

Working with Sequences in a Functional Way



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<http://csharpmentor.com>



Using Collections



Consume a collection of objects

This module



Modify a collection of objects

Next module



Understanding Collections of Objects



List

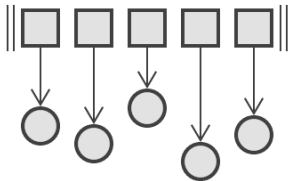
Understanding Collections of Objects



List

Array

Understanding Collections of Objects

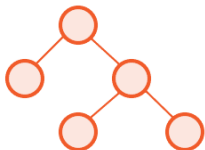


List

Array

Dictionary

Understanding Collections of Objects



List

Array

Dictionary

Tree

Understanding Collections of Objects



List

Array

Dictionary

Tree

Stack

Understanding Collections of Objects



List

Array

Dictionary

Tree

Stack

Queue

Understanding Collections of Objects



List

Array

Dictionary

Tree

Stack

Queue

used to build a compiler

Understanding Collections of Objects



List

Array

Dictionary

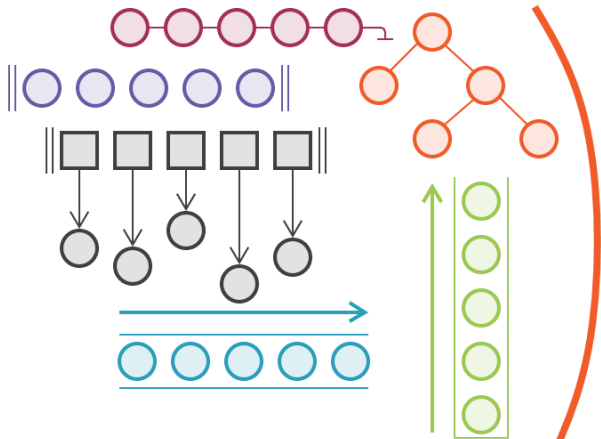
Tree

Stack

Queue

used to pass an exam

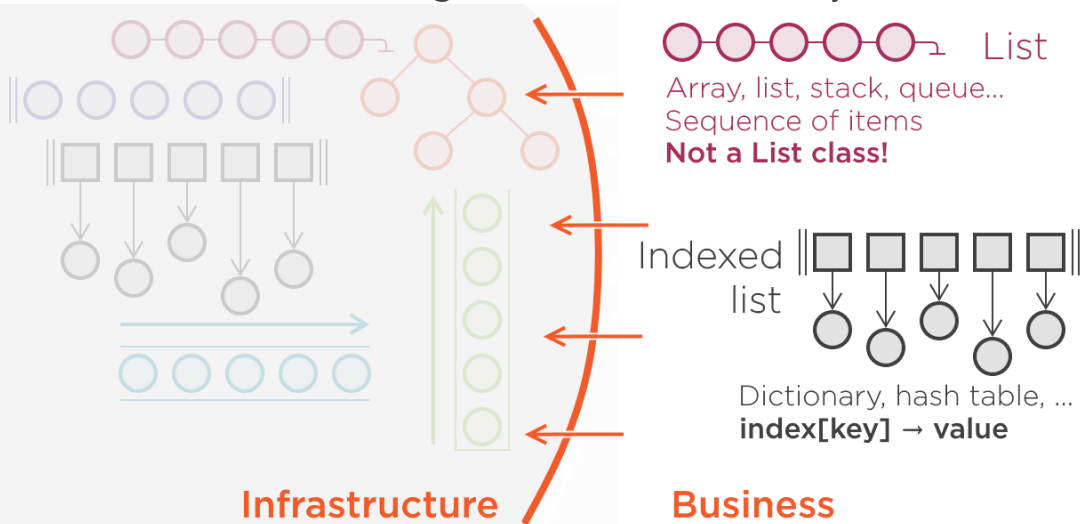
Understanding Collections of Objects



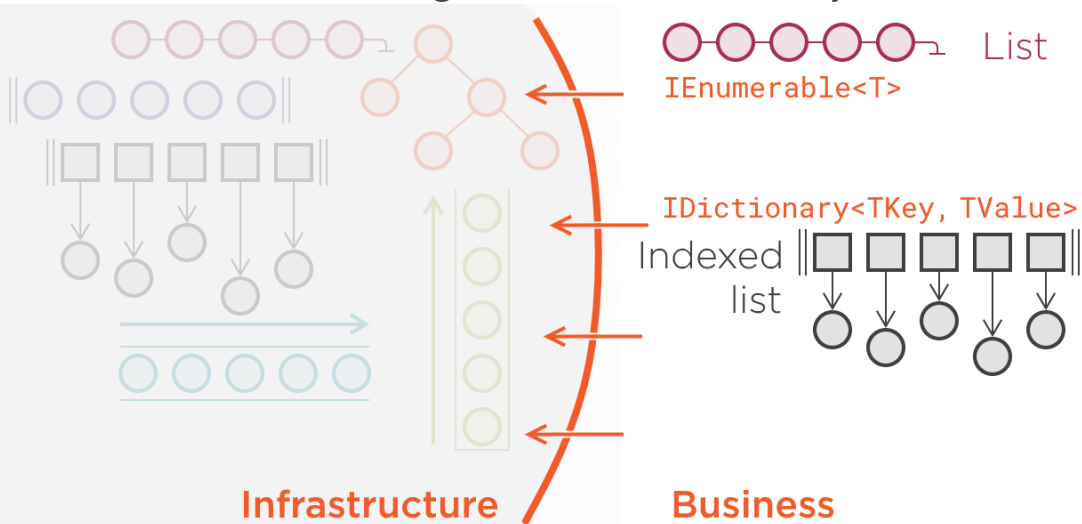
Infrastructure

Business

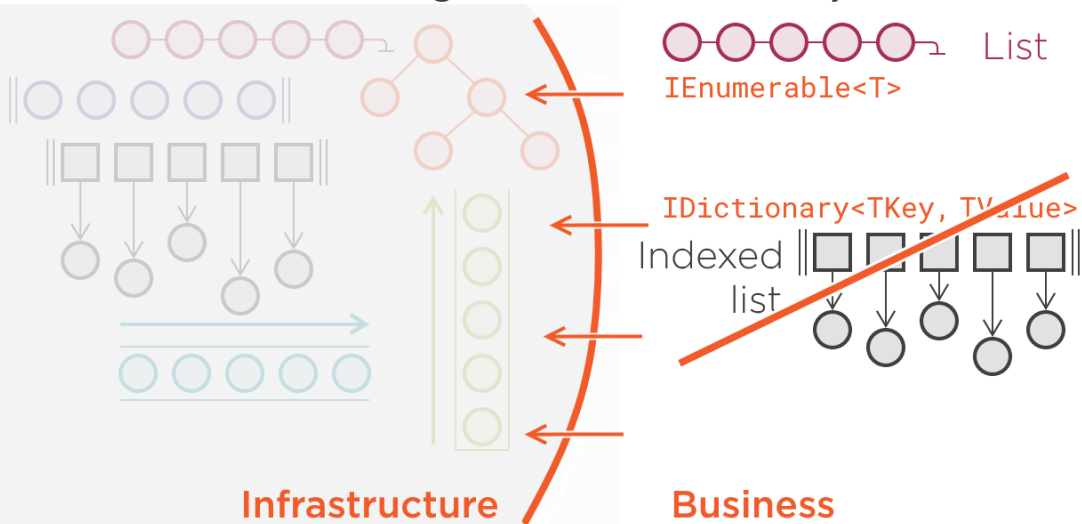
Understanding Collections of Objects



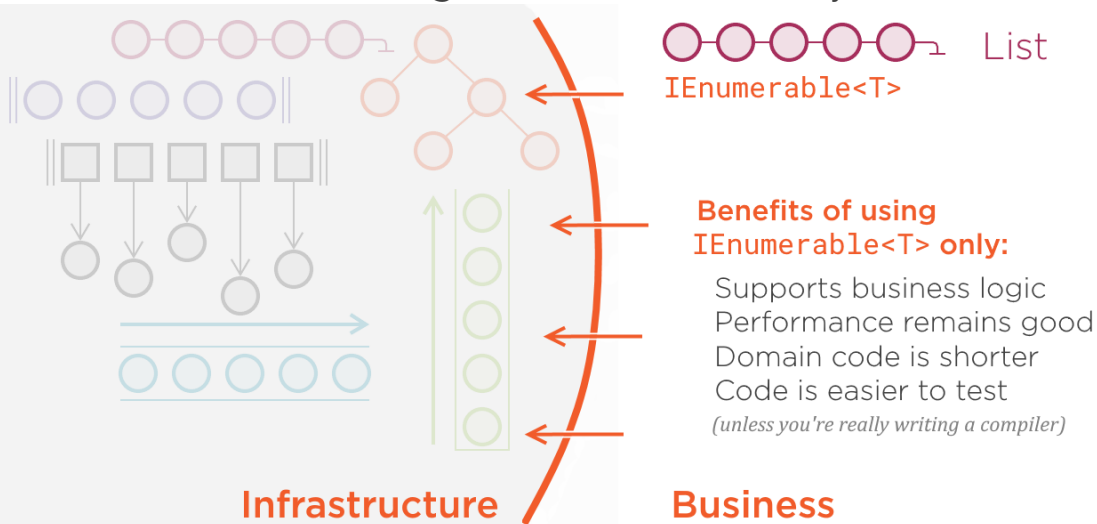
Understanding Collections of Objects



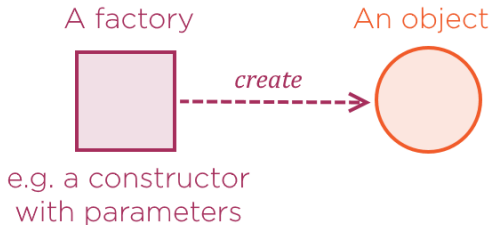
Understanding Collections of Objects



Understanding Collections of Objects



Understanding .NET List Comprehension



Can we construct
a sequence like a
common object?

Understanding .NET List Comprehension

Set comprehension (mathematics)

$$P = \{2k | k \in N\}$$
$$\{2, 4, 6, 8, \dots\}$$

Set

An unordered collection
of values.

