

BCBB Workshop

Statistical Testing

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OCICB Bioinformatics and Computational Biosciences Branch (BCBB)

- Part of NIAID
- Group of ~50
- Software developers
- Computational Biologists
- Project Management & Analysis Professionals
- Biostatistics, Phylogenetics, Genomics, Structural Biology, Proteomics, Programming



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How to contact us?

1. Submit Request

Send emails to bioinformatics@niaid.nih.gov OR fill a request online at [Online Request](#)

2. Attend our workshops

http://www.eventzilla.net/user/NIAID_OCICB_BCBB

3. Tell us what statistical topics you want to learn about

[BCBB Statistical Training – Suggest a class!](#)

4. Join our Slack group!

The invitation will be sent out after this workshop



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Learning materials

■ Online Statistics Education: An Interactive Multimedia Course of Study

<http://onlinestatbook.com/2/index.html>

■ Statistics Glossary v1.1

This site is a glossary of statistical terms searchable by topic or in alphabetical order.

Created by Valerie J. Easton & John H. McColl

<http://www.stats.gla.ac.uk/steps/glossary/>



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www.nature.com/nature/authors/gts

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Statistical checklist

Authors providing statistical analysis in their papers are asked to check the following points to ensure statistical adequacy.

It is helpful to the editors and the referees if authors confirm in their submission and resubmission cover letters that they have applied all relevant checks from the list below to the work described in their paper.

IN THE METHODS SECTION:

Type and applicability of test used

- Comparisons of interest are clearly defined
- Name of tests applied are clearly stated
- All statistical methods identified unambiguously
- Justification for use of test is given
- Data meet all assumptions of tests applied (with particular attention paid to non-normal data sets or small sample sizes, which should be identified in the text as such)
- Adjustments made for multiple testing is explained

Details about the test

- n is reported at the start of the study and for each analysis thereafter
- Sample size calculation (or justification) is given
- Unit of analysis is given for all comparisons
- Alpha level is given for all statistical tests
- Tests are clearly identified as one- or two-tailed
- Randomisation procedures or other ways to eliminate bias in sampling (in particular for experiments involving animals) described
- Actual P values are given for primary analyses

Descriptive statistics summary

- n for each data set is clearly stated
- A clearly labelled measure of centre (e.g. mean or median) is given
- A clearly labelled measure of variability (e.g. standard deviation or range) is given
- All numbers following a ± sign are identified as standard errors (s.e.m.) or standard deviations (s.d.)

Anomalies

- Any unusual or complex statistical methods are clearly defined and explained for Nature's wide readership. (Authors are encouraged to use Supplementary Information for long explanations.)
- Any data exclusions are stated and explained
- Any discrepancies in the value of a between analyses are clearly explained and justified
- Any method of treatment assignment (randomization, etc) is explained and justified
- Any data transformations are clearly described and justified

WITHIN INDIVIDUAL GRAPHS:

Distortions

- Any distorted effect sizes (e.g. by truncation of y axis) are clearly labelled and justified

Clear labelling

- Error bars are present on all graphs, where applicable.
- All error bars are clearly labelled

PLEASE HELP US

Many statistical analyses published in Nature are highly sophisticated and outside the scope of this checklist, particularly in the case of some studies in physical sciences disciplines. Authors and referees who have specific suggestions for additional entries to this list are encouraged to send them by e-mail to authors@nature.com or referees@nature.com. Nature will update this checklist at intervals in an effort to ensure that papers published are statistically robust.

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Outline

1. Statistical Testing Process

- 1.1. Formulate Null and Alternative hypotheses
- 1.2. Calculate the appropriate test statistics
- 1.3. Compute the probability of observing the test statistic under the null hypothesis
- 1.4. Make statistical decision and biological conclusion

2. Common Statistical Tests

- 2.1. Choose appropriate tests
- 2.2. Data Preprocessing
- 2.3. Correlation
- 2.4. Two-sample T-test
- 2.5. ANOVA
- 2.6. Multiple Comparisons

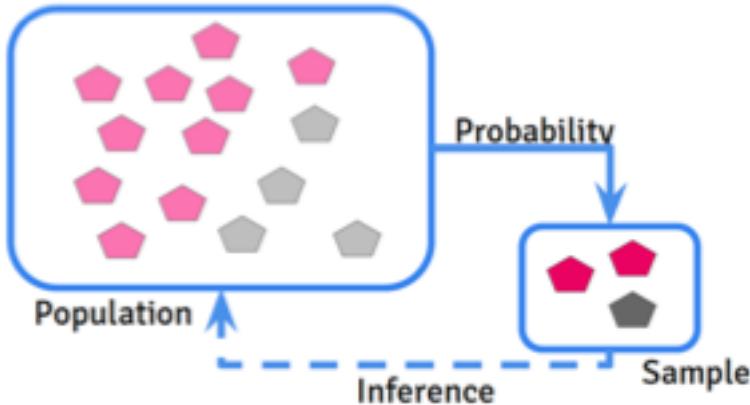
3. Application in Prism and R

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1. Statistical Testing Process

The best way to determine whether a statistical hypothesis is true would be to examine the entire population. Since that is often impractical, researchers typically examine a random sample from the population. If sample data are not consistent with the statistical hypothesis, the hypothesis is rejected.



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1.1. Formulate Null and Alternative hypotheses

- E.g. (null) $H_0: \mu_1 = \mu_2$ vs. (alternative) $H_A: \mu_1 \neq \mu_2$

1.2. Calculate the appropriate test statistics

- E.g. Student's *t*-test, Wilcoxon test, ...

1.3. Compute the probability of observing the test statistic (i.e. your sample data) under the null hypothesis

- i.e. Compute *p*-value and confidence interval

1.4. Make a statistical decision

- "Reject the null hypothesis" or "fail to reject the null hypothesis"

1.5. Make a biological conclusion

- E.g. New drug reduces viral load, vitamin C helps prevent cancer



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1.1. Formulate Null And Alternative Hypotheses

- Two Types of Statistical Hypotheses
- One-Sided vs. Two-sided Tests



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➤ Two Types of Statistical Hypotheses

Null hypothesis: states that a population parameter (such as the mean, the standard deviation, and so on) is equal to a hypothesized value. The null hypothesis is often an initial claim that is based on previous analyses or specialized knowledge.

Alternative hypothesis: states that a population parameter is smaller, greater, or different than the hypothesized value in the null hypothesis. The alternative hypothesis is what you might believe to be true or hope to prove true.

The diagram illustrates the two types of statistical hypotheses using a plant growth experiment. On the left, a green watering can labeled 'X' is shown pouring water onto a small seedling. A question mark is above a dashed box containing a taller, more developed plant. This represents the alternative hypothesis (H_1): Application of bio-fertilizer 'X' increases plant growth. On the right, the same watering can 'X' is shown pouring water onto a small seedling, with a question mark above a dashed box containing a shorter plant. This represents the null hypothesis (H_0): Application of bio-fertilizer 'X' does not increase plant growth. A legend at the bottom defines the terms: 'Alternative hypothesis' is shown with a checkmark and the text 'The alternative hypothesis is a hypothesis which the researcher tries to prove.'; 'Null hypothesis' is also shown with a checkmark and the text 'The null hypothesis is a hypothesis which the researcher tries to disprove, or nullify.'

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➤ One-Sided vs. Two-sided Tests

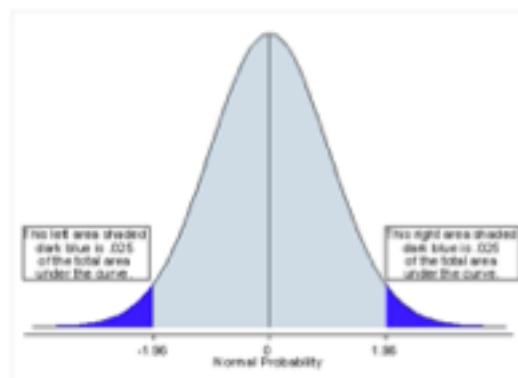
Two-sided Test

If you are using a significance level of α , a two-sided test allots half of your α to test the statistical significance in one direction and half of your α to test statistical significance in the other direction.

For example:

$$\begin{aligned} H_0: \mu &= k \\ H_a: \mu &\neq k. \end{aligned}$$

A two-sided test will test both if the mean is significantly greater than k **AND** if the mean is significantly less than k .



One-sided Test

If you are using a significance level of α , an one-sided test allots all of your α to test the statistical significance in one direction of interest.

For Example:

$$H_0: \mu = k$$

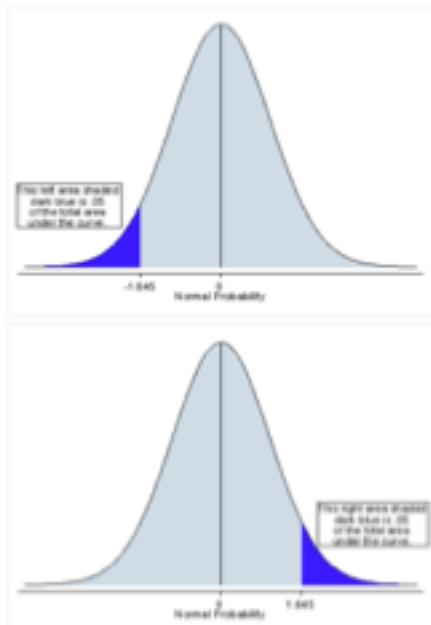
$$H_a: \mu > k$$

or

$$H_0: \mu = k$$

$$H_a: \mu < k.$$

The one-sided test provides more power to detect an effect in one direction by not testing the effect in the other direction.



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When is a one-sided test appropriate?

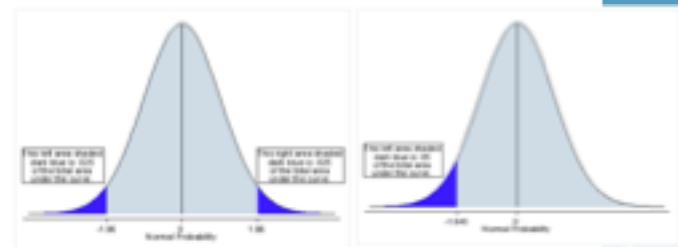
If you consider the consequences of missing an effect in the untested direction and conclude that they are negligible and in no way irresponsible or unethical, then you can proceed with an one-sided test.

For example, developing a new and cheaper drug.

When is an one-sided test NOT appropriate?

