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1 Template

```
#include <bits/stdc++.h>
#include <unistd.h>

#ifdef COMPPROG_LOCAL
#include <fmt/format.h>
#define dbg(...) fmt::print(stderr, __VA_ARGS__)
#define debug_assert assert
#else
```

```
#define dbg(...)
#define debug_assert(...)
#endif
using namespace std;
using uint = unsigned;
using ll = long long;
using ull = unsigned long long;
template <typename E = uint> using Graph =
vector<vector<E>>;
template <typename T>
using min priority queue = priority queue<T, vector<T>,
std::greater<T>>;
#define rep(a, b) for (int a = 0; a < (b); ++a)
#define urep(a, b) for (uint a = 0; a < (b); ++a)
#define all(a) (a).begin(), (a).end()
#define endl '\n'
int main() {
    ios::sync with stdio(false);
    cin.tie(nullptr):
    cout.precision(10);
}
```

2 Data Structures

2.1 Union Find

```
struct UnionFind {
    vector<uint> p, size;
    UnionFind(uint n) : p(n), size(n, 1) { iota(p.begin(),
p.end(), 0); }
    auto raw_key(uint i) const {
       while (p[i] != i) i = p[i];
        return i;
    void update_key(uint i, const uint k) {
        while (p[i] != k) i = exchange(p[i], k);
    auto key(uint i) {
        const auto k = raw_key(i);
        update_key(i, k);
        return k;
    void unite(uint i, uint j) {
        const auto ki = raw_key(i), kj = raw_key(j);
       if (ki == kj) return;
        const auto k = size[ki] >= size[kj] ? ki : kj;
        size[k] = size[ki] + size[kj];
        update_key(i, k);
        update_key(j, k);
};
```

2.2 Range

```
struct Range {
    ull start, end:
    // static Range from_ends(ull start, ull end) { return
{start, end}; }
   bool operator==(const Range &rhs) const {
        return (is_empty() && rhs.is_empty()) || (start ==
rhs.start && end == rhs.end);
   }
    bool is subset of(Range other) const { return
other.start <= start && end <= other.end; }
    Range intersect_with(Range other) const {
        return Range{
            .start = max(start, other.start),
            .end = min(end, other.end),
       };
   bool is_empty() const { return start >= end; }
    ull size() const {
        if (is empty()) return 0;
        else return end - start;
    bool contains(ull point) const { return start <= point</pre>
&& point < end: }
    pair<Range, Range> split at mid() const {
       assert(!is empty());
       auto m = start + (end - start) / 2;
        return {{start, m}, {m, end}};
};
```

2.3 Sparse Table

```
template <typename T, auto op, T neutral_element> struct
SparseTable {
    // op needs to
    // - be associative
    // - be idempotent
    // - have neutral element neutral_element

    uint n;
    vector<T> aggs;

    uint idx(uint i, uint row) const { return n * row + i; }

    SparseTable(span<T const> vals) : n(vals.size()), aggs(n * (bit_width(n) + 1)) {

        ranges::copy(vals, aggs.begin());

        for (uint row = 1, agg_size = 2; agg_size < n; + +row, agg_size <<= 1) {</pre>
```

```
for (uint i = 0; i + (agg_size / 2) < n; ++i) {
                aggs[idx(i, row)] =
                    op(aggs[idx(i, row - 1)], aggs[idx(i +
(agg size / 2), row - 1));
           }
   // zero-based
   T range_query(Range range) const {
        if (range.is_empty()) return neutral_element;
        auto agg_index = bit_width(range.size()) - 1;
        auto agg size = 1u << agg index;</pre>
        return op(aggs[idx(range.start, agg_index)],
aggs[idx(range.end - agg_size, agg_index)]);
   }
};
```

2.4 Segment Tree

```
template <typename T, typename Op, T neutral_element> struct
SegmentTree {
   Op op;
   uint n;
   vector<T> tree;
   vector<T> lazy;
   SegmentTree(uint n)
       : n(bit ceil( n))
        , tree(2 * n + 1, neutral_element)
        , lazy(2 * n + 1, neutral_element) {}
   bool is leaf(uint v) const { return n <= v && v < 2 *
   void recalc(uint v) { tree[v] = op(tree[left_child(v)],
tree[right_child(v)]); }
   void recalc_all_parents(uint v) {
       v = parent(v);
       while (root <= v) recalc(v), v = parent(v);</pre>
   }
   static const uint root = 1;
   static uint parent(uint v) { return v / 2; }
   static uint left child(uint v) { return 2 * v; }
   static uint right child(uint v) { return 2 * v + 1; }
   void push_lazy(uint v) {
       if (lazy[v] == neutral element) return;
       apply_lazy(left_child(v), lazy[v]);
       apply_lazy(right_child(v), lazy[v]);
       lazy[v] = neutral_element;
   void apply lazy(uint v, T value) {
       tree[v] = op(tree[v], value);
       if (!is_leaf(v)) lazy[v] = op(lazy[v], value);
   }
```

```
void push_all_lazy(uint v) {
        for (uint bits_to_shift = bit_width(v) - 1;
bits_to_shift > 0; --bits_to_shift)
           push lazy(v >> bits to shift);
   }
    void range_update(Range range, T value) {
        push all lazy(n + range.start - 1);
        push all lazy(n + range.end - 2);
        for (auto l = n + range.start - 1, r = n + range.end
-1; l < r;
             l = parent(l), r = parent(r)) {
           if (l & 1) apply lazy(l++, value);
           if (r & 1) apply_lazy(--r, value);
       }
        auto first_touched = [](auto x) { return x >>
countr zero(x); };
        recalc all parents(first touched(n + range.start -
1)):
        recalc_all_parents(first_touched(n + range.end - 1)
- 1);
   T range_query(Range range) {
        auto agg = neutral element;
       push_all_lazy(n + range.start - 1);
        push all lazy(n + range.end - 2);
        for (auto l = n + range.start - 1, r = n + range.end
-1; l < r;
            l = parent(l), r = parent(r)) {
           if (l & 1) agg = op(tree[l++], agg);
           if (r \& 1) agg = op(agg, tree[--r]);
       }
        return agg;
   }
};
```

