

FORMALLY VERIFYING COMPLEX SYSTEMS USING

TLA⁺



WHOAMI

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- > PHD IN MATHEMATICS
- > (BIG) DATA CONSULTANT
- > SENIOR BIG DATA ENGINEER USING PYTHON, GO AND SCALA

FORMAL METHODS

WHY?



ACTOR SYSTEM



⋮

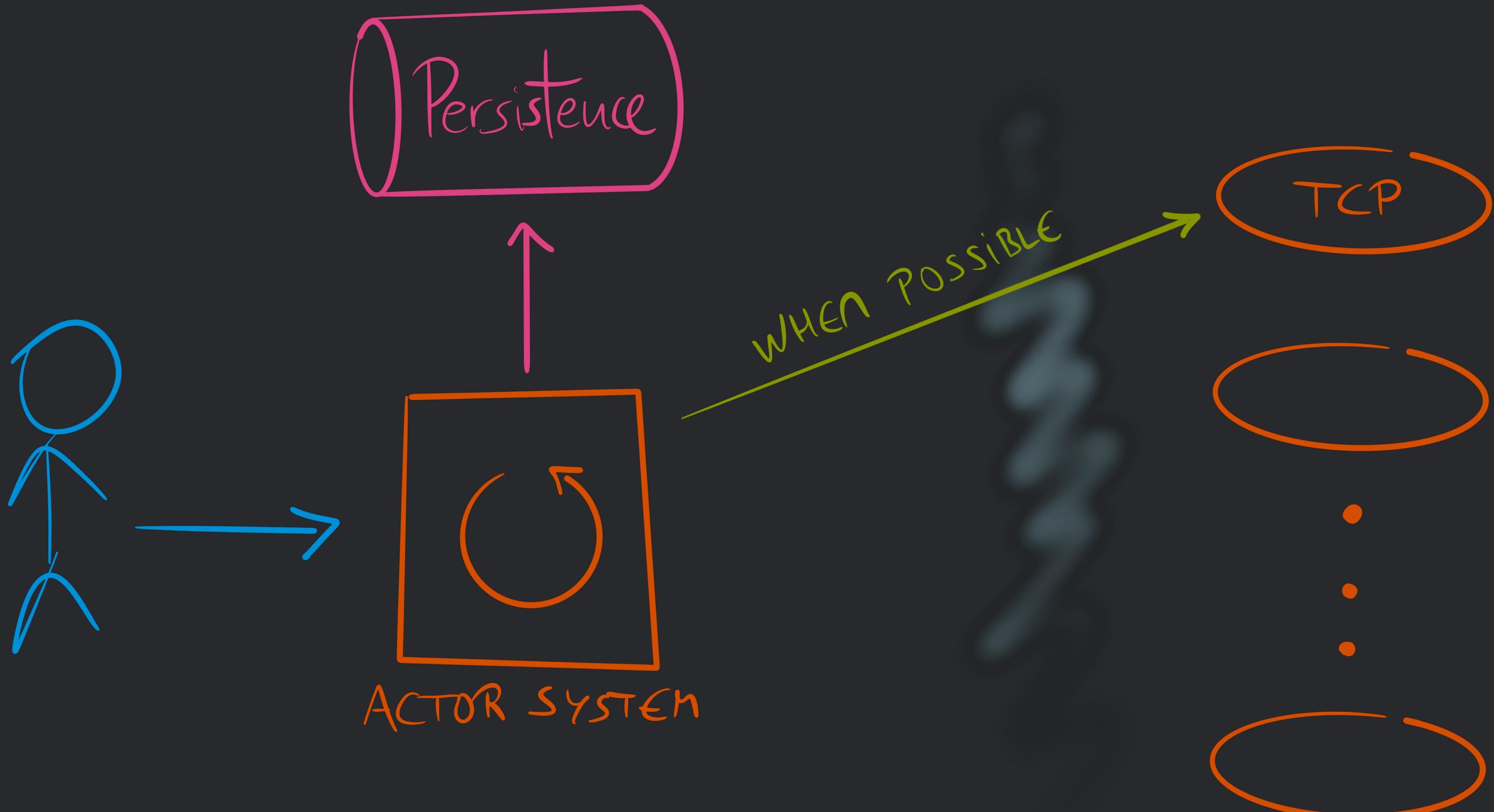