- When you have no idea of the direction or it is unacceptable to ignore the effect in the untested direction
- Choosing a one-tailed test for the sole purpose of attaining significance is not appropriate. Choosing a one-tailed test after running a two-tailed test that failed to reject the null hypothesis is not appropriate

	PROS	CONS
One-Tailed Tests	<ul style="list-style-type: none"> • Requires less traffic • Gains significance faster (read: more significance does not equal validity) 	<ul style="list-style-type: none"> • Only accounts for one scenario • Can lead to inaccurate and biased results
Two-Tailed Tests	<ul style="list-style-type: none"> • Accounts for all three scenarios • Leads to accurate and reliable results 	<ul style="list-style-type: none"> • Requires more traffic • Takes longer to gain significance



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1.2. Statistical Tests

- What is Statistical Test
- Variance, Standard Deviation and Spread
- Common Statistical Tests



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➤ What is statistical test

$$\text{Test} = \frac{\text{Difference}}{\text{Error}} = \frac{\text{Statistic} - \text{Null Value}}{\text{Error}}$$

- Almost all tests used in inferential statistics can be generalized as the ratio of a "difference" over an "error"
 - Difference between a statistic and null value (usually 0)
 - A **statistic** is nothing more than a numeric summary of the experimental data with respect to the null hypothesis
 - A **null value** is an assumption about the population under the null hypothesis
 - An **error** is an estimate of the sampling distribution error



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Example: Two-sample Student's T-test

$$T^* = \frac{\text{statistic} \rightarrow \bar{X}_1 - \bar{X}_2 - 0 \leftarrow \text{null value}}{\sqrt{\left(\frac{1}{n_1} + \frac{1}{n_2} \right) \frac{(n_1-1)s_1^2 + (n_2-1)s_2^2}{n_1 + n_2 - 2}}} \leftarrow \text{standard error}$$

- The "statistic" in a two-sample t-test is a difference between the two sample means and the null value is zero
 - The hypothesis $\mu_1 = \mu_2$ implies $\mu_1 - \mu_2 = 0$
- The standard error is an estimate of the common variance



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Variance, Standard Deviation and Spread

The standard deviation of the mean (SD) is the most commonly used measure of the spread of values in a distribution. SD is calculated as the square root of the variance (the average squared deviation from the mean).

Variance in a population is:

$$\sigma^2 = \frac{\sum(x - \mu)^2}{n}$$

[x is a value from the population, μ is the mean of all x, n is the number of x in the population, Σ is the summation]

Variance is usually estimated from a sample drawn from a population. The unbiased estimate of population variance calculated from a sample is:

$$s^2 = \frac{\sum(x_i - \bar{x})^2}{n - 1}$$

[x_i is the ith observation from a sample of the population, \bar{x} is the sample mean, n (sample size) - 1 is degrees of freedom, Σ is the summation]

The spread of a distribution is also referred to as dispersion and variability. All three terms mean the extent to which values in a distribution differ from one another.

SD is the best measure of spread of an approximately normal distribution. This is not the case when there are extreme values in a distribution or when the distribution is skewed, in these situations interquartile range or semi-interquartile are preferred measures of spread. Interquartile range is the difference between the 25th and 75th centiles. Semi-interquartile range is half of the difference between the 25th and 75th centiles. For any symmetrical (not skewed) distribution, half of its values will lie one semi-interquartile range either side of the median, i.e. in the interquartile range. When distributions are approximately normal, SD is a better measure of spread because it is less susceptible to sampling fluctuation than (semi-)interquartile range.

If a variable y is a linear ($y = a + bx$) transformation of x then the variance of y is b² times the variance of x and the standard deviation of y is b times the variance of x.

The standard error of the mean is the expected value of the standard deviation of means of several samples, this is estimated from a single sample as:

$$SEM = \frac{s}{\sqrt{n}}$$

[s is standard deviation of the sample mean, n is the sample size]

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Flow Chart for Selecting Commonly Used Statistical Tests

```

graph TD
    PA([Parametric Assumptions:  
1. Independent, unbiased samples  
2. Data normally distributed  
3. Equal variances]) --> TypeData[Type of data?]
    TypeData -- Continuous --> TypeQ[Type of question]
    TypeData -- Discrete, categorical --> ChiSquare[Chi-square tests  
one and two sample]
    
    TypeQ -- Relationships --> DoIV[Do you have a true independent variable?]
    DoIV -- Yes --> Regression[Regression Analyses]
    DoIV -- No --> Correlation[Correlation Analysis]
    
    TypeQ -- Differences --> DiffQ[Differences between what?]
    DiffQ -- Means --> TestEV[Tests for Equal Variances  
Fmax test, Brown and Smythe's test, Bartlett's tests]
    TestEV --> NumGroupsQ[How many treatment groups?]
    
    NumGroupsQ -- Two groups --> ParamAss1Q[Parametric assumptions satisfied?]
    ParamAss1Q -- Yes --> StudentT[Student's unpaired t-test, Paired t-test]
    ParamAss1Q -- No --> DataTransform1[Data transform worked?]
    DataTransform1 -- Yes --> MannWhitneyU[Mann-Whitney U or Wilcoxon Rank sums test]
    DataTransform1 -- No --> Nonparametric1[Nonparametric]
    
    NumGroupsQ -- More than two groups --> ParamAss2Q[Parametric assumptions satisfied?]
    ParamAss2Q -- Yes --> ANOVA[ANOVA]
    ParamAss2Q -- No --> DataTransform2[Data transform worked?]
    DataTransform2 -- Yes --> KruskalWallis[Kruskal-Wallis Test]
    DataTransform2 -- No --> Nonparametric2[Nonparametric]
    
    Nonparametric1 --> DunnTest[Dunn's Test]
    Nonparametric2 --> DunnTest
    
    IfPostHoc[If significant, do a post hoc test, e.g. Tukey's or Bonferroni's] --> ANOVA
  
```

How to choose appropriate statistical test?

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Parametric vs. Non-parametric Tests?

In practice:

- Parametric statistical procedures rely on assumptions about the shape of the distribution (i.e., assume a normal distribution) in the underlying population and about the form or parameters (i.e., means and standard deviations) of the assumed distribution.
- Nonparametric statistical procedures rely on **NO** or **FEW** assumptions about the shape or parameters of the population distribution from which the sample was drawn.



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Why don't we always use nonparametric tests?

Two Main Drawbacks.

- Nonparametric tests generally are less statistically powerful than parametric procedures when the data truly are approximately normal.
- The results of nonparametric tests are often harder to interpret than the results of parametric tests because many nonparametric tests use rankings of the values in the data rather than using the actual data.

--> In short, nonparametric procedures are useful in many cases and necessary in some, but they are not a perfect solution.



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Outline

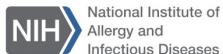
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1.3. Probability of Observing the Test Statistic under the Null Hypothesis

➤ P-value

- *What is p-value*
- *How to calculate p-value*
- *How to interpret p-value*

➤ Confidence Interval

- *What is confidence interval*
- *How to calculate confidence interval*
- *Z-intervals vs. T-intervals*
- *How to interpret confidence interval*



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P-value

- P-value is a measure of strength of the evidence against null hypothesis.
- P-value is the probability of getting the observed value of test statistic, or value with even greater evidence against null hypothesis (H_0), if the null hypothesis of a study question is true. For example, tossing a coin 10 times.
- P-value is NOT the probability of the means in the two samples being equal



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How to calculate p-value?

1. Obtained according to the asymptotic distribution of the test statistic
 - *When the sample size is sufficiently large.*
 - *E.g: Student's t-test*
2. Calculate p-value empirically.
 - *E.g: Fisher's exact test*
3. Resampling-based procedures
 - *When the asymptotic distribution is either unreliable due to insufficient sample size or unavailable for complicated test statistics*
 - *E.g: permutation or bootstrap*

[Comparison between resampling methods](#)



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Example:

Suppose a pharmaceutical company manufactures ibuprofen pills. They need to perform some quality assurance to ensure they have the correct dosage, which is supposed to be 500 milligrams. This is a two-sided test because if the company's pills are deviating significantly in either direction, meaning there are more than 500 milligrams or less than 500 milligrams, this will indicate a problem.

$$H_0: \mu = 500 \text{ mg}$$

$$H_A: \mu \neq 500 \text{ mg}$$

In a random sample of 125 pills, there is an average dose of 499.3 milligrams. The standard deviation of the population is known as 6 milligrams. Because this is quantitative data, 500 mg is the population mean. We can use the following formula to calculate the z-score:

$$z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}}$$

$$\bar{x} = \text{sample mean} = 499.3 \text{ mg}$$

$$\mu = \text{population mean} = 500 \text{ mg}$$

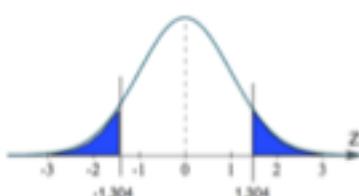
$$\sigma = \text{population standard deviation} = 6 \text{ mg}$$

$$n = \text{sample size} = 125$$

$$z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}} = \frac{499.3 - 500}{\frac{6}{\sqrt{125}}} = \frac{-0.7}{\frac{6}{\sqrt{125}}} = \frac{-0.7}{\frac{6}{11.18}} = \frac{-0.7}{0.53667} = -1.304$$



We get a z-score of negative 1.304. Because this is a two-sided test, it is not enough to just look at the left tail. We also have to look at the equivalent of the right tail, or a positive 1.304.



The first way to find the p-value is to use the z-table. In the z-table, the left column will show values to the tenths place, while the top row will show values to the hundredths place. If we have a z-score of -1.304, we need to round this to the hundredths place, or -1.30. In the left column, we will first find the tenths place, or -1. In the top row, we will find the hundredths place, or 0.

This results in a p-value of 0.0968, or 9.68%, for a z-score of negative 1.304. We also need to take the positive 1.304 into account, which is the upper right tail. To calculate the true p-value, we just need to multiply 0.0968 by two, or 0.1936. This would be a p-value of 19.36%.



How to interpret p-value?

In the majority of analyses, an alpha of 0.05 is used as the cutoff for significance.

- If the p-value is less than 0.05, we reject the null hypothesis that there's no difference between the means and conclude that a significant difference does exist.
- If the p-value is larger than 0.05, we *cannot* conclude that a significant difference exists.



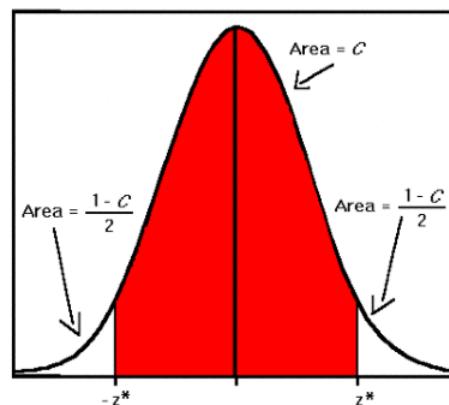
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Confidence Interval

"A confidence interval gives an estimated range of values which is likely to include an unknown population parameter, the estimated range being calculated from a given set of sample data."

----- Valerie J. Easton and John H. McColl's [Statistics Glossary v1.1](#)

Strictly speaking a 95% confidence interval means that if we were to take 100 different samples and compute a 95% confidence interval for each sample, then approximately 95 of the 100 confidence intervals will contain the true mean value (μ).



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How to calculate confidence interval?

1. Obtained according to the asymptotic distribution of the test statistic
 - *When the sample size is sufficiently large.*
2. Resampling-based procedures
 - *When the asymptotic distribution is either unreliable due to insufficient sample size or unavailable for complicated test statistics*
 - *E.g: permutation or bootstrap*



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The **confidence interval estimate (CI)** is consist of:

- Point estimate, e.g., the sample mean
- Investigator's desired level of confidence C (most commonly 95%)
- Sampling variability or the standard error of the point estimate.



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Z-Intervals

Use a z-interval when:

the sample size is greater than or equal to 30 and population standard deviation known OR Original population normal with the population standard deviation known.

Formula for the z-interval

If these conditions hold, we will use this formula for calculating the confidence interval:

$$\bar{x} \pm z_c \left(\frac{\sigma}{\sqrt{n}} \right)$$

where z_c is a critical value from the normal distribution (see below) and n is the sample size.

Common values of z_c are:

CONFIDENCE LEVEL	CRITICAL VALUE
90%	1.645
95%	1.96
99%	2.575



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❖ Understanding the t-distribution and its normal approximation

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Example using a z-interval

Suppose that in a sample of 50 college students in Illinois, the mean credit card debt was \$346. Suppose that we also have reason to believe (from previous studies) that the population standard deviation of credit card debts for this group is \$108. Use this information to calculate a 95% confidence interval for the mean credit card debt of all college students in Illinois.