Only defines
"belongs to" relation.

Sequence comprehension (mathematics)

$$S = (a_k)_{k=1}^{\infty}, a_i = 2i$$

yields $(2, 4, 6, 8, \dots)$

Infinite sequence

Possible on the set of
natural numbers.

Not possible on **Int32**!

Understanding .NET List Comprehension

Set comprehension
(mathematics)

$$P = \{2k | k \in N\}$$

Sequence comprehension
(mathematics)

$$S = (a_k)_{k=1}^{\lfloor MaxInt/2 \rfloor}, a_i = 2i$$

List comprehension
with **yield return**

```
IEnumerable<int> Evens()  
{  
    int n = 0;  
    while (n <= Int32.MaxValue - 2)  
    {  
        n += 2;  
        yield return n;  
    }  
}
```

```
Evens().Take(12).Count();
```

Exactly 12 iterations will execute!



Understanding .NET List Comprehension

Set comprehension
(mathematics)

$$P = \{2k | k \in N\}$$

List comprehension
with **yield return**

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    }  
}
```

Sequence comprehension
(mathematics)

$$S = (a_k)_{k=1}^{\lfloor MaxInt/2 \rfloor}, a_i = 2i$$

List comprehension
with **Select**

```
IEnumerable<int> Evens() =>  
    Enumerable.Range(1, Int32.MaxValue)  
        .Where(i => i % 2 == 0);
```

Understanding .NET List Comprehension

Set comprehension
(mathematics)

$$P = \{2k | k \in N\}$$

Sequence comprehension
(mathematics)

$$S = (a_k)_{k=1}^{\lfloor MaxInt/2 \rfloor}, a_i = 2i$$

List comprehension
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    while (n <= Int32.MaxValue - 2)  
    {  
        n += 2;  
        yield return n;  
    }  
}
```

List comprehension
with **Select**

```
IEnumerable<int> Evens() =>  
    Enumerable.Range(1, Int32.MaxValue)  
        .Where(i => i % 2 == 0);
```

Filtering is not
an efficient strategy

Dividing by 100
would throw away
99% of objects!

Understanding .NET List Comprehension

Set comprehension
(mathematics)

$$P = \{2k | k \in N\}$$

List comprehension
with **yield return**

```
IEnumerable<int> Evens()  
{  
    int n = 0;  
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        n += 2;  
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    }  
}
```

Sequence comprehension
(mathematics)

$$S = (a_k)_{k=1}^{\lfloor MaxInt/2 \rfloor}, a_i = 2i$$

List comprehension
with **Select**

```
IEnumerable<int> Evens() =>  
    Enumerable.Range(1, Int32.MaxValue / 2)  
        .Select(i => 2 * i);
```

Understanding .NET List Comprehension

Set comprehension
(mathematics)

$$P = \{2k | k \in N\}$$

List comprehension
with **yield return**

```
IEnumerable<int> Evens()  
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Sequence comprehension
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$$S = (a_k)_{k=1}^{\lfloor MaxInt/2 \rfloor}, a_i = 2i$$

List comprehension
with **Select**

```
IEnumerable<int> Evens() =>  
    Enumerable.Range(1, Int32.MaxValue / 2)  
        .Select(i => 2 * i);
```

Lazy evaluated

Understanding .NET List Comprehension

Set comprehension
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$$P = \{2k | k \in N\}$$

List comprehension
with **yield return**

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}
```

Sequence comprehension
(mathematics)

$$S = (a_k)_{k=1}^{\lfloor MaxInt/2 \rfloor}, a_i = 2i$$

List comprehension
with **Select**

```
IEnumerable<int> Evens() =>  
    Enumerable.Range(1, Int32.MaxValue / 2)  
        .Select(i => 2 * i);
```

Every index is used

Understanding .NET List Comprehension

Set comprehension
(mathematics)

$$P = \{2k | k \in N\}$$

List comprehension
with **yield return**

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Sequence comprehension
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$$S = (a_k)_{k=1}^{\lfloor \text{MaxInt}/2 \rfloor}, a_i = 2i$$

List comprehension
with **Select**

```
IEnumerable<int> Evens() =>  
    Enumerable.Range(1, Int32.MaxValue / 2)  
        .Select(i => 2 * i);
```

$(a_k)_{k=1}^{\lfloor \text{MaxInt}/2 \rfloor}, a_i = 2i$

Understanding .NET List Comprehension

Set comprehension
(mathematics)

$$P = \{2k | k \in N\}$$

Sequence comprehension
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List comprehension
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```

List comprehension
with **Select**

```
IEnumerable<int> Evens() =>  
    Enumerable.Range(1, Int32.MaxValue / 2)  
        .Select(i => 2 * i);
```

And what about
`IEnumerable<IMoney>`?