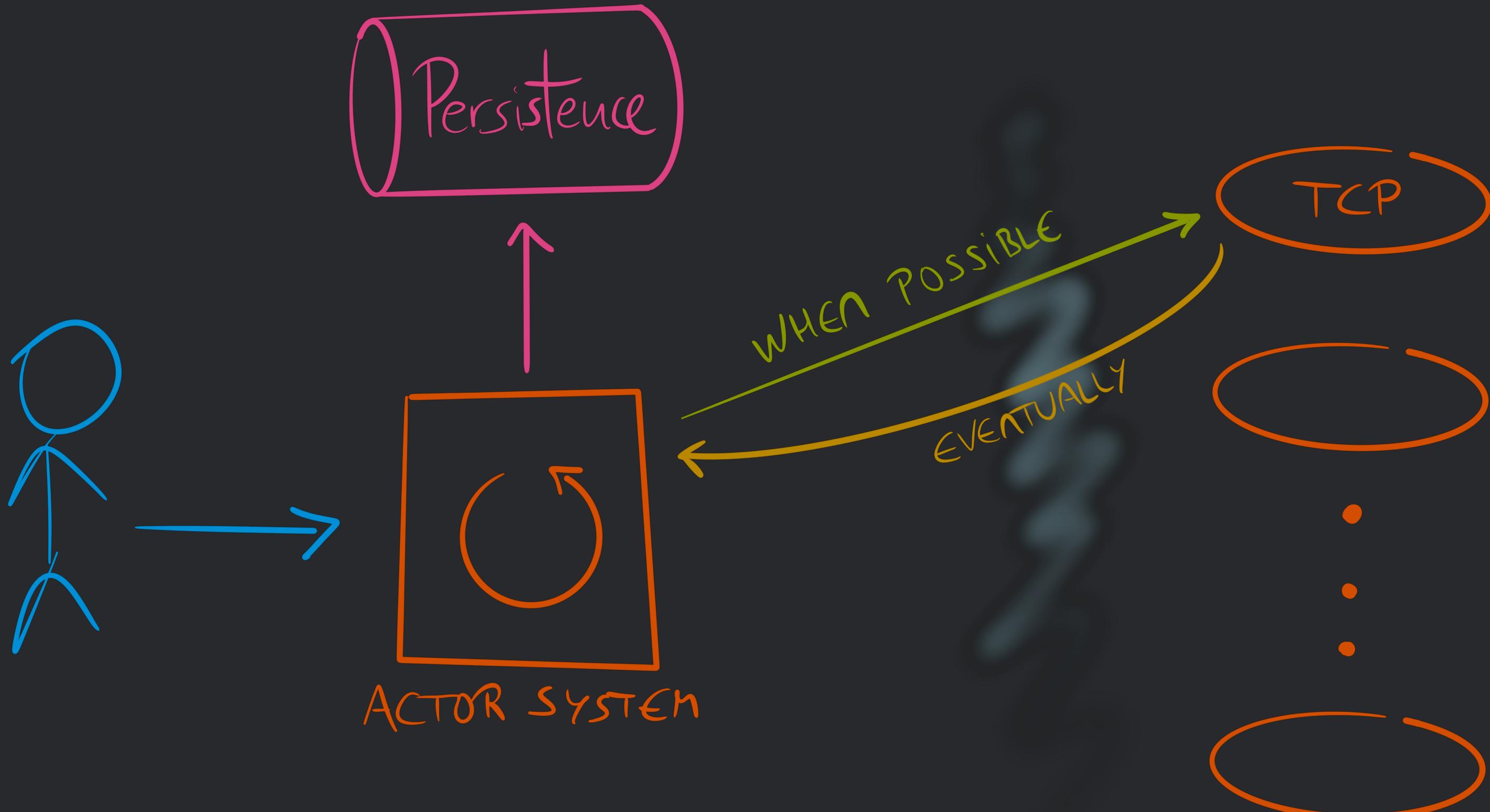
Persistence

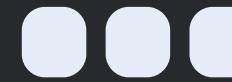


ACTOR SYSTEM



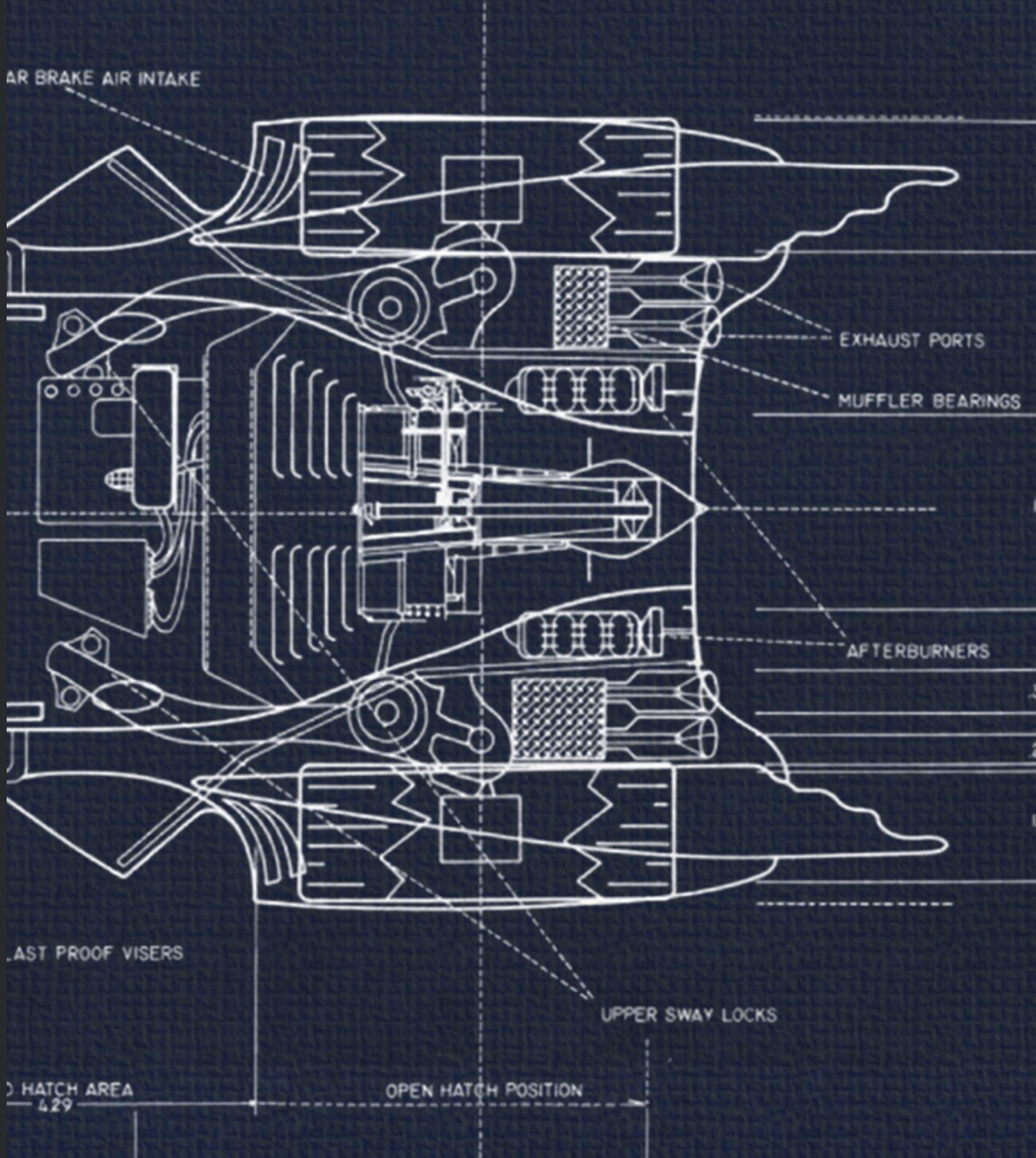






WHAT ARE FORMAL METHODS?

- › TECHNIQUE FOR SPECIFYING THE BEHAVIOUR OF HARDWARE OR SOFTWARE
- › BASED ON SOME MATHEMATICAL FORMALISM OR THEORY



EXAMPLES

- > LAMBDA CALCULUS
- > (POSSIBLY DEPENDENT) TYPE SYSTEMS
- > TLA (TEMPORAL LOGIC OF ACTIONS)

WHAT DOES FORMAL VERIFICATION REQUIRE?

- > WRITE A SPECIFICATION OF WHAT THE SYSTEM IS SUPPOSED TO DO
 - > COMPUTATIONALLY VERIFY THE DESIRED PROPERTIES
- > OPTIONALLY/ADDITIONALLY: PROVE THE DESIRED PROPERTIES OF THE SYSTEM

WHAT IS TLA^+ ?

