

Wide and Deep Convolutional Neural Networks for Electricity-Theft Detection to Secure Smart Grids

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Abstract—Electricity theft is harmful to power grids. Integrating information flows with energy flows, smart grids can help to solve the problem of electricity theft owning to the availability of massive data generated from smart grids. The data analysis on the data of smart grids is helpful in detecting electricity theft because of the abnormal electricity consumption pattern of energy thieves. However, the existing methods have poor detection accuracy of electricity theft since most of them were conducted on onedimensional (1-D) electricity consumption data and failed to capture the periodicity of electricity consumption. In this paper, we originally propose a novel electricity-theft detection method based on wide and deep convolutional neural networks (CNN) model to address the above concerns. In particular, wide and deep CNN model consists of two components: the wide component and the deep CNN component. The deep CNN component can accurately identify the nonperiodicity of electricity theft and the periodicity of normal electricity usage based on 2-D electricity consumption data. Meanwhile, the wide component can capture the global features of 1-D electricity consumption data. As a result, wide and deep CNN model can achieve the excellent performance in electricity-theft detection. Extensive experiments based on realistic dataset show that wide and deep CNN model outperforms other existing methods.

Index Terms—Convolutional neural networks (CNNs), deep learning, electricity-theft detection, machine learning, smart grids.

I. INTRODUCTION

E LECTRICITY has become a necessity in our life. Losses often occur during electricity generation, transmission,

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and distribution. The electricity losses can be generally categorized into technical losses and Nontechnical losses (NTLs) [1]. One of the primary NTLs is *electricity theft*. This misbehavior usually includes bypassing the electricity meter, tampering the meter reading, or hacking the meter [2]. Electricity theft can result in the surging electricity, the heavy load of electrical systems, the huge revenue loss of power company, and the dangers to public safety (such as fires and electric shocks). For example, it is reported in [3] that the losses due to electricity theft approximate 100 million Canadian dollars every year; this lost electricity can even supply 77 000 homes for a year.

There is a substantial body of studies on detecting electricity theft. Conventional electricity-theft detection methods include: humanly checking problematic meter installation or misconfiguration, comparing the abnormal meter readings with the normal ones, examining the bypassed power transmission line, etc. However, these methods are extremely time-consuming, expensive, and inefficient.

The appearance of *smart grids* brings opportunities in solving electricity theft. Smart grids essentially consist of traditional power grids, communications networks connecting intelligent devices (such as smart meters and sensors) in grids, and computing facilities to sense and control grids [4]. Both energy flows and information flows in smart grids connect users and utility companies together. In this manner, smart meters or sensors can collect data, such as electricity usage, status information of grids, electricity price, and financial information [5]. The data of smart grids is helpful for us to design demand response management schemes [6], forecast the electricity price [7], and schedule the electricity in more profitable way [8], [9]. In addition, some recent works, such as [2], [10]–[13], show that data analysis on smart grids can help to detect electricity theft. However, most of these approaches have the following limitations:

- a) many of them require specific devices [1];
- b) most of them are based on artificial feature extraction according to domain knowledge (requiring manual interventions):
- many methods [such as support vector machine (SVM) and linear regression] have low electricity-theft detection accuracy.

Therefore, in this paper, we aim to design a novel electricitytheft detection method to address the above concerns. In particular, we originally propose a wide and deep convolutional

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neural networks (CNN) model to learn the electricity consumption data and identify the electricity thieves. Our wide and deep CNN model consists of a wide component with a fully connected layer of neural networks and a deep CNN component with multiple convolutional layers, a pooling layer and a fully connected layer. Essentially, the wide component can learn the global knowledge while the deep CNN component can capture the periodicity of electricity consumption data. This model integrates the benefits of the wide component and the deep CNN component consequently resulting in good performance in electricity-theft detection.

The primary research contributions of this paper can be summarized as follows.

- 1) We originally propose a wide and deep CNN model to analyze electricity theft in smart grids. To the best of our knowledge, it is the first study to propose the wide and deep CNN model and apply it to analyze electricity theft in smart grids.
- 2) Our model has numerous merits:
 - a) *memorization* of the global knowledge brought by the wide component;
 - b) *generalization* of the new knowledge brought by the deep CNN model;
 - c) accuracy in electricity-theft detection.
- 3) We have conducted extensive experiments on massive realistic electricity consumption dataset. Experimental results show that our wide and deep CNN model outperforms than other existing approaches.

The remainder of the paper is organized as follows. Section II presents an overview on related literature. We present the problem analysis in Section III. Section IV presents the wide and deep CNN model. We then give the experimental results in Section V. Finally, we conclude the paper in Section VI.

II. RELATED WORK

In this section, we first present a survey on electricity-theft detection in Section II-A and an overview on anomaly detection in Section II-B.

A. Electricity-Theft Detection

We roughly categorize the studies on electricity-theft detection into two types: hardware-based solutions and data-driven solutions. In particular, hardware-based solutions concentrate on designing specific metering devices and infrastructures so that electricity theft can be easily detected. Typical electricity-theft detection equipments include smart meters with antitempering sensors, radio-frequency identification tags and sensors [14]–[16]. The main limitations of hardware-based solutions include

- 1) the cost of deploying smart metering devices;
- 2) the vulnerability of hardware devices (e.g., failure due to rush weather condition);
- 3) the difficulty in maintaining devices (e.g., replacing batteries of devices).

