UNIVERSITY OF TORONTO

FACULTY OF APPLIED SCIENCE AND ENGINEERING DEPARTMENT OF MECHANICAL & INDUSTRIAL ENGINEERING

Third Year - MIE302S

VIBRATIONS

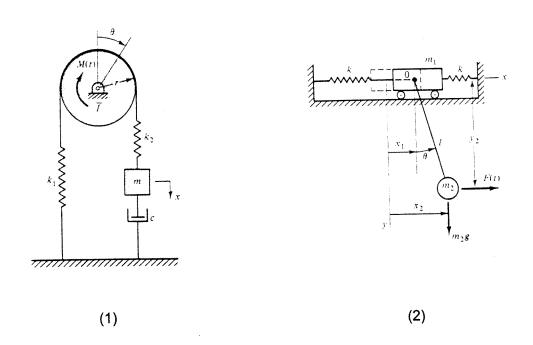
Final Examination

Examiner: J.W. Zu Date: April 13, 2000 Time: 9:30:-12:00

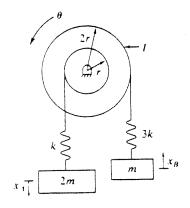
Instructions:

- 1. Answer all the questions.
- 2. Open textbook only.
- 3. Only non-programmable calculators are allowed.

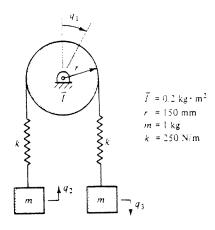
1. (30%) Establish the equations of motion of the following systems using Lagrange's Equations and find the corresponding [M], and [K] matrices, assuming small displacement. (15% each)



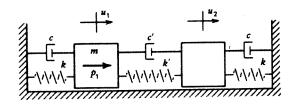
2. (20%) For the system shown, find the stiffness matrix of the system using the definition of the stiffness influence coefficient.



- 3. (10%) The natural frequencies of a three-degree-of-freedom system are found to be $\omega_1 = 1$, $\omega_2 = 3$, $\omega_3 = 6$. Derive the frequency equation (polynomial equation from the determinant).
- 4. (20%) For the system shown in the figure, find natural frequency and mode shapes.



5. (20%) For a 2-DOF system shown, determine the steady-state response using mode superposition method.



$$p_1 = P_1 \cos \Omega t$$

 $k = 987, \quad k' = 217, \quad m = 1$
 $c = 0.6284, \quad c' = 0.0628$