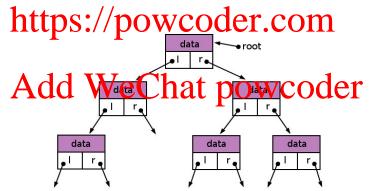
Dynamic Data Structures

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Dynamic Data Structures

Assignmentur Projectudes salamin Flelp The problems seen so far involved fixed length lists

- In most languages we have a simple way to implement this efficiently
 - https://powcoder.com
- Our algorithms assumed some sort of array type was available

Other problems require dynamic data structures such as

- Lists Add nd Wee Chat powcoder
- Sets and Dictionaries

These are designed to hold variable, essentially unlimited amounts of data.

Ordered Data Structures

A *list* is an ordered collection of {nodes, items, elements}.

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push adds an element to the end of the list

http removes the last element of the list on shut removes the first element of the list unshift adds an element to the front of the list insert adds an element at a given position element at a given position iterate returns the items in order.

- Plus sorting, searching, copying, joining, splitting ...
- The most appropriate implementation depends on which operations are needed.

Stacks

A *stack* is a last-in first-out (LIFO) list.

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• Stacks are usually pictured as a vertical (stacked!) structure https://powcoder.com

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 Stacks support recursive algorithms including fundamental operations such as calling subprocedures and evaluating arithmetic expressions

Stacks

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Question

How would to trip stem for the power coder.com

- Must be able to add "unlimited" objects
- Push And Poor must implement LIFO behaviour powcoder

Stack Implementation

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- Array has fixed capacity
- Link d list has higher overheads https://powcoder.com

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- Can make array dynamic (variable size)
- Integer sp points to the top of the stack
- Update sp within Push and Pop

Dynamic Array-Based Stack

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```
if s.sp == k // array is full

s' = new stack of size 2k

fitpsto/k powcoder.com

s' [i] = s[i] powcoder.com

s = s'

s[s.sp] = X + WeChat powcoder
```

• push increases the capacity of the stack if it is full

Dynamic Array-Based Stack

- pop decreases the capacity if it is too big
- a full implementation should have a minimum size

Performance of Push

Question

Aigraisachement of purche the lorg asmine Help complexity of push?

- Assume: time to insert (copy, add) one object to array is c
- · Assunttrips capacipo wcoder.com

The time taken for pushing objects is:

* c, c, Add WeChat powcoder

- Worst time to push a single object is Nc
- So T(N) = O(N)
- Want to reflect fact that most pushes are not O(N)

Performance of Push

Assignment Project Exam Help Given an empty stack, what is the worst case time to push N objects?

Assume: initial capacity is 4

· Assumet tips: inserpropriate to the compact compact

The time taken for the each push is still:

- c, c, Add WeChat powcoder
 For N pushes the worst single push is No wooder
- $T(N) = O(N^2)$

However, this is a big overestimate

Performance of Push

Abstright Project Exam Help $T(N) = Nc + (4c + 8c + \cdots + (N/2)c + Nc)$

where https://powcoder.com

- the first Nc is the cost of writing N elements
- the rest is for copying to new arrays

The time A copying We 4c gentotes in swing energy

- $T(N) \le 3Nc 4c$
- T(N) = O(N)

Amortisation

Abstriegramment (Project Exam Help A single push is effectively a constant time operation

- More correctly: push is amortised $\Theta(1)$
- No https://powcoder.com

Amortisation

- Related to accountancy method used to defer large costs
- Amorthed dysivor Goers had en of Wation CET
- Cost of individual ops is "amortised" across the sequence
- Unlike accountancy, must never be in debt

Amortised Analysis

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- Pick a representative subsequence
- Subsequence is some, "cycle" that repeats
- Pickhttps://powcoder.com
- Show that paying amortised cost covers all costs (never in debt)

Exercise Add WeChat powcoder Find a representative cycle (subsequence) of pushes into the stack and

show that the amortised cost of 3c covers all costs.

Amortised Analysis

• Start after any expensive push

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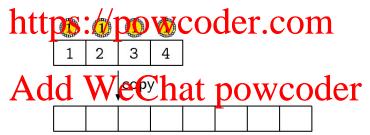
- Cheap pushes each put 2c in the bank
- Have enough to cover extra costs when next expensive push occurs
- (If you started with a copy you are immediately over budget)

Amortised Analysis

Argument only works because array is initially empty and size is doubled

Assignment copy we always push of more Exam Help

This is how cost is covered



Multiplying by any factor will do - will affect amortisation constant

Queues

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- The earliest one added (FIFO Queue)
- The one with highest priority (Priority Queue) https://powcoder.com

Questions

- How could you implement a priority queue (PQ)?
- Given Profellowing your designation mains? My object sewhat would be the worst case time to add a new object? (Each object has a key attribute that determines its priority.)

Priority Queue Design

If we maintain a total ordering of the queue:

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Can search a sorted array quickly but have to shift existing objects

Pinding position in a linked list is O(N)https://powcoder.com

9, 8, 7, 6, 3

Max Priority Queue

of, 9, 7, 3, 8

add items

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Do not actually need total ordering.

- Queue does not support indexed access
- Just want to find object with highest priority

Priority Queue Design

Solution is to divide and conquer the data

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- Key Property: Maintain order within each branch
- Highest (or lowest) key will be at the root
- Behaves like lots of mini queues

Priority Queue Design

Solution is to divide and conquer the data

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Question

A new object could go in any branch. (Do you agree?) So, where should it go? Why?

Heap: a Tree in an Array

We want to know where the "end" of the tree is:

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9 7 2 5 4 1

https://powcoder.com

- Track end using "stack pointer"
- Navigate by indices
- Leaving a loll blank hears: hat powcoder
 - children of a[n] are a[2*n] and a[2*n+1]

Exercise

How should a new object be added to a max binary heap? (i.e. the greatest key should be at the root).

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- Restore the "shape"
- Then restore the order

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Heap: a Tree in an Array

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- . Trackettps://pow.coder.com
- Leaving a[0] blank means:
 - parentiof a [m] visya [n/2] nata [1340] WCOCCT

Exercise

How should the object with the greatest key be removed from a max binary heap?

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- Restore the "shape"
- Then restore the order

To remove the object at the root Assignment Project Exam Help owcoder, c' Add We Chat powcoder

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Binary Heap Performance

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Question

Given a heap containing N objects, what is the time complexity for adding or removing one object?

Binary Heap Performance

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Both operations are $O(\log_2 N)$

- Height of the heap is $\Theta(\log_2 N)$
- Each operation confined to one branch

Heapsort

Heaps also provide us with the Heapsort algorithm (JWJ Williams, 1964) SSIGNMENT Project Exam Help

- Create an empty heap H
- Remove each element of H and add it to H COM
- HALT
- What Add si Wee Chat powcoder
- Performance is again $\Theta(Nlog_2N)$
- Can also be implemented in place by setting up list and heap partitions within a single array