#### Direct Access Sets?

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• Better: in a tree sorted by key

Can data https://powcoder.com

#### Questions

How could such indexing work?

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Assuming such indexing, how long would put and get take in a set containing N objects?

#### Indexed Sets

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- $\bullet$  The key is converted to an integer index by a hash function h
- So, an object with key k is stored at T[h(k)]https://powcoder.com

  key: k

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The time taken by h depends only on k

• New object added into N object set in  $\Theta(1)$  time (theoretical only!)

#### Numerical Encoding

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Map any key object to a natural number

- Requirement: equal keys have same result
   Requirement Sinequa Reg. W. C. REC. COM

#### Exercise

Design a factor of the number

### **Encoding Function**

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 $k = s[0] + s[1] * 128 + s[2] * 128^2 + \dots$ 

### converts hetytagu string to with the converts hetytagu string to with the converts hetytagu string to the converts hetytagu st

- Treat each character as a digit
- · Same Arindiple cambe applied recursively of two coder

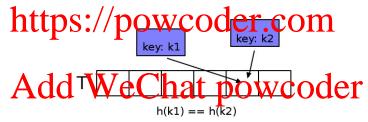
#### Question

What is the problem with this as a practical solution?

#### **Collisions**

## Assignment Project Exam Help Very space inefficient, even if it's possible

Result: collisions



Will need a way to resolve collisions (store both objects)

#### A Hash Function Part 2

Map the numerical code k from Step 1 to a position in the table

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 $h(k) = k \mod m$ 

### New requirettps:nin/speliswcoder.com

• spread the keys as evenly as possible

### What happens to the ASCI string keys if powcoder

- All keys starting a.. hash to same slot
- If all keys start a... only one slot used
- Using a prime radix for k limits the problem

### **Uniform Hashing**

## Assestes of ways to hash; universal, fingerprint, cryptographic, Help

More uniform, often slower

### Definition https://poweoder.com

Given a hash table T with m slots, using hash faunction h, the simple uniform hashing assumption (SUHA) states that each new key k is equally likely to hash into any of the probability that h(k) = i, for every slot 1 - i is 1/m.

- SUHA is an assumption about both h and input data
- Allows analysis to ignore details of both

### Hash Table Memory

Recall: need a way to resolve collisions (store both objects)

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h(k1) == h(k2)

### Exercise Add WeChat powcoder

Design a way to resolve collisions

- Table has to store both objects somewhere
- What is the worst case time to add a new object?

### Chaining

With collision resolution by Chaining

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- The table contains a pointer to the list
- So, T[i] contains a list of objects x where h(x.key) = i
  https://powcoder.com
  key: k2

  Add WeChat powcoder
  T

h(k1) == h(k2)

### Performance of Chaining

# Add object x to table T: Assignment he Parpiect Exam Help

• takes  $\Theta(1)$  time

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Search for an object with Pey k

Search list at T[h(k)] for an object where x.key == k

### In a table Arding We Chat powcoder

- Worst case is N elements in one chain: O(N) search
- Under SUHA, expected time is O(N/m)
- N/m is called the load factor

### Expected Time To Search

- k equally likely to hash to all m positions
- Probability of searching chain at T[i] is 1/m. Expected number of comparisons is

## Add We That powcoder

If N is proportional to m, expected running time for Search is  $\Theta(1)$ 

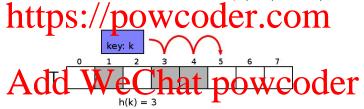
- The design of the table needs to ensure N/m is  $\Theta(1)$
- Successful search reasoning is similar: O(N/m)

### **Probing**

In an open address hash table objects are stored directly in the table

## Assignmental Project Exam Help To insert an object we probe the table until we find a space

• The hash function generates a sequence  $\langle h(k,0),\ldots,h(k,m-1)\rangle$ 



The simplest form (above) is linear probing

• Consecutive slots are probed, beginning with h(k), up to h(k) - 1

### Performance of Probing

Given a hash table with m slots, a hash function produces uniform hashing if, for an unknown key k, the probability that the probe sequence of k is p, where p is a permutation of  $\langle 0, \ldots, m-1 \rangle$  is the same for all such p.

- Uniform hashing first implies that every permutation is possible
- Linear probing does not produce uniform hashing

Assuming an object depends on the load factor N/m

ullet Each probe is to a random slot, with probability N/m it is occupied

If N is proportional to m, expected time for insert (and search) is  $\Theta(1)$ 

#### Limitations

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Hash tables do not support operations such as:

- In order iteration
- Nexther posci / powcoder.com
- Minimum key
- Maximum key we chat now coder since objects are dored, by each at an own coder