

# **Normal Approximation for the Box Model**

# Review

## Box Model

*... is like* drawing \_\_\_\_\_ times from the box \_\_\_\_\_ with replacement and summing the draws.

## Example #1

Rolling a die 40 times and summing the numbers shown

*...is like...*

drawing \_\_\_\_\_ times from the box \_\_\_\_\_ with replacement and summing the draws.

# Review

## Example #1

Rolling a die 40 times and summing the numbers shown  
*...is like...*

drawing 40 times from the box 1, 2, 3, 4, 5, 6 with  
replacement and summing the draws.

*the expected value* ↓  
*the standard error* ↓  
The sum will be about \_\_\_\_\_ give or take \_\_\_\_\_ or so.

## Equations

**expected value for sum = (number of draws)  $\times$  (average of box)**

**SE for sum =  $\sqrt{\text{number of draws} \times (\text{SD of box})}$**

## Helpful Hints

Suppose the box is a “big-small box” that only has big numbers B and small numbers S (e.g., the box 2, 2, 2, 2, 14, 14), then

**SD of big-small box =  $(B - S) \times \sqrt{(\text{fraction that are B}) \times (\text{fraction that are S})}$**

Suppose the box is a “0-1 box” that only has 0s and 1s (e.g., the box 0, 0, 0, 1), then

**SD of 0-1 box =  $\sqrt{(\text{fraction that are 0}) \times (\text{fraction that are 1})}$**

# Review

## Example #1

Rolling a die 40 times and summing the numbers shown  
*...is like...*

drawing 40 times from the box 1, 2, 3, 4, 5, 6 with replacement and summing the draws.

*the expected value*  
*the standard error*

The sum will be about 140 give or take 11 or so.

## Question

Whats the chance that the sum is more than 155?

# Normal Approximation

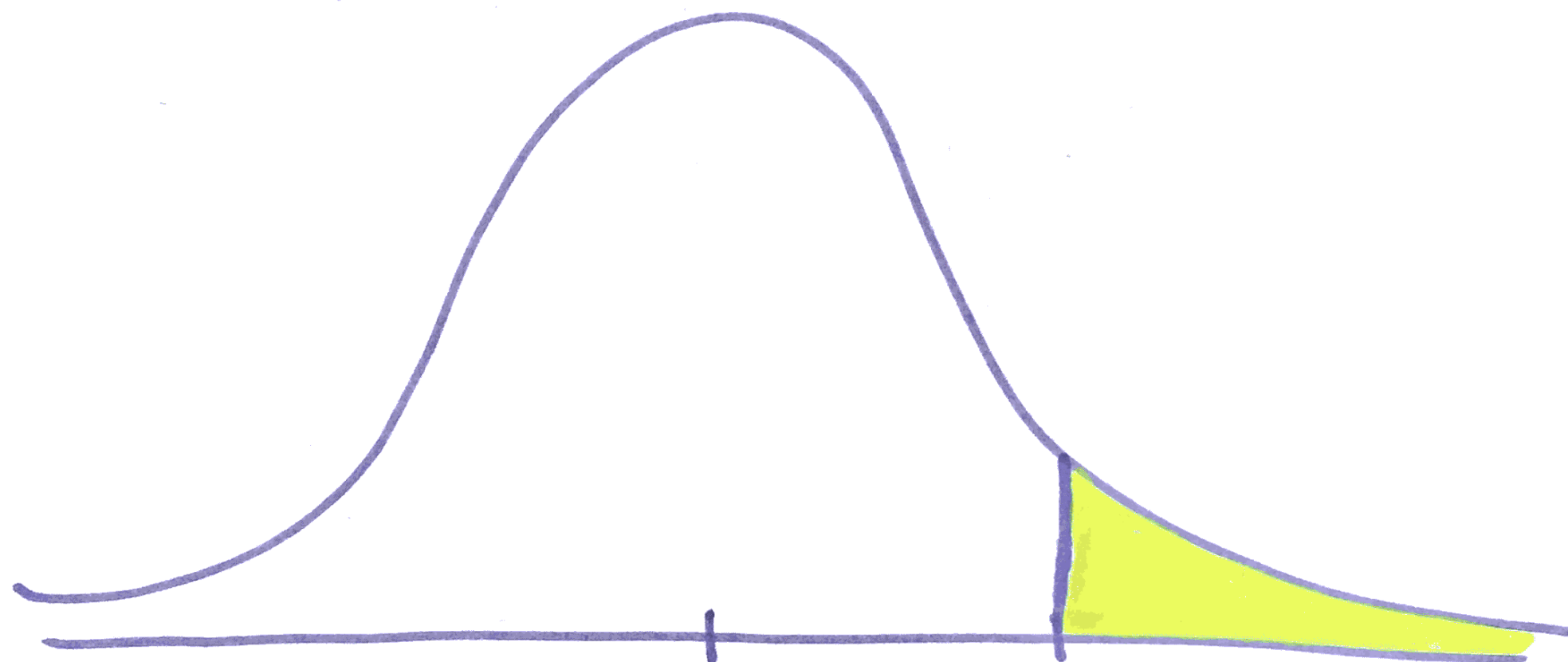
## 1. Draw a picture!