Solution

Since we wish to estimate the mean, we immediately know we will be using either a t-interval or a z-interval. Looking a bit closer, we see that we have a large sample size ($n = 50$) and we know the population standard deviation. Therefore, we will use a z-interval with $z_c = 1.96$. From reading the problem, we also have:

- Mean is \$346: $\bar{x} = 346$
- Population standard deviation is 108: $\sigma = 108$

Applying the formula:

$$\bar{x} \pm z_c \left(\frac{\sigma}{\sqrt{n}} \right)$$

$$346 \pm 1.96 \left(\frac{108}{\sqrt{50}} \right)$$

The \pm indicates that we need to perform two different operations: a subtraction and an addition.

Left hand endpoint:

$$346 - 1.96 \left(\frac{108}{\sqrt{50}} \right) = 316.1$$

Right hand endpoint:

$$346 + 1.96 \left(\frac{108}{\sqrt{50}} \right) = 375.9$$

This gives our 95% confidence interval for μ , the population mean, as $(316.1, 375.9)$.



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T-Intervals:

Use a t-interval when:

Population standard deviation UNKNOWN and original population normal OR sample size greater than or equal to 30 and Population standard deviation UNKNOWN.

Formula for the t-interval

The formula for a t-interval is:

$$\bar{x} \pm t_c \left(\frac{s}{\sqrt{n}} \right)$$

where t_c is a critical value from the t-distribution, s is the sample standard deviation and n is the sample size.

Finding t_c

The value of t_c depends on the sample size through the use of "degrees of freedom" where $df = n - 1$. We will use this to look up the value of t_c in a table (a nice [free version of that table can be found here](#), or typically in the back of your textbook if you are currently taking a class).



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Example using a t-interval

Suppose that a sample of 38 employees at a large company were surveyed and asked how many hours a week they thought the company wasted on unnecessary meetings. The mean number of hours these employees stated was 12.4 with a standard deviation of 5.1. Calculate a 99% confidence interval to estimate the mean amount of time all employees at this company believe is wasted on unnecessary meetings each week.

Solution

As before, since we are estimating a mean with a confidence interval, we know it will either be a t-interval or a z-interval. In this case, we have a large sample ($n = 38$), but we only have the sample standard deviation. If you aren't sure of that - read closely. The standard deviation of 5.1 was in the context of the sample, so $s = 5.1$. Thus, we will go ahead and use a t-interval since σ is unknown.

Before we can do that however, we need to look up the critical value. To know which row in the t-table to look at, we find the degrees of freedom which is $n - 1 = 38 - 1 = 37$. Using the table linked [here](#):

df	Confidence Intervals, α					
	99%	98%	95%	90%	80%	99.9%
Level of Significance for One-Tailed Test, α						
37	2.770	2.763	2.708	2.478	2.328	3.080
38	2.767	2.760	2.705	2.473	2.323	3.074
39	2.764	2.757	2.702	2.470	2.320	3.068
40	2.762	2.755	2.700	2.468	2.318	3.062

Now that we have that, we plug the values into the formula and do the calculations to get our two endpoints. Remember that we have:

- Sample mean: $\bar{x} = 12.4$
- Sample size: $n = 38$
- Sample standard deviation: $s = 5.1$
- Critical value: $t_c = 2.715$



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Therefore the interval is:

$$\bar{x} \pm t_c \left(\frac{s}{\sqrt{n}} \right)$$

$$12.4 \pm 2.715 \left(\frac{5.1}{\sqrt{38}} \right)$$

This gives us the following two endpoints for our interval.

Left hand endpoint:

$$12.4 - 2.715 \left(\frac{5.1}{\sqrt{38}} \right) = 10.2$$

Right hand endpoint:

$$12.4 + 2.715 \left(\frac{5.1}{\sqrt{38}} \right) = 14.6$$

99% Confidence Interval for μ : (10.2, 14.6)

Interpretation

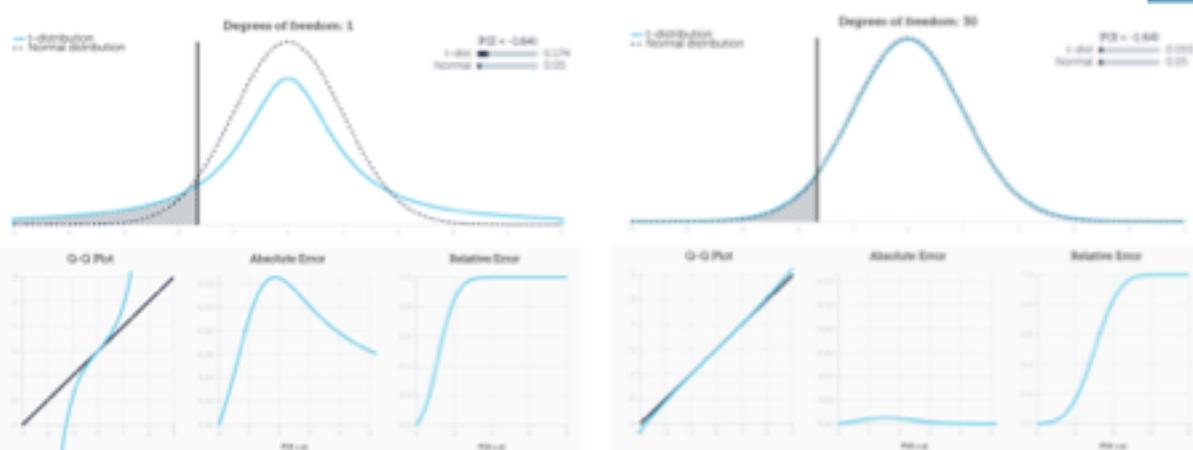
"We are 99% confident that the mean amount of time that all employees at this company think is wasted on meetings each week is between 10.2 and 14.6 hours."



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Understanding the t-distribution and its normal approximation



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❖ [Interactive reference with different degrees of freedom](#)

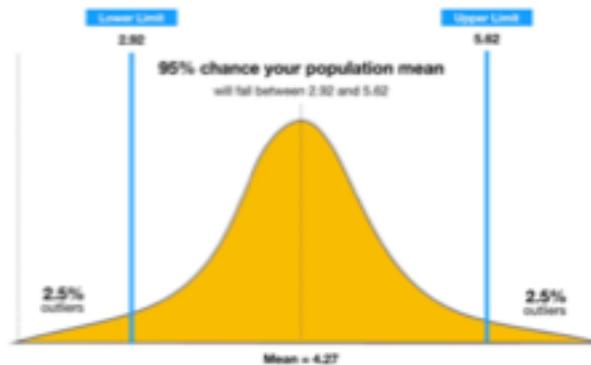
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How to interpret confidence interval?

Once you have taken a sample and constructed the confidence interval (CI), there is no longer any “randomness” left in a CI statement

That is, when reporting a CI:

- “I am 95% confident that the mean is between 25.1 and 32.6” is correct.
- “There is a 95% probability that the mean is between 25.1 and 32.6” is WRONG. Either μ is in that interval or not; there is no probability associated with it.



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95% Confidence Interval simply means that if I take out samples a large number of times (tending to infinity) from a population with 0.05 significance level then 95% of those intervals will encompass the true parameter value.

There are two cases throwing a ball into a mug or throwing mug over a fixed lying ball. Most people think Confidence Interval as the first case but the things are other way round.

Randomness is not associated with parameter but the randomness is associated with interval. True parameters are fixed. But intervals estimated are random.

Roughly you can understand it like this. It is like, a ball (true parameter) is lying and you are throwing a mug(CI with 0.05 significance level) over it a large number of times. And asymptotically 95% of those throws will cover the ball.

So if I say in terms of frequentist then in future if you take out a sample with 95% CI then there is 0.95 probability that it will encompass true parameter value.



Ring
Toss
Game



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❖ [More Details](#)

Outline

1. Statistical Testing Process

- 1.1. Formulate Null and Alternative hypotheses
- 1.2. Calculate the appropriate test statistics
- 1.3. Compute the probability of observing the test statistic under the null hypothesis
- 1.4. Make statistical decision and biological conclusion**

2. Common Statistical Tests

- 2.1. Choose appropriate tests
- 2.2. Data Preprocessing
- 2.3. Correlation
- 2.4. Two-sample T-test
- 2.5. ANOVA
- 2.6. Multiple Comparisons

3. Application in Prism and R



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1.4. Statistical Decision and Biological Conclusions

- Statistical Decision
 - Type I and Type II errors
- Biological Conclusions



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- A **statistical decision** is a choice to “reject the null hypothesis” or “fail to reject the null hypothesis”
 - The decision is based on a critical value or decision rule
 - E.g. Reject the null hypothesis if $p\text{-value} < 0.05$
- A **biological conclusion** is the final interpretation of the statistical testing process in plain language
 - E.g. Vitamin C prevents cancer, drug reduced viral loads, ...
 - Make sure conclusion can be justified by the hypotheses



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Type I and Type II Errors

- **Type I error (“false positive”):** The error of rejecting a TRUE null hypothesis.
- **Type II error (“false negative”):** The error of not rejecting a FALSE null hypothesis

For example, when the null hypothesis is “You’re not pregnant”, and the alternative hypothesis is “You are pregnant”:



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The chances of committing these two types of errors are inversely proportional

- To decrease the chance of committing Type I error: make your alpha (p) value more stringent.
- To decrease the chance of committing Type II error: increase your analyses' power by either increasing your sample size or relaxing your alpha level

	H ₀ rejected	Fail to reject H ₀
H ₀ false	Correct	Type II error
H ₀ true	Type I error	correct

$$\text{Alpha } (\alpha) = \text{Prob}(\text{Type I error})$$

$$\text{Beta } (\beta) = \text{Prob}(\text{Type II error})$$

$$\text{Power} = 1 - \beta$$



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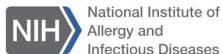
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2.1. Choose Appropriate Tests

We might need to answer some questions:

1. *How many independent variables/factors?*
 2. *How many levels do the independent variables have? i.e, how many groups do we have?*
 3. *What is the nature of the independent variables/factors? Continuous? Categorical?*
 4. *What is the nature of the dependent variable? ordinal or nominal?*
 5. *Is the dependent variable normally distributed?*
-



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Useful References for choosing appropriate tests

1. Choosing the Correct Statistical Test in SAS, Stata, SPSS and R ([link](#))
 - *The flow chart to choose the best statistical test and the related codes with SAS, Stata, SPSS and R*
2. Summary and Analysis of Extension Program Evaluation in R ([link](#))
 - *A dictionary of statistical testing methods and the related R codes*
3. Analysis Data Model (ADaM) Examples in Commonly Used Statistical Analysis Methods ([link](#))
 - *Commonly used statistical analysis methods in clinical trials (proved by FDA)*