LINQ Operators vs. Common Functions

List comprehension
with LINQ

sequence $\xrightarrow{\text{transform}}$ sequence

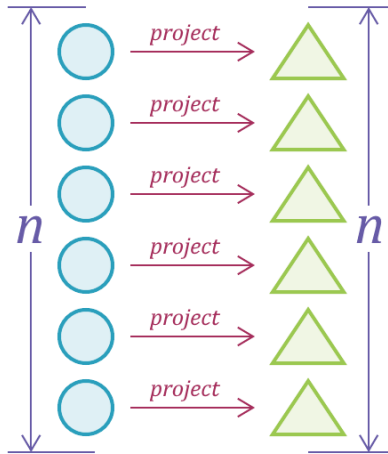
Object construction
with functions

object $\xrightarrow{\text{function}}$ object

Understanding LINQ Operators

Mapping

Select(map)



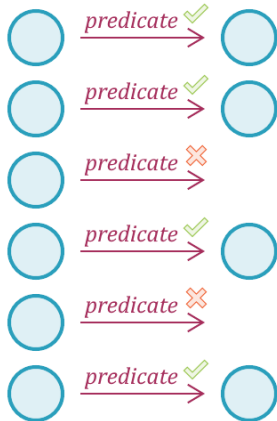
Understanding LINQ Operators

Mapping

Select(map)

Filtering

Where(predicate)



Understanding LINQ Operators

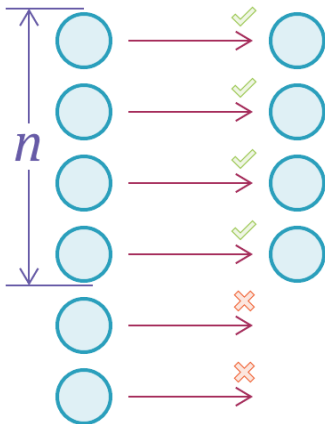
Mapping

Select(map)

Filtering

Where(predicate)

Take(n)



Understanding LINQ Operators

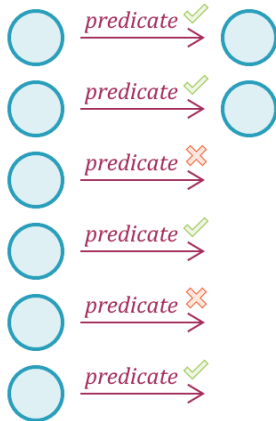
Mapping

Select(map)

Filtering

Where(predicate)

Take(n), TakeWhile(predicate)



Understanding LINQ Operators

Mapping

Select(map)

Filtering

Where(predicate)

Take(n), TakeWhile(predicate)

Skip(n)



Understanding LINQ Operators

Mapping

Select(map)

Filtering

Where(predicate)

Take(n), TakeWhile(predicate)

Skip(n), SkipWhile(predicate)



Understanding LINQ Operators

Mapping

Select(map)

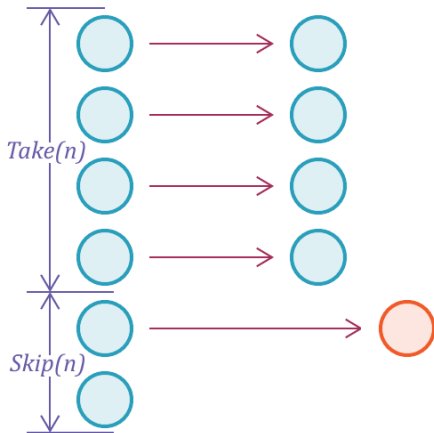
Filtering

Where(predicate)

Partitioning

Take(n), TakeWhile(predicate)

Skip(n), SkipWhile(predicate)



Understanding LINQ Operators

Mapping

Select(map)

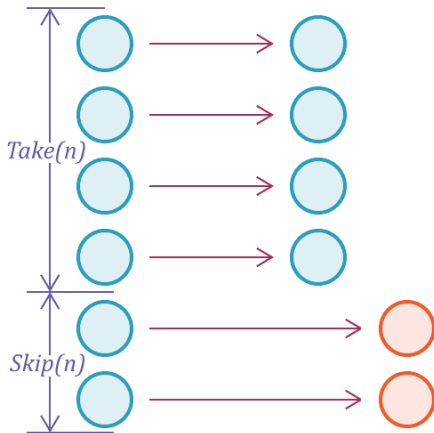
Filtering

Where(predicate)

Partitioning

Take(n), TakeWhile(predicate)

Skip(n), SkipWhile(predicate)



Understanding LINQ Operators

Mapping

Select(map)

Filtering

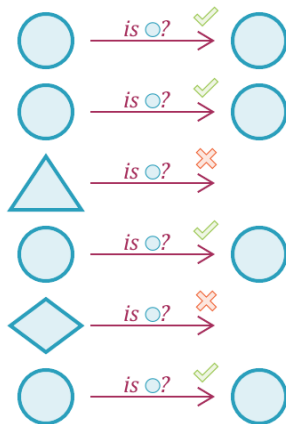
Where(predicate)

Partitioning

Take(n), TakeWhile(predicate)

Skip(n), SkipWhile(predicate)

OfType<T>



Understanding LINQ Operators

Mapping

Select(map)

Filtering

Where(predicate)

