

# OPTIMIZING 3D MODELS FROM 2D IMAGES

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## Abstract

Here comes the abstract

## 1 Introduction

### 1.1 Related work

### 1.2 FIT3D toolbox

### 1.3 Organization of this thesis

## 2 Projective Geometry

## 3 Skyline detection

### 3.1 Introduction

The sky and the earth are separated by a skyline in images. The detection of this skyline has proven to be very succesful computer vision application in a wide range of domains. In this domain it is used to provide a countour of a building. This contour is in a next step used to refine a 3D model of this building.

The organisation of this chapter is as follows. First related work on skyline detection is discussed, then a new algorithm of the skyline algorithm is described and finally some results are presented.

### 3.2 Related work

A lot of related work on skyline detection is done and it is used in a wide range of domains. [1] yields a good introduction of different skyline detection techniques, these are listed below.

### 3.2.1 Cloud detection for Mars Exploration Rovers (MER)

Mars Exploration Rovers (MER) are used to detect clouds and dust devils on Mars. In [1] their approach is to first identify the sky (equivalentl, the skyline) and then determine if there are clouds in the region segmented as sky.

### 3.2.2 Horizon detection for Unmanned Air Vehicles (UAV)

In this domain, the horizon detector for UAVs can take advantage of the high altitude of the vehicle and therefor the horizon can be approximated to be a straigt line. This turns the detection problem into a line-fitting problem. Ofcourse this work is not applicable for detecting a building countour as the straight line assumption doesn't work. But it needs to be mentioned that from this idea some inspiration on line fitting is done because the building countour has straight line segments.

### 3.2.3 Planetary Rover localisation

In [9] they use the skyline detection in planetary rovers, their approach is to combine the detected skyline with a given map of the landscape (hills, roads) to detect its current location. The advantage of their technique is the simplicity and effectiveness of the algorithm which makes it suitable for this project. A big drawback is that it is geared toward speed over extremely high accuracy because it is interactive system where an operator refines the skyline.

As mentioned in the introduction, in this project we use the skyline to extract the building contour to eventually update a 3D model which is a brand new purpose of skyline detection. There is no user interaction present, and the accuracy is a matter of high importance. This makes it different from existing skyline techniques and caution should be taken by using existing algorithms. From the related work the Planetary Rover localisation [9] seemed to fit most on this project. Therefor method [9] is used, but as a basis, and a custom algorithm with higher accuracy is developed. This is explained in the next section.

*todo why?*

## 3.3 The Algorithm

### 3.3.1 The original algorithm

The skyline detection algorithm as described in [9] works as follows: The frames are first preprocessed by converting them to Gaussian smoothed images. The skyline of a frame is then detected by analysing the the image columns seperately. The smoothed intensity gradient is calculated from top to bottom. This is done by taking the derivative of the gaussian smoothed image. The system takes the first pixel with gradient higher then a threshold to be classified as a skyline element. This is done for every column in the image. The result is a set

of coordinates of length  $W$ , where  $W$  is the width of the image, that represent the skyline.

Taking the smoothed intensity gradient is the most basic method of edge detection and has the disadvantage that it is not robust to more vague edges. This is not surprising as its purpose was a interactive system where the user refines the result. It is clear that an optimization is needed.

### 3.3.2 The optimization

The column based approach seem te be very useful and is therefor unchanged. The effectiveness of the algorithm is totally depended of the method of edge detection and the preprocessing of the images. The original algorithm uses the smoothed intensity gradient as a way of detecting edges. This is a very basic method and more sophisticated edge detection algorithms are present.

To select a proper edge detector, a practical study is done on the different Matlab build in edge detection techniques. The output of the different edge detection techniques was studied and the Sobel edge detector came with the most promising results. The Sobel edge detector outputs a binary image, therefor the column inlier threshold method is replaced by finding the first white pixel. This is as the original algorithm done from top to bottom for every column in the image.

To make the algorithm more precise, two preprocessing steps are introduced. First the contrast of the image is increased, this makes sharp edges stand out more. Secondly the image undertakes a Gaussian blur, this removes a large part of the noise.

The system now has several parameters which has to be set manually by the user:

- contrast,
- intensity (window size) of Gaussian blur,
- Sobel edge detector threshold,

*Should I write down what parameter values I used or is this of too much detail*  
If the user introduces a new dataset these parameters needs to be changed as the image quality and lightning condition are probably different.

## 3.4 Results

The system assumes that the first sharp edge (seen from top to bottom) is always the skyline/building edge. This gives raise to some outliers, for for example a streetlight or a tree. These outliers are removed as described in the next section. The Skyline detector without outlier removal has an accuracy of 80 %  
Some results from the Floriande dataset:

*TODO Results images TODO make UML scheme skyline -j 3d -j etc.*



Figure 1: abc

## 4 Skyline projection

### 4.1 Introduction

The retrieved skyline is used to update a sparse 3D model of the building. This section describes how the skyline of the 2D images are used to get the 3D contour of the building.

*TODO convert to algorithm or method*

### 4.2 Project to 3D space

*TODO situation scheme* Every 2D pixel of an input image presents a 3D point in space. No information is known about the distance from the 3D point to the camera. What is known is the 2D location of the pixel, this reduces the possible points in 3D space to an infinite line. This line is known and spanned by two coordinates:

- The camera center
- $K'p$ , where  $K$  is the Calibration matrix of the camera and  $p$  is the homogeneous pixel coordinate.

