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- Module ReliableBroadcast -
EXTENDS LearnerGraph, FiniteSets
CONSTANTS
    LG, the learner graph
    B, the set of malicious acceptors
    W, the set of well-behaved acceptors, i.e. honest and available
    V the set of values that can be broadcast
Assume B \cap W = \{\}
Assume IsValidLearnerGraph(LG)
Learner \triangleq LG.learners
Acceptor \triangleq LG.acceptors
HonestAcceptor \triangleq Acceptor \setminus B
 Note that HonestAcceptor is not necessary equal to W
  --algorithm ReliableBroadcast{
    variables
         bcast \in \left( \text{SUBSET} \;\; V \right) \setminus \left\{ \left\{ \right\} \right\} \;; \quad \text{the value(s) broadcast; multiple values model a malicious sender} \;
        echo = [a \in Acceptor \mapsto \{\}];
        ready = [a \in Acceptor \mapsto [l \in Learner \mapsto \{\}]];
    define {
        ProvenMalicious(a) \triangleq \exists v1, v2 \in V:
             \wedge v1 \neq v2
             fair process ( learner \in Learner )
        variables
             output = \langle \rangle;
        with ( v \in V ) {
l0:
            when \exists Q \in LG.quorums[self]:
                \forall a \in Q : v \in ready[a][self];
            output := v;
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}

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process ( acceptor \in HonestAcceptor ) {
l0:
        while (TRUE)
        either
            with ( v \in V ) {
                 when v \in bcast \land echo[self] = \{\};
                 echo[self] := echo[self] \cup \{v\};
             }
        \mathbf{or}
            with (v \in V)
            with (l \in Learner)
            with ( Q \in LG.quorums[l] ) {
                 when ready[self][l] = \{\};
                 \mathbf{when} \,\, \forall \, a \in \mathit{Q} : v \  \, \in \mathit{echo}[a] \, ;
                 ready[self][l] := ready[self][l] \cup \{v\};
             }
        \mathbf{or}
            with ( v \in V )
            with (l \in Learner)
            with ( readyForV = \{a \in Acceptor : v \in ready[a][l]\} ) {
                 when \forall Q \in LG.quorums[l]:
                     \vee Q \cap readyForV \neq \{\}
                      TODO: this is wrong:
                      \vee \exists a \in Q : ProvenMalicious(a);
                 ready[self][l] := ready[self][l] \cup \{v\};
             }
     }
    process ( byzAcceptor \in B ) {
        while (TRUE) {
l0:
            with (v \in V)
                 echo[self] := echo[self] \cup \{v\};
            with (rdy \in [Learner \rightarrow V])
                 ready[self] := [l \in Learner \mapsto ready[self][l] \cup \{rdy[l]\}];
             }
         }
     }
 }
```

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TypeOK \triangleq
      \land \ bcast \in (\texttt{SUBSET} \ V) \setminus \{\{\}\}
      \land echo \in [Acceptor \rightarrow (SUBSET V)]
      \land ready \in [Acceptor \rightarrow [Learner \rightarrow (SUBSET V)]]
      \land \quad output \in [Learner \to V \cup \{\langle \rangle \}]
Two learners must agree if one of their safe sets is fully well-behaved: Entangled(l1,\ l2)\ \stackrel{\triangle}{=}\ \exists\ S\in LG.safeSets[\langle l1,\ l2\rangle]:
      S \cap B = \{\}
LiveLearner \stackrel{\Delta}{=} \{l \in Learner :
      \exists Q \in LG.quorums[l] : Q \subseteq W\}
Safety \triangleq
      \land \ \forall \, l \in Learner:
            \land pc[l] = "Done"
            \land \exists Q \in LG.quorums[l] : Q \cap B = \{\}
            \Rightarrow \exists l2 \in Learner : output[l] \in bcast
      \land \forall l1, l2 \in Learner:
            \land Entangled(l1, l2)
            \wedge pc[l1] = "Done"
            \land pc[l2] = "Done"
            \Rightarrow output[l1] = output[l2]
Liveness \triangleq
      \land \quad Cardinality(bcast) = 1 \Rightarrow
                 \forall \, l \in \mathit{LiveLearner} : \Diamond(\mathit{pc}[l] = \text{``Done''} \land \mathit{bcast} = \{\mathit{output}[l]\})
        This one is interesting (I think this is the best we can guarantee):
       \land \forall l1, l2 \in LiveLearner : Entangled(l1, l2) \Rightarrow
               \Box(pc[l1] = \text{"Done"} \Rightarrow \Diamond(pc[l2] = \text{"Done"}))
FairSpec \triangleq
      \land Spec
      \land \forall a \in W : WF_{vars}(acceptor(a))
```