Data-driven electricity-theft detection has drawn considerable attentions recently. For example, the work in [2] is based on the

data fusion from sensors and advanced metering infrastructure. Many recent studies [17]–[19] are based on SVM. The main idea of SVM methods is to classify the normal users and the electricity thieves. In addition to SVM, artificial neural networks can also be used to electricity-theft detection [10], [11]. However, most of these studies are less accurate in electricity-theft detection and require artificial feature extraction according to domain knowledge.

B. Anomaly Detection in Smart Grids

Anomaly detection in smart grids represents a substantial body of works related to data-driven electricity-theft detection. In particular, anomaly detection (a.k.a. outlier detection) is the procedure of detecting abnormal patterns that do not conform the expected behavior [20]. Anomaly detection has been widely used in many research areas, such as intrusion detection [21], fraud detection [22], and industrial control systems [23].

Recently, anomaly detection has received extensive attention from the smart grid community since it can help in improving operational safety, enhancing the control reliability, and detecting faults in smart metering infrastructure [24]–[26]. The typical approaches used in anomaly detection in smart grids mainly include SVM, clustering, and classification [27]. Besides, decision tree and rough sets can also be used in fraud detection in power systems [28]. Moreover, [29] presents a rule-based model to detect the NTLs.

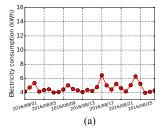
However, most of the related studies in either electricity-theft detection or anomaly detection are based on the analysis on one-dimensional (1-D) electricity consumption data and fail to capture the periodicity of electricity consumption. Therefore, it is the purpose of this study to propose a novel analytical model to overcome the limitations of the above existing works.

III. PROBLEM ANALYSIS

Electricity theft is a criminal behavior of stealing electrical power from power grids. This malicious behavior can be done by bypassing the electricity meter, tampering the meter reading, or hacking the meter. Since electricity theft can result in the abnormal patterns of electricity consumption, the data-driven electricity-theft detection approaches have received extensive attention recently due to the availability of smart-meter readings and electricity consumption data from smart grids. We next illustrate the abnormality of electricity consumption data of energy thieves, which can be potentially captured by machine-learning tools.

We conduct a preliminary analysis on electricity consumption data. This dataset released by State Grid Corporation of China (SGCC)¹ contains the electricity consumption data of 42 372 electricity customers within 1035 days (details about the dataset will be given in Section V-A). In particular, Fig. 1(a) shows an example of electricity consumption of normal usage by a customer in a month (i.e., August 2016). We observe that there is a fluctuation on the electricity consumption data day by day. It is hard to capture the key characteristics of electricity thieves and

¹State Grid Corporation of China http://www.sgcc.com.cn/



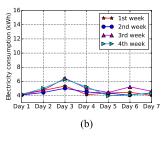
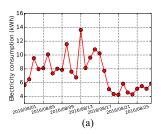


Fig. 1. Example of electricity consumption of normal usage. (a) Electricity consumption (kWh) by date. (b) Electricity consumption (kWh) by week.



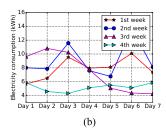
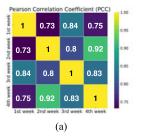


Fig. 2. Example of electricity consumption of electricity theft. (a) Electricity consumption (kWh) by date. (b) Electricity consumption (kWh) by week.

normal customers from this 1-D data. However, we can observe that there is a periodicity on the electricity consumption of this customer if we plot the data in 2-D manner by week as shown in Fig. 1(b). We can find from Fig. 1(b) that the electricity consumption reaches the peak on day 3 every week, whereas it often reaches the bottom on day 5 every week (the exception is on the 2nd week, when there is the lowest consumption on day 6). In fact, we can have similar findings for the whole dataset (i.e., electricity consumption data with 1035 days). Without too many repetitions, we only show an excerpt data from the whole dataset. We can observe that there is a *periodicity* for most of the normal customers if we align the electricity consumption data of all the 35 months together.

In contrast, Fig. 2 shows an example of electricity consumption of an electricity theft in a month. Similar to Fig. 1, we also plot the electricity consumption by date [as shown in Fig. 2(a)] and the electricity consumption by week [as shown in Fig. 2(b)]. As shown in Fig. 2, we observe that the electricity consumption in the first two weeks (i.e., the 1st week and the 2nd week) fluctuates periodically. For example, the electricity consumption reaches the peak on day 3 and on day 6 every week. However, there is a distinct loss of the electricity consumption from the third week and the electricity consumption has remained at the low level after that.

To better analyze the periodicity of normal customers and nonperiodicity of energy thieves. We conduct a correlation analysis on the electricity consumption data. Fig. 3 shows Pearson correlation coefficient (PCC) of electricity consumption of both normal customers and energy thieves by week. In particular, Fig. 3(a) shows PCC values of normal customers while Fig. 3(b) shows those of energy thieves. We can find from Fig. 3(a) that there is a strong correlation of electricity consumption data of normal customers, i.e., most of PCC values are greater than 0.8



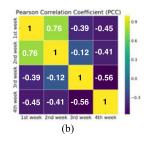
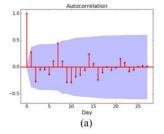


Fig. 3. PCC of electricity consumption by week.



