Note The due date for this assignment is **Friday** 5/5, so that it will not be due too soon after the Midterm. However, the last problem set will be due soon after, on Tuesday 5/9 (the last day of class). It will be posted by Wednesday 5/3. So I would recommend doing as much of this one as possible by Wednesday to leave time to move on to the next. The last set will be a bit shorter, however.

Written problems:

1. Textbook exercise 6.1 (Elliptic curve arithmetic over $\mathbb{R}$)
2. Textbook exercise 6.5, parts (a) and (b) (Listing the points of an EC over $\mathbb{Z}/p\mathbb{Z}$)

   Hint. You can save some time by making two lists in advance: values of y^2 for various y and values of $x^3 + Ax + B$ for various values of x, then checking for numbers occurring in both lists)
3. Textbook exercise 6.6(a) (addition table for an elliptic curve over $\mathbb{Z}/5\mathbb{Z}$)
4. Textbook exercise 6.9 (listing all solutions n to an equation $Q = n \cdot P$ on an elliptic curve).
5. Textbook exercise 6.16. (A more concise way to send EC points; you should read Proposition 2.26 to do part (b))

Programming problems:

1. Write a function `ecAdd(P,Q,A,B,p)` to compute the sum $P \oplus Q$ of two points on the Elliptic Curve over $\mathbb{Z}/p\mathbb{Z}$ defined by $Y^2 \equiv X^3 + AX + B \pmod{p}$. You may assume that P and Q are both valid points on the curve[1]. The points P and Q will be either pairs (x, y) of elements of $\mathbb{Z}/p\mathbb{Z}$, or the integer `0` (as a stand-in for the point $\mathcal{O}$ at infinity), and the function should return the result in the same format.
2. Write a function `ecMult(n,P,A,B,p)` that computes an integer multiple $n \cdot P$ of a point P on an elliptic curve $Y^2 \equiv X^3 + AX + B \pmod{p}$. Points will be formatted (x, y), with $0 \leq x, y < p$, while the point at infinity should be denoted simply as 0. Your code will need to be able to scale to very large values of n; I suggest adapting the fast-powering algorithm from modular arithmetic to elliptic curves.

[1] Though of course if you were using this code in real life, you should add some error handling that checks this.