2.5 Treap

```
struct Treap {
    struct Lazy {
       bool reversed = false;
        bool operator==(const Lazy &) const = default;
   };
    struct Agg {
        ull sum;
        ll max:
   };
   static inline mt19937 gen;
    static inline uniform_int_distribution<uint> dist;
   struct Node {
       uint value;
       uint priority;
       Node *left = nullptr, *right = nullptr;
```

```
Agg agg;
       Lazy lazy{};
        uint size = 1;
       Node(uint value) : value( value),
priority(dist(gen)), agg({value, value}) {}
        void push lazy() {
            if (lazy.reversed) {
                swap(left, right);
                if (left) left->lazy.reversed ^= 1;
                if (right) right->lazy.reversed ^= 1;
            lazy = Lazy{};
       }
        void update_agg() {
            debug_assert(lazy == Lazy{});
            agg.sum = value;
            agg.max = value;
            size = 1;
            if (left) {
                agg.sum += left->agg.sum;
                agg.max = max(agg.max, left->agg.max);
                size += left->size;
            }
            if (right) {
                agg.sum += right->agg.sum;
                agg.max = max(agg.max, right->agg.max);
                size += right->size;
           }
       }
        const Node *get_kth(uint k) {
            debug_assert(1 <= k);</pre>
            debug assert(k <= size);</pre>
            push lazy();
            if (k <= sz(left)) return left->get_kth(k);
            else if (k == 1 + sz(left)) return this;
            else return right->get_kth(k - 1 - sz(left));
        void update_kth(uint k, uint new_value) {
            debug_assert(1 <= k);</pre>
            debug_assert(k <= size);</pre>
            push lazy();
            if (k <= sz(left)) left->update kth(k,
new value);
            else if (k == 1 + sz(left)) value = new_value;
            else right->update_kth(k - 1 - sz(left),
new value);
            update_agg();
       }
   };
   static Node *merge(Node *a, Node *b) {
       if (!a) return b;
       if (!b) return a;
```

```
if (a->priority < b->priority) {
           a->push_lazy();
           a->right = merge(a->right, b);
           a->update agg();
           return a;
       } else {
           b->push lazy();
           b->left = merge(a, b->left);
           b->update agg();
           return b;
       }
   }
   static uint sz(Node *v) { return v ? v->size : 0; }
   static pair<Node *, Node *> split_size(Node *v, uint
left size) {
       if (!v) return {nullptr, nullptr};
       v->push_lazy();
       if (1 + sz(v->left) \le left size) {
           auto [rl, rr] = split size(v->right, left size -
1 - sz(v->left));
           v->right = rl;
           v->update agg();
           return {v, rr};
       } else {
           auto [ll, lr] = split_size(v->left, left_size);
           v->left = lr;
           v->update_agg();
           return {ll, v};
   }
   Node *root = nullptr;
   Treap(span<uint> initial vals) {
        for (auto v : initial_vals) root = merge(root, new
Node(v));
   }
   static tuple<Node *, Node *, Node *>
extract_inner_range(Node *v, Range range) {
       auto [lm, r] = split_size(v, range.end - 1);
       auto [l, m] = split size(lm, range.start - 1);
       return {l, m, r};
   }
   void insert after(uint pos, uint value) { root =
insert all after(root, pos, new Node(value)); }
   static Node *insert all after(Node *v, uint pos, Node
*vals) {
       auto [l, r] = split size(v, pos);
       return merge(merge(l, vals), r);
   }
   void remove(uint pos) {
```

```
auto [l, single, r] = extract_inner_range(root,
\{pos, pos + 1\}\};
        debug_assert(sz(single) == 1);
        dbg("Removed node with value {}\n", single->value);
        root = merge(l, r);
    const Node *at(uint pos) { return root->get_kth(pos); }
    void update(uint pos, uint value) { root-
>update kth(pos, value); }
    Agg range_query(Range range) {
        auto [l, m, r] = extract_inner_range(root, range);
       Agg result = m ? m->agg : Agg{};
        root = merge(l, merge(m, r));
        return result;
    }
    void move range(Range range, uint to pos) {
        auto [l, m, r] = extract inner range(root, range);
        root = merge(l, r);
        root = insert_all_after(root, to_pos - 1, m);
    void reverse in range(Range range) {
        auto [l, m, r] = extract inner range(root, range);
       m->lazy.reversed ^= 1;
        root = merge(l, merge(m, r));
    template <typename F> static void visit_in_order(Node
*v, F &f) {
        if (!v) return;
       v->push lazy();
        visit in order(v->left, f);
        f(*v);
        visit_in_order(v->right, f);
    void debug print all() {
#ifdef COMPPROG LOCAL
        auto visit = [](Node &v) { dbg("{} ", v.value); };
        visit_in_order(root, visit);
#endif
   }
};
```