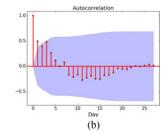


Fig. 4. ACF of electricity consumption by week.

(a larger PCC value close to 1 means the stronger correlation [30]). However, we cannot observe the correlation of electricity consumption data of energy thieves as shown in Fig. 3(b) (i.e., most of PCC values are less than 0.7 and many of them are even negative). We further plot autocorrelation function (ACF) of the electricity consumption data of both normal customers and energy thieves by day in Fig. 4. Fig. 4 shows ACF of the electricity consumption data of normal customers by day in contrast to that of energy thieves. It is observed from Fig. 4 that the electricity consumption patterns of normal customers have obvious periodicity, i.e., the similar pattern longs for about 7 days [see Fig. 4(a)] while there is no obvious periodicity of electricity consumption of energy thieves [see Fig. 4(b)].

After statistically analyzing the electricity consumption data of both normal customers and energy thieves, we can find that the electricity consumption data of energy thieves are usually less periodic or nonperiodic, compared with that of normal customers. We believe that this observation can also be confirmed by other electricity consumption datasets from different countries and regions as implied by recent work [31]. This observation has motivated us to investigate the periodicity of the electricity consumption and identify the abnormal electricity usage.

However, it is challenging to analyze the periodicity of the electricity consumption data due to the following reasons:

- 1) the electricity consumption data are often erroneous and noisy;
- it is difficult to analyze the periodicity of the electricity consumption data since it is 1-D time series data with massive size;
- 3) many conventional data analysis approaches such as SVM and artificial neural network cannot be directly applied to the electricity consumption data due to the computation complexity and the limited generalization capability [7], [31] –[33].

In order to address the above challenges, we propose wide and deep CNNs framework, which will be described in detail in Section IV.

IV. OUR APPROACH

Our analytical process mainly includes two stages: 1) data preprocess (to be presented in Section IV-A) and 2) data analysis based on the wide and deep CNN framework (to be presented in Section IV-B).

A. Data Preprocess

Electricity consumption data often contains missing or erroneous values; this is mainly caused by various reasons such as the failure of smart meters, the unreliable transmission of measurement data, the unscheduled system maintenance and storage issues [34]. In this paper, we exploit the interpolation method to recover the missing values according to the following equation:

$$f(x_i) = \begin{cases} \frac{x_{i-1} + x_{i+1}}{2} & x_i \in \mathsf{NaN}, x_{i-1}, x_{i+1} \notin \mathsf{NaN} \\ 0 & x_i \in \mathsf{NaN}, x_{i-1} \ or \ x_{i+1} \in \mathsf{NaN} \\ x_i & x_i \notin \mathsf{NaN}, \end{cases} \tag{1}$$

where x_i stands for the value in the electricity consumption data over a period (e.g., a day). If x_i is a null or a non-numeric character, we represent it as NaN (NaN is a set).

Moreover, we have also found that there are erroneous values (i.e., outliers) in the electricity consumption data. In particular, we restore the value by the following equation according to "Three-sigma rule of thumb" [35]

$$f(x_i) = \begin{cases} \operatorname{avg}(\mathbf{x}) + 2 \cdot \operatorname{std}(\mathbf{x}) & \text{if } x_i > \operatorname{avg}(\mathbf{x}) + 2 \cdot \operatorname{std}(\mathbf{x}), \\ x_i & \text{otherwise,} \end{cases}$$

where \mathbf{x} is a vector that is composed of x_i day by day, $avg(\mathbf{x})$ is the average value of \mathbf{x} , and $std(\mathbf{x})$ is the standard deviation of \mathbf{x} . This method can effectively mitigate the outliers.

After dealing with the missing values and the outliers, we need to normalize the electricity consumption data because the neural network is sensitive to the diverse data. In particular, we choose the MAX–MIN scaling method to normalize the data according to the following equation:

$$f(x_i) = \frac{x_i - \min(\mathbf{x})}{\max(\mathbf{x}) - \min(\mathbf{x})}$$
(3)

where $\min(\mathbf{x})$ is the minimum value in \mathbf{x} , and $\max(\mathbf{x})$ is the maximum value in \mathbf{x} .

B. Wide and Deep CNN Framework

As shown in Fig. 5, the Wide and Deep CNN framework mainly consists of two major components: the wide component and the deep CNN component. We then explain them in detail as follows

1) Wide Component: As shown in Fig. 5, the wide component (enclosed in the red dash box) is a fully connected layer of neural networks and it learns the global knowledge from the 1-D electricity consumption data. According to the preliminary

analysis in Section III, the electricity consumption of customers fluctuates from time to time while the normal electricity usage reveals the periodicity and the electricity consumption of energy thieves is less periodic or nonperiodic. The electricity consumption of one customer is essentially 1-D time series data. Motivated by the previous study [36], we choose the wide component to learn the frequent co-occurrence of features by *memorizing* the 1-D time series data.