Partitioning

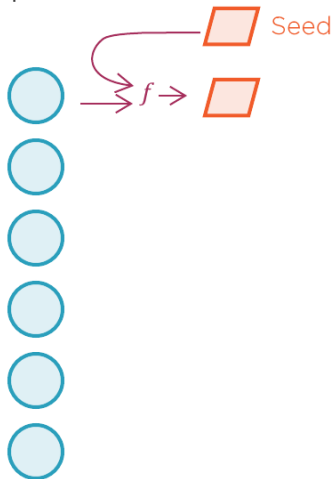
Take(n), TakeWhile(predicate)

Skip(n), SkipWhile(predicate)

OfType<T>

Aggregating

Aggregate(seed, f)



Understanding LINQ Operators

Mapping

Select(map)

Filtering

Where(predicate)

Partitioning

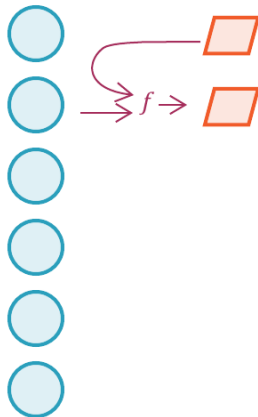
Take(n), TakeWhile(predicate)

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Understanding LINQ Operators

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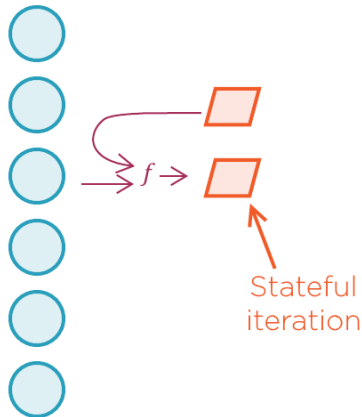
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Understanding LINQ Operators

Mapping

Select(map)

Filtering

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Partitioning

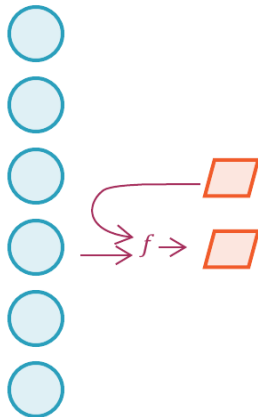
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Understanding LINQ Operators

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Select(map)

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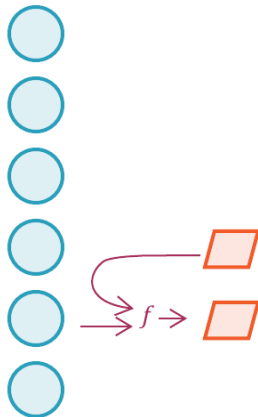
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Understanding LINQ Operators

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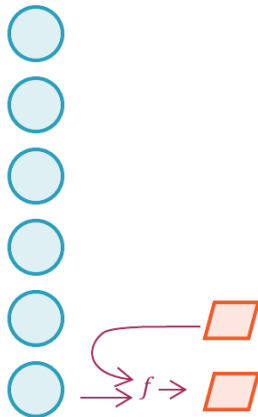
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Understanding LINQ Operators

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Understanding LINQ Operators

Mapping

Select(map)

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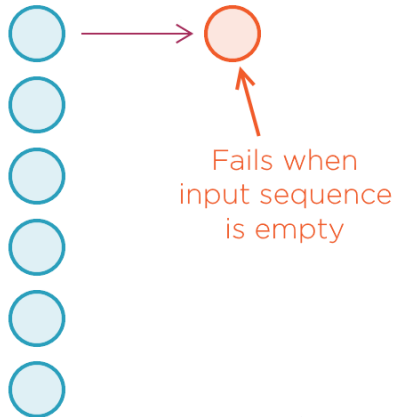
Skip(n), SkipWhile(predicate)

OfType<T>

Aggregating

Aggregate(seed, f)

Aggregate(f)



Understanding LINQ Operators

Mapping

Select(map)

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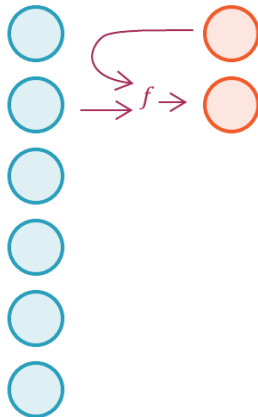
Skip(n), SkipWhile(predicate)

OfType<T>

Aggregating

Aggregate(seed, f)

Aggregate(f)



Understanding LINQ Operators

Mapping

Select(map)

Filtering

Where(predicate)

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Take(n), TakeWhile(predicate)

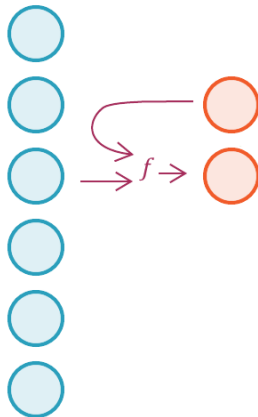
Skip(n), SkipWhile(predicate)

OfType<T>

Aggregating

Aggregate(seed, f)

Aggregate(f)



Understanding LINQ Operators

Mapping

Select(map)