2.6 Vector

```
struct Vec {
    using K = double;
    K x;
    K y;

    Vec operator+(const Vec &other) const {
        return Vec{x + other.x, y + other.y};
    }
    Vec operator-() const { return Vec{-x, -y}; }
    Vec operator-(const Vec &other) const { return *this + (-other); }
```

```
K dot(const Vec &other) const { return x * other.x + y *
other.y; }
   K cross_val(const Vec &other) const { return x * other.y
- y * other.x; }
   K len_sqr() const { return this->dot(*this); }
   K len() const { return sqrt(len_sqr()); }
};
```

3 Graph

3.1 Dijkstra

```
vector<ull> dist(n, inf);
min priority queue<pair<ull, uint>> pq;
dist[start] = 0;
pq.push({dist[start], start});
while (!pq.empty()) {
    auto [weight_in, u] = pq.top();
    pq.pop();
    // u might be added multiple times for longer path, but
we only care about the first time it
    // is removed from the queue
    if (weight_in > dist[u]) continue;
    for (auto [v, w] : g[u]) {
        if (dist[u] + w < dist[v]) {</pre>
            dist[v] = dist[u] + w;
            pq.push({dist[v], v});
       }
   }
}
```

3.2 Floyd Warshall

3.3 Kruskal

```
struct Edge {
    ll w;
    uint u, v;

auto operator<=>(const Edge &) const = default;
```

```
};

vector<Edge> kruskal(uint n, vector<Edge> edges) {
    ranges::sort(edges);

    vector<Edge> mst;
    UnionFind uf(n);
    for (auto edge : edges) {
        if (uf.key(edge.u) == uf.key(edge.v)) continue;
        uf.unite(edge.u, edge.v);
        mst.push_back(edge);
    }
    return mst;
}
```

3.4 Topological Order

```
vector<uint> topo;
urep(u, n) if (!in_deg[u]) topo.push_back(u);
urep(i, n) for (auto u : g[topo[i]]) if (!--in_deg[u])
topo.push back(u);
```

3.5 Bridges

```
vector<uint> st;
vector<vector<uint>> components;
vector<int> depth_of(n, -1);
vector<pair<uint, uint>> bridges;
auto dfs = [&] (uint v, uint parent, uint depth, auto &rec) -
> uint {
   auto old_size = size(st);
   st.push_back(v);
   uint up = 0;
    depth_of[v] = depth;
    for (auto neigh : q[v]) {
        if (depth_of[neigh] == -1) up += rec(neigh, v, depth
+ 1. rec):
        up += (depth of[neigh] < depth);</pre>
        up -= (depth_of[neigh] > depth);
   }
   if (up == 1) {
        bridges.emplace back(parent, v);
   }
   if (depth == 0 || up == 1) {
        components.emplace back(st.begin() + old size,
st.end());
        st.resize(old_size);
   }
    return up:
dfs(0, 0, 0, dfs);
```

3.6 Cut-Vertices

```
// returns earliest discover time
// reachable via 1 edge from my subtree
int dfs(int v) {
    int low = disc[v] = time++;
    int kids = 0;
    for (int v2 : adj[v]) {
        int st_pos = size(st);
        if (disc[v2] == -1) \{ // tree edge
            ++kids;
            int low2 = dfs(v2, v):
            low = min(low, low2);
            if (low2 >= disc[v]) { // exiting comp
                comps.emplace_back(begin(st) + st_pos,
end(st)):
                st.resize(st pos);
                if (p[v] != -1 \&\& kids > 1) {
                    // v is cut-vertex
                }
        if (disc[v2] < disc[v]) // from below</pre>
            st.push back({v, v2});
        low = min(low, disc[v2]);
    }
    return low;
}
```

