

UNIVERSITY OF TORONTO  
FACULTY OF APPLIED SCIENCE AND ENGINEERING

FINAL EXAMINATIONS, DECEMBER 2001

Third Year - Program 6 - Chemical

CHE332F - APPLIED REACTION KINETICS

Examiner - C. A. Mims

**Instructions:** There are 5 questions, 4 with multiple parts. Total marks = 100. Indicate **prominently** the number and part (a,b,c, etc.) of each question by its solution in the exam booklet(s).

*DON'T PANIC!*

17 total marks	<p><b>1. Theories of reactions:</b> The reaction of oxygen atoms with methane</p> $[1] \quad \text{O} + \text{CH}_4 \rightarrow \text{OH} + \text{CH}_3$ <p>has a rate constant of <math>1.3 \times 10^6 \text{ L mol}^{-1} \text{ s}^{-1}</math> at 500K.</p>
10 marks	<p>➤(a) Estimate the rate constant for the reaction of O atoms with neo-pentane (tetramethylmethane, <math>\text{C}(\text{CH}_3)_4</math> at 500K, i.e.</p> $\text{O} + \text{C}(\text{CH}_3)_4 \rightarrow \text{C}(\text{CH}_3)_3(\text{CH}_2) + \text{OH}$ <p>Molecular diameters: neo-pentane = 600pm; methane = 400pm; O atom = 150pm Molar masses: neopentane = 0.072kg; methane = 0.016 kg; O atom = 0.016 kg. Energy needed (energy barrier) with neopentane is 6 kJ/mol lower than for methane (because of slightly weaker C-H bond in neopentane).</p> <p>State any assumptions you made in the calculation above and justify them..</p>
2 marks	➤(b)➤ Draw a qualitative structure for the transition state in reaction [1] above.
3 marks	➤(c)➤ True or false? A smaller pre-exponential factor in the rate constant corresponds to a more positive entropy of activation in transition state theory. Explain in 25 words or less.
2 marks	➤(d)➤ How are theories of elementary reactions useful to the applied chemist/engineer? (be brief).

50 total marks	2. Ideal reactors: The following data were obtained in a laboratory CSTR for the reforming of methanol.										
		mass of catalyst	$FA_0$ $CH_3OH$ (liquid, 25°C)	Feed ratios (mole basis)			Dry gas (no $H_2O$ , $CH_3OH$ ) Outlet mole fraction				
	$T$ (°C)	g	mol min <sup>-1</sup>	$H_2O/CH_3OH$	$N_2/CH_3OH$	$CO_2/CH_3OH$	$H_2$	$CO_2$	$(CH_3)_2O$	CO	$N_2$
	256	35	0.46	1.1	0.4	0.1	0.565	0.188	0.00534	0.0006	0.241
7 marks	➤(a)➤ Calculate the reaction rate (mol kg <sub>cat</sub> <sup>-1</sup> min <sup>-1</sup> ) for production of $CO_2$ , $H_2$ , CO, and dimethyl ether $(CH_3)_2O$ in this reactor. Use the $N_2$ tracer.										
8 marks	➤(b)➤ Calculate the methanol conversion and the carbon-based selectivities to CO, $CO_2$ , and dimethyl ether. (Assume there are no unmeasured carbon-containing products).										
3 marks	➤(c)➤ Why are CSTRs useful for laboratory investigations of reaction kinetics to determine rate laws? Make a comparison to PFRs in your answer.										
	<p>The following reaction network is fit to data on this system.</p> <p>[1] <math>CH_3OH + H_2O \rightarrow CO_2 + 3H_2</math> <math>r_1 = k_1 P_{CH_3OH}^{1/2} P_{H_2O}^{1/2}</math></p> <p>[2] <math>2 CH_3OH \rightarrow (CH_3)_2O + H_2O</math> <math>r_2 = k_2 P_{CH_3OH} P_{H_2O}^{-1/2}</math></p> <p>[3] <math>CO_2 + H_2 \rightarrow CO + H_2O</math> <math>r_3 = k_3 P_{CO_2} P_{H_2}^{1/2} P_{H_2O}^{-1/2}</math></p> <p><math>k_1</math> (300°C) = 71 mol atm<sup>-1</sup> kg<sub>cat</sub><sup>-1</sup> min<sup>-1</sup></p> <p><math>k_2</math> (300°C) = 0.45 mol atm<sup>-1/2</sup> kg<sub>cat</sub><sup>-1</sup> min<sup>-1</sup></p> <p><math>k_3</math> (300°C) = 0.013 mol atm<sup>-1</sup> kg<sub>cat</sub><sup>-1</sup> min<sup>-1</sup></p> <p>A 1:1 mixture of <math>CH_3OH:H_2O</math> (only) is fed at 300°C and at 1 atm pressure in the reactor. Answer the following, using these conditions and the rate laws above.</p>										
6 marks	➤(d)➤ What are the initial (at very low conversion) carbon-based selectivities to the three products: CO, $CO_2$ , and dimethyl ether.										
6 marks	➤(e)➤ Sketch (qualitatively) the dependence of the selectivities to CO, $CO_2$ , and dimethyl ether as a function of the methanol conversion in a PFR.										
17 marks	➤(f)➤ Assume only reaction 1 is occurring. Calculate how much catalyst will be needed to react 0.100 L/min of liquid methanol feed (density = 0.8 g cm <sup>-3</sup> ) to 98% conversion										
3 marks	➤(g)➤ Discuss the importance of selectivity in chemical process engineering. (be brief)										

