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- MODULE ReliableBroadcast
EXTENDS LearnerGraph, FiniteSets
CONSTANTS
    LG, the learner graph
    B, the set of malicious acceptors
    W, the set of well-behaved acceptors, i.e. honest and available
    V the set of values that can be broadcast
Assume B \cap W = \{\}
Assume IsValidLearnerGraph(LG)
Learner \triangleq LG.learners
Acceptor \triangleq LG.acceptors
HonestAcceptor \triangleq Acceptor \setminus B
 Note that HonestAcceptor is not necessary equal to W
  --algorithm ReliableBroadcast{
    variables
         bcast \in (SUBSET\ V) \setminus \{\{\}\}\}; the value(s) broadcast; multiple values model a malicious sender
         echo = [a \in Acceptor \mapsto \{\}];
         ready = [a \in Acceptor \mapsto [l \in Learner \mapsto \{\}]];
    define {
         ProvenMalicious(a) \triangleq \exists v1, v2 \in V:
              \wedge v1 \neq v2
              \land \{v1, v2\} \subseteq echo[a]
         NotEntangled(l1, l2) \triangleq
              \wedge l1 \neq l2 a learner is always entangled with itself
              \land \forall S \in LG.safeSets[\langle l1, l2 \rangle]:
                    \exists a \in S : ProvenMalicious(a)
    fair process ( learner \in Learner )
         variables
             output = \langle \rangle;
        with ( v \in V ) {
             when \exists Q \in LG.quorums[self]:
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 $\forall a \in Q : v \in ready[a][self];$

output := v;

} }

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process ( acceptor \in HonestAcceptor ) {
l0:
        while (TRUE)
        either
            with (v \in V)
                 when v \in bcast \land echo[self] = \{\};
                 echo[self] := echo[self] \cup \{v\};
             }
        \mathbf{or}
            with (v \in V)
            with (l \in Learner)
            with ( Q \in LG.quorums[l] ) {
                 when ready[self][l] = \{\};
                 when \forall a \in Q : v \in echo[a];
                  check for conflicts:
                 when \forall l2 \in Learner : \forall v2 \in V \setminus \{v\} :
                     v2 \in ready[self][l2] \Rightarrow NotEntangled(l, l2);
                 ready[self][l] := ready[self][l] \cup \{v\};
             }
        \mathbf{or}
            with (v \in V)
            with ( l1 \in Learner, l2 \in Learner ) {
                 when v \in bcast;
                 when \forall Q \in LG.quorums[l1]:
                     \exists a2 \in Q : v \in ready[a2][l2];
                  check for conflicts:
                 when \forall l3 \in Learner \setminus \{l1\} : \forall v2 \in V \setminus \{v\} :
                     v2 \in ready[self][l3] \Rightarrow NotEntangled(l1, l3);
                 ready[self][l1] := ready[self][l1] \cup \{v\};
             }
         }
    process ( byzAcceptor \in B ) {
l0:
        while (TRUE) {
            either
            with (v \in V)
                 echo[self] := echo[self] \cup \{v\}
            or
            with ( l \in Learner ) {
                 with (v \in V)
                     ready[self][l] := ready[self][l] \cup \{v\};
             }
         }
     }
 }
```

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TypeOK \triangleq
      \land \ bcast \in (\texttt{SUBSET} \ V) \setminus \{\{\}\}
      \land echo \in [Acceptor \rightarrow (SUBSET V)]
      \land ready \in [Acceptor \rightarrow [Learner \rightarrow (SUBSET V)]]
      \land \quad output \in [Learner \to V \cup \{\langle \rangle \}]
Two learners must agree if one of their safe sets is fully well-behaved: Entangled(l1,\ l2)\ \stackrel{\triangle}{=}\ \exists\ S\in LG.safeSets[\langle l1,\ l2\rangle]:
     S \cap B = \{\}
LiveLearner \stackrel{\Delta}{=} \{l \in Learner : 
     \exists Q \in LG.quorums[l] : Q \subseteq W\}
Safety \triangleq
      \land \ \forall \, l \in Learner:
            \land pc[l] = "Done"
            \land \exists Q \in LG.quorums[l] : Q \cap B = \{\} SafeLearner
            \Rightarrow output[l] \in bcast
       \land \forall l1, l2 \in Learner:
            \land Entangled(l1, l2)
            \wedge pc[l1] = "Done"
            \land pc[l2] = "Done"
            \Rightarrow output[l1] = output[l2]
Liveness \triangleq
      \land \quad Cardinality(bcast) = 1 \Rightarrow
                 \forall l \in LiveLearner : \Diamond(pc[l] = \text{``Done''} \land bcast = \{output[l]\})
       This one is interesting (I think this is the best we can guarantee):
       \land \forall l1 \in Learner : \forall l2 \in LiveLearner : Entangled(l1, l2) \Rightarrow
               \Box(pc[l1] = \text{"Done"} \Rightarrow \Diamond(pc[l2] = \text{"Done"}))
FairSpec \triangleq
      \land Spec
      \land \forall a \in W : WF_{vars}(acceptor(a))
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