

# Multiclass classification with neural networks

Softmax regression

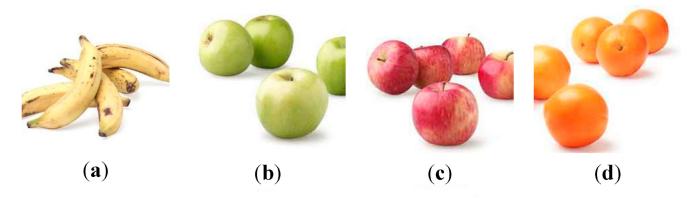
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From: Wang et al., 2015 (Entropy)

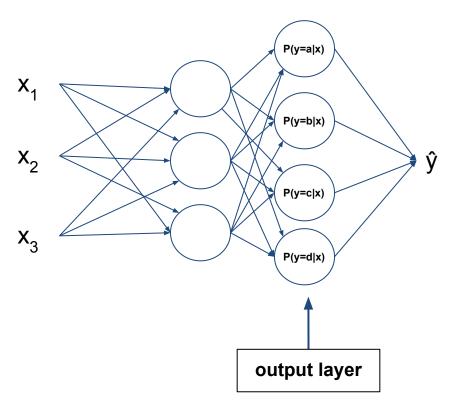
- **more than two classes** to recognize
- in this case, 4 classes: bananas, green apples, red apples, oranges
- need to extend logistic regression to estimating the probabilities of samples to belong to each of the four classes











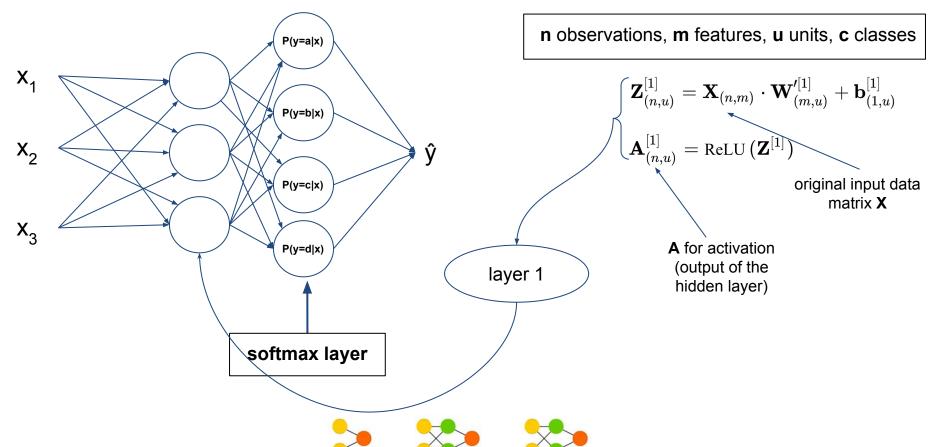
- the output layer has now 4 nodes (instead of just one as in binary classification)
- the activation function is now the softmax function
- this is why the output layer is also called the softmax layer, and multiclass classification is called softmax regression