15 total marks	<p><b>3. Rate Laws:</b> The following data were obtained for the oxidation of soot (solid carbon) by NO<sub>2</sub> at 350°C on an active diesel exhaust catalytic filter.</p> $\text{C(solid)} + 2 \text{NO}_2 \rightarrow \text{CO}_2 + \text{NO}$ <table> <tr> <th><math>P_{\text{NO}_2} / \text{atm}</math></th><th>rate / mol C (mol C<sub>present</sub>)<sup>-1</sup> hour<sup>-1</sup></th></tr> <tr> <td>0.000300</td><td>0.073</td></tr> <tr> <td>0.000800</td><td>0.317</td></tr> <tr> <td>0.002700</td><td>1.96</td></tr> </table>	$P_{\text{NO}_2} / \text{atm}$	rate / mol C (mol C <sub>present</sub> ) <sup>-1</sup> hour <sup>-1</sup>	0.000300	0.073	0.000800	0.317	0.002700	1.96
$P_{\text{NO}_2} / \text{atm}$	rate / mol C (mol C <sub>present</sub> ) <sup>-1</sup> hour <sup>-1</sup>								
0.000300	0.073								
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6 marks	<p>➤(a)➤ Show that this reaction obeys a power law in P<sub>NO<sub>2</sub></sub> over the measured range. Calculate the best reaction order and value for the rate constant (with units).</p> <p>At 390°C, the rate is 0.745 mol C (mol C<sub>present</sub>)<sup>-1</sup> hour<sup>-1</sup> in the presence of .000500 atm of NO<sub>2</sub>. Assume the rate law is separable (temperature - composition) and Arrhenius temperature dependence is followed.</p>								
6 marks	➤(b)➤ Calculate the values (with units) of the activation energy and pre-exponential factor for this reaction.								
3 marks	➤(c)➤ What other parameters besides temperature and P <sub>NO<sub>2</sub></sub> could the rate of this reaction depend on?								
15 total marks	<p><b>4.</b> The mechanism of a simple reaction A → 2C involves the following steps</p> $\begin{aligned} \text{A} &\rightarrow 2\text{B}^*; \text{ rate constant } k_1 \\ 2\text{B}^* &\rightarrow \text{A}; \text{ rate constant } k_2 \\ \text{B}^* &\rightarrow \text{C}; \text{ rate constant } k_3 \end{aligned}$								
5 marks	➤(a)➤ Treat B* as a reactive intermediate and derive the rate law for the reaction applying the stationary state approximation								
5 marks	➤(b)➤ What is the simplified rate law if $k_1, k_2 \gg k_3$ ? and what activation energy would be measured in this case if $E_{A_1} = 95\text{kJ/mol}$ , $E_{A_2} = 35\text{kJ/mol}$ and $E_{A_3} = 112\text{kJ/mol}$ ?								
5 marks	➤(c)➤ Reaction 2 in question 2 is equilibrium limited (i.e. reversible). The equilibrium constant is 0.04 at 300°C. Write a general equation for the net rate of this reaction taking the equilibrium limit into account. Discuss the relevance to reactor design.								
3 marks	➤4.➤ Compose a short quantitative question (about reaction kinetics) for next year's class. Base it on something I didn't ask about on this exam.								

Enjoy your vacation/holiday !

POSSIBLY USEFUL INTEGRALS:

$$\int (a + bx)^n dx = \frac{(a + bx)^{n+1}}{(n+1)b} \quad n \neq -1$$

$$\int \frac{dx}{a + bx} = \frac{1}{b} \ln(a + bx)$$

$$\int \frac{x dx}{a + bx} = \frac{x}{b} - \frac{a}{b^2} \ln(a + bx)$$