Every neuron in the fully connected layer calculates its own score by using the 1-D electricity consumption data according to the following equation:

$$y_j := \sum_{i=1}^n \mathbf{w}_{i,j} x_i + b_1 \tag{4}$$

where y_j is the output of the fully connected layer in the jth neuron, n is the length of 1-D input data (\mathbf{x}) , $\mathbf{w}_{i,j}$ stands for the neuron weight between ith input value, and jth neuron and b_1 is the bias. After the calculation, it will send this value to the connected units in the higher layer through an activation function to determine how much it contributes to the next step prediction. The activation function is given as follows:

$$u_j := f(y_j) = \max(0, y_j) \tag{5}$$

where u_j is the output after activation calculation and $f(\cdot)$ stands for the activation function. In this paper, we use rectified linear unit as the activation function, which will only activate the positive value. This function can effectively prevent the overfitting [37]. This procedure is called the forward pass. The backpropagation works in an opposite direction. During the backpropagation, every unit computes its weights according to the loss value sent from higher layer.

2) Deep CNN Component: Our preliminary analytical results (refer to Section III) reveal the periodicity of the normal electricity usage and the nonperiodicity of the electricity theft. However, it is difficult to identify the periodicity or the nonperiodicity of electricity usage from the 1-D electricity consumption data since the electricity consumption in every day fluctuates in a relatively independent way. Nevertheless, our preliminary results also imply that we can easily identify the abnormal electricity usage if we analyze the electricity consumption by aligning the consumption data of several weeks together. The previous work in [36] also indicates that the deep learning can help to derive new features (i.e., *generalization*). Motivated by this observation, we design a deep CNN component to process the electricity consumption data in 2-D manner. In particular, we transform the 1-D electricity consumption data into 2-D data according to weeks. It is worth mentioning that we can transform 1-D data into 2-D data according to different number of days (e.g., 10 days or 15 days). However, we have found that the weekly transformation in practice has the best performance compared with other types of transformations (confirming our previous observation in Section III).

We next let the deep CNN component be trained on the 2-D electricity consumption data. Fig. 5 shows that deep CNN component (enclosed in the blue dash box) consists of multiple

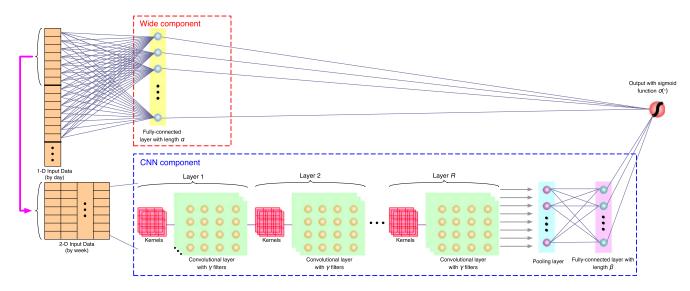


Fig. 5. wide and deep CNN framework.

convolutional layers, a pooling layer and a fully connected layer. We then explain them in details as follows.

Multiple convolutional layers: One of the limitations of regular neural networks is the poor scalability due to the full connectivity of neurons. CNN overcomes the disadvantages of regular neural networks by connecting each neuron to its neighboring neurons (not all the neurons). The local region consisting of a small set of neurons is also called as the *receptive field* [38]. Then, a filter (i.e., a vector) with the same size of the receptive field will be used to conduct the convolution operation with the input 2-D data. One convolution layer essentially consists of a number of filters working independently. When the input 2-D data are passing through the filters, convolution operations are conducted. We assume that there are R CNN layers connecting adjacently as shown in Fig. 5. In this manner, we finally obtain a 2-D feature map. In this paper, we choose γ filters; the number of filters γ is adjustable in the experiments. Moreover, we also design unique kernels to fulfill the periodicity of electricity consumption data. We next describe the technical details as follows.

We use the 2-D convolution layer to extract the periodic features from the input 2-D electricity consumption data. We denote the electricity consumption of a customer of the pth week by vector $\mathbf{v}_p \in \mathbf{R}^d$, where d is 7 in this paper. Note that we choose d=7 because a week has 7 days; this setting is implied by our observation in Section III. We then represent the concatenated electricity consumption of m weeks (denoted by $\mathbf{v}_{1:m}$) as follows:

$$\mathbf{v}_{1:m} := \begin{bmatrix} \mathbf{v}_1 \\ \mathbf{v}_2 \\ \dots \\ \mathbf{v}_m \end{bmatrix} \tag{6}$$

where $m = \lceil \frac{n}{7} \rceil$. In general, let $\mathbf{v}_{p:p+k}$ refer to the concatenation of weekly electricity consumption $\mathbf{v}_p, \mathbf{v}_{p+1}, \dots, \mathbf{v}_{p+k}$.

Traditionally, a convolution operation involves a filter $\hat{\mathbf{w}}$, which is applied to a window of size 3×3 to produce a new feature. This method is effective in image processing and

recognition. However, the 2-D electricity consumption data are different from the image data. Therefore, we design the unique kernels to process the 2-D electricity consumption data. In particular, we consider a feature $\mathbf{c}_{p+1,q+1}$, which can be generated from a window of matrix $\mathbf{v}_{p:p+2,q:q+2}$ by the following equation:

$$\mathbf{c}_{p+1,q+1} := f(\hat{\mathbf{w}}(g_1(\mathbf{v}_{p:p+2,p:p+2}) + g_2(\mathbf{v}_{p:p+2,p:p+2})) + b_2)$$
(7)