3.7 SCC

```
uint scc count = 0;
vector<vector<uint>> scss;
vector<uint> scc_of(g.size(), inf);
vector<uint> disc(g.size(), inf);
vector<uint> some node in scc;
auto dfs = [&, time = Ou, st = vector<uint>(), in_stack =
vector(g.size(), false)](
               uint v, auto &rec) mutable -> uint {
    uint old size = st.size();
    st.push_back(v);
    in_stack[v] = true;
    uint low = disc[v] = time++;
    for (auto v2 : g[v]) {
        if (disc[v2] == inf) low = min(low, rec(v2, rec));
        else if (in_stack[v2]) low = min(low, disc[v2]);
   if (low == disc[v]) {
        for (uint i = old size; i < st.size(); ++i) {</pre>
            scc of[st[i]] = scc count;
            in_stack[st[i]] = false;
        some_node_in_scc.push_back(v);
        scc count++;
        sccs.emplace back(st.begin() + old size, st.end());
```

```
st.resize(old_size);
}
return low;
};
urep(v, g.size()) if (disc[v] == inf) dfs(v, dfs);
```

4 Flows

4.1 Ford Fulkerson

```
template <typename T> using Mat = vector<vector<T>>;
using Cap = ull;
auto bfs(const Mat<Cap> &g, vector<int> &parent, const uint
s, const uint t, const Cap min cap) {
    vector<bool> seen(g.size(), false);
    queue<uint> q;
    q.push(s);
    seen[s] = true;
    parent[s] = -1;
   while (!q.empty()) {
        auto cur = q.front();
       q.pop();
       urep(neigh, g.size()) if (!seen[neigh] && g[cur]
[neigh] >= min_cap) {
            parent[neigh] = cur;
            if (neigh == t) {
                return true;
            seen[neigh] = true;
            q.push(neigh);
       }
   }
    return false;
}
auto max_flow(Mat<Cap> &g, const uint s, const uint t) {
    Cap flow = 0;
    vector<int> parent(g.size());
    Cap min_cap = *ranges::max_element(g[s]);
   while (min cap) {
       while (bfs(g, parent, s, t, min_cap)) {
            uint prev = t, cur;
            Cap bottleneck = numeric_limits<Cap>::max();
            while (prev != s) {
                cur = parent[prev]:
               bottleneck = min(bottleneck, g[cur][prev]);
                prev = cur;
```

```
prev = t;
       while (prev != s) {
            cur = parent[prev];
            g[cur][prev] -= bottleneck;
            g[prev][cur] += bottleneck;
            prev = cur;
       flow += bottleneck;
   }
   min_cap /= 2;
return flow;
```

```
4.2 Dinitz
struct Edge {
    uint from, to;
    ll cap;
    II flow = 0;
    Edge *rev = nullptr;
};
Graph<Edge *> g(n);
auto add_edge = [&](uint u, uint v, ll cap) {
    if (cap == 0) return;
    auto uv = new Edge{u, v, cap};
    auto vu = new Edge{v, u, 0};
    uv -> rev = vu;
    vu -> rev = uv;
    g[u].push back(uv);
    g[v].push_back(vu);
};
ll total flow = 0;
while (true) {
    // build L
    const auto inf = numeric_limits<uint>::max();
    vector<uint> dist(g.size(), inf);
    dist[source] = 0;
    queue<uint> q;
    q.push(source);
    while (!q.empty()) {
        auto u = q.front();
        q.pop();
        for (auto e : g[u]) {
            if (dist[e->to] == \inf \&\& e->flow < e->cap) {
                q.push(e->to);
                dist[e->to] = dist[u] + 1;
            }
        }
    if (dist[target] == inf) break;
    // augment
```

```
vector<uint> current_edge_index(g.size(), 0);
    auto dfs = [&](uint u, ll bottleneck_so_far, auto &rec)
-> ll {
        if (u == target) return bottleneck so far;
        for (auto &i = current_edge_index[u]; i <</pre>
g[u].size(); ++i) {
            auto e = g[u][i];
            if (e->flow == e->cap) continue;
            if (dist[e->to] != dist[u] + 1) continue;
            auto pushed = rec(e->to, min(bottleneck_so_far,
e->cap - e->flow), rec);
            if (pushed == 0) continue;
            e->flow += pushed;
            e->rev->flow -= pushed;
            return pushed;
        }
        return 0;
   };
    while (true) {
        auto bottleneck = dfs(source,
numeric limits<ll>::max(), dfs);
        if (bottleneck == 0) break;
        total_flow += bottleneck;
   }
}
```

4.3 Path Decomposition

```
vector<uint> current_edge_index(n, 0);
vector<pair<ll, vector<uint>>> paths;
while (true) {
    vector<Edge *> path_edges;
    vector<uint> path;
    auto dfs = [&](uint u, ll bottleneck_so_far, auto &rec)
-> ll {
        if (u == target) return bottleneck so far;
        for (auto &i = current_edge_index[u]; i <</pre>
g[u].size(); ++i) {
           auto e = g[u][i];
           if (e->cap != 0 \&\& e->flow > 0) {
                path edges.push back(e);
                path.push_back(u);
                return rec(e->to, min(bottleneck_so_far, e-
>flow), rec):
        }
        return 0;
   };
    auto bn = dfs(source, numeric limits<ll>::max(), dfs);
   if (bn == 0) break:
    for (auto e : path edges) e->flow -= bn, e->rev->flow +=
bn;
    path.push back(target);
```

```
paths.push_back(make_pair(bn, move(path)));
```