Filtering

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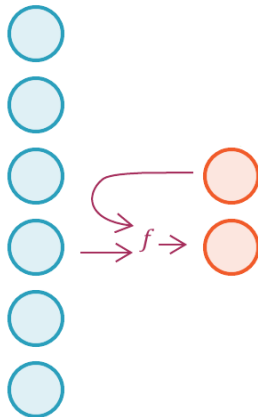
Skip(n), SkipWhile(predicate)

OfType<T>

Aggregating

Aggregate(seed, f)

Aggregate(f)



Understanding LINQ Operators

Mapping

Select(map)

Filtering

Where(predicate)

Partitioning

Take(n), TakeWhile(predicate)

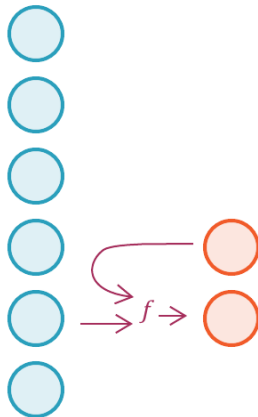
Skip(n), SkipWhile(predicate)

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Aggregating

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Aggregate(f)



Understanding LINQ Operators

Mapping

Select(map)

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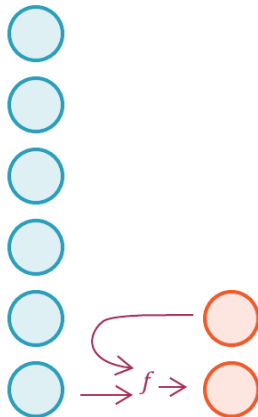
Skip(n), SkipWhile(predicate)

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Aggregating

Aggregate(seed, f)

Aggregate(f)



Understanding LINQ Operators

Mapping

Select(map)

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OfType<T>

Aggregating

Aggregate(seed, f)

Aggregate(f)



Understanding LINQ Operators

Mapping

Select(map)

Filtering

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Partitioning

Take(n), TakeWhile(predicate)

Skip(n), SkipWhile(predicate)

OfType<T>

Aggregating

Aggregate(seed, f)

Aggregate(f)

Min, Max, Average, Sum, Count

Returns zero
on an empty sequence

Throws **InvalidOperationException**
on an empty sequence

Understanding LINQ Operators

Mapping

Select(map)

Filtering

Where(predicate)

Partitioning

Take(n), TakeWhile(predicate)

Skip(n), SkipWhile(predicate)

OfType<T>

Aggregating

Aggregate(seed, f)

Aggregate(f)

Min, Max, Average, Sum, Count

First, Last

FirstOrDefault, LastOrDefault

Understanding LINQ Operators

Mapping

Select(map)

Filtering

Where(predicate)

Partitioning

Take(n), TakeWhile(predicate)

Skip(n), SkipWhile(predicate)

OfType<T>

Aggregating

Aggregate(seed, f)

Aggregate(f)

Min, Max, Average, Sum, Count

First, Last

FirstOrDefault, LastOrDefault

Concatenation

SelectMany

Understanding LINQ Operators

Mapping	Select(map)
Filtering	Where(predicate)
Partitioning	Take(n), TakeWhile(predicate) Skip(n), SkipWhile(predicate) OfType<T>
Aggregating	Aggregate(seed, f) Aggregate(f) Min, Max, Average, Sum, Count First, Last FirstOrDefault, LastOrDefault
Concatenation	SelectMany Concat

Understanding LINQ Operators

Mapping	Select(map) GroupBy(keySelector)
Filtering	Where(predicate)
Partitioning	Take(n), TakeWhile(predicate) Skip(n), SkipWhile(predicate) OfType<T>
Aggregating	Aggregate(seed, f) Aggregate(f) Min, Max, Average, Sum, Count First, Last FirstOrDefault, LastOrDefault
Concatenation	SelectMany Concat



Eager execution!

Less efficient:

```
seq.GroupBy(x => x.key).Take(10)
```

More efficient:

```
seq.Select(x => x.key).Take(10)
```

Understanding LINQ Operators

Mapping	Select(map) GroupBy(keySelector) OrderBy(keySelector)
Filtering	Where(predicate)
Partitioning	Take(n), TakeWhile(predicate) Skip(n), SkipWhile(predicate) OfType<T>
Aggregating	Aggregate(seed, f) Aggregate(f) Min, Max, Average, Sum, Count First, Last FirstOrDefault, LastOrDefault
Concatenation	SelectMany Concat



Often questionable
in domain logic



Useful in
presentation logic

Understanding LINQ Operators

Mapping	Select(map) GroupBy(keySelector) OrderBy(keySelector) Join
Filtering	Where(predicate)
Partitioning	Take(n), TakeWhile(predicate) Skip(n), SkipWhile(predicate) OfType<T>
Aggregating	Aggregate(seed, f) Aggregate(f) Min, Max, Average, Sum, Count First, Last FirstOrDefault, LastOrDefault
Concatenation	SelectMany Concat

Subset of a Cartesian product

```
leftSeq.Join(  
    rightSeq,  
    x => x.Id,  
    y => y.Id,  
    (x, y) => (x.a, y.b));
```

