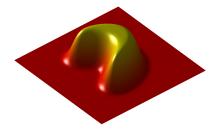
## Smoothness Multivariable Calculus

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## 1 Intuitive Sense



For a curve to be considered smooth, it needs to be *smooth*. There cannot be corners.

## 2 Mathematical Sense

To express that some function f(x) is smooth, we express it with the differentiability class

$$f(x) \in C^{(n)} | n \in \mathbb{N}$$

In other words, all derivative functions of f(x), up to the  $n^{th}$  derivative of the function, are continuous.

If a functions is in itself continuous, then

$$f(x) \in C^{(0)}$$

This is also the minimum requirement for a "smooth" curve.

A curve can also be differentiable for derivative of all orders in its domain, where it is called "infinity differentiable"

$$f(x) \in C^{(\infty)}$$

## 3 Examples

1. f(x) = 0 is considered smooth, and also infinitely differentiable, since derivatives of any order is 0.

- 2.  $e^x$  is also smooth and infinitely differentiable, since it stays the same.
- 3.  $\sin(x)$  is also a function that is differentiable for all orders.