4.4 Min Cost Flow

```
struct Edge {
    const uint from;
    const uint to;
    ll flow;
    const ll cap;
    const ll cost;
    Edge *rev = nullptr;
};
auto add_edge = [&g, &all_edges](uint u, uint v, ll cap, ll
cost) mutable {
    auto *uv = new Edge(u, v, 0, cap, cost);
    auto *vu = new Edge(v, u, 0, 0, -cost);
    uv -> rev = vu:
    vu -> rev = uv;
    g[u].push_back(uv);
    g[v].push_back(vu);
};
ll total flow = 0;
vector<ll> johnson_offset(g.size(), inf);
    // Bellman Ford to get johnson offsets
    auto &dist = johnson offset;
    dist[source] = 0;
    queue<uint> q;
    q.push(source);
    vector<bool> in_q(g.size());
    in_q[source] = true;
    while (!q.empty()) {
        auto u = q.front();
        q.pop();
        in_q[u] = false;
        for (auto e : q[u]) {
            if (e->flow == e->cap) continue;
            if (dist[e->from] == inf) continue;
            if (dist[e->from] + e->cost >= dist[e->to])
continue;
            dist[e->to] = dist[e->from] + e->cost;
            if (in q[e->to]) continue;
            q.push(e->to);
            in_q[e->to] = true;
       }
    }
}
while (true) {
    // try to find shortest path according to cost
    vector<ll> dist(g.size(), inf);
    dist[source] = 0;
```

```
vector<Edge *> incoming(g.size());
    priority_queue<pair<ll, uint>, vector<pair<ll, uint>>,
greater<>> q;
    q.push({0, source});
    vector<bool> done(g.size());
    while (!q.empty()) {
        auto [_, u] = q.top();
        q.pop();
        done[u] = true;
        for (auto e : g[u]) {
            if (done[e->to]) continue;
            if (e->flow == e->cap) continue;
            if (dist[e->from] == inf) continue;
            const auto john cost = e->cost +
johnson_offset[e->from] - johnson_offset[e->to];
            if (dist[e->from] + john_cost >= dist[e->to])
continue;
            dist[e->to] = dist[e->from] + john_cost;
            incoming[e->to] = e;
            q.push({dist[e->to], e->to});
        }
    }
    if (dist[target] == inf) break;
    urep(v, g.size()) johnson_offset[v] += dist[v] -
dist[target];
    // find bottleneck
    ll bottleneck = inf;
    for (auto v = target; v != source; v = incoming[v]-
>from)
        bottleneck = min(bottleneck, incoming[v]->cap -
incoming[v]->flow);
    total_flow += bottleneck;
    // augment
    for (auto v = target; v != source; v = incoming[v]-
>from) {
        incoming[v]->flow += bottleneck;
        incoming[v]->rev->flow -= bottleneck;
   }
}
ll total cost = 0;
for (auto &row : g)
    for (auto e : row) total_cost += e->flow * e->cost;
total cost /= 2;
```

5 Matchings

5.1 Maximum Weight Bipartite Matching

Use min-cost-flow, but make sure to look at current cost in each iteration, because max-flow might not be max-weight.

5.2 Stable Matching (Gale Shapley)

```
using Matching = vector<pair<uint, uint>>;
```

```
Matching gale_shapley(
    const vector<vector<uint>> &preference_lists_left,
    const vector<vector<uint>> &preference lists right) {
    auto right rank =
        vector(preference lists right.size(),
               vector(preference_lists_left.size(), Ou));
   urep(w, preference lists right.size()) {
       right rank[w].assign(
           preference_lists_left.size(),
            preference_lists_right[w].size());
       urep(i, preference_lists_right[w].size())
            right rank[w][preference lists right[w][i]] = i;
   }
    queue<uint> free_left;
    urep(u, preference_lists_left.size()) free_left.push(u);
    vector<uint> next index(preference lists left.size(),
    vector<uint> current_partner_index(
        preference lists right.size());
    urep(w, preference lists right.size())
        current partner index[w] =
            preference_lists_right[w].size();
    while (!free left.empty()) {
        auto u = free left.front();
        free_left.pop();
       auto asking_index = next_index[u]++;
       if (asking index == preference lists left[u].size())
            continue:
        auto w = preference_lists_left[u][asking_index];
       if (current partner index[w] ==
               preference lists right[w].size() ||
            right rank[w][u] <
                right_rank[w][current_partner_index[w]]) {
           if (current_partner_index[w] <</pre>
               preference lists right[w].size()) {
               auto cur partner = preference lists right
                    [w][current_partner_index[w]];
               free_left.push(cur_partner);
            current partner index[w] = right rank[w][u];
    }
    Matching m;
    urep(w, preference_lists_right.size()) {
       if (current_partner_index[w] !=
           preference_lists_right[w].size()) {
            const auto u = preference lists right
                [w][current_partner_index[w]];
            m.emplace back(u, w);
```

```
}
return m;
}
```