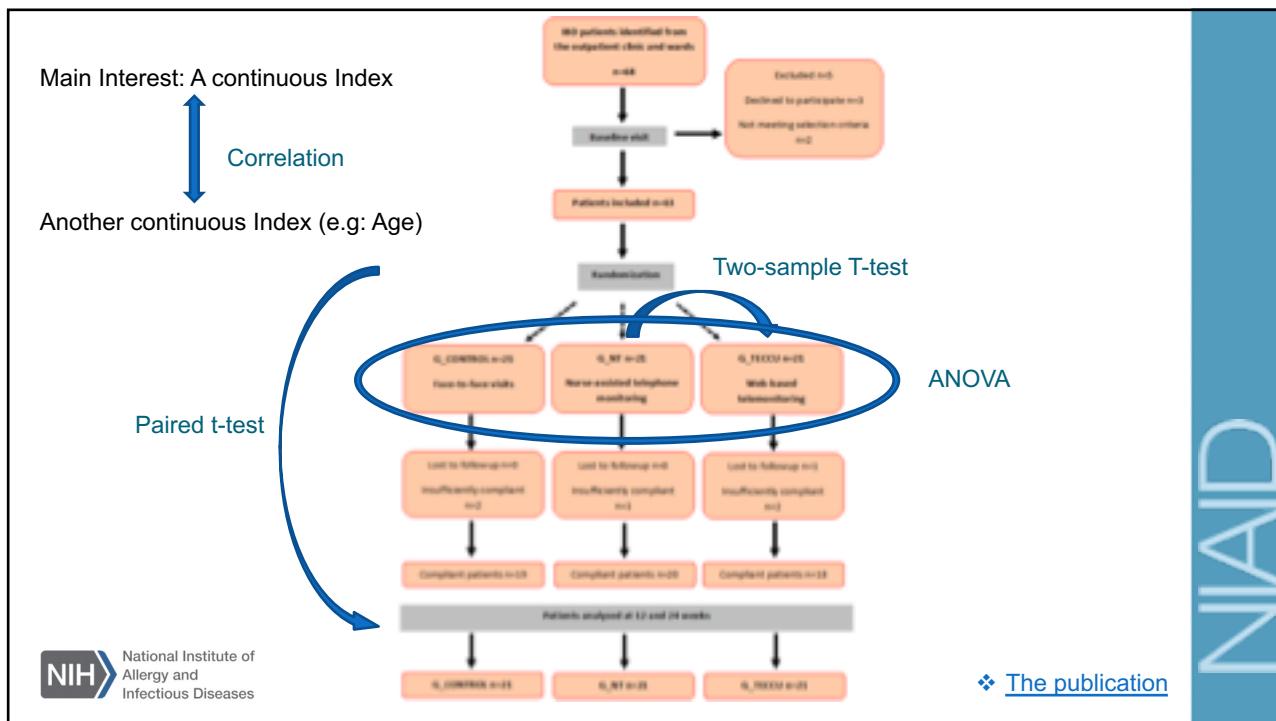
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Common Statistical Tests

Type of Test:	Use:
Correlational	These tests look for an association between variables
Pearson correlation	Tests for the strength of the association between two continuous variables
Spearman correlation	Tests for the strength of the association between two ordinal variables (does not rely on the assumption of normal distributed data)
Chi-square	Tests for the strength of the association between two categorical variables
Comparison of Means:	
Paired T-test	Tests for difference between two related variables
Independent T-test	Tests for difference between two independent variables
ANOVA	Tests the difference between group means after any other variance in the outcome variable is accounted for
Regression:	
Simple regression	Tests how change in the predictor variable predicts the level of change in the outcome variable
Multiple regression	Tests how change in the combination of two or more predictor variables predict the level of change in the outcome variable
Non-parametric:	
are used when the data does not meet assumptions required for parametric tests	
Wilcoxon rank-sum test	Tests for difference between two independent variables - takes into account magnitude and direction of difference
Wilcoxon sign-rank test	Tests for difference between two related variables - takes into account magnitude and direction of difference
Sign test	Tests if two related variables are different – ignores magnitude of change, only takes into account direction



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Analysis Type	Example	Parametric Procedure	Nonparametric Procedure
Compare means between two distinct/independent groups	Is the mean systolic blood pressure (at baseline) for patients assigned to placebo different from the mean for patients assigned to the treatment group?	Two-sample t-test	Wilcoxon rank-sum test
Compare two quantitative measurements taken from the same individual	Was there a significant change in systolic blood pressure between baseline and the six-month follow-up measurement in the treatment group?	Paired t-test	Wilcoxon signed-rank test
Compare means between three or more distinct/independent groups	If our experiment had three groups (e.g., placebo, new drug #1, new drug #2), we might want to know whether the mean systolic blood pressure at baseline differed among the three groups?	Analysis of variance (ANOVA)	Kruskal-Wallis test
Estimate the degree of association between two quantitative variables	Is systolic blood pressure associated with the patient's age?	Pearson coefficient of correlation	Spearman's rank correlation

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Outline

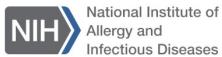
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2.2.Data Preprocessing

- Data Transformation
- Missing Data



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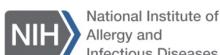
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Data Transformation

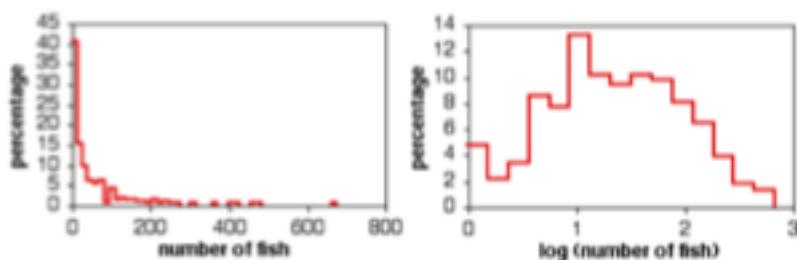
Assumption: Normal distribution?

If your data do not come from Normal distributions, you have three options:

- Your best option is to transform the values to make the distributions more normal.
- Use the nonparametric procedures instead of parametric procedures.
- Use parametric procedures anyway, knowing that some parametric procedures are fairly robust to violations of a Normal distribution with large samples.



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Eastern mudminnow (*Gasterosteus aculeatus*).

Histograms of number of Eastern mudminnows per 75 m section of stream (samples with 0 mudminnows excluded). Untransformed data on left, log-transformed data on right.

Steps:

- Transform Data
- Do Statistical Test on a transformed data
- Back-transform your results!!!

	Mean	Confidence Interval
Log-transformed	1.044	(0.7, 1.388)
Back-transformed	$10^{1.044}$	$(10^{(0.7)}, 10^{(1.388)})$

❖ More Info



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How to choose the right transformation?

- Use a transformation that other researchers commonly use in your field
- Decide which transformation to use before you do the statistical test

Symmetric Distribution: Mean = Median

Right-Skewed Distribution: Median < Mean

Left-Skewed Distribution: Mean < Median

Function	Comments
$Y = Y^K$	Enter K in the box provided.
$Y = Y + K$	-
$Y = Y - K$	-
$Y = Y/K$	-
$Y = Y \text{ squared}$	Enter K in the box provided.
$Y = Y^2/K$	-
$Y = \log(Y)$	Log base 10
$Y = -\log(Y)$	Natural logarithm (base e)
$Y = \ln(Y)$	-
$Y = 10^Y$	Ten to the Y^{10} power (inverse of log).
$Y = \exp(Y)$	e^Y (inverse of ln)
$Y = 1/Y$	Square root.
$Y = \sqrt[3]{Y}$	$\sqrt[3]{Y+1-Y}$
$Y = \log_{10}(Y)$	Y must be between 0.0 and 1.0. See notes below.
$Y = \text{probit}(Y)$	Column rank. Smallest Y value gets rank of 1.
$Y = \text{rank}(Y)$	Number of SDs from the column mean.
$Y = \text{zscore}(Y)$	Y is in radians.
$Y = \sin(Y)$	-
$Y = \cos(Y)$	-
$Y = \tan(Y)$	Result is in radians.
$Y = \arcsin(Y)$	Absolute value.
$Y = \text{ABS}(Y)$	Gaussian. Mean=0. SD=K (you enter).
$Y = Y + \text{Random}$	-
$Y = X/Y$	-
$Y = Y/X$	-
$Y = Y - X$	-
$Y = Y + X$	-
$Y = Y^X/X$	-
$Y = X - Y$	-
$Y = K - Y$	-
$Y = K/Y$	-
$Y = \log_2(Y)$	Enter K in the box provided.
$Y = 2^Y$	-
$Y = \text{log}_2(2^Y)$	Logarithm base 2
$Y = 2^{\ln Y}$	2.0 to the power of Y

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Missing Data

How does Prism handle missing values?

- Some statistical tests work fine with unequal sample size/missing values
 - E.g: Unpaired t, the Mann-Whitney nonparametric test, ordinary one-way ANOVA.
- Some statistical tests require matched sample sizes without missing values
 - If one value is missing, that subject (row) is ignored
 - E.g: Paired t-test, Wilcoxon matched pairs test, ANOVA with repeated measures.

Complete Case (CC) Analysis

❖ More Imputation Methods

Outline

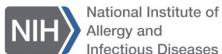
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2.3. Correlation

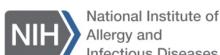
When two variables vary together, statisticians say that there is a lot of covariation or correlation.



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The Difference between Correlation and Regression

	Correlation	Regression
Goal	Quantifies the degree to which two variables are related	Finds the best line that predicts Y from X
Data	Both variables are measured	X is a variable you manipulate
Does it matter which variable is X and which is Y?	No	Yes
Assumptions	Both X and Y are measured and sampled from Gaussian distributions (Pearson correlation). OR makes no assumption about the distribution, as the calculation are based on ranks (Spearman nonparametric correlation)	The X values are not assumed to be sampled from a Gaussian distribution. The distances of the points from the best-fit line is assumed to follow a Gaussian distribution, with the SD of the scatter not related to the X or Y values.
Results	Correlation computes the value of the Pearson correlation coefficient, r . Its value ranges from -1 to +1	Quantifies goodness of fit with r^2 , sometimes shown in uppercase as R^2



Correlation Coefficient

Value of r/r_s	Interpretation
1.0	Perfect correlation
0 to 1	The two variables tend to increase or decrease together.
0.0	The two variables do not vary together at all.
-1 to 0	One variable increases as the other decreases.
-1.0	Perfect negative or inverse correlation.

If r or r_s is far from zero, there are four possible explanations:

- Changes in the X variable causes a change the value of the Y variable.
- Changes in the Y variable causes a change the value of the X variable.
- Changes in another variable influence both X and Y.
- X and Y don't really correlate at all, and you just happened to observe such a strong correlation by chance. The P value quantifies the likelihood that this could occur.



r²

r² is a value that ranges from zero to one, and is the fraction of the variance in the two variables that is “shared”.

How to explain r²?

- 59% of the variance in X can be explained by variation in Y
- 59% of the variance in Y can be explained by variation in X
- 59% of the variance is shared between X and Y

if $r^2=0.59$

P-value

- If the P value is small, you can reject the idea that the correlation is due to random sampling.
- If the P value is large, the data do not give you any reason to conclude that the correlation is real.



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Try It!

~ 5 mins

- Try to run correlation in Prism
- Try to run correlation in R
- Compare the results of Prism and R



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Outline

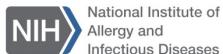
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2.4.Two-sample T-test

Two-sample t-test measures whether the means of the measurement variable are different in the two groups. There are two kinds of two-sample t-test: paired and unpaired.

