# **Stack Safety for Free**

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### Hello!

- I'm Phil, I write Haskell and PureScript
- paf31 on Twitter/GitHub

Consider this Haskell function:

```
replicateM_ :: Monad m => Int -> m a -> m ()
replicateM_ 0 _ = return ()
replicateM_ n x = x >> replicateM_ (n - 1) x
```

We can test this using GHC:

```
main = print $ replicateM_ 100000000 (Just ())
```

This gets compiled to a tight loop:

But how would we write this function in a strict language like *PureScript*?

#### **PureScript**

- a strict Haskell-like language compiling to JS
- features type classes, HKP
- see <u>purescript.org</u>

#### In PureScript:

```
replicateM_ :: ∀ m a. Monad m => Int -> m a -> m Unit
replicateM_ 0 _ = pure unit
replicateM_ n x = x *> replicateM_ (n - 1) x
```

#### This fails quickly with

```
RangeError: Maximum call stack size exceeded
```

(demo)

#### Recap:

A tail recursive function can either

- return a value
- or loop, modifying some function arguments

at each step.

The compiler can turn such a function into a *loop*.

For example:

```
replicateM_ :: \( \text{m a. Monad m => Int -> m a -> m Unit} \)
replicateM_ n \( x = loop \) (pure unit) n where
  loop :: m Unit -> Int -> m Unit
  loop acc 0 = acc
  loop acc n = loop (x *> acc) (n - 1)
```

This works for some monads, like Maybe:

```
> replicateM_ 1000000 (Just 42)
Just unit
```

but still fails for others, like Eff:

```
> replicateM_ 1000000 (log "testing")
RangeError: Maximum call stack size exceeded
```

- " A tail recursive function can either
  - return a value
  - or loop, modifying some function arguments

Now let's reify those constraints as a data structure:

```
data Step a b
= Done b
| Loop a
```

Now we can write a general-purpose tail-recursive function of one argument:

```
tailRec :: ∀ a b. (a -> <mark>Step</mark> a b) -> a -> b
```

This can be used to write variants with multiple arguments:

This is enough to reimplement replicateM\_:

```
replicateM_ :: \forall m a. Monad m => Int -> m a -> m Unit
replicateM_ n x = tailRec2 loop (pure unit) n where
  loop :: m Unit
        -> Int
        -> Step { fst :: m Unit, snd :: Int } (m Unit)
  loop acc 0 = Done acc
  loop acc n = Loop { fst: x *> acc, snd: n - 1 }
```

Of course, this doesn't solve the problem, yet

The trick:

Generalize tailRec to monadic tail recursion using a new type class

```
class Monad m <= MonadRec m where
  tailRecM :: (a -> m (Step a b)) -> a -> m b
```

What should the laws be?

tailRecM should be equivalent to the default definition:

```
tailRecM f a =
  step <- f a
  case step of
  Done b -> pure b
  Loop a1 -> tailRecM f a1
```

However, we can provide a more efficient implemenation!

#### Example: ExceptT

```
newtype ExceptT e m a = ExceptT (m (Either e a))
instance MonadRec m => MonadRec (ExceptT e m) where
tailRecM f = ExceptT <<< tailRecM \a ->
    case f a of ExceptT m ->
    m >>= \m' ->
    pure case m' of
    Left e -> Done (Left e)
    Right (Loop a1) -> Loop a1
    Right (Done b) -> Done (Right b)
```

#### **More Examples**

- Identity
- StateT s
- WriterT w
- ReaderT r
- Eff eff
- Aff eff

We can fix replicateM\_ by requiring MonadRec:

```
replicateM_ :: \forall m a. MonadRec m => Int -> m a -> m Unit
replicateM_ n x = tailRecM loop n where
  loop :: Int -> m (Step Int Unit)
  loop @ = pure (Done unit)
  loop n = x $> Loop (n - 1)
```

This is stack-safe for any law-abiding MonadRec instance!

We can also implement other functions like mapM and foldM.

#### **Taxonomy of Recursion Schemes**

- StateT: Additional accumulator
- WriterT: Tail-call modulo "cons"
- ExceptT: Tail-call with abort

# **Applications**

The free monad for a functor f

represents sequences of instructions defined by f.

#### **Example:**

```
data DatabaseF a
    = Insert Key Value a
    | Select Key (Maybe Value -> a)

type Database = Free DatabaseF

insert :: Key -> Value -> Database Unit
insert k v = liftFree (Insert k v unit)

select :: Key -> Database (Maybe Value)
select k = liftFree (Select k id)
```

#### Interpretation:

#### **Testing**

```
type Test = State (Map Key Value)
testDB :: ∀ a. Database a -> Test a
testDB = runFree go where
  go :: DatabaseF (Database a) -> Test (Database a)
  go (Insert k v next) = do
    modify (insert k v)
    next
  go (Select k next) = do
    v <- gets (lookup k)
    next v
```

#### **Problem:**

runFree uses monadic recursion.

We cannot interpret deep or infinite computations without the risk of blowing the stack.

#### **Solution:**

Instead we use

```
runFree :: ∀ m f a
. MonadRec m
=> (f (Free f a) -> m (Free f a))
-> Free f a
-> m a
```

runFree can be written using tailRecM directly and uses a constant amount of stack.

### 2. Free Monad Transformers

### **Free Monad Transformers**

The free monad transformer:

```
newtype FreeT f m a =
  FreeT (m (Either a (f (FreeT f m a))))
```

interleaves effects from the base monad m.

### **Free Monad Transformers**

The previous technique extends to the free monad transformer:

```
runFreeT :: ∀ m f a
. MonadRec m
=> (f (FreeT f m a) -> m (FreeT f m a))
-> FreeT f m a
-> m a
```

(see the paper)

The free monad transformer gives a nice (safe!) model for coroutines over some base monad.

For example:

```
data Emit o a = Emit o a 
type Producer o = FreeT (Emit o)
```

Producer \_ (Aff \_) is useful for modelling asynchronous generators

#### Consumers:

```
data Await i a = Await (\underline{i} \rightarrow \underline{a})
type Consumer i = FreeT (Consumer \underline{i})
```

Consumer \_ (Aff \_) is useful for modelling asynchronous enumerators

E.g. chunked handling of HTTP responses

#### **Fusion**

```
type Fuse f g h = ∀ a b c
                . (a -> b -> c)
               -> f a
               -> g b
               -> h c
fuse :: ∀ f g h m a
      . (Functor f, Functor g, Functor h, MonadRec m)
     => Fuse f g h
     -> FreeT f m a
     -> FreeT g m a
     -> FreeT h m a
```

#### **Producer - Producer**

```
Fuse (Emit o1) (Emit o2) (Emit (Tuple o1 o2))
```

#### **Consumer - Consumer**

```
Fuse (Await i1) (Await i2) (Await (Tuple i1 i2))
```

#### **Producer - Consumer**

```
Fuse (Emit o) (Await o) Identity
```

#### **Applications:**

- Websockets
- File I/O
- AJAX
- Cooperative multitasking

(Demo)

# Conclusion

### Conclusion

- MonadRec can make a variety of tasks safe in a strict language like PureScript
- We trade off some instances for a safe implementation
- MonadRec has been implemented in PureScript, Scalaz, cats and fantasy-land.
- Check out the paper: <u>functorial.com/stack-safety-for-free/index.pdf</u>

# Thanks!