6 Trees

6.1 Binary lifting

```
auto lift_by = vector(bit_width(g.size()), vector(g.size(),
root));
urep(v, n) lift by[0][v] = parent[v];
lift_by[0][root] = root;
urep(prev_height, lift_by.size() - 1)
    urep(v, n) lift by[prev height + 1][v] =
lift by[prev height][lift by[prev height][v]];
auto lca = [&](uint u, uint v) {
    if (depth[u] > depth[v]) swap(u, v);
    const auto depth diff = depth[v] - depth[u];
    urep(i, lift_by.size()) if (depth_diff & (1 << i)) u =</pre>
lift_by[i][u];
    debug_assert(depth[u] == depth[v]);
    if (u == v) return u;
    for (int i = lift_by.size() - 1; i >= 0; --i)
        if (lift by[i][u] != lift by[i][v]) u = lift by[i]
[u], v = lift_by[i][v];
    return parent[u];
};
```

6.2 Heavy Light Decomposition

```
const auto inf = numeric limits<uint>::max();
vector<uint> size(n, 0), parent(n, inf), depth(n, inf);
vector<uint> heavy child(n, inf);
auto dfs1 = [&](auto v, auto &rec) -> void {
    size[v] = 1:
    for (auto child : g[v])
        if (child != parent[v]) {
            parent[child] = v;
            depth[child] = depth[v] + 1;
            rec(child, rec);
            size[v] += size[child];
            if (heavy child[v] == inf ||
size[heavy_child[v]] < size[child]) heavy_child[v] = child;</pre>
};
const uint root = 0;
depth[root] = 0;
parent[root] = root;
dfs1(root, dfs1);
// heavy light
vector<uint> head(n), pos(n);
vector<uint> initial values(n);
auto dfs2 = [&, next_index = 1u](uint v, uint cur_head, auto
&rec) mutable -> void {
    head[v] = cur_head;
```

```
niklasmohrin/cp
    pos[v] = next_index++;
   initial_values[pos[v] - 1] = value_for_node[v];
   if (heavy_child[v] != inf) rec(heavy_child[v], cur_head,
rec);
    for (auto child : g[v])
       if (child != parent[v] && child != heavy child[v])
rec(child, child, rec);
};
dfs2(root, root, dfs2);
SegmentTree seg(initial_values);
uint u = a, v = b;
SegmentTree::Node ans = SegmentTree::neutral element;
for (; head[u] != head[v]; v = parent[head[v]]) {
   if (depth[head[u]] > depth[head[v]]) swap(u, v);
    ans = SegmentTree::op(ans,
seg.range_query({pos[head[v]], pos[v] + 1}));
if (depth[u] > depth[v]) swap(u, v);
ans = SegmentTree::op(ans, seg.range_query({pos[u], pos[v] +
6.3 Centroids
uint find_centroid(Graph<> &g, const uint n, const uint
   uint centroid = root:
```

```
root, span<Data const> data) {
check:
   for (uint i = 0; i < g[centroid].size();) {</pre>
       const auto child = g[centroid][i];
       if (data[child].deleted) {
           swap_remove(g[centroid], i);
            continue;
       }
       ++i;
       if (child != data[centroid].parent && 2 *
data[child].sz > n) {
            centroid = child;
           goto check;
       }
   }
   return centroid;
```

Note: Slides mention centroid tree for radius queries.

7 Strings

7.1 P and Z functions

```
auto prefix(string view x) {
   // P[i] is the length of the longest proper prefix of x
that is a suffix of
```

```
// x[..i]
    vector<unsigned> P(x.length());
    P[0] = 0;
    for (unsigned i = 1; i < x.length(); i++) {
       auto j = P[i - 1];
       while (j > 0 \&\& x[i] != x[j]) j = P[j - 1];
        if (x[i] == x[j]) j++;
        P[i] = j;
   }
    return P:
}
auto string z(string view x) {
    // Z[i] is the length of the longest common prefix of t
and t[i..]
    vector<unsigned> Z(x.length(), 0);
    unsigned l = 0, r = 0;
    for (unsigned i = 1; i < x.length(); i++) {
        if (i \le r) Z[i] = min(r - i + 1, Z[i - l]);
       while (i + Z[i] < x.length() && x[Z[i]] == x[i +
Z[i]]) Z[i]++;
       if (i + Z[i] - 1 > r) {
           l = i:
            r = i + Z[i] - 1;
       }
    }
    return Z;
}
```

7.2 Rolling hashes

```
constexpr ull base = 28;
constexpr ull base inv = 535714297;
constexpr ull mod = 1000000021;
constexpr array<ull, 32> a_powers = ([]() {
    array<ull, 32> res;
    res[0] = base;
    urep(i, 31) res[i + 1] = (res[i] * res[i]) % mod;
    return res:
})();
auto to_num = [](char c) { return 1ull + c - 'a'; };
auto pow a = [\&a powers](auto exp) {
    ull res = 1;
    urep(i, 32) {
        if (exp & 1) res = (res * a_powers[i]) % mod;
        exp >>= 1:
   }
    return res;
};
string s;
ull hash = 0:
rep(i, len) hash = (((hash * base) % mod) + to num(s[len - 1
- i])) % mod;
```

