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Asymptotic Notation

Algorithm performance is often expressed using asymptotic notation which

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- The sets denote a bound on the functions.
- A full stion f is in //powcoder.com
 - o O(g) if g is an asymptotic lower bound for f
 - $\Omega(g)$ if g is an asymptotic lower bound for f;
 - $\Theta(g)$ if g is an asymptotically tight bound for f.

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- The definitions of O, Ω and Θ are broad coefficients are not significant.
- So, (A) and (B) above are both in O(N), but (C) and (D) are not because they grow too fast.

Big O: Upper Bound

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$$O(g(N)) = \left\{ egin{array}{ll} f(N) \mid & ext{there are positive constants c and n_0} \\ & ext{such that } 0 \leq f(N) \leq c \, g(N) ext{ for all } N \geq n_0 \end{array}
ight\}$$

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Big Omega: Lower Bound

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$$\Omega(g(N)) = \left\{ \begin{array}{cc} f(N) \mid & \text{there are positive constants } c \text{ and } n_0 \\ & \text{such that } 0 \leq c \, g(N) \leq f(N) \text{ for all } N \geq n_0 \end{array} \right\}$$

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Big Theta: Tight Bound

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$$\Theta(g(N)) = \left\{ egin{array}{ll} f(N) \mid & ext{there are positive constants } c_1, \ c_2 \ ext{and } n_0 \\ & ext{such that} \\ & 0 \leq c_1 \, g(N) \leq f(N) \leq c_2 \, g(N) \ ext{for all } N \geq n_0 \end{array}
ight.$$

Asymptotic Notation

Aven though O(N) etc. are sprouped are fusually stated like This elp

- $T(N) = O(N^2)$
- (ratifatteps://powcoder.com

Also, even though asymptotic notation applies to functions, it is (abusively) applied to algorithms too.

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We use the same notation to talk about other resources:

• We say "the space complexity of MergeSort is $\Theta(N)$ "

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Space Complexity

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- $\Theta(1)$ space for the best case
- \bullet $\Theta(1)$ space for the worst case
- 9(1https://powcoder.com

"1" is the normal reference function for any constant

- The space used by the input is ignored
 If not the Gold Mask Civierent actue to Ogwich CodeT
- SimpleSearch only needs space for a few local variables (e.g. a loop counter). This does not depend on N.

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Better Search

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$$k = 10$$
a **https://powsoder.com**

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- It uses the fact that elements are ordered.
- Checking an element in the middle means you can discount half the remaining data.

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Binary Search: Design

Assignment Project Exam Help Binary Search creates regions in a. What properties should the algorithm

Binary Search creates regions in a. What properties should the algorithm maintain for it to be correct?

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Loop Invariants: A Design Tool

A loop invariant is a property that is true before every iteration of a loop.

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$$k = 10$$
https://powcoder.com
 $5 \mid 6 \mid 7 \mid 21 \mid 23 \mid 29 \mid 50$
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In Binary Search we assert that:

- Elements left of index I are known to be less than k;
- Elements at index r or above are known to be greater than k;

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• so $a[I, \ldots, r-1]$ is unsearched.

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Loop Invariants

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initialisation The invariant must be true before the loop begins

maintenance, If the invariant is true before a loop iteration, then it is still ntip of over the work coder.com

termination When the loop ends the invariant implies a useful property of the algorithm

A tricky proceeding to the tricky proceeding to the tricky proceeding to the tricky procedure and the tricky procedure an

• The three conditions help see how (and if) it would work in detail

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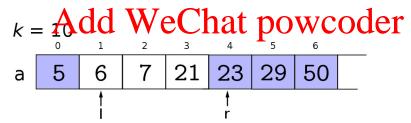
Loop Invariants

For Binary Search:

Anisistis it is not have the property of the p

maintenance The invariants must hold before each iteration, which gives

the form of updates of / and returns are ned, which gives the loop condition



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Loop Invariants

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• a[I,...,r-1] is unsearched

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Performance

What is the worst case time complexity of Binary Search?

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Intuition: loop executes log₂ N times.

Performance

Alternative: analyse the recursive form of the program.

Assignment Project Exam Help if (1 >= r) return False m = https://powcoder.acom

```
return True c5
else if (k < a[m]) c6
```

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return BinSearch(a, m+1, r, k) T(N''

- where N' and N'' are numbers left to search
- Exercise: what are N' and N'' in the worst case? Be exact.

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Worst Case Recursion

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- m is a vay process to the contract powcoder of N is odd: N' = N'' e N'
- if N is even: N' = |N/2|, N'' = |N/2| 1
- So the worst case is when k < a[0]
 - If N > 0, will have |N/2| unsearched elements

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Performance

We now have enough information to write a worst-case formula for T(N) BinSearck (A, T, k)

```
if (1 >= r)
representation (1 >= r)
representation (2 com
m = 1 + (r-1) / 2 powcoder
c3
if (k == a[m])
return True
else Act C alwechat powcoder
return BinSearch(a, 1, m, k)
else
return BinSearch(a, m+1, r, k)
?
```

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