where $b_2 \in R$ is a bias term and $f(\cdot)$ is a nonlinear function such as the hyperbolic tangent [38]. It is worth noting that we design kernel functions $g_1(\cdot)$ and $g_2(\cdot)$ dedicated for the 2-D electricity consumption data. In particular, $g_1(\cdot)$ is defined as follows:

$$g_{1}(\cdot) := g_{1}(\mathbf{v}_{p:p+2,p:p+2})$$

$$:= \begin{bmatrix} 2\mathbf{v}_{p,p:p+2} - \mathbf{v}_{p+1,p:p+2} - \mathbf{v}_{p+2,p:p+2} \\ 2\mathbf{v}_{p+1,p:p+2} - \mathbf{v}_{p,p:p+2} - \mathbf{v}_{p+2,p:p+2} \\ 2\mathbf{v}_{p+2,p:p+2} - \mathbf{v}_{p,p:p+2} - \mathbf{v}_{p+1,p:p+2} \end{bmatrix}. (8)$$

Essentially, $g_1(\cdot)$ transforms the current row values by subtracting the other two rows; it captures fluctuations and trends in different periods.

We define $g_2(\cdot)$ as follows:

$$g_2(\cdot) := g_1(\mathbf{v}_{p:p+2,p:p+2}^T)^T.$$
 (9)

Specifically, $g_2(\cdot)$ transforms current column values by subtracting the other two columns; it essentially captures fluctuations and trends in the same period.

We then apply this filter to data blocks denoted by $\mathbf{v}_{1:3,1:3}, \mathbf{v}_{1:3,2:4}, \dots, \mathbf{v}_{m-2:m,m-2:m}$, respectively, to produce a feature map as given as follows:

$$\mathbf{c} := \begin{bmatrix} \mathbf{c}_{1,1} & \cdots & \mathbf{c}_{1,7} \\ \vdots & \ddots & \vdots \\ \mathbf{c}_{m,1} & \cdots & \mathbf{c}_{m,7} \end{bmatrix}$$
(10)

where c is the generated feature map having the same size as the raw matrix because the zero-padding of 1 is used.

Pooling layer: The pooling layer has been typically used in CNN to reduce the number of parameters (e.g., training weights

and filters) and the redundant features. Besides, a pool layer can also be used to control the convergence of neural networks (e.g., avoid overfitting). One of the most typical pooling operations is the *max* pooling [39]. In this way, the pooling layer will choose the maximum value of the field covered by the pooling filter. We also use the max pooling operation in this paper. In particular, we define the max pooling operation as $\hat{\mathbf{c}} = \max(\mathbf{c})$, which takes the generated feature map [defined in (10)] as the inputs. Essentially, there are two directed passing procedures in CNN: 1) during the forward passing procedure, the pooling layer will choose the maximum value of the field covered by the pooling filter; 2) during the backpropagation procedure, the pooling layer will route the gradients (weights) to the preceding filter with the highest value.

Fully-connected layer: The fully-connected layer in the deep CNN component is similar to that in the wide component while they are different in size (i.e., the size of the wide component is α and that of CNN is β). The fully connected layer in the deep CNN component is used to obtain the principal features, which can be calculated in a similar way to the fully connected layer in the wide component like (4) and (5).

Finally, the wide component and the deep CNN component are combined using a weighted sum of their output as hidden features; these features are then fed to one *logistic loss* function for the joint training and prediction [36]. In the joint training and prediction procedure, we consider the sum of the weights of both the wide component and the deep CNN component together and optimize the generated parameters at the same time. Motivated by the similar idea of the wide and deep learning model [36], we have achieved the joint training and prediction procedure by backpropagation. In particular, the prediction of the model is finally given as follows:

$$P(\mathbf{Y} = 1|\mathbf{x}) := \delta(\mathbf{W}[\mathbf{x}_{\text{Wide}}, \mathbf{x}_{\text{CNN}}] + \mathbf{b})$$
 (11)

where \mathbf{Y} is the binary class label, $\delta(\cdot)$ is the sigmoid function, \mathbf{x}_{Wide} and \mathbf{x}_{CNN} represent the features of the wide component and those of the CNN component, respectively, \mathbf{W} is the joint weights of the wide component and the CNN component, and \mathbf{b} is the bias term.

V. EXPERIMENTAL RESULTS

In this section, we present the experiment results. In Section V-A, we describe the experiment settings. Section V-B presents the performance comparison of our proposed wide and deep CNN approach with other existing methods. We then investigate the performance with evaluations by varying related parameters in Section V-C. Section V-D finally exams the convergence of our proposed method.