*TODO why K’p,I don’t remember the theory behind it and can’t find it in Isaac’s paper* For every skyline pixel a line spanned by the above two coordinates is derived.

### 4.3 Intersect with building

The line is reduced to a point in 3D by intersecting it with a rough indication of the building. This point is used to update the 3D model.

To create a rough indication of the building a top-view photograph of the building is used together with an estimate of the height of the building.

In order to refine this sparse 3D model we need to know which skyline part belongs to which part of the 3D model. This is done as follows.

The building is first divided into different walls. Every wall of the building spans a plane. As described in the previous section every part (pixel) of the skyline presents an infinite line in 3D. Intersections are calculated between these infinite lines and the planes of the building walls.

*Isaac, should I put a intersection formula down here or is this trivial?*

Because the lines and the planes are both infinite and they have a very low change of being exactly parallel, the algorithm returns  $w$  intersections for every skylinepixel (where  $w$  is the number of walls).

Next challenge is to reduce the number of intersection for every skylinepixel to one. In other words, to determine the wall that has the largest probability of being responsible for that pixel. This is ofcourse needed to update the 3D model at the right place.

### 4.4 Find most likely wall

#### 4.4.1 When is a wall responsible?

Lets define the intersection between the projected skylinepixel line and the plane of the wall as intersection point  $isp$ . And the wall sides as  $w1, w2, w3, w4 \in W$ . And  $d$  as a distance measure which is explained later on.

If we assume that a certain wall was responsible for that pixel, the intersection (i.e. projected pixel) must lie either

(1) Somewhere on the wall

or

(2) On a small distance  $d$  from that wall (1) is calculated by testing if the pixel lies inside the polygonal representation of the wall. This is done using the Matlabs `buildin` in-polygon algorithm. If this test succeeds we consider  $d$  to be 0.

(2) Note that this is treated as an inlier because the 3D model is sparse and the height of the building is estimated. It is calculated as follows:

First the distances from  $isp$  to four wall sides are calculated. For every wall the minimum distance is stored.

$$\min_{w \in W} d(isp, w)$$

This is done for every wall. The wall with the smallest distance is the one that most likely presents the pixel.

$\text{argmin}_{W \in \text{Walls}}(\min_{w \in W} d(isp, w))$

*do I write this down correctly?*

If there are two (or even more) walls that are classified equally well to present the pixel (that is if they succeed the in-polygon or have exactly the same  $d$  value) then the nearest wall is selected. The nearest wall is calculated by taking the wall with the smallest distance from the  $isp$  to the camera center. *formula here? or: trivial?*

How this intersection point - wall distance  $d$  is calculated is explained in the next section.

#### 4.4.2 Calculate the intersection point - wall distance

A wall consists of four corner points. The corner-point pairs that are on a side of the wall connect line segments, there are four line segments. These line segments span infinite lines.

The intersection point ( $isp$ ) is projected orthogonally on these four lines, a projected  $isp$  is called  $isp_{proj}$ . *todo image? todo projection formula?*

If  $isp$  is close to a wallside,  $e(isp, isp_{proj})$  (where  $e$  is defined as the Euclidean distance) is small. But this doesn't mean that if  $e(isp, isp_{proj})$  is small  $isp$  is always close to the wall. In fact there are some candidates that happen to have a very small  $d(isp, isp_{proj})$  but in fact lie far away from the wall. This is because  $isp$  is projected to an infinite line spanned by the wallside and could be projected far next to the wallside. *An example can be seen in figure: TODO Figure* Because of this artefact, it is not robust to calculate the perpendicular projection distance. Instead  $d$  is calculated differently if  $isp_{proj}$  doesn't lie on the wallside. In this case the Euclidean distance between  $isp_{proj}$  and the closest corner-point of the wallside is returned.

Formally: Let  $c1, c2, c3, c4 \in \text{Cornerpoints}$  be the corners of a wall.

Let  $\text{between}(a, b, c)$  be a function that returns true if  $a$  lies between  $b$  and  $c$ .

if  $\text{between}(isp_{proj}, c1, c2)$

$d = e(isp, isp_{proj})$

otherwise

$d = \min_{c \in \text{Cornerpoints}} e(isp, c)$

*TODO nice latex code with large } sign*

#### 4.4.3 Appendix?: Determine whether $isp_{proj}$ lies on or next to a wallsegment

To determine whether the  $isp_{proj}$  lies on or next to a wallsegment the projection calculation is skipped and  $isp$  is used instead together with a computational

cheap trick.

*todo insert [http://softsurfer.com/Archive/algorithm\\_0102/Pic\\_segment.gif](http://softsurfer.com/Archive/algorithm_0102/Pic_segment.gif) here*  
First consider Figure ?? , the angles between the segment P0P1 and the vectors P0P and P1P from the segment endpoints to P. If both angles are equal to or less than  $90^\circ$  then the  $isp_{proj}$  will be on the line segment P0 P1. If not, the  $isp_{proj}$  lies to the left or to the right of segment P according to whether one of the angles is acute or obtuse. The angles are acute or obtuse if the dot product of the vectors involved are respectively positive or negative.

To summarize: determining in which region the  $isp_{proj}$  lies is boiled down to two dot product calculations with the advantage that the actual projection calculation can be skipped.

*Todo come back on outlier removal*

## 4.5 Results

# 5 Update 3D model

# 6 References

- [1] Castano, Automatic detection of dust devils and clouds on Mars.
- [9] Cozman, Outdoor visual position estimation for planetary rovers.