Looks like we need
this as a new type

Understanding LINQ Operators

Mapping	Select(map) GroupBy(keySelector) OrderBy(keySelector) Join
Filtering	Where(predicate)
Partitioning	Take(n), TakeWhile(predicate) Skip(n), SkipWhile(predicate) OfType<T>
Aggregating	Aggregate(seed, f) Aggregate(f) Min, Max, Average, Sum, Count First, Last FirstOrDefault, LastOrDefault
Concatenation	SelectMany Concat
Set operators	Distinct

Understanding LINQ Operators

Mapping	Select(map) GroupBy(keySelector) OrderBy(keySelector) Join
Filtering	Where(predicate)
Partitioning	Take(n), TakeWhile(predicate) Skip(n), SkipWhile(predicate) OfType<T>
Aggregating	Aggregate(seed, f) Aggregate(f) Min, Max, Average, Sum, Count First, Last FirstOrDefault, LastOrDefault
Concatenation	SelectMany Concat
Set operators	Distinct, Except

Understanding LINQ Operators

Mapping	Select(map) GroupBy(keySelector) OrderBy(keySelector) Join
Filtering	Where(predicate)
Partitioning	Take(n), TakeWhile(predicate) Skip(n), SkipWhile(predicate) OfType<T>
Aggregating	Aggregate(seed, f) Aggregate(f) Min, Max, Average, Sum, Count First, Last FirstOrDefault, LastOrDefault
Concatenation	SelectMany Concat
Set operators	Distinct, Except Intersect

Understanding LINQ Operators

Mapping	Select(map) GroupBy(keySelector) OrderBy(keySelector) Join
Filtering	Where(predicate)
Partitioning	Take(n), TakeWhile(predicate) Skip(n), SkipWhile(predicate) OfType<T>
Aggregating	Aggregate(seed, f) Aggregate(f) Min, Max, Average, Sum, Count First, Last FirstOrDefault, LastOrDefault
Concatenation	SelectMany Concat
Set operators	Distinct, Except Intersect, Union

Understanding LINQ Operators

Mapping

Select(map)
GroupBy(keySelector)
OrderBy(keySelector)
Join

Filtering

Where(predicate)

Partitioning

Take(n), TakeWhile(predicate)
Skip(n), SkipWhile(predicate)
OfType<T>

Aggregating

Aggregate(seed, f)
Aggregate(f)
Min, Max, Average, Sum, Count
First, Last
FirstOrDefault, LastOrDefault

Concatenation

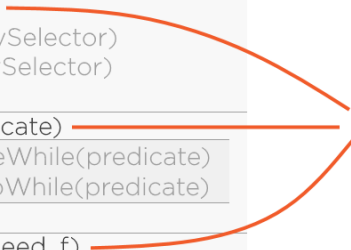
SelectMany
Concat

Set operators

Distinct, Except
Intersect, Union

General-purpose operators

(very efficient)