FORMAL SPECIFICATION LANGUAGE DEVELOPED ON TOP OF TLA BY LESLIE LAMPORT¹

MODELS WRITTEN IN TLA^+ CAN BE CHECKED USING TLC

¹THE LA FROM *LATEX* AND THE WELL KNOWN AUTHOR OF THE PAXOS) CONSENSUS ALGORITHM. AMONG MANY OTHER THINGS

A PSEUDOCODE-LIKE LANGUAGE.
PLUSCAL TRANSPILES INTO TLA^+ .
AND CAN BE USED FOR SEQUENTIAL
ALGORITHMS

COMES IN TWO FLAVOURS. **P**² AND **C**³

²P OF PASCAL? begin while do stuff end while;

³C AS IN C. {CURLY CURLY}

AN ADDITIONAL PROOF SYSTEM TLAPS⁴ CAN BE USED TO CHECK PROOFS

THIS IS HOW BIZANTYNE PAXOS⁵ WAS PROVEN. AND HAS BEEN USED IN SEVERAL INDUSTRY PROJECTS

⁴CAN BE FOUND [HERE](#). IT'S SEPARATE FROM THE TLA+ TOOLBOX

⁵MECHANICALLY CHECKED SAFETY PROOF OF A BYZANTINE PAXOS ALGORITHM

SYSTEM	COMPONENTS	LINES OF CODE	RESULT
S3	FAULT TOLERANT NETWORK ALGO	804 (PLUSCAL)	2 BUGS. FURTHER BUGS IN LATER OPTIMISATIONS
S3	BACKGROUND REDISTRIBUTION	645 (PLUSCAL)	1 BUG. 1 BUG IN THE FIX
DYNAMODB	REPLICATION & MEMBERSHIP	939 (PLUSCAL)	3 BUGS (35 STEP TRACE)
EBS	VOLUME MANAGEMENT	223 (PLUSCAL)	BETTER CONFIDENCE
INTERNAL LOCK MANAGER	REPLICATION	318 TLA+	1 BUG

HOW DOES $T A^+$
LOOK LIKE?

```
-- MODULE ThemeSong --  
  
EXTENDS Integers  
  
VARIABLES s, count  
  
vars == <<s, count>>  
  
Sinit == s = "na" /\ count = 2  
  
Na == s' = "na" /\ count' = count - 1  
ToB == s' = "Batman" /\ count' = 0  
  
Snext == IF count > 0 THEN /\ ( Na \vee ToB)  
           ELSE /\ ToB  
  
Spec == Sinit /\ [] [Snext]_vars /\ WF_vars(ToB)  
  
Batman == s = "Batman" /\ count = 0  
  
Liveness == <>Batman
```



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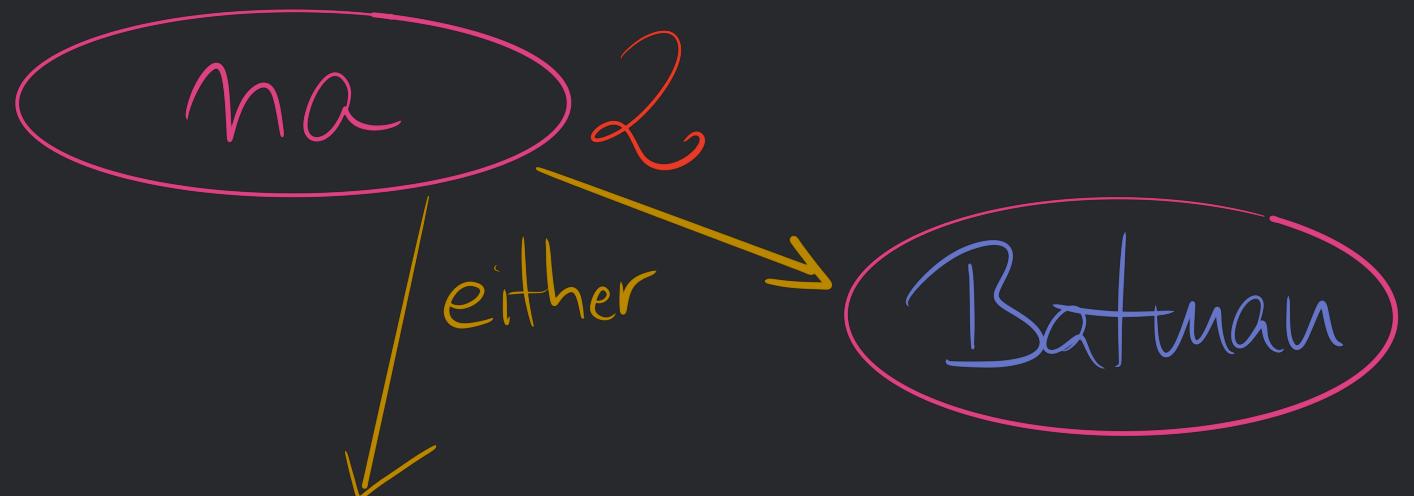
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