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More Terminology

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- Each edge in a weighted graph has an associated cost or weight
- We denote the weight of the edge $\{u, v\}$ by w(u, v)

More Terminology

A tree is pair (6, 7) where the project Exam Help vertex of G, called the root.

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A nonrooted tree is a connected, acyclic graph

More Terminology

Definition (Spanning Tree)

Aignoring Tree)

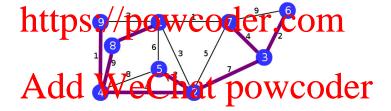
Aignoring Tree

Spanning Tree

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spanning Tree

Aignoring Tree



Given some network (road, phone, water \dots) a minimum spanning tree (MST) is an important attribute

• Lowest cost way to connect all points

Minimum Spanning Tree

Assignment Project Exam Help Given graph G = (V, E), find a new graph T such that T is an MST of G.

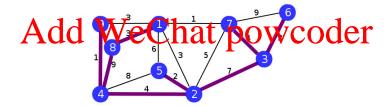
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Question Assignment Project Examuthelp the MST problem, and then test them:

- What would you generate?
 What this propowcoder.com

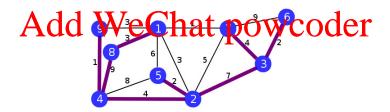


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An MST for G will comprise

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• If such a tree also has minimal weight it is an MST

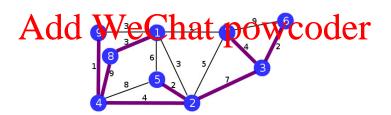


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Exercise

Five grage by rash definition of a concept of the ledges that in the policy of the ledges that in the policy of the ledges that in the ledges that

- What are the inputs?
- What refet to base/cape Owcoder.com
 How many instances of this problem are there?



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A minimal weight set of *n* edges, chosen from E[1,...,i] is: Assignment Project Exam Help

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- (Does the problem have optimal substructure?)
- $min_edges(|E|, |V| 1)$ has $|E| \times (|V| 1)$ subproblems
- Unfortunately, min_edges might not produce MST. Why?

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Update to tree_edges and only return a set of edges that forms a tree Assignment sProject Exam Help

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 \begin{cases} E_{T} & \text{if } |E_{T}| = |V| - 1 \\ \min_{w \in \mathbb{Z}} (i - 1, E_{T}) ] & \text{otherwise} \end{cases}
```

- Subproventions white test a fact (using evidence fedges)
- If $\{E[i]\} \cup E_T$ not a tree, do not use E[i]
- If $|E_T| + (i-1) < |V| 1$, insufficient edges
- $tree_edges(|E|,\varnothing)$ still has $|E| \times (|V|-1)$ subproblems

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A New Strategy

Assesignation when i Projecte Exam Help

- De met edd edm
- Do not add edge i

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 - Maybe this time a greedy approach will actually work!
 - A greedy algorithm picks the 'obvious' first step
 - This As alcomating established powerder
 - It leaves just one subproblem to solve

So, we identify edge g, the greedy edge, and continue with $E_{\mathcal{T}} \cup \{E[g]\}$

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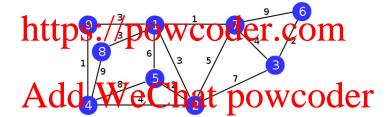
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Assignment Project Exam Help We have to show that the choice must lead to a correct solution

- (As you have seen, much easier to prove if greed is bad)
- Theorem https://powcoder.com

Let G be a connected, weighted graph. If e_m is an edge of least weight in G, then e_m is in some minimum spanning tree for G.

The general method of proving that the greedy choice is of is.

- Suppose you have an optimal solution to the problem
- Show that it is still optimal when the greedy choice is included

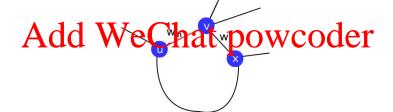
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Proof

T is some MST for G

Assignment Project Exam Help • Suppose e_m is not in T

Let $e_m = \{u, v\}$, let the path from u to v in T include the edge $\{v, x\}$, and let the vertex $\{v, v\}$ and let the vertex $\{v, v\}$ and $\{v, v\}$ are $\{v, v\}$ and $\{v, v\}$ and $\{v, v\}$ and $\{v, v\}$ are $\{v, v\}$ and $\{v, v\}$ and $\{v, v\}$ are $\{v, v\}$ and $\{v, v\}$ and $\{v, v\}$ are $\{v,$



Proof

Now construct T' by removing $\{v,x\}$ from T and adding $\{u,v\}$

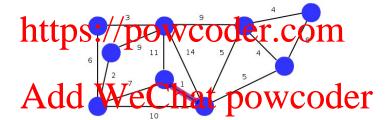
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- Since T is a spanning tree, T' is a spanning tree
- Since T is an MST and $w_m \leq w$, T' is an MST
- e_m is in T'
- QED

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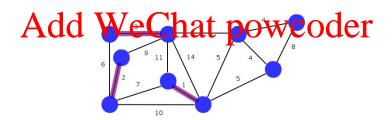


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More Greed

Our greedy choice can be made more general

The series of the set of edges $\{u,v\}$ where exactly one of $\{u,v\}$ is $\{u,v\}$ is $\{u,v\}$ is $\{u,v\}$ and $\{u,v\}$ is $\{u,v\}$ and $\{u,v\}$ is $\{u,v\}$ where $\{u,v\}$ is $\{u,v\}$ is $\{u,v\}$ and $\{u,v\}$ is $\{u,v\}$ is $\{u,v\}$ and $\{u,v\}$ is $\{u,v\}$



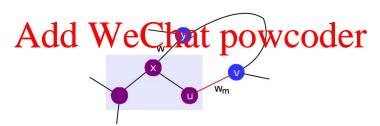
Proof

The proof is similar

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• Suppose e_m is not in T

Let $e_m = \{u, v\}$ and let the weights of $\{u, v\}$ and $\{x, y\}$ be w_m and w



Proof

Now construct T' by removing $\{x,y\}$ from T and adding $\{u,v\}$ Assignment Project Exam Help https://powcoder.com

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Since T is a spanning tree, T' is a spanning tree

- Since T is an MST and $w_m < w$, T' is an MST
- \bullet e_m is in T'
- QED