

University of Toronto  
Faculty of Applied Science and Engineering  
FINAL EXAMINATION, April 24, 2001  
MIE 418 - FLUID MECHANICS II

Examiner: D.F. James

Duration: 2 1/2 hours

**NOTES:**

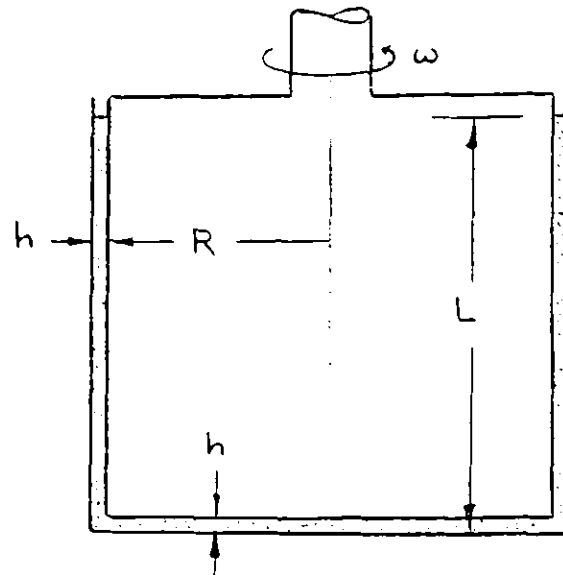
1. Allowed aids are a textbook, personal notes, homework solutions, handouts, and a hand calculator.
  2. An examination is an exercise in communication.
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**Question 1 (10%)**

- (a) Explain the purpose of ailerons on aircraft wings.
- (b) Explain the purpose of flaps.

**Question 2 (25%)**

A shaft is positioned to be concentric with a circular housing. The gap distance is everywhere  $h$ , as indicated in the diagram, where  $h$  is much smaller than the shaft radius  $R$ . The shaft end is flat, as is the cylinder bottom. In the space between the shaft and cylinder is a liquid of viscosity  $\mu$ , which fills the space to a depth  $L$ . The shaft rotates at a steady angular speed  $\omega$ .



- (a) What is the torque  $T$  on the shaft, in terms of the given parameters?
- (b) If the bottom of the shaft were cone-shaped instead of flat, with the vertex just touching the cylinder bottom and with a maximum gap of  $h$ , what would be the torque  $T$  in this case?
- (c) Which shape is preferable for rheometry, and why?
- (d) To use the preferred shape for rheometry, what conditions and assumptions are necessary?

**Question 3 (20%)**

A parachutist jumps from an airplane at 8000 ft. (2420 m), where the air density is  $0.960 \text{ kg/m}^3$ . The parachute has a diameter of 28 ft. and the weight of the chute and person is 185 lbf.

- (a) Estimate the person's terminal velocity at this height.
- (b) Estimate the time to reach the ground, at 100 m above sea level, in minutes.

**Question 4 (15%)**

A tube has an inner diameter  $D_1$  and an outer diameter  $D_2$ , and the tube wall is porous with permeability  $k$ . A liquid of viscosity  $\mu$  flows from inside to outside at a flow rate  $q$  per unit length of tube. The pressure drop across the wall is  $\Delta p$ .

If the flow were from outside to inside instead, would the pressure drop  $\Delta p$  be the same? Justify your answer.

If particles are suspended in the liquid, is the time for transport of a particle across the wall the same for both directions, for the same  $q$ ?

**Question 5 (30%)**

A rectangular channel 60 ft. wide carries a discharge of  $2700 \text{ ft}^3/\text{sec}$ . The slope of the bottom is 0.0081 and the depth of uniform flow is 2.50 ft.

- (a) What is the upstream Froude number?
- (b) What is the uniform flow depth downstream of the transition, to 2 significant figures?
- (c) What is the downstream Froude number?
- (d) Sketch the transition in depth, showing how and where the transition takes place. Justify your answer by qualitative arguments.