A. Experiment Settings

1) Raw Electricity Consumption Data: We conduct the experiments on a realistic electricity consumption dataset, which was released by SGCC. Table I presents the metadata information of this dataset, where # means "the number of." In particular, this dataset contains the electricity consumption data of 42 372 electricity customers within 1035 days (from January

TABLE I METADATA INFORMATION

Description	Value
Time window for electricity consumption # of the customers (total) # of normal electricity customers # of electricity thieves	2014/01/01- 2016/10/31 42 372 38 757 3 615

TABLE II
EXPERIMENT PARAMETERS FOR BASELINE METHODS

Method Features		Parameters		
TSR	Raw (1-D)	$\theta = 1, 2, 3, 4$		
LR	Raw (1-D)	Penalty: L2		
	` ′	Inverse of regularization strength: 1.0		
RF	Raw (1-D)	# of trees in forest: 200		
	` ′	Function to measure the quality of a split: gini		
SVM	Raw (1-D)	Penalty parameter of the error term: 1.0		
	` /	kernel: radial basis function (RBF)		
Wide	Raw (1-D)	Same as Wide component of our approach		
CNN	Raw (2-D)	Same as CNN component of our approach		

- 1, 2014 to October 31, 2016). It is worth mentioning that the dataset contains some erroneous data and missing values. Therefore, we exploit the data preprocessing method as described in Section IV-A to address this issue.
- 2) Ground Truth: Along with the released dataset, SGCC also explicitly indicated that the dataset contains 3615 electricity thieves (as shown in Table I). The electricity thieves occupy nearly 9% of all the customers; this implies that the electricity theft in China is quite serious. We use the the given electricity thieves as the ground truth to evaluate the performance of the proposed scheme and other related schemes.
- *3) Performance Metrics:* In this paper, we conduct the experiments by considering two performance metrics: area under curve (AUC) [40] and mean average precision (MAP) [41]. We briefly introduce them as follows.

AUC is often used to evaluate the classification/rank accuracy. The AUC value is equivalent to the probability that a randomly chosen positive sample ranks higher than a randomly chosen negative sample. The equivalent formula for AUC calculation is given as follows:

$$AUC = \frac{\sum_{i \in positiveClass} Rank_i - \frac{M(1+M)}{2}}{M \times N}$$
 (12)

where Rank_i represents the rank value of sample i, M is the number of positive samples, and N is the number of negative samples. It is worth mentioning that samples are sorted in the ascending order according to the prediction of positive samples for scoring.

MAP is often used to judge the quality of information retrieval. In this paper, we use this metric to evaluate the accuracy of our model. Before using MAP to evaluate, the label of test set is sorted according to the prediction score. We then choose the top N labels to evaluate the performance.

Methods	T	Training ratio = 50%			Training ratio = 60%		Training ratio = 70%		Training ratio $= 80\%$			
	AUC	MAP@100	MAP@200	AUC	MAP@100	MAP@200	AUC	MAP@100	MAP@200	AUC	MAP@100	MAP@200
TSR (1)	0.5705	0.5056	0.5140	0.5698	0.5111	0.5140	0.5593	0.5365	0.5332	0.5676	0.5284	0.5363
TSR (2)	0.5903	0.5755	0.5577	0.5847	0.5955	0.5737	0.5720	0.5255	0.5277	0.5801	0.5764	0.5654
TSR (3)	0.5514	0.5362	0.5336	0.5526	0.4774	0.4989	0.5513	0.5281	0.5326	0.5498	0.5458	0.5266
TSR (4)	0.5069	0.4973	0.5039	0.5115	0.4988	0.4979	0.5135	0.5560	0.5383	0.5034	0.5676	0.5452
LR	0.6773	0.6442	0.5669	0.6944	0.6612	0.5746	0.6916	0.6666	0.5783	0.7060	0.6560	0.5781
SVM	0.7183	0.6862	0.5919	0.7317	0.7192	0.6071	0.7276	0.7244	0.6068	0.7413	0.7353	0.6195
RF	0.7317	0.9078	0.8670	0.7325	0.8869	0.8525	0.7372	0.9259	0.8864	0.7385	0.9054	0.8536
Wide	0.6751	0.8013	0.7675	0.6950	0.8096	0.7841	0.6866	0.8116	0.7768	0.6965	0.8096	0.7646
CNN	0.7636	0.9059	0.8835	0.7837	0.9394	0.9077	0.7779	0.9547	0.9154	0.7797	0.9229	0.8853
Wide & Deep CNN	0.7760	0.9404	0.8961	0.7922	0.9555	0.9297	0.7860	0.9686	0.9327	0.7815	0.9503	0.9093

TABLE III

PERFORMANCE COMPARISON OF OUR PROPOSED WIDE AND DEEP CNN MODEL AND OTHER CONVENTIONAL SCHEMES (PARAMETERS $\alpha=90, \beta=60, \gamma=90$)

In order to calculate MAP, we first define precision at k (denoted by P@k) as follows:

$$P@k = \frac{Y_k}{k} \tag{13}$$

where Y_k denotes the number of correctly predicted electricity thieves before the location k.

We then denote the mean of all P@k situations by MAP@N (with top N labels), which is given as follows:

$$MAP@N = \frac{\sum_{i=1}^{r} P@k_i}{r}$$
 (14)

where r is the number of electricity thieves in top N labels and k_i ($i = 1 \dots r$) is the position of the electricity theft.

B. Performance Comparison

In this section, we present the experimental results over the given dataset to have a performance comparison with conventional data analytical schemes. In the experiments, we choose the following elementary schemes:

1) Three-Sigma Rule (TSR): TSR is a typical anomaly detection method. Different from data preprocess as presented in Section IV-A, we use it as a baseline method to detect whether an electricity customer is an electricity thief. The electricity-theft detection in TSR can be expressed as the following equation:

$$TSR(\theta) = \frac{\sum_{i=1}^{n} I(x_i, \mathbf{x}, \theta)}{n}$$
 (15)

where $I(x_i, \mathbf{x}, \theta)$ is an indicator function defined as follows:

$$I(x_i, \mathbf{x}, \theta) = \begin{cases} 1 & \text{if } x_i > \text{avg}(\mathbf{x}) + \theta \cdot \text{std}(\mathbf{x}) \\ 0 & \text{otherwise} \end{cases}$$
 (16)

where x_i is the *i*th value of \mathbf{x} , n is the length of \mathbf{x} , θ is the outlier threshold (we typically choose $\theta = 1, 2, 3, 4$).

