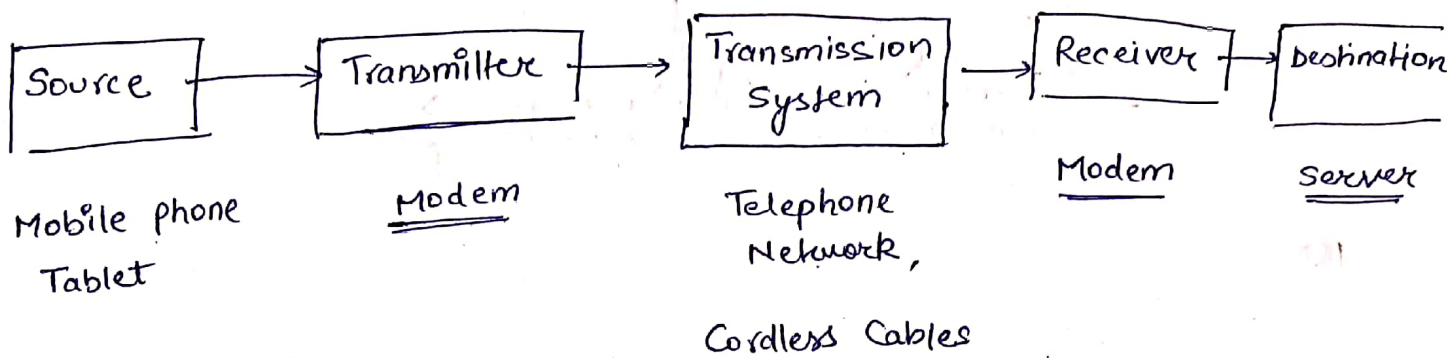


①



③

$$f(t) = (100 \cos t)^2$$

$$\Rightarrow 100 \cos^2 t = 100 \left(\frac{1 + \cos 2t}{2} \right) \quad \{ \text{Trigo identity} \}$$

$$f(t) = 50 (1 + \cos 2t)$$

From $f(t)$ we can see $2\pi f = 2$

$$f = \frac{1}{\pi}$$

$$\boxed{T = \frac{1}{f} = \pi} \quad \text{Ans.}$$

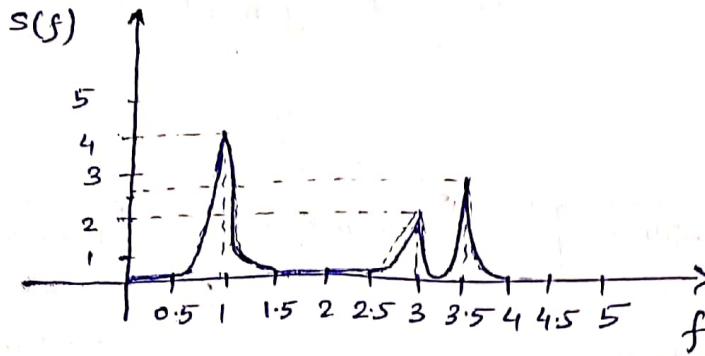
② The layered design has following advantages:

- (a) It improves flexibility, maintainability and scalability
- (b) It provides resilience and stability
- (c) It provides extensibility and abstraction

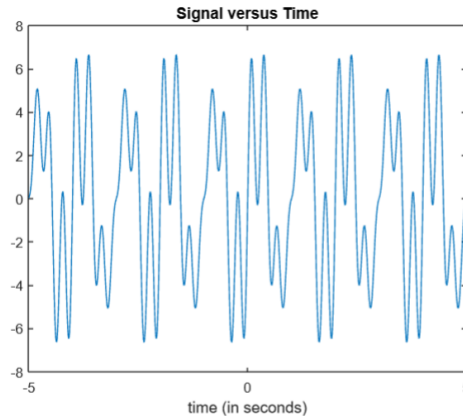
The following are some of the disadvantages of layered architecture:

- (a) Functional duplication
- (b) The difficulty of detecting poor interactions b/w layers
- (c) Data overhead and processing

④ $S(t) = 4 \sin(2\pi t) + 2 \sin(6\pi t) + \left(\frac{8}{\pi}\right) \sin(7\pi t)$



for



Frequencies in $s(t) \Rightarrow 1, 3, 3.5$

Absolute Bandwidth = $\max(f) - \min(f)$
of spectrum

$$f_{\max} = 3.5 \text{ Hz} ; f_{\min} = 1 \text{ Hz}$$

$$\text{Absolute Bandwidth} = 2.5 \text{ Hz}$$

⊛ Effective bandwidth takes into account the frequencies which account for the max. energy of the signal.