7.3 Suffix Array

```
pair<vector<vector<uint>>, vector<uint>>
build suffix array(const auto &s) {
    debug assert(has_single_bit(s.size()));
    vector<uint> order(s.size());
    iota(all(order), 0);
    ranges::sort(order, [&](auto i, auto j) { return s[i] <</pre>
s[i]; });
    auto equiv = vector(ceil(log2(s.size())) + 1,
vector(s.size(), Ou));
    urep(i, s.size() - 1) equiv[0][order[i + 1]] =
        equiv[0][order[i]] + (s[order[i]] != s[order[i +
111):
    for (uint k = 0; (1 << k) < s.size(); ++k) {
        const auto &cur_equiv = equiv[k];
        vector<uint> count(s.size(), 0);
        urep(i, s.size()) count[cur equiv[i]]++;
        partial sum(all(count), count.begin());
        vector<uint> by_second(s.size());
       urep(i, s.size()) by second[i] =
            ((((int)order[i] - (1 << k)) % s.size()) +
s.size()) % s.size();
        ranges::reverse(by_second);
        for (auto i : by second) order[--
count[cur_equiv[i]]] = i;
        const auto parts = [&](auto i) {
            return pair(cur_equiv[i], cur_equiv[(i + (1 <<</pre>
k)) % s.size()]);
       };
       // ranges::sort(order,
                        [&](auto i, auto j) { return
parts(i) < parts(j); });</pre>
        auto &next_equiv = equiv[k + 1];
       urep(i, s.size() - 1) next_equiv[order[i + 1]] =
            next equiv[order[i]] + (parts(order[i]) !=
parts(order[i + 1]));
   }
    return pair(move(equiv), move(order));
}
string s;
while (!has single bit(s.size())) s += '$';
const auto [_equivs, _suf] = build_suffix_array(s);
const auto &equivs = _equivs;
const auto &suf = suf;
```

```
const auto lcp = [&](uint i, uint j) {
    debug_assert(i != j);

uint len = 0;
    for (int k = equivs.size() - 1; k >= 0; --k) {
        if (equivs[k][i] == equivs[k][j]) {
            len += 1 << k;
            i += 1 << k;
            j += 1 << k;
            }
    }
    return len;
};</pre>
```

7.4 Aho-Corasick

```
struct AhoCorasick {
    constexpr static uint A = 26;
   static uint to_num(char c) { return c - 'a'; }
   struct Node {
       array<uint, A> next = {};
       uint matches here = 0;
   };
    constexpr static uint root = 0;
   vector<Node> trie:
   AhoCorasick() : trie(1) {}
   void add string(string view s) {
       uint v = root:
       for (auto c : s) {
           c = to_num(c);
           if (!trie[v].next[c]) {
                trie[v].next[c] = trie.size();
                trie.emplace back();
           }
           v = trie[v].next[c];
        ++trie[v].matches here;
   }
   void finalize() {
       queue<array<uint, 4>> q;
       q.push({0, 0, 0, 0});
       while (!q.empty()) {
           auto [v, p, plink, pch] = q.front();
           q.pop();
           const auto link = p == 0 ? 0:
trie[plink].next[pch];
           urep(c, A) {
               if (trie[v].next[c])
q.push({trie[v].next[c], v, link, c});
                else trie[v].next[c] = trie[link].next[c];
```

```
    trie[v].matches_here += trie[link].matches_here;
}

uint count_matches(string_view text) {
    uint v = root;
    uint count = trie[v].matches_here;
    for (auto c : text) {
        c = to_num(c);
        v = trie[v].next[c];
        count += trie[v].matches_here;
}

return count;
}

};
```

8 Math

8.1 Chinese Remainder Theorem

```
array<ll, 3> gcd_ext(ll a, ll b) {
    if (!a) return {b, 0, 1};
    auto [d, x1, y1] = gcd_ext(b % a, a);
    return {d, y1 - (b / a) * x1, x1};
}
pair<ll, ll> crt(ll a, ll m, ll b, ll n) {
    auto [g, x, y] = \gcd ext(m, n);
    ll l = m / g * n;
    ll ret = (a + ((x * (b - a) / g) % (l / m)) * m) % l;
    return {(b - a) % g ? -1 : (ret + l) % l, l};
}
pair<ll, ll> crt(span<ll const> a, span<ll const> m) {
    ll sol = a[0], l = m[0];
    for (uint i = 1; i < a.size(); i++) {</pre>
        tie(sol, l) = crt(sol, l, a[i], m[i]);
        if (sol == -1) break;
    return {sol, l};
}
```