2) Logistic Regression: This method is a basic model in binary classification, which is equivalent to one layer of neural network with sigmod activation function.

- 3) Random Forest (RF): This method is basically an ensemble tree model. In the previous study [42], decision tree was used to identify power quality disturbances. RF model is essentially an integration of multiple decision trees. Compared with a single decision tree, RF model can achieve better performance while maintaining the effective control of over-fitting.
- 4) *Support Vector Machine:* Many previous studies exploit SVM to infer the presence of electricity theft [17]–[19].
- 5) *Wide:* This scheme can be regarded as a variant of our proposed wide and deep CNN model with the removal of the CNN component. Note that the training data for the wide scheme is the 1-D electricity consumption data (the same as our wide and deep CNN model).
- 6) Convolutional Neural Network: This scheme can be regarded as a variant of our proposed wide and deep CNN model with the removal of the wide component and the preservation of CNN. Note that the training data for CNN is the 2-D electricity consumption data (the same as our wide and deep CNN model).

Table II summarizes the parameters used for the baseline methods and the extracted features to train these models. It is worth mentioning that we only used raw data and did not artificially modify the models based on any expert domain knowledge (it is relatively fair to evaluate the learning capability of each model).

Table III presents the performance comparison of our proposed wide and deep CNN scheme and other schemes. It is worth noting that we randomly choose a subset of electricity consumption records according to the *training ratio*, which is defined by the ratio of the size of training samples to the size of all the samples. We conduct four groups of experiments with training ratio being 50%, 60%, 70%, and 80%, respectively. Moreover, we choose parameters $\alpha = 90$, $\beta = 60$, $\gamma = 15$ for both our wide and deep CNN model and CNN model (without parameter α). In each group of experiments, we evaluate the performance metrics (AUC and MAPN) for the five schemes (note that we choose N = 100 and N = 200 for MAPN).

It is shown in Table III that our proposed wide and deep CNN scheme performs better than conventional schemes, such

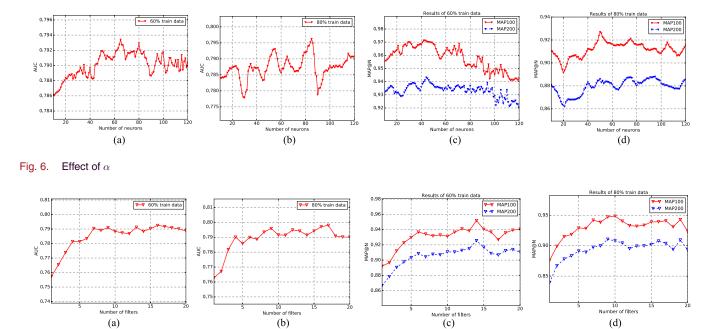


Fig. 7. Effect of γ

as LR, RF, Wide, SVM, and CNN in terms of AUC, MAP100, and MAP200 in all four groups of experiments. For example, wide and deep CNN can achieve the maximum MAP100 value with 0.9404 compared with other schemes when the training ratio is 50%. This implies that our proposed method has the higher accuracy in electricity-theft detection than other conventional schemes. This improvement may owe to the integration of *memorization* and *generalization* features brought by the wide component and the deep CNN component, respectively.

C. Parameter Study

We then investigate the impacts of various parameters on the performance of our proposed wide and deep CNN scheme.

1) Effect of α : α is a parameter controlling the number of neurons in the fully connected layer of the wide component. To investigate the impact of α on the prediction results, we vary the values of α from 10 to 120 with the step value of 1. At the same time, we fix $\beta=64$ and $\gamma=10$. We conduct two groups of experiments with the training ratio with 60% or 80%, respectively.

Fig. 6 shows the experiment results. We can see from Fig. 6 that both AUC and MAP increase at first when the number of neurons (i.e., α) increases while they decrease when α is greater than a certain value. For example, when α is smaller than 50, AUC always increases in both these two groups of experiments as shown in Fig. 6(a) and (b) and it drops when α is greater than 50 while it increases again when α is greater than 60. But, the best performance was obtained when $\alpha = 50$. This is because the wide component may lack of enough neurons to learn from the 1-D electricity consumption data when α is too small. However, when α is too large, too many neurons will make the neural networks complicated, consequently resulting in overfitting. Therefore, there may exist a threshold on α to

optimize the AUC performance. In the two groups experiments, the threshold on α is 50.

We have similar findings in the MAP performance in both two groups of experiments. Take Fig. 6(c) and (d) as an example. MAP@N reaches the peak when $\alpha=60$ in the first group of experiments (with training ratio 60%) and reaches the peak when $\alpha=80$ in the second group of experiments (with training ratio 80%). This result implies that there are different thresholds on α when we optimize AUC and MAP. Therefore, it is worthwhile for us to investigate how to choose an appropriate number of neurons in the wide component to optimize both AUC and MAP. This will be left as one of the future works.