- i. bell curve
- ii. label values
- iii. shade area of interest

## 2. Convert to standard units (use expected value instead of average and standard error instead of SD).

## 3. Use rules.

- i. normal table (p. A-104)
- ii. 100%
- iii. symmetric



140



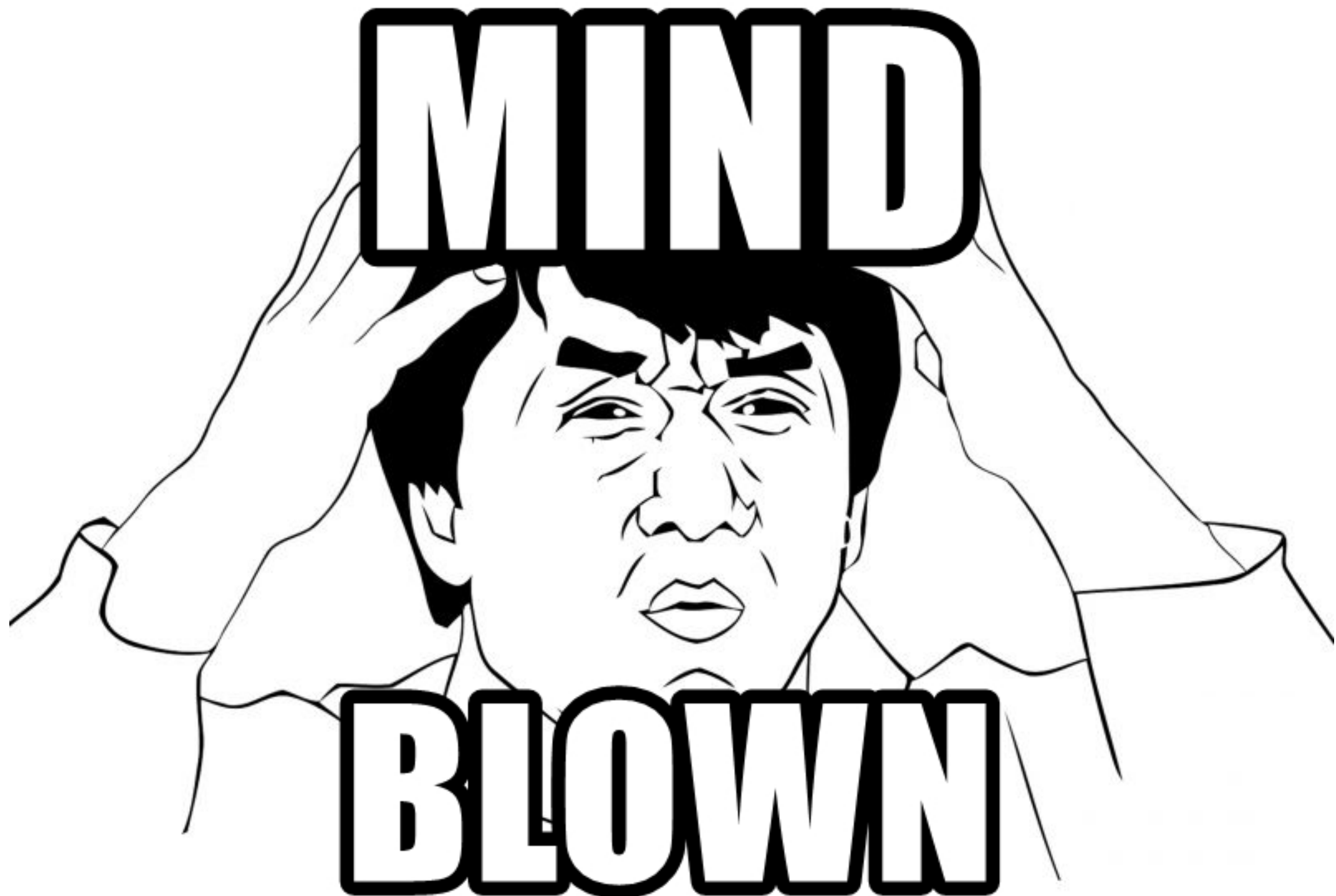
expected  
value

155



point of  
interest

As long as the number of draws is sufficiently large,  
**the sum follows the normal curve.**





# proof by example

<https://carlislerainey.shinyapps.io/box-model/>

## An App to Repeatedly Execute the Box Model

Box Model: Draw \_\_\_\_\_ times from the box \_\_\_\_\_  
with replacement and sum the draws.