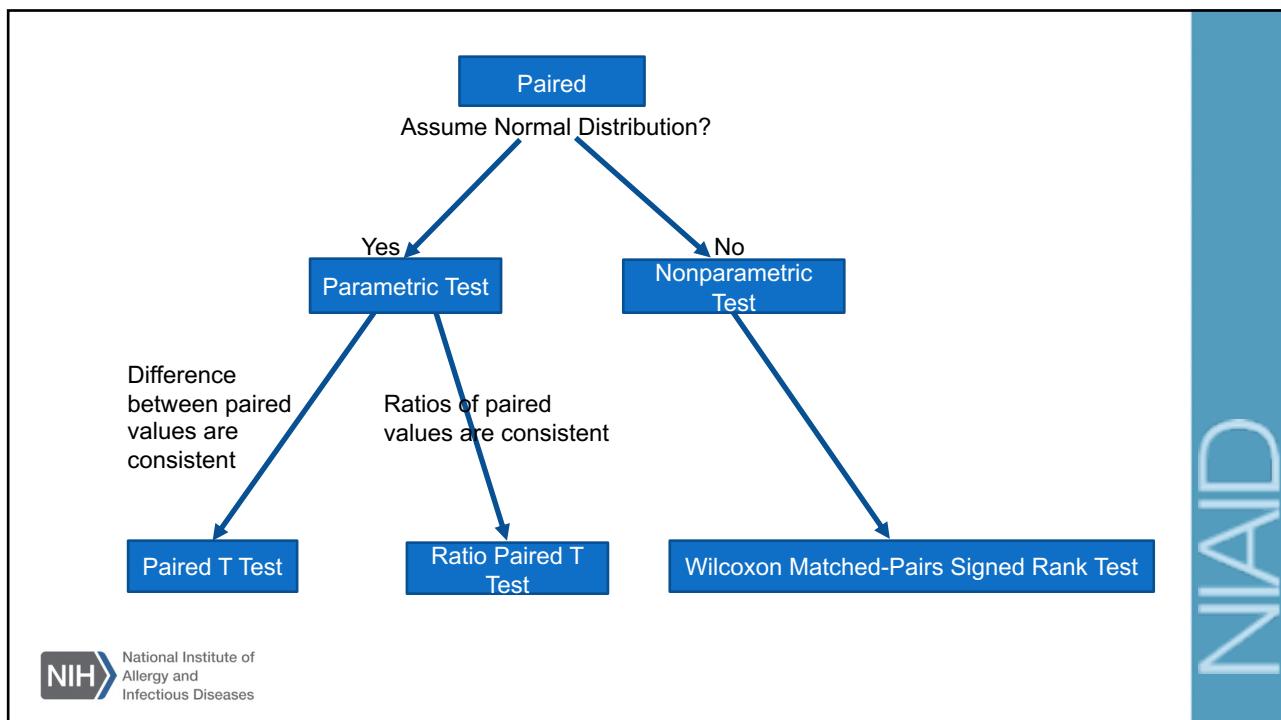
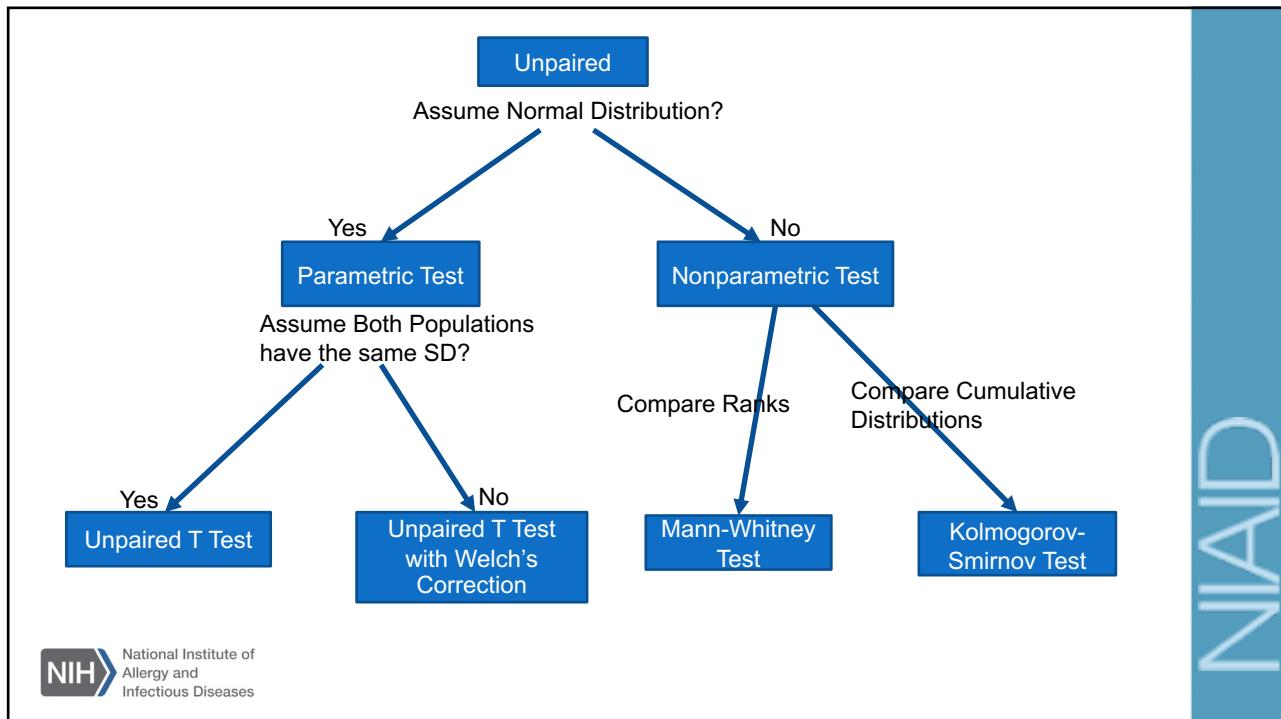
Paired

Choose a paired test when the columns of data are matched. That means that values on the same row are related to each other. Here are some examples:

- You measure a variable in each subject before and after an intervention.
- You recruit subjects as pairs, matched for variables such as age, ethnic group, and disease severity. One of the pair gets one treatment; the other gets an alternative treatment.
- You run a laboratory experiment several times, each time with a control and treated preparation handled in parallel.
- You measure a variable in twins or child/parent pairs.



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Unpaired t test Example in Prism:

There are two groups, the male group which includes 5 subjects while the female group includes 6 subjects:

	Group A	Group B
	Male	Female
	Y	Y
1	54	43
2	23	34
3	45	65
4	54	77
5	45	46
6		65



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Normal distribution?

Prism offers four normality tests. The normality tests all report a P value. To understand any P value, you need to know the null hypothesis. In this case, the null hypothesis is that all the values were sampled from a population that follows a Normal distribution.

- When p-value is high: The data are not inconsistent with a Normal distribution
- When p-value is low: Reject that null hypothesis and so accept the alternative hypothesis that the data are not sampled from a Gaussian population.

The difference between different normality tests

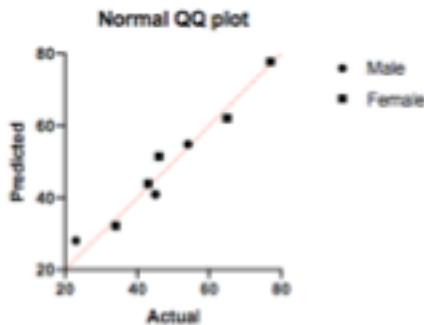
	A	B
	Male	Female
1 Test for normal distribution		
2 Anderson-Darling test		
3 AZ^*		N too small
4 P value		N too small
5 Passed normality test (alpha=0.05)?		
6 P value summary		
7		
8 D'Agostino & Pearson test		
9 K^2		N too small
10 P value		N too small
11 Passed normality test (alpha=0.05)?		
12 P value summary		
13		
14 Shapiro-Wilk test		
15 W	0.8970	0.8936
16 P value	0.9923	0.8979
17 Passed normality test (alpha=0.05)?	Yes	Yes
18 P value summary	ns	ns
19		
20 Kolmogorov-Smirnov test		
21 KS distance	0.3252	0.2298
22 P value	0.0906	>0.1000
23 Passed normality test (alpha=0.05)?	Yes	Yes
24 P value summary	ns	ns
25		
26 Number of values	5	6



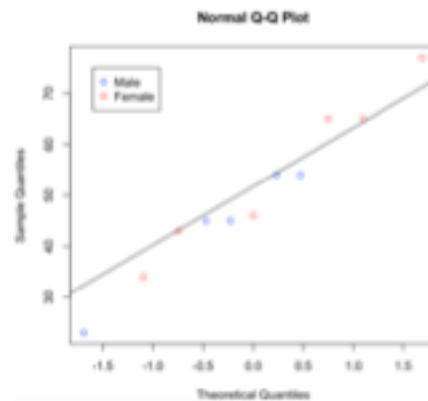
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QQ Normality Plots

[QQ plot in Prism](#)



[QQ plot in R](#)



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How to check Same Standard Deviation?

Formula of F-test

The test statistic can be obtained by computing the ratio of the two variances S_A^2 and S_B^2 .

$$F = \frac{S_A^2}{S_B^2}$$

The degrees of freedom are $\nu_A = 1$ (for the numerator) and $\nu_B = 1$ (for the denominator).

✓ Note that, the more this ratio deviates from 1, the stronger the evidence for unequal population variances.

✗ Note that, the F-test requires the two samples to be [normally distributed](#).



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Check same SDs

In Prism, no matter what t test you choose, unpaired t test or unpaired t test with Welch's correction, it will provide the comparison between variance.

If the answer to the question "Significantly different" is No, unpaired t test is preferred.

```
> FES..ftest
    F test to compare two variances

data: Y by Gender
F = 1.6881, num df = 5, denom df = 4, p-value = 0.6254
alternative hypothesis: true ratio of variances is not equal to 1
95 percent confidence interval:
 0.1794174 12.4127534
sample estimates:
ratio of variances
 1.688149
```

Unpaired t test		Welch's t test	
1 Table Analyzed	Unpaired t test data	1 Table Analyzed	Unpaired t test data
2		2	
3 Column B	Female	3 Column B	Female
4 vs.	vs.	4 vs.	vs.
5 Column A	Male	5 Column A	Male
6		6	
7 Unpaired t test:		7 Unpaired t test with Welch's correction	
8 P value	0.2613	8 P value	0.2561
9 P value summary	ns	9 P value summary	ns
10 Significantly different (P < 0.05)?	No	10 Significantly different (P < 0.05)?	No
11 One- or two-tailed P value?	Two-tailed	11 One- or two-tailed P value?	Two-tailed
12 t, df	t=1.199, df=9	12 Welch-corrected t, df	t=1.230, df=8.972
13		13	
14 How big is the difference?		14 How big is the difference?	
15 Mean of column A	44.20	15 Mean of column A	44.20
16 Mean of column B	55.00	16 Mean of column B	55.00
17 Difference between means (B - A) ± SEM	10.80 ± 8.010	17 Difference between means (B - A) ± SEM	10.80 ± 8.783
18 95% confidence interval	-8.583 to 31.18	18 95% confidence interval	-8.078 to 30.68
19 R squared (eta squared)	0.1377	19 R squared (eta squared)	0.1442
20		20	
21 F test to compare variances		21 F test to compare variances	
22 F, DFn, DDo	1.688, 5, 4	22 F, DFn, DDo	1.688, 5, 4
23 P value	0.6254	23 P value	0.6254
24 P value summary	ns	24 P value summary	ns
25 Significantly different (P < 0.05)?	No	25 Significantly different (P < 0.05)?	No
26		26	
27 Data analyzed		27 Data analyzed	
28 Sample size, column A	5	28 Sample size, column A	5
29 Sample size, column B	6	29 Sample size, column B	6

