances for survival by creating the greatest distance from a predator.

3 When optimal strategy matters

An optimum adopts a different meaning if it corresponds to a shallow peak in performance or 124 defines a local peak that is much smaller than the global maximum. We considered whether 125 these conditions exist in evasion strategy by calculating how the payoff in this pursuit model, 126 the minimum distance (Weihs and Webb, 1984), varies with escape angle and the relative 127 speed of the predator. This was considered by formulating a performance landscape of prey 128 strategy. As an alternative to analytical mathematics (Eqn. 3), we first formulated this 129 landscape with a numerical approach that is simple enough to execute in a spreadsheet, 130 but which we implemented in Matlab (MathWorks, Natick, MA, USA). This was done by 131 defining a series of time values at an equal interval, which was used to calculate the positions 132 of the predator $(X_{\text{pred}} = Ut, Y_{\text{pred}} = 0)$ and prey $(X_{\text{prey}} = Vt \cos \alpha, Y_{\text{prey}} = Vt \sin \alpha)$. The 133 minimum value of the distance between them was determined in this way for variable escape 134 angle and predator speed, over a range of K and α values (Fig. 2B). This yielded results that were coincident with the analytical equation for \overline{D}_{\min} formulated by Weihs and Webb (1984) for relatively fast predators (K > 1, Eqn. 3). However, the advantage of the numerical 137 calculations was that they allowed us to examine variation in the minimum distance for 138 slower predators (i.e. K < 1) as well. The resulting performance landscape (Fig. 2B) 139 illustrates how the minimum distance varies over a broad range of values in the relative 140 speed of the predator and escape angle of the prev. 141

Our results suggest that the fast start is unlikely to be effective at any escape angle when a prey is approached by a very fast predator. For example, if a predator is an order of magnitude faster than its prey (i.e. K = 10), then the prey can do no better than

displace its body by 10% of its initial distance from the predator (Fig. 2B). In addition,
differences in escape angle have little effect on the minimum distance. An escape that is
24.5° larger or smaller than the optimum yields a minimum distance that is less than the
value at the optimum by 0.1 (i.e. 1% of the starting position of the prey). These metrics
become increasingly unfavorable for the prey when approached by an even faster predator
(Fig. 2B). At these speeds, inaccuracy in the feeding strike is likely a more decisive factor
to prey survival than anything the prey may do in response.

A different picture emerges when one considers prey that move more quickly than their predators (i.e. K < 1). This condition occurs when predators brake or glide slowly on their approach toward a prey (Higham, 2007; Higham et al., 2005) while the prey initiates a rapid escape. For a variety of escape angles, the fast start of these prey cause the predator to reach no closer than the starting distance (i.e. $\overline{D}_{\min} = 1$, Fig. 2B). In order to define the bounds of this domain, it is useful to consider the first derivative of the distance function with respect to time:

$$\frac{\partial D^2}{\partial t} = 2(t(U^2 + V^2) - UX_0 + V(X_0 - 2tU)\cos\alpha). \tag{6}$$

A prey achieves an optimal escape $(\overline{D}_{\min} = 1)$ when the distance function only increases as a function of time (i.e. $\frac{\partial D^2}{\partial t} \geq 0$). This holds true for $\alpha = 0$, which Weihs and Webb proposed as the optimal direction (Weihs and Webb, 1984). However, it also holds true that distance increases for another solution to Eqn. 4 ($\alpha = \pm \arccos K$) and all values in between. Therefore, the following defines the domain of optimal directions when the prey is faster than the predator (K < 1):

$$\overline{D}_{\min} = 1 \text{ if } -\arccos(K) \le \alpha \le \arccos(K).$$
 (7)

This analysis suggests that if the escape response of a prey is capable of exceeding the approach speed of the predator, then a wide range of angles yield equally successful escapes for the prey and thereby define a performance plateau.

The domain where optimal the optimal strategy matters the most resides between where
the prey and predator are equivalent in speed and where the predator is an order of magnitude faster (1 < K < 10). In this domain, prey are capable of attaining appreciable
minimum distance values and there is a penalty for deviating from the optimal angle (Fig.
2B). Therefore, a prey fish has an incentive to conform to the optimal prediction when
encountering a slightly faster predator.

⁷⁴ 4 Comparing models with measurements

We were interested in examining whether optimal strategy matters under experimental con-175 ditions. This was addressed with recent measurements on larval zebrafish, which are preyed 176 upon by adults of the same species (Stewart et al., 2013). This work included experiments 177 that used a robot to simulate the approach of a predator toward prey in the dark, with 178 recordings of the position at which the prey responded with a fast start and the direction of 179 that response (Stewart et al., 2014). This evasive action was stimulated by the lateral line 180 system of the prey, which detected the water flow generated by the approaching predator. 181 As detailed above, the predictions of the model depend on the speed of the predator 182 relative to the prey. The approach speed of the robot, and consequently K, was varied to span the range of values observed for a live predator (Stewart et al., 2013). Our calculations 184 of K used a prey speed $(U = 22 \text{ cm s}^{-1})$ from the literature that approximates the maximum value attained during a fast start for larvae of this species (Budick and O'Malley, 2000; Müller and van Leeuwen, 2004). As a consequence of the relatively slow approach made by these suction-feeding predators, the prey had the potential to move faster at all approach speeds, which yielded K-values that were uniformly less than unity (Fig. 3A).