**Number of Draws**

10

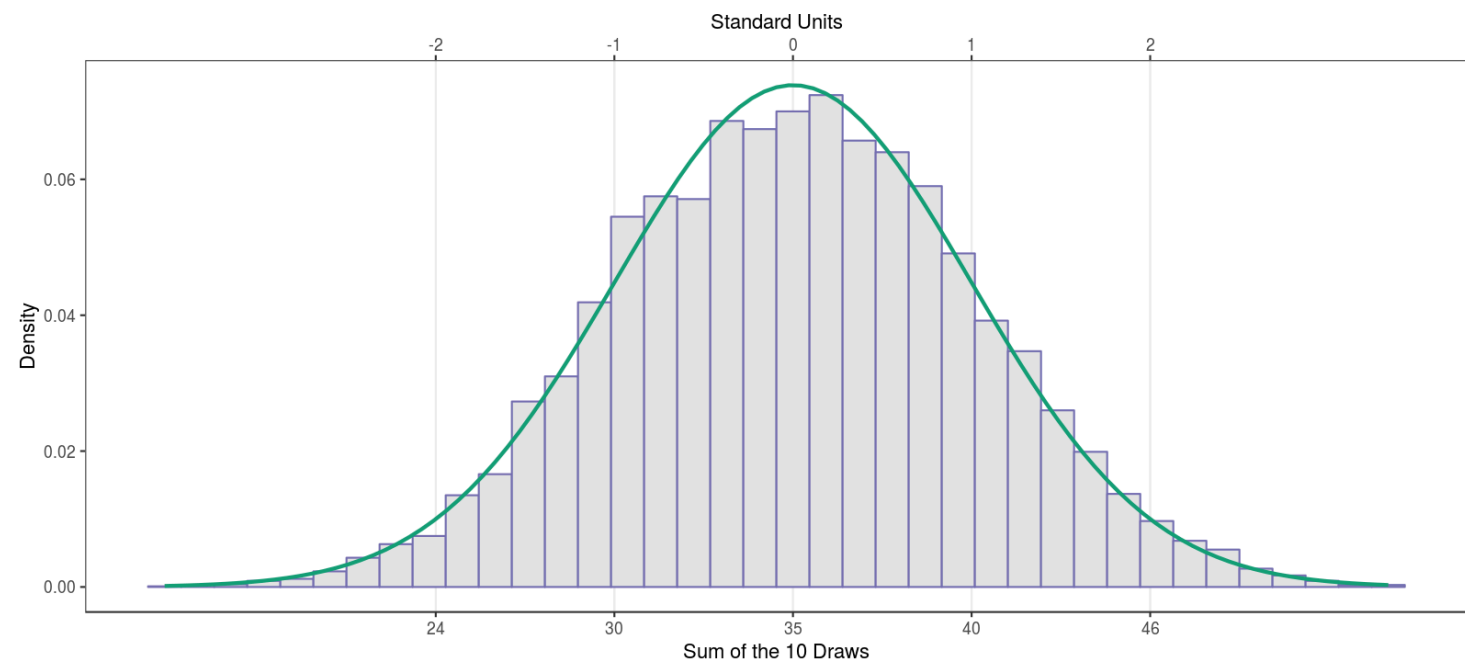
**Box (e.g., 1, 2, 2, -14):**

1, 2, 3, 4, 5, 6

Quantity	Value
Number of Draws	10
Box	1, 2, 3, 4, 5, 6
Average of Box	3.5
SD of Box	1.71
Expected Value for Sum	35
Standard Error for Sum	5.4

A Histograms of Sums

...if we execute the box model 10,000 times.



# Practice Problem I

**If I toss a coin 50 times, what's the chance I get more than 30 heads?**

**Initial guess?**

What's the box model?

What's the expected value and standard error?

What's the normal approximation?

draw picture

convert to standard units

use rules

# Practice Problem II

**Suppose I give an exam with 9 true-false questions. A student isn't well-prepared, so they decide to guess on each.**

**What's the chance they pass?**

**Initial guess?**

How many correct answer do you need to pass (more than 70%)?

What's the box model?

What's the expected value and standard error?

What's the normal approximation?

draw picture

convert to standard units

use rules