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Unpaired T-Test

```
> FES
    Two Sample t-test

data: Y by Gender
t = 1.1986, df = 9, p-value = 0.2613
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 -9.583046 31.183046
sample estimates:
mean in group Female mean in group Male
 55.0               44.2
```

Unpaired t test		Welch's t test	
1 Table Analyzed	Unpaired t test data	1 Table Analyzed	Unpaired t test data
2		2	
3 Column B	Female	3 Column B	Female
4 vs.	vs.	4 vs.	vs.
5 Column A	Male	5 Column A	Male
6		6	
7 Unpaired t test:		7 Unpaired t test with Welch's correction	
8 P value	0.2613	8 P value	0.2561
9 P value summary	ns	9 P value summary	ns
10 Significantly different (P < 0.05)?	No	10 Significantly different (P < 0.05)?	No
11 One- or two-tailed P value?	Two-tailed	11 One- or two-tailed P value?	Two-tailed
12 t, df	t=1.199, df=9	12 Welch-corrected t, df	t=1.230, df=8.972
13		13	
14 How big is the difference?		14 How big is the difference?	
15 Mean of column A	44.20	15 Mean of column A	44.20
16 Mean of column B	55.00	16 Mean of column B	55.00
17 Difference between means (B - A) ± SEM	10.80 ± 8.010	17 Difference between means (B - A) ± SEM	10.80 ± 8.783
18 95% confidence interval	-8.583 to 31.18	18 95% confidence interval	-8.078 to 30.68
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20		20	
21 F test to compare variances		21 F test to compare variances	
22 F, DFn, DDo	1.688, 5, 4	22 F, DFn, DDo	1.688, 5, 4
23 P value	0.6254	23 P value	0.6254
24 P value summary	ns	24 P value summary	ns
25 Significantly different (P < 0.05)?	No	25 Significantly different (P < 0.05)?	No
26		26	
27 Data analyzed		27 Data analyzed	
28 Sample size, column A	5	28 Sample size, column A	5
29 Sample size, column B	6	29 Sample size, column B	6

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How to explain the results?

- When the **p-value** of the test is less than the significance level alpha = 0.05, We can conclude that male's average is significantly different from female's average.
- When the **p-value** of the test is larger than the significance level alpha = 0.05, we *cannot* conclude that a significant difference exists between male and female.



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Try It!

~ 5 mins

- Try the same process of unpaired two-sample t-test in Prism
- Try to run the R codes
- Compare the results of Prism and R



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2.5.ANOVA

One-Way ANOVA

The one-way ANOVA compares the means between the groups you are interested in and determines whether any of those means are statistically significantly different from each other.

Specifically, it tests the null hypothesis:

$$H_0: \mu_1 = \mu_2 = \mu_3 = \dots = \mu_k$$

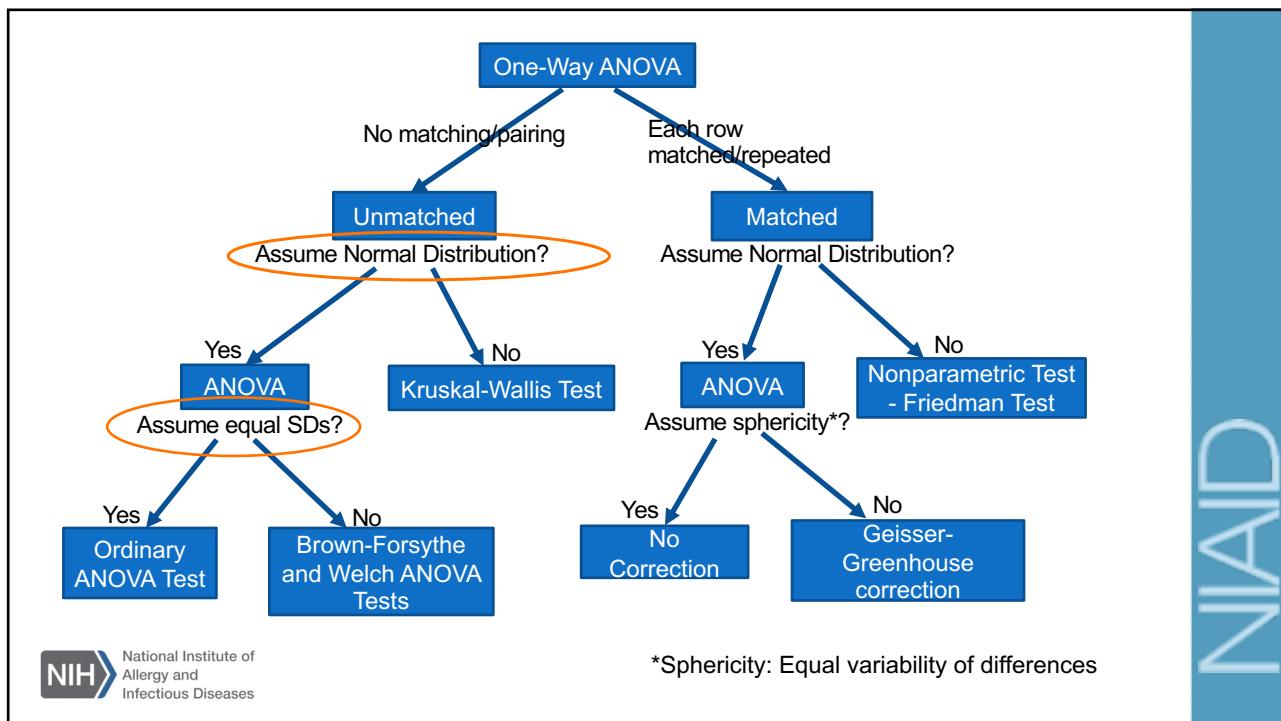
Where μ = group mean and k = number of groups. If the one-way ANOVA returns a statistically significant result, we reject the null hypothesis and conclude that at least two group means are statistically significantly different from each other.

Note: One-way ANOVA is an **omnibus** test statistic



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Sphericity

Briefly sphericity means that you waited long enough between treatments for any treatment effect to wash away.

		A			
		Control	Treatment 1	Treatment 2	Treatment 3
1	GS	54	43	78	111
2	JM	23	34	85	99
3	HM	45	85	99	78
4	DR	54	77	79	90
5	PG	45	46	87	95

Should we assume sphericity?

- If your experimental design relies on matching rather than repeated measurements, then you can assume sphericity, as violations are essentially impossible.
- If your experiment design is repeated measures, we recommend that you do not assume sphericity.

In this case, it is ANOVA with repeated measures.

Unmatched One-Way ANOVA example

The following is an example provided by Prism. In this case, there are three groups: *Control* (n = 6), *Treated* (n = 5) and *Treated + Antagonist* (n = 6).

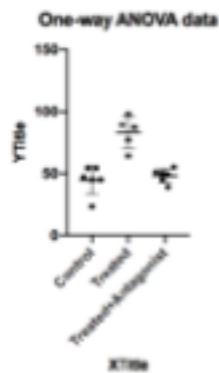
	Group A	Group B	Group C
	Control	Treated	Treated+Antagonist
	Y	Y	Y
1	54	87	45
2	23	98	39
3	45	64	51
4	54	77	49
5	45	89	50
6	47		55



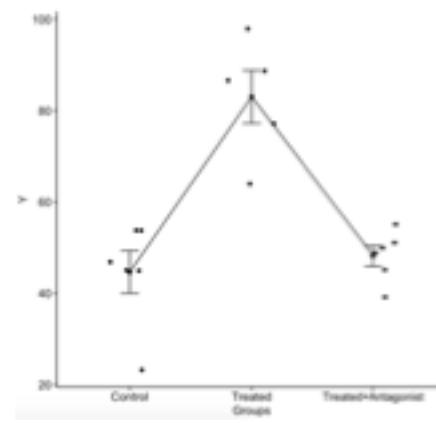
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Plots

[box-plot in Prism](#)



[box-plot in R](#)



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Considering that the first group, the control group doesn't pass the normality test, it is better to use nonparametric test – Kruskal-Wallis Test

	Normality and Lognormality Tests			
	Tabular results			
	A	B	C	
	Control	Treated	Treated+Antagonist	
1	Test for normal distribution			
2	Anderson-Darling test			
3	AZ [*]	N too small	N too small	N too small
4	P value			
5	Passed normality test (alpha=0.05)?			
6	P value summary			
7				
8	D'Agostino & Pearson test			
9	K2	N too small	N too small	N too small
10	P value			
11	Passed normality test (alpha=0.05)?			
12	P value summary			
13				
14	Shapiro-Wilk test			
15	W	0.7990	0.9843	0.9817
16	P value	0.0467	0.8376	0.7537
17	Passed normality test (alpha=0.05)?	No	Yes	Yes
18	P value summary	n	n	n
19				
20	Kolmogorov-Smirnov test			
21	KD distance	0.3450	0.2210	0.2398
22	P value	0.0248	>0.1000	>0.1000
23	Passed normality test (alpha=0.05)?	No	Yes	Yes
24	P value summary	n	n	n
25				
26	Number of values	6	5	6

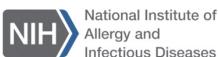


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Kruskal-Wallis Test?

Kruskal-Wallis test by ranks is also called as one-way ANOVA on ranks, which extends the Mann–Whitney U test, which is used for comparing only two groups

To perform this test, Prism first ranks all the values from low to high, paying no attention to which group each value belongs. The smallest number gets a rank of 1. The largest number gets a rank of N, where N is the total number of values in all the groups. The discrepancies among the rank sums are combined to create a single value called the Kruskal-Wallis statistic (some books refer to this value as H). A large Kruskal-Wallis statistic corresponds to a large discrepancy among rank sums.



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- As the p-value is less than the significance level 0.05, we can conclude that there are significant differences between these treatment groups.

```
> kruskal.test(Y ~ Group, data = unmatched_one_way_anova)

Kruskal-Wallis rank sum test

data: Y by Group
Kruskal-Wallis chi-squared = 18.18, df = 2, p-value = 0.000158
```

Kruskal-Wallis test		
1	Table Analyzed	One-way ANOVA data
2		
3	Kruskal-Wallis test	
4	P value	0.000158
5	Exact or approximate P value?	Exact
6	P value summary	--
7	Do the medians vary significantly? (P < 0.05)?	Yes
8	Number of groups	3
9	Kruskal-Wallis statistic	18.18
10		
11	Data summary	
12	Number of treatments (columns)	3
13	Number of values (total)	17



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Assumption: Normal distribution?

The assumption - Normal distribution, is not too important with large samples, but it is important with small sample sizes (especially with unequal sample sizes).

If your data do not come from Normal distributions, you have three options:

- Your best option is to transform the values (perhaps to logs or reciprocals) to make the distributions more normal.*
- Use the Kruskal-Wallis nonparametric test instead of ANOVA.*
- Use ANOVA anyway, knowing that it is fairly robust to violations of a Normal distribution with large samples.*



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Assumption: same standard deviation?

- The assumption, same standard deviation, is not very important when all the groups have the same (or almost the same) number of subjects, but is very important when sample sizes differ.
- Prism tests for equality of variance with two tests: The Browne-Forsythe test and Bartlett's test.
- Don't base your conclusion solely on these tests. Also think about data from other similar experiments. If you have plenty of previous data that convinces you that the variances are really equal, ignore these tests (unless the P value is really tiny) and interpret the ANOVA results as usual.



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Let's run ANOVA anyway to see the output provided by Prism and R.