2) Effect of γ : In the CNN component of our wide and deep CNN method, γ is a parameter controlling the number of filters in the convolutional layer. To investigate the impact of γ on the prediction results, we vary γ from 1 to 20 with the step value of 1. Similarly, we also conduct two groups of experiments with the training ratio with 60% or 80%, respectively. Note that we also fix $\alpha=60$ and $\beta=60$ in both the two groups of experiments.

Fig. 7 shows the experiment results. When γ increases, AUC also increases at first. However, when γ surpasses a certain threshold, AUC decreases. A similar trend can be found in MAP. This is because the CNN component may not have enough neurons to learn from the 2-D electricity consumption data when γ is small while too large value of γ may cause overfitting. Similar to γ , there may exist different threshold values of γ to optimize AUC and MAP.

3) Effect of β : β is a parameter controlling the number of neurons in the fully connected layer in the CNN component immediately following the pooling layer. To investigate the impact of β on the prediction results, we vary the values of β from 50 to 100 with the step value of 1. At the same time, we fix $\alpha=60$ and $\gamma=15$. We also conduct two groups of experiments

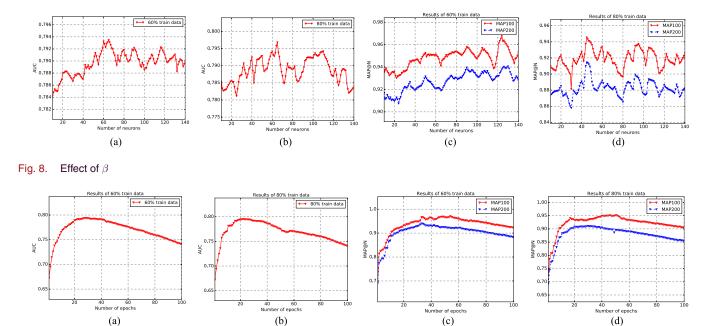


Fig. 9. Convergence analysis

TABLE IV EFFECT OF ${\cal R}$

# of layers R	Training ratio = 80%						
	AUC	MAP@100	MAP@200				
1	0.7815	0.9190	0.8674				
2	0.7872	0.9353	0.9051				
3	0.7890	0.9449	0.9034				
4	0.7923	0.9524	0.9080				
5	0.8001	0.9565	0.9128				

with the similar settings on the training ratio with 60% or 80%, respectively.

Fig. 8 shows experiment results. We have the similar findings to those in investigating the effect of α . In fact, β plays a similar role in the CNN component like α in the wide component. So, to avoid the repetition, we do not explain the experiment results of β in detail. However, it is worth mentioning that the range of β is usually different from that of α since the input data size for the fully connected layer in the CNN component is different from that in the wide component.

4) Effect of R: We choose R to control the number of layers in the deep CNN component. To investigate the impact of R on the prediction results, we vary the values of R from 1 to 5 with the step value of 1. Table IV shows experiment results. Note that we choose a general setting with the training ratio 80% in CNN. It is shown in Table IV that AUC of wide and deep CNN increases with the increased number of layers. MAP@N has the upward trend similar to AUC with the increased number of layers. Overall, the increased number of layers in wide and deep CNN can improve the prediction performance. The performance improvement mainly owes to the effect that deep CNN can capture features of 2-D data better with the increased number of layers.

D. Convergence Analysis

In our wide and deep CNN method, the epoch is a parameter controlling the train round. An epoch is defined by one forward pass and one backward pass of all training samples. We choose the similar settings like parameter study to investigate the impact of the epoch. In particular, we vary the epoch values from 10 to 100 with the step value of 1 and we fix $\alpha=60$, $\gamma=15$, $\beta=120$. Similarly, we also conduct two groups of experiments with different training ratio (60% or 80%).

Fig. 9 presents the results (in terms of AUC and MAP). We can see that like the parameter study, when the epoch value increases, both AUC and MAP increase at first. But after a certain threshold on the epoch, both AUC and MAP drop while they increase again later. This phenomenon can be explained as follows. When we choose a smaller epoch value, it may be not enough to let our wide and deep CNN system learn from both 1-D and 2-D data. However, it may cause overfitting when we choose a larger epoch value. Therefore, there also exists a threshold on the epoch value to optimize the training procedure in our wide and deep CNN. For example, the best performance was achieved when the number of epochs reaches 30 when the training ratio is 60%.

VI. CONCLUSION AND FUTURE WORK

In this paper, we propose a wide and deep CNN model to detect electricity theft in smart grids. In particular, our wide and deep CNN model consists of the wide component and the deep CNN component; it gains the benefits of memorization and generalization brought by the wide component and the deep CNN component, respectively. We conduct extensive experiments on realistic electricity consumption data released by SGCC, the largest electricity supply company in China. The experiment results show that our proposed wide and deep CNN outper-

forms existing methods, such as linear regression, SVM, RF, and CNN. In fact, the proposed wide and deep CNN model is quite general; it can be applied to other scenarios, especially for industrial applications. For example, indoor marihuana growing companies often steal electricity from the power grid [43]. Since it consumes extremely high amounts of electricity to grow marihuana, the abnormal electricity usage patterns can be captured by the proposed wide and deep CNN model.

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