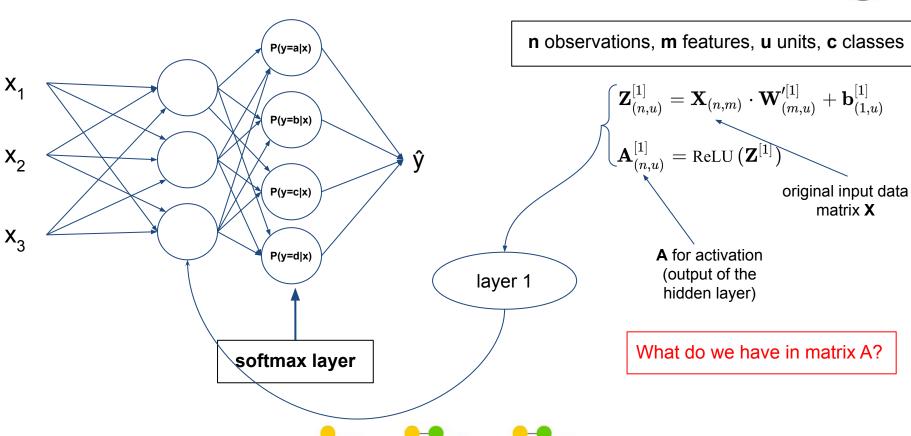




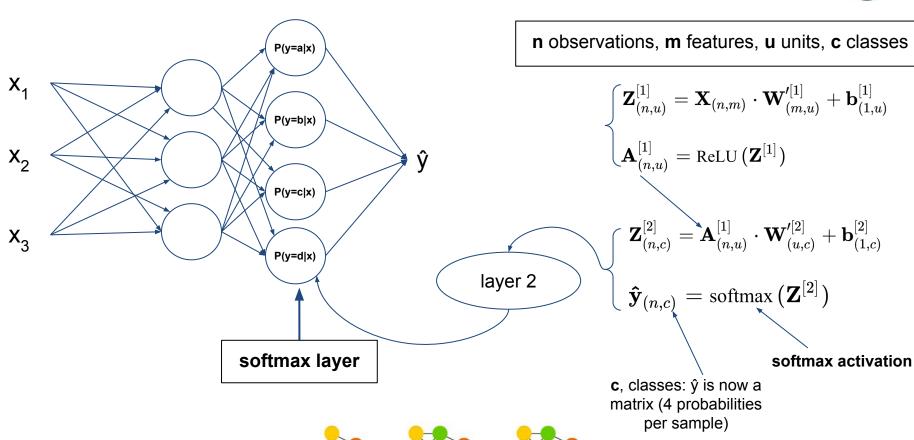




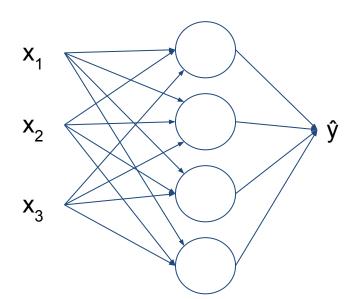












- as we did for binary classification, we can also represent softmax regression with no hidden layers
- this would essentially reduce to multinomial logistic regression, with no neural networks involved
- we'll see this implementation in the ipynb file
   4c, part 1







# Loss function for softmax regression



$$L(\hat{y},y) = -\left(y \cdot \log\left(\hat{y}
ight) + (1-y) \cdot \log\left(1-\hat{y}
ight)
ight) ullet$$

loss function for logistic regression

$$L(\hat{y},y) = -\sum_{j=1}^{c} y_j \cdot \log\left(\hat{y_j}
ight)$$
 — Loss function for softmax regression

- generalization of the loss function for logistic regression over c classes
- you then sum up the loss for each sample (and divide by the number of samples) →
  cost function for the entire dataset







# Loss function for softmax regression



$$L(\hat{y},y) = -\left(y \cdot \log\left(\hat{y}
ight) + (1-y) \cdot \log\left(1-\hat{y}
ight)
ight) leftarrow 0$$

loss function for logistic regression

$$L(\hat{\mathbf{y}},\mathbf{y}) = -\sum_{j=1}^{c} y_j \cdot \log\left(\hat{y_j}
ight)$$
 —

loss function for softmax regression

these are actually vectors of length c (number of classes)!







# Recap



- we can represent logistic and softmax regression as neural networks models
- when we add layers and units we repeat several times the regression model with a twist given by the ReLU activation
- these multiple regression models all use the same input data, but are all different because they learn different weights (parameters)
- as we progress along the layers, we get farther and farther from the original input data → we learn new (more abstract) representations of the data
- when we "go deep" we move away from the linear decision boundaries of logistic (and softmax regression) and learn complex non-linear functions of the data









- multiclass logistic regression
- neural network for softmax regression

→ day2\_code04 keras multiclass classification.ipynb