Understanding Deferred/Lazy Evaluation

Input sequence



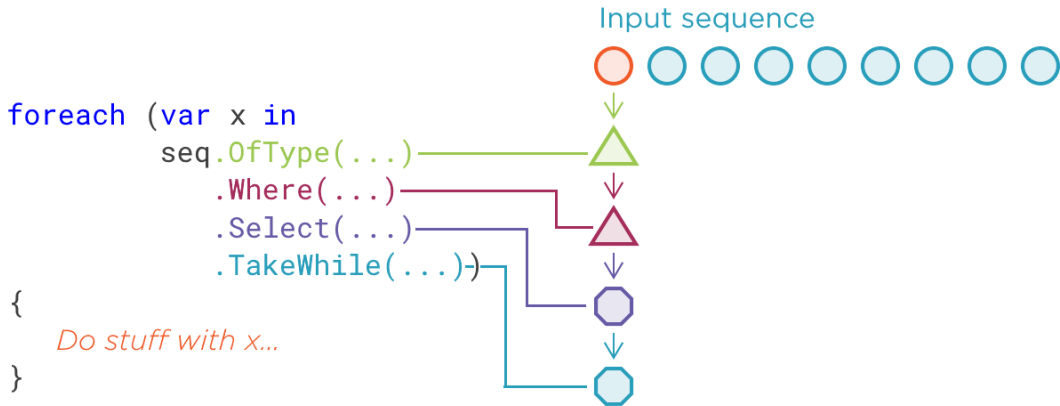
`seq.Select(...).TheNextOne()`

`seq.Where(...).TheNextOne()`

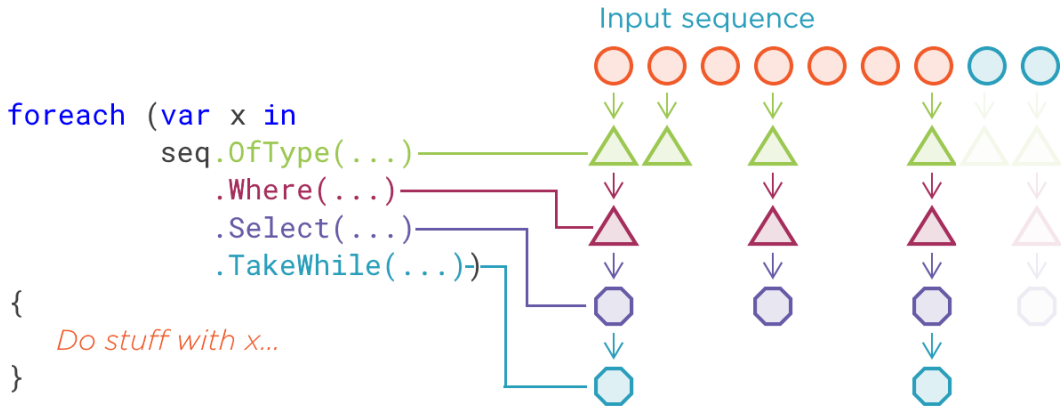


Consumer pulls objects
from a deferred operator

Understanding Deferred/Lazy Evaluation

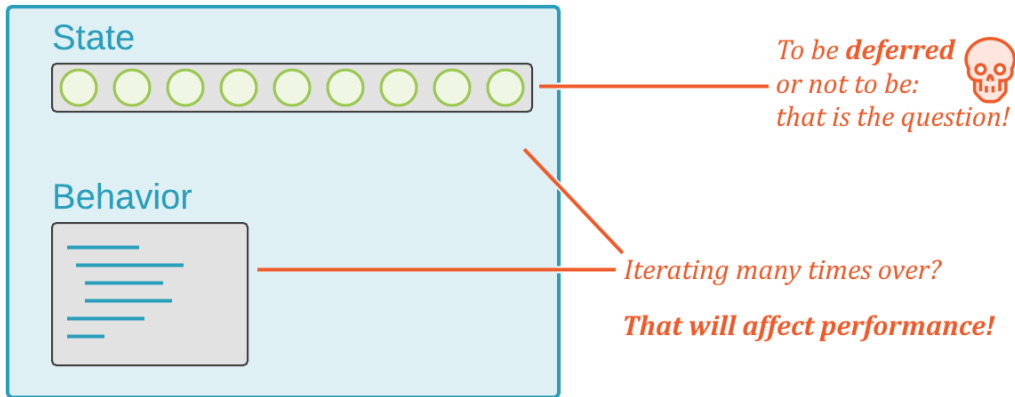


Understanding Deferred/Lazy Evaluation



Lazy vs. Eager Evaluation

An object



Lazy vs. Eager Evaluation



Deferred list
evaluation
can cost a lot

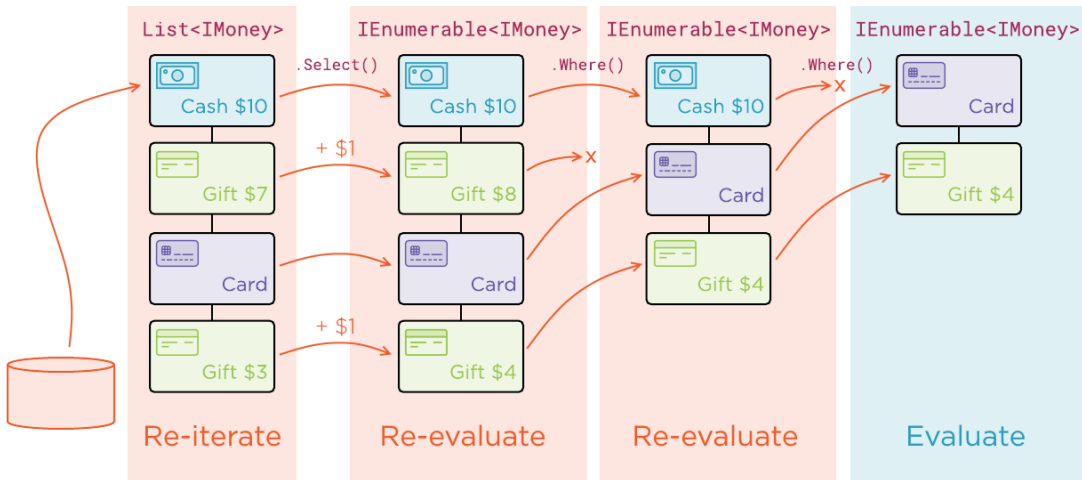
Call **seq.ToList()**
on a sequence
stored as state

Otherwise,
object will
work slow
sometimes

Lazy sequence

Not visible to automated tests!

Inadvertently Consuming Lazy Sequences



Summary



Functional list processing

- Lean on `IEnumerable<T>` for lists
- Abstraction of a list of items
- Real collection might not even exist!

Dealing with sequences

- Focus on list mapping
- Do not think of the data structure



Summary



LINQ library

- Process lists almost as common objects
- Construct - map - map - take result

Operations on sequences

- Map to a new sequence
- Filter to a new sequence
- Aggregate to a single object
- Plus many other operators
- Mapping, filtering and aggregation operators are very efficient



Summary



Lazy evaluation on sequences

- Many LINQ operators defer evaluation
- Repeated evaluation is wasteful
- No distinction between “eager” and “lazy” `IEnumerable<T>`
- Represent eager sequence with a custom type
- Or make sure to not forget `ToList()`



Next module:

Treating Sequences as
Immutable Objects

