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Assignment Project Fxam Help

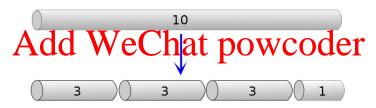
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Back To Solving Problems

The Rod Cutting Problem

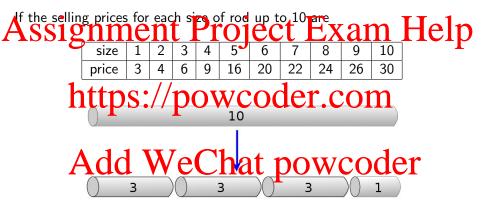
Assignment roproject letter Help They will cut the rods into smaller pieces to sell on

- Each rod size has a different market value
- · Whattps://poweoder.com/?



Is
$$p(3) + p(3) + p(3) + p(1) > p(4) + p(4) + p(2)$$
?

Instance of The Problem



Then the answer for N=10 is 32 $(1 \times 6 + 4 \times 1, \text{ or } 2 \times 5)$

Rod Cutting

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						5					
1.	price	3	#/	6	9	16	20	122	24	26	30
n	ittp	S.	//	po		NC	O	ie)	r.C	OI	n

Question

Given an array of prices $P = [P_1, \dots, P_k]$ and an integer N between 1 and k, how can RU be complete? $P = [P_1, \dots, P_k]$

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Possible https://powcoder.com

- Choose some sizes $s \equiv \langle s_1, \dots, s_i \rangle$ that sum to N
- (Values can repeat in s)
- Compared We Chat powcoder
- For all possible s
- Update current best R(N) as you go

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ı											
	price	3	4	6	9	16	20	22	24	26	30
	size	1	2	3	4	5	6	7	8	9	10

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Question

How do you generate (only) sequences s that sum to N?

At this point it will be useful to think about reducing the problem to solving one or more smaller subproblems.

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Choosing sizes:

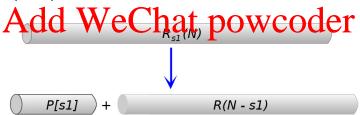
- Pick https://powcoder.com
- Then s is s_1 followed by $\langle s_2, \dots \rangle$ that sum to $N-s_1$

Can now see the drutter of the problem: powcoder

- For each possible s₁
- Find all solutions for $N-s_1$, and combine with s_1
- Base case: only sequence that sums to 0 is ()



- Pick an s₁
- Max nette Sing suppose $R(N-s_1)$ is overall solution for rod length $(N-s_1)$
- One option per value for s₁



A Simple Recursive Solution

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return 0

elshttps://powcoder.com

choices[i] = P[i] + SimpleRodCut(N-i, P)
return max(choices)

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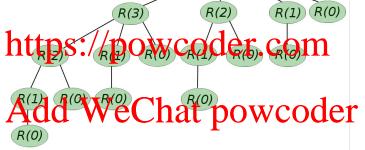
- max finds the maximum of the choices

How does this run?

Simple Rod Cut — Reflection

WOW that was sloooooowww.

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Question

Solving R(0) takes $\Theta(1)$ time. What about R(N)?

Time for Simple Solution

The time taken by SimpleRodCut is

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$$T(0) = \Theta(1)$$

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or

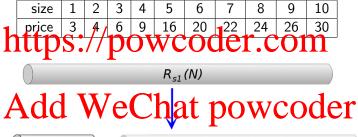
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so
$$T(N) = \Theta(2^N)$$
.

- The running time grows exponentially.
- This is not a practical solution.

Divide & Conquer?

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$$P[s1] + R(N-s1)$$

New Strategy

What is there that we can take advantage of?

Assignment Project Exam Help R(1)Add WeChat powcoder R(0) R(0)R(3) R(2) R(1,

Dynamic Programming

13 / 21

Dynamic Programming

Assignment Programming makes a space-time tradeoff Assignment Programming makes a space-time tradeoff the Research Resea

- Compute it once and save the answer in a table
- Check the table before computing each subproblem

This is called memorsation we are making a note for later)

```
MemoisedRodCut(Input: N, P = [P_1, ..., P_k])

for A=Q to WeChat powcoder

return MemoiseAux(N, P, R)
```

R is the table to be filled in

Memoisation

```
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   if R[N] > 0
   rhttps://powcoder.com
    choices[i] = P[i] + MemoiseAux(N-i, P, R)
   R[N] = max(choices)
   retuAdd WeChat powcoder
```

- If R[N] was already computed (R[N] > 0) it is returned immediately
- Otherwise we compute it, save it, and then return it
- Also called Top Down (set out to solve the biggest problem)

The 'Bottom Up' Method

We know which problems depend on which others

Assivement the Problem Exam Help

```
BottomUpRodCut(Input: N, P = [P_1, ..., P_k])

R[ALUDS://powcoder.com

for i = 1 to N

choices = [0, ..., 0]

facility e Chat powcoder

R[i] = max(choices)

return R[N]
```

• What is the running time?

Dynamic Programming

Project Exam Help • The problem has optimal substructure

- The problem has overlapping subproblems

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- the problem can be decomposed into subproblems
- an optimal solution uses optimal solutions to the subproblems

In rod cutting did optimil excitat wp new coder

•
$$P[i] + R[N - i]$$
, where $1 \le i < N$

and each R[N-i] was an optimal solution for N-i.

Optimal Substructure

Assignment Project Exam Help Problem Enweighted Shortest Path)

Input: graph G = (V, E).

Input terpices u/powcoder.com
Output: the simple path from u to v containing the fewest edges

Problem (Noweighted Wiggest Pub) at powcoder

Input: vertices $u, v \in V$.

Output: the simple path from u to v containing the most edges

Optimal Substructure

A shortest path is composed of optimal solutions to subproblems

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The shortest path from 1 to 2 (via x) is

- shortest path from 1 to x
- plus the shortest path from x to 2

Optimal Substructure

How about a longest path? Assignment Project Exam Help ler.com Add WeChat powcoder

- Independent subproblem solutions do not make an optimal solution
- In an optimal solution the subproblems will interfere

Overlapping Subproblems

The second property we need when applying dynamic programming is

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- The same problems are generated over and over
- The subproblems must still be independent
- The set of all subproblems is the subproblem space
- The smaller the subproblem space the quicker the (dynamic) algorithm