** BUT in this case, ANOVA might not be acceptable because of the violation of Normal distribution.

```
> summary(res.anov)
      Df  Sum Sq Mean Sq F value    Pr(>F)
Group       2   4768   2388.2   22.57 4.16e-05 ***
Residuals  14   1476   105.4
...
Signif. codes:  0 '*****' 0.001 '***' 0.001 ' '**' 0.01 ' *' 0.05 ' .' 0.1 ' ' 1
```

Ordinary one-way ANOVA					
	One-way ANOVA data				
1	Table Analyzed				
2	Data sets analyzed				
3					
4	ANOVA summary				
5	F				
6	P value				
7	P value summary				
8	Significant diff. among means (P < 0.05)?				
9	R square				
10					
11	Brown-Forsythe test				
12	F (DFn, DFd)				
13	P value				
14	P value summary				
15	Are SDs significantly different (P < 0.05)?				
16					
17	Bartlett's test				
18	Bartlett's statistic (corrected)				
19	P value				
20	P value summary				
21	Are SDs significantly different (P < 0.05)?				
22					
23	ANOVA table				
24	Treatment (between columns)	88	DF	MS	F (DFn, DFd) P value
25	Residual (within columns)	4760	2	2380	F (2, 14) = 22.57 P<0.0001
26	Total	1476	14	105.4	
27		6236	16		
28					
29	Data summary				
30	Number of treatments (columns)	3			
31	Number of values (total)	17			



Try It!

~ 5 mins

- Try the same process of unmatched one-way ANOVA in Prism
- Try to run the R codes
- Compare the results of Prism and R



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Repeated measures one-way ANOVA example:

This example is provided by Prism. The four columns represent four sequential treatments. Each row represents a different subject (or a different set of matched data).

Repeated-measures ANOVA compares the means of three or more matched groups.

Table format: Column		Group A	Group B	Group C	Group D
		Control	Treatment 1	Treatment 2	Treatment 3
1	GS	54	43	78	111
2	JM	23	34	37	41
3	HM	45	65	99	78
4	DR	31	33	36	36
5	PS	15	25	30	26



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Check if it follows normal distribution

And the answer is YES!

Normality and Lognormality Tests Tabular results		A	B	C	D
		Control	Treatment 1	Treatment 2	Treatment 3
1	Test for normal distribution				
2	Anderson-Darling test				
3	A^2				
4	P value	N too small	N too small	N too small	N too small
5	Passed normality-test (alpha=0.05)?				
6	P-value summary				
7					
8	D'Agostino & Pearson test				
9	K_2				
10	P value	N too small	N too small	N too small	N too small
11	Passed normality-test (alpha=0.05)?				
12	P-value summary				
13					
14	Shapiro-Wilk test				
15	W	0.8646	0.8908	0.8917	0.8954
16	P value	0.8393	0.3613	0.1434	0.3045
17	Passed normality-test (alpha=0.05)?	Yes	Yes	Yes	Yes
18	P-value summary	ns	ns	ns	ns
19					
20	Kolmogorov-Smirnov test				
21	KD distance	0.1649	0.2119	0.3320	0.2858
22	P value	>0.1000	>0.1000	0.0780	>0.1000
23	Passed normality-test (alpha=0.05)?	Yes	Yes	Yes	Yes
24	P-value summary	ns	ns	ns	ns
25					
26	Number of values	5	5	5	5

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- The P value answers this question: If all the populations really have the same mean, what is the chance that random sampling would result in means as far apart (or more so) as observed in this experiment?
- If the overall P value is large: the data does not give you any reason to conclude that the means differ.
- If the overall P value is small: it is unlikely that the differences you observed are due to random sampling. You can reject the idea that all the populations have identical means.

NIH one-way ANOVA					
Table Analyzed	Repeated measures one-way ANOVA data				
Requested measures ANOVA summary					
Assume sphericity?	Yes				
F	3.018				
P value	0.0873				
P-value summary	ns				
Statistically significant ($P = 0.05$)?	No				
Geschen-Greenhouse's epsilon	0.9793				
R square	0.4792				
Was the matching effective?					
F	10.43				
P value	0.0007				
P-value summary	**				
Is there significant matching ($P = 0.05$)?	Yes				
R square	0.6464				
ANOVA table	SS	df	MS	F(DFn, DFd)	P value
Treatment (between columns)	2175	3	725.0	$F(3, 9) = 3.618$	P=0.053
Individual (between rows)	8972	4	2243.0	$F(4, 12) = 10.43$	P=0.0007
Residual (random)	2454	12	204.4		
Total	12611	19			
Data summary					
Number of treatments (columns)	4				
Number of subjects (rows)	5				
Number of missing values	0				

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```

> summary(modell,multivariate=F)

Univariate Type III Repeated-Measures ANOVA Assuming Sphericity

Sum Sq num Df Error SS den Df F value Pr(>F)
(Intercept) 44886      1    8371.7      4 21.8643 0.01011 *
Trials       2375      3    2484.3     12  3.6184 0.04549 *
---
Signif. codes:  0 '****' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Mauchly Tests for Sphericity

Test statistic p-value
Trials   0.057644 0.19416

Greenhouse-Geisser and Huynh-Feldt Corrections
for Departure from Sphericity

GG eps Pr(>F[GG])
Trials 0.57928 0.08727 .
---
Signif. codes:  0 '****' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

HF eps Pr(>F[HF])
Trials 0.9856654 0.04648165

```



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Try It!

~ 5 mins

- Try the same process of Repeated measures one-way ANOVA
- Try to run the R codes
- Compare the results of Prism and R



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Two-way ANOVA

Two-way ANOVA, also called two-factor ANOVA, is used to evaluate simultaneously the effect of two grouping variables (A and B) on a response variable.

Two-way ANOVA test hypotheses

1. There is no difference in the means of factor A
2. There is no difference in means of factor B
3. There is no interaction between factors A and B

The alternative hypothesis for cases 1 and 2 is: the means are not equal.

The alternative hypothesis for case 3 is: there is an interaction between A and B.



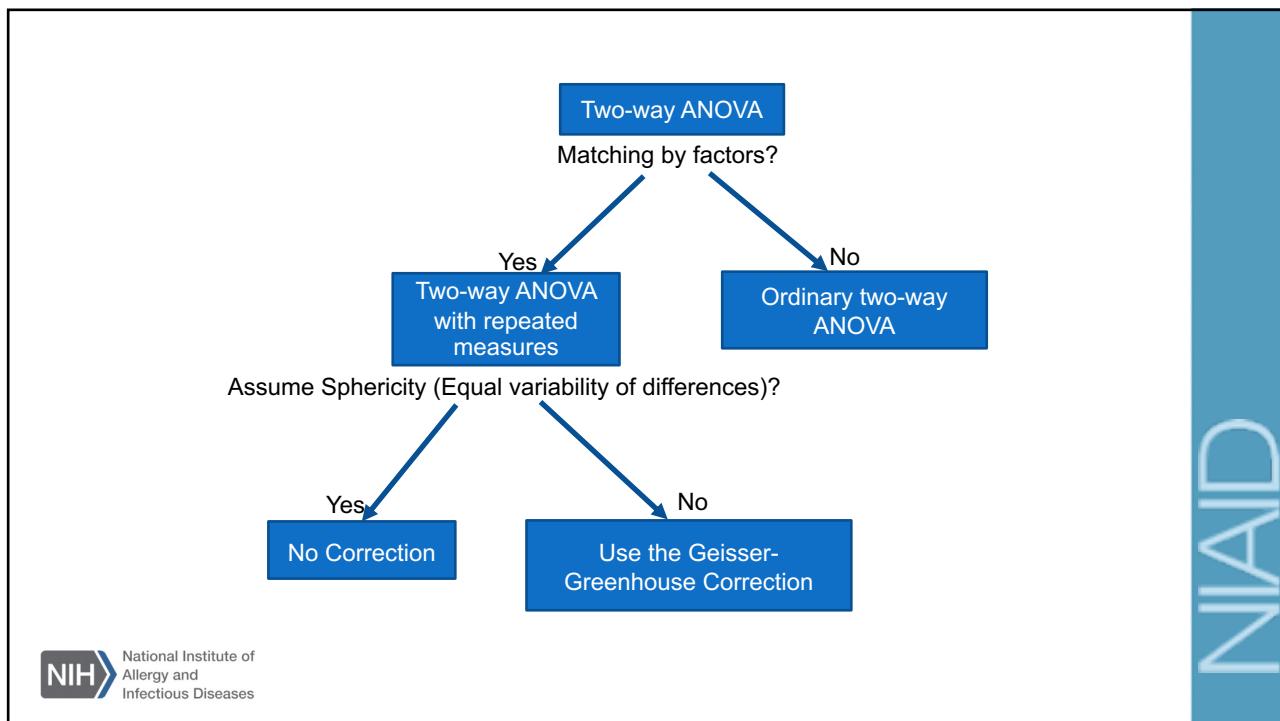
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One-Way vs Two-Way ANOVA Differences Chart

	One-Way ANOVA	Two-Way ANOVA
Definition	A test that allows one to make comparisons between the means of three or more groups of data.	A test that allows one to make comparisons between the means of three or more groups of data, where two independent variables are considered.
Number of Independent Variables	One.	Two.
What is Being Compared?	The means of three or more groups of an independent variable on a dependent variable.	The effect of multiple groups of two independent variables on a dependent variable and on each other.
Number of Groups of Samples	Three or more.	Each variable should have multiple samples.



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Ordinary Two-way ANOVA Example

The columns represent two cell lines. The rows represent two treatments. Within each treatment for each cell line, five replicate values are entered into subcolumns. This experiment has no matching or repeated measures. For this reason, it is OK that one of the values is missing

		Group A					Group B				
		Wild-type cells					GFP5 cell line				
		A:Y1	A:Y2	A:Y3	A:Y4	A:Y5	B:Y1	B:Y2	B:Y3	B:Y4	B:Y5
Table format:	Grouped										
①		34	36	41		43	98	87	96	99	88
1	Serum-starved										
2	Normal culture	23	19	26	29	25	32	29	26	33	30

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ANOVA table

The ANOVA table breaks down the overall variability between measurements (expressed as the sum of squares) into four components:

- *Interactions between row and column.*
- *Variability among columns.*
- *Variability among rows.*
- *Residual or error. Variation among replicates not related to systematic differences between rows and columns.*

Two-way ANOVA ANOVA results				
Table Analyzed	Two-way ANOVA - not RRI			
Two-way ANOVA	Ordinary			
Alpha	0.05			
Source of Variation	% of Total variation	P value	P value summary	Significant?
Interaction	19.87	<0.0001	***	Yes
Row Factor	48.74	<0.0001	***	Yes
Column Factor	28.12	<0.0001	***	Yes
ANOVA table	MS (Type II)	df	SS	F (DFn, DFd) P value
Interaction	2889	1	2889	F(1, 15) = 162.8 P<0.0001
Row Factor	7088	1	7088	F(1, 15) = 452.4 P<0.0001
Column Factor	4308	1	4308	F(1, 15) = 249.2 P<0.0001
Residual	293.4	15	1798	
Difference between column means				
Predicted (L2) mean of 1000 type cells			31.45	
Predicted (L2) mean of CPTPS cell line			81.70	
Difference between predicted means			-50.25	
SD of difference			1.932	
95% CI of difference			-54.37 to -46.13	
Difference between row means				
Predicted (L2) mean of Serum derived			65.95	
Predicted (L2) mean of Normal culture			27.20	
Difference between predicted means			38.75	
SD of difference			1.932	
95% CI of difference			34.82 to 42.67	
Interaction CI				
Mean diff. A1 - B1			-64.30	
Mean diff. A2 - B2			-6.60	
(A1-B1)-(A2-B2)			-48.30	
95% CI of difference			-67.93 to -41.67	
(B1-A1)-(B2-A2)			49.30	
95% CI of difference			41.27 to 57.33	

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Interaction P value

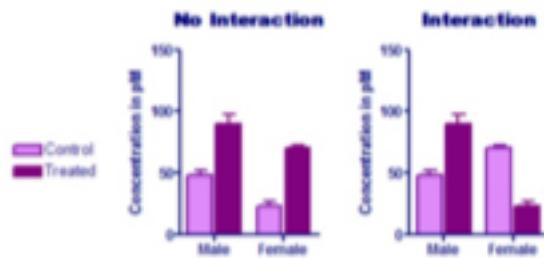
The null hypothesis is that there is no interaction between columns and rows. Often the test of interaction is the most important of the three tests. For example, If columns represent drugs and rows represent gender, then the null hypothesis is that the differences between the drugs are consistent for men and women.