8.2 Primality and Factoring

```
bool miller_rabin(ull n) {
    assert(n > 1);
    constexpr static array<ll, 12> witnesses = {2, 3, 5, 7,
11, 13, 17, 19, 23, 29, 31, 37};
    if (n < 38) return find(all(witnesses), n) !=
    witnesses.end();
    auto d = n - 1;
    auto s = countr_zero(d);
    d >>= s;
    return ranges::all of(witnesses, [=](auto witness) {
```

```
ll x = mod_pow(witness, d, n);
        if (x == 1 \mid \mid x == n - 1) return true;
        rep(_, s - 1) {
            x = (x * x) % n;
            if (x == n - 1) return true;
        return false;
    });
}
ll rho(ll n, ll x0 = 2, ll c = 1) {
    if (n % 2 == 0) return 2;
    auto f = [=](ll x) \{ return (((x * x) % n) + c) % n; \};
    11 x = x0:
    ll y = f(x0);
    ll g = gcd((((x - y) % n) + n) % n, n);
    while (q == 1) {
        x = f(x);
       y = f(f(y));
        g = gcd((((x - y) % n) + n) % n, n);
    return g;
}
void factorize(auto n, auto &callback) {
    static mt19937 64 gen;
    static uniform int distribution<> distrib(2, 1000);
    assert(n > 1);
    if (miller rabin(n)) {
        callback(n);
        return;
    }
    auto d = rho(n, 2, distrib(gen));
    while (d == n) d = rho(n, 2, distrib(gen));
    factorize(d, callback);
    factorize(n / d, callback);
```

8.3 Fast Fourier Transform

```
using C = complex<long double>;
constexpr auto pi = std::numbers::pi_v<C::value_type>;
using Polynomial = vector<C>;
using PointForm = Polynomial;

void fft_iter(Polynomial &a, const span<const C> z) {
    const auto n = a.size();
    const auto log_n = bit_width(n) - 1;
    for (uint i = 0, j = 0; i < n - 1; ++i) {
        if (i < j) swap(a[i], a[j]);
        const uint x = countr_one(i) + 1;
        j ^= ((1 << x) - 1) << (log_n - x);
    }
    for (uint k = 1; 2 * k <= n; k *= 2) {</pre>
```

```
for (uint i = 0; i < n; i += 2 * k) {
           urep(j, k) {
                const auto u = a[i + j], v = a[i + j + k];
                a[i + j] = u + v * z[j * n / (2 * k)];
                a[i + j + k] = u - v * z[j * n / (2 * k)];
       }
   }
Polynomial multiply(Polynomial a, Polynomial b) {
   const auto na = a.size(), nb = b.size();
   const auto n = bit ceil(na + nb - 1);
   a.resize(n, 0);
   b.resize(n, 0);
   PointForm z(n);
   urep(i, n) z[i] = polar(C::value type(1), i * 2 * pi /
n);
    fft_iter(a, z);
    fft iter(b, z);
   PointForm c(n);
   urep(i, n) c[i] = a[i] * b[i] / C(n);
   fft_iter(c, z);
    reverse(c.begin() + 1, c.end());
   c.resize(na + nb - 1);
    return c;
```

8.4 Number Theoretic Transform

```
template <const ull MOD, const ull prim_root> struct NTT {
    constexpr static ull modmul(ull a, ull b) {
        return (a * b) % MOD;
       // ll ret = a * b - MOD * ull(1.L / MOD * a * b);
       // return ret + MOD * (ret < 0) - MOD * (ret >=
(ll)MOD);
   }
    constexpr static ull modpow(ull b, ull e) {
       ull ans = 1:
        for (; e; b = modmul(b, b), e /= 2)
           if (e \& 1) ans = modmul(ans, b);
        return ans;
    constexpr static ull modinv(ull x) { return modpow(x,
MOD - 2); }
   static_assert(modpow(prim_root, MOD - 1) == 1);
   using Polynomial = vector<ull>;
   using PointForm = Polynomial;
   static void ntt iter(Polynomial &a) {
        const auto n = a.size();
```

```
debug assert(has single bit(n));
        const auto log_n = bit_width(n) - 1;
        for (uint i = 0, j = 0; i < n - 1; ++i) {
            if (i < j) swap(a[i], a[j]);</pre>
            const uint x = countr one(i) + 1;
            j = ((1 << x) - 1) << (log_n - x);
       }
       for (uint k = 1; 2 * k <= n; k *= 2) {
            debug assert((MOD - 1) % (2 * k) == 0);
            const auto zn = modpow(prim_root, (MOD - 1) / (2
* k));
            for (uint i = 0; i < n; i += 2 * k) {
                ull z = 1;
                urep(j, k) {
                    const auto u = a[i + j], v = a[i + j +
k];
                    const auto vv = modmul(v, z);
                    a[i + j] = (u + vv) % MOD;
                    a[i + j + k] = (u + (MOD - vv)) % MOD;
                    z = modmul(z, zn);
                }
           }
        }
    }
   // Repeated application
    static void ntt_q(Polynomial &a, ull q) {
        const auto factor = modpow(a.size(), ((q / 4) * 2));
        for (auto &x : a) x = modmul(x, factor);
       urep(_, q % 4) ntt_iter(a);
   }
};
```