↳ So effective bandwidth = $3.5 - 1$
= 2.5 Hz

⊛ We see absolute bandwidth = effective bandwidth of signal which is expected since for a signal with finite absolute bandwidth effective and absolute bandwidths are same.

⑤ $SNR = 3dB = 10^{0.3} = 1.995$

Bandwidth $= B = 300Hz$

Applying Shannon's assumption equation :

$$\begin{aligned} C &= B \log_2 (1 + SNR) \\ &= 300 \times \log_2 (1 + 1.995) \\ &= 300 \times 1.583 \\ &= 474.9 \text{ bps} \end{aligned}$$

channel capacity $= 474.9 \text{ bits per sec.}$

⑥ signal encoding with 4 bits word ; Given $C = 9600 \text{ bps}$
 $M = 2^4 = 16$

Applying Nyquist's assumption eqⁿ :

$$C = 2B \log_2 M$$

$$9600 = 2B \log_2 16$$

$$B = \frac{9600}{2 \cdot 4} = 1200 \text{ Hz} \rightarrow \text{Min. required bandwidth}$$

⑦ Thermal ~~noise~~ noise is given as

$$N = kTB$$

$T = 50^\circ C = 323 \text{ K}$

$B = 10 \text{ kHz}$

$$\begin{aligned} N &= ~~1.38 \times 10^{-23}~~ 1.381 \times 10^{-23} \times 323 \times 10 \times 10^3 \\ &= 446.06 \times 10^{-19} \end{aligned}$$

$$\Rightarrow 4.46 \times 10^{-17} \text{ W}$$



Thermal Noise level

$$\begin{aligned} N_{dB} &= 10 \log_{10}(N) \\ &= -163.51 \text{ dBW} \end{aligned}$$

Ans

⑨ Voltage Gain = 30 dB

$$30 = 10 \log \left(\frac{V_2}{V_1} \right)^2$$

$$\boxed{\frac{V_2}{V_1} = 10^{1.5} = 31.623}$$

⑧ $s(t) = \sin(2\pi f_1 t) + \frac{1}{3} \sin(2\pi(3f_1)t) + \frac{1}{5} \sin(2\pi(5f_1)t) + \frac{1}{7} \sin(2\pi(7f_1)t)$

$$T = 1 \text{ ms} \Rightarrow f_1 = \frac{1}{T} = 1 \text{ kHz} = f_1$$

→ Low pass filter of 8 kHz
implies that frequencies greater than ~~8 kHz~~ 8 kHz will not pass

→ Frequencies in $s(t) \Rightarrow 1 \text{ kHz}, 3 \text{ kHz}, 5 \text{ kHz}, 7 \text{ kHz}$

↓
highest frequency = 7 kHz < 8 kHz

and hence all frequencies
pass through filter

⑨ ① Avg. power = $\frac{A^2}{2}$

$$\text{Avg. power of output waveform} \Rightarrow \frac{1}{2} \left(1^2 + \frac{1}{3^2} + \frac{1}{5^2} + \frac{1}{7^2} \right)$$

$$= 0.586 \text{ W}$$

② $B = 8 \text{ kHz}$; Output Noise Power : $N = B N_0$

$$N_0 = 0.1 \mu\text{W/Hz}$$

$$N = 0.8 \text{ mW}$$

$$\text{Output SNR} = \frac{\text{Output signal power}}{\text{Output Noise Power}}$$

$$= \frac{0.586}{0.8 \times 10^{-3}} = \underline{\underline{732.5}}$$

$$\text{SNR}_{\text{dB}} = 10 \log(\text{SNR}) = 10 \log(732.5) = \underline{\underline{28.65 \text{ dB}}}$$