One discrepancy between the model and our experiments was that the majority of prey
fish did not exhibit an initial position that was aligned with the heading of the predator
robot. This condition has biological relevance because it corresponds to a situation where
a predator fails to approach with a prey with perfect accuracy. We therefore modified the
Weihs and Webb model by adding a lateral component to the initial position of the prey in
our distance function. However, we followed the same procedure (as in Eqns. 2–3) to arrive
at a minimum distance function (see Supplemental Materials for details). We found that
our solutions were was simplified by the use of polar coordinates. For example, we found the
following equation for the minimum distance:

$$\overline{D}_{\min}^{2} = \frac{D_{\min}^{2}}{R_{0}^{2}} = \frac{(\sin(\alpha - \theta_{0}) + K \sin \theta_{0})^{2}}{K^{2} - 2K \cos \alpha + 1}$$
(8)

where R_0 and θ_0 are the initial radial and angular positions of the prey relative to the mouth of the predator (Fig. 2A). Numerical solutions to this equation show a broad range of angular positions and escape angles that define a performance plateau where $D_{\min} = 1$ (Fig. 3B). We found the margins of this plateau using a similar procedure as outlined above. Specifically, we solved for the conditions where the derivative of the minimum distance with respect to

$$0 = \frac{\partial \overline{D}_{\min}^2}{\partial \alpha} = \frac{2(K\cos\alpha - 1)(K\cos\theta_0 - \cos(\alpha - \theta_0))(K\sin\theta_0 + \sin(\alpha - \theta_0))}{(K^2 - 2K\cos\alpha + 1)^2},$$
 (9)

We found the solutions that satisfy this equation by setting the terms in the numerator

equal to zero. The solution for K > 1 was similar to Eqn. 5, though the angular position determines the sign of the optimal angle:

$$\alpha_{\text{opt}} = \frac{\theta_0}{|\theta_0|} \arccos(K^{-1}).$$
 (10)

This solution indicates that the same optimal direction exists when the predator is faster than the prey, irrespective of the starting position of the prey. As detailed above, we found that the escape angle is equally effective (i.e. $\overline{D}_{\min} = 1$) when the prey is aligned with the predator for a broad range of values (Eqn. 7). This result holds true when prey are positioned lateral to the predator, but this performance plateau depends on the initial angular position of the prey. We found that the following equation defines the the bounds of this plateau among the solutions that satisfy Eqn. 8 for K < 1:

$$\overline{D}_{\min} = 1 \text{ if } 0 \le \alpha \le [|\theta_0| + \arccos(K\cos|\theta_0|)], \tag{11}$$

This demonstrates that the performance plateau reduces in area with increasing predator speed (Fig. 3B). Therefore, fewer combinations of starting positions and escape angles yield equivalent escape performance for faster predators.

Using this formulation of the pursuit model, we evaluated how the measured responses of prey compared to the model predictions (Fig. 3C). This comparison revealed that the vast majority of larvae responded upon the performance plateau and therefore at a position and escape direction that was predicted to yield maximal performance ($\overline{D}_{\min} = 1$). This was true even at the fastest predator approach speed (K = 0.90), where a larger number of individuals responded outside of the plateau. According to the model's predictions, the large variation in observed escape direction incurs no penalty in the evasive performance of most larvae.

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$_{227}$ 6 Predator strategy

Although the present pursuit models were formulated with a focus on prey fish, they provide the opportunity to consider the strategy of fish predators. It first merits pointing out that the 229 payout considered presently is normalized by the initial response distance of the prey (Figs. 230 2-3). Therefore, the absolute distance traversed by a prey is predicted to be proportional 231 to the initial response distance. The predator may act to minimize this distance with a 232 slower approach, which will serve to reduce the stimulus intensity for the visual (CITE) and 233 lateral line (CITE) systems. This is one benefit to the braking behavior that suction-feeding 234 predators exhibit before a strike (Higham, 2007; Higham et al., 2005). Another potential 235 benefit to a slow approach is greater accuracy in the timing and direction of a suction-feeding strike, which is restricted to a brief duration over a relatively small region around a predator's mouth.

Our results indicate some of the strategic advantages for predators to approach prey relatively quickly. Moving faster than the escaping prey can greatly diminish the escape angles that are beneficial for evasion (Fig. 2B). As we discussed above ("Optimal prey strategy"), the fast start can become ineffective at offering any benefit to predator evasion when the predator is substantially faster than the prey and headed directly at the prey. Such a high-speed approach may present a challenge for a predator to coordinate the timing of the strike (Higham, 2007; Higham et al., 2005), but we have also found that it offers some advantages to the evasiveness of the prey.

We conducted a series of simulations that examine the effect of an inaccurate strike by
a fast predator. As in the simulations we used to compare with experimental results, we
calculated the minimum distance for a range of values in escape angle and initial angular
position. If we assume that predator fish lack the interception targeting used by bats Ghose
et al. (2006) and birds Kane and Zamani (2014), we may interpret deviation from a zero
angular position as an indication of strike inaccuracy by the predator.

The model's assumptions could be violated by the system. For example, a prey fish cannot move in an optimal direction that maximizes its distance from a predator if it cannot detect the predator's speed (Weihs and Webb, 1984).

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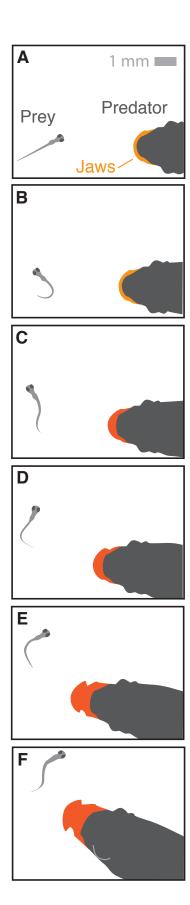
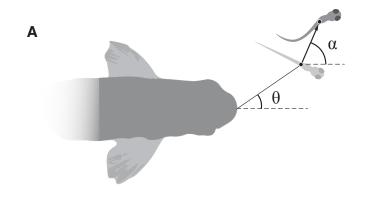


Figure 1: A predator-prey interaction in zebrafish. (A)



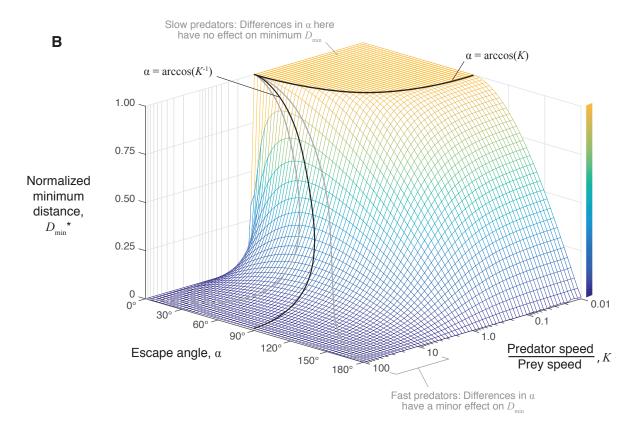


Figure 2: The Homicidal Chauffeur model, applied to prey strategy. (A) Simulations predict the direction of a prey's fast start relative to initial position and velocity of a predator. (B) Numerical simulations were run at varying escape angle and predator approach speed to examine variation in the minimum distance. At K > 1, the optimal angle.

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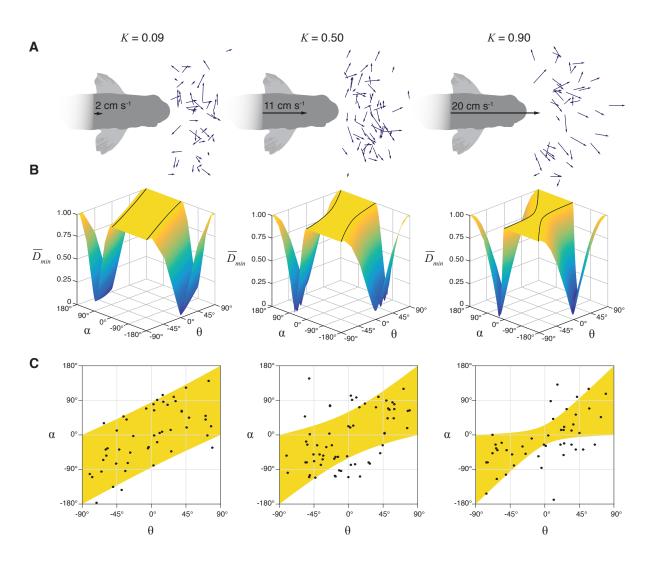


Figure 3: Model predictions and measurements of the fast start. (A)

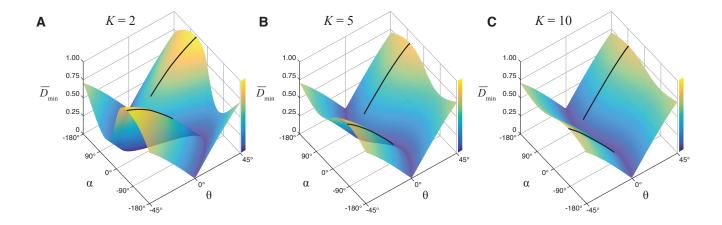


Figure 4: Title. (A)