```
> summary(res.anov2)
    Df Sum Sq Mean Sq F value Pr(>F)
Treatment      1   8276   8276   471.3 9.58e-13 ***
Cell          1   3917   3917   223.1 2.06e-10 ***
Treatment:Cell 1   2859   2859   162.8 1.86e-09 ***
Residuals     15   263     18
---
Signif. codes:  0 '****' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
1 observation deleted due to missingness
```

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The graph on the left below shows no interaction. The treatment has about the same effect in males and females. The graph on the right, in contrast, shows a huge interaction. the effect of the treatment is completely different in males (treatment increases the concentration) and females (where the treatment decreases the concentration).

In this two-way ANOVA example, the test for interaction leads to statistically significant results, we probably won't learn anything of interest from the other two P values. In the example above, a statistically significant interaction means that the effect of the treatment (difference between treated and control) differs between cell groups.



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Try It!

~ 5 mins

- Try the same process of Ordinary Two-way ANOVA
- Try to run the R codes
- Compare the results of Prism and R



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Outline

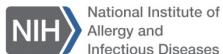
1. Statistical Testing Process

- 1.1. Formulate Null and Alternative hypotheses
- 1.2. Calculate the appropriate test statistics
- 1.3. Compute the probability of observing the test statistic under the null hypothesis
- 1.4. Make statistical decision and biological conclusion

2. Common Statistical Tests

- 2.1. Choose appropriate tests
- 2.2. Data Preprocessing
- 2.3. Correlation
- 2.4. Two-sample T-test
- 2.5. ANOVA
- 2.6. Multiple Comparisons**

3. Application in Prism and R



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2.6. Multiple Comparisons

Once ANOVA test has been completed, what's next?

- Subgroup differences among the different experimental and control groups
- The subgroup differences are called “*pairwise*” differences

❖ [Multiple Comparisons in Prism](#)



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Interpreting multiple P values is difficult. If you test several independent null hypotheses and leave the threshold at 0.05 for each comparison, the chance of obtaining at least one “statistically significant” result is greater than 5% (even if all null hypotheses are true).



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Three Approaches to Multiple Comparisons

1. Don't correct for multiple comparisons
2. Control the Type I error rate for the family of comparisons
3. Control the False Discovery Rate (FDR)



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Approach 1: Don't correct for multiple comparisons

When it makes sense to not correct for multiple comparisons?

1. Account for multiple comparisons when interpreting the results rather than in the calculations
2. Corrections for multiple comparisons may not be needed if you make only a few planned comparisons
3. Corrections for multiple comparisons are not needed when the comparisons are complementary

Fisher's Least Significant Difference (LSD)



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Approach 2: Control Type I error rate for the family of comparisons

What are multiplicity adjusted P values?

The P value from a single comparison is the answer to two equivalent questions:

- If the null hypothesis were true, what is the chance that random sampling would result in a difference this large or larger?
- What is the smallest definition of the threshold (α) of statistical significance at which this result would be statistically significant?

The adjusted P-value answers this question:

- What is the smallest significance level, when applied to the entire family of comparisons, at which this particular comparison will be deemed statistically significant?



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Methods:

	Bonferroni	Sidak	Holm-Sidak	Tukey	Dunnett	Newman-Keuls
Only as follow-up test to ANOVA?	No	No	No	Yes	Yes	
Compare every mean with every other mean?	Yes	Yes	Yes	Yes	No	Yes
Compare means within rows/columns	Yes	Yes	Yes	No	No	No
Compare every mean to a control mean	Yes	Yes	Yes	No	Yes	No
CI?	Yes	Yes	No	Yes	Yes	No
Multiplicity adjusted P values	Yes	Yes	Yes	Yes	Yes	No
Assume independence?	No	Yes				

❖ [More details](#)



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Approach 3: Control the False Discovery Rate (FDR)

	"Discovery"	"Not a discovery"	Total
No difference. Null hypothesis true	A	B	A+B
A difference truly exists	C	D	C+D
Total	A+C	B+D	A+B+C+D

Discovery: Statistically significant

False Discovery rate: The ratio $A/(A+C)$ Usually called Q

The usual approach to statistical significance and multiple comparisons asks the question:

- If the null hypothesis is true what is the chance of getting "statistically significant" results?

The False Discovery Rate (FDR) answers a different question:

- If a comparison is a "discovery", what is the chance that the null hypothesis is true?



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Three Methods used to Control the FDR:

1. Original Method of Benjamin and Hochberg
 - Assumes “test statistics are independent or positive dependent”
2. Two-stage step-up method of Benjamini, Krieger and Yekutieli
 - has more power than the Benjamini and Hochberg method, while making the same assumptions
3. Corrected method of Benjamini & Yakutieli
 - Requires no assumption about how the various comparisons correlate with each other.
 - has less power; The method is very conservative.



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Ordinary Two-way ANOVA Example (with multiple comparisons)

The columns represent two cell lines. The rows represent two treatments. Within each treatment for each cell line, five replicate values are entered into subcolumns. This experiment has no matching or repeated measures. For this reason, it is OK that one of the values is missing

Table format: Grouped		Group A					Group B				
		Wild-type cells					GFP5 cell line				
		A:Y1	A:Y2	A:Y3	A:Y4	A:Y5	B:Y1	B:Y2	B:Y3	B:Y4	B:Y5
1	Serum-starved	34	36	41		43	98	87	96	99	88
2	Normal culture	23	19	26	29	25	32	29	26	33	30



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Uncorrected Fisher's LSD	Mean Diff.	95.00% CI of diff.	Significant?	Summary	Individual P Value
Serum starved:Wild-type cells vs. Serum starved:GPPS cell line	-54.90	-60.89 to -48.91	Yes	****	<0.0001
Serum starved:Wild-type cells vs. Normal culture:Wild-type cells	14.10	8.108 to 20.09	Yes	***	0.0002
Serum starved:Wild-type cells vs. Normal culture:GPPS cell line	8.500	2.508 to 14.49	Yes	**	0.0085
Serum starved:GPPS cell line vs. Normal culture:Wild-type cells	69.00	63.35 to 74.65	Yes	****	<0.0001
Serum starved:GPPS cell line vs. Normal culture:GPPS cell line	63.40	57.75 to 69.05	Yes	****	<0.0001
Normal culture:Wild-type cells vs. Normal culture:GPPS cell line	-5.800	-11.25 to 0.64894	No	ns	0.0918

Tukey's multiple comparisons test	Mean Diff.	95.00% CI of diff.	Significant?	Summary	Adjusted P Value
Serum starved:Wild-type cells vs. Serum starved:GPPS cell line	-54.90	-63.00 to -46.80	Yes	****	<0.0001
Serum starved:Wild-type cells vs. Normal culture:Wild-type cells	14.10	5.998 to 22.20	Yes	***	0.0008
Serum starved:Wild-type cells vs. Normal culture:GPPS cell line	8.500	0.3981 to 16.68	Yes	*	0.0383
Serum starved:GPPS cell line vs. Normal culture:Wild-type cells	69.00	61.36 to 76.64	Yes	****	<0.0001
Serum starved:GPPS cell line vs. Normal culture:GPPS cell line	63.40	55.76 to 71.04	Yes	****	<0.0001
Normal culture:Wild-type cells vs. Normal culture:GPPS cell line	-5.800	-13.24 to 2.039	No	ns	0.1936



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Tukey multiple pairwise-comparisons

```

> TukeyHSD(res.anov2)
Tukey multiple comparisons of means
 95% family-wise confidence level

Fit: aov(formula = Y ~ Treatment + Cell + Treatment:Cell, data = two_way_anova)

Treatment
  diff      lwr      upr p adj
Serum Starved-Normal Culture 41.8 37.69614 45.98386   0

Cell
  diff      lwr      upr p adj
Wild-Type cells-GPPS cell line -28.71111 -32.81497 -24.68725   0

Treatment:Cell
  diff      lwr      upr p adj
Serum Starved:GPPS cell line-Normal Culture:GPPS cell line  63.4 55.7614984 71.03851 0.0000000
Normal Culture:Wild-Type cells-Normal Culture:GPPS cell line -5.6 -13.2385096 2.03851 0.1936359
Serum Starved:Wild-Type cells-Normal Culture:GPPS cell line  8.5 0.3981371 16.68186 0.0382585
Normal Culture:Wild-Type cells-Serum Starved:GPPS cell line -69.0 -76.6385096 -61.36149 0.0000000
Serum Starved:Wild-Type cells-Serum Starved:GPPS cell line -54.9 -63.0018629 -46.79814 0.0000000
Serum Starved:Wild-Type cells-Normal Culture:Wild-Type cells 14.1 5.9981371 22.28186 0.0007918

```



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Try It!

~ 5 mins

- Try the same process of Ordinary Two-way ANOVA (with multiple comparisons)
- Try to run the R codes
- Compare the results of Prism and R



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Two interesting facts about Multiple Comparisons

1. If the overall ANOVA finds a significant difference among groups, am I certain to find a significant post multiple comparison test?

This is not necessarily true

Because It is possible that the overall mean of group A and group B combined differs significantly from the combined mean of groups C, D and E.

2. If the overall ANOVA finds no significant difference among groups, are the multiple comparisons test results valid?

All the multiple comparisons tests offered by Prism are valid even if the overall ANOVA did not find a significant difference among means.



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Outline

1. Statistical Testing Process

- 1.1. Formulate Null and Alternative hypotheses
- 1.2. Calculate the appropriate test statistics
- 1.3. Compute the probability of observing the test statistic under the null hypothesis
- 1.4. Make statistical decision and biological conclusion

2. Common Statistical Tests

- 2.1. Choose appropriate tests
- 2.2. Data Preprocessing
- 2.3. Correlation
- 2.4. Two-sample T-test
- 2.5. ANOVA
- 2.6. Multiple Comparisons

3. Application in Prism and R



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How to learn R?

- [Datacamp - Introduction to R](#): Interactive course for R beginners

How to learn Prism?

- [Statistics with Prism](#): Official Prism tutorials provided by Prism



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Conclusions

- Statistical Testing methods are much more than these!
- The materials of this seminar will be updated on: [Github - Statistical Testing](#)
- If you have any specific statistical problem, please send email to
bioinformatics@niaid.nih.gov
- Check our training schedule: http://www.eventzilla.net/user/NIAID_OCICB_BCBB
- Take the survey and tell us what statistical topics you want to learn about next:
[BCBB Statistical Training – Suggest a class!](#)
- Ask question on slack group!

The invitation to the slack group will be sent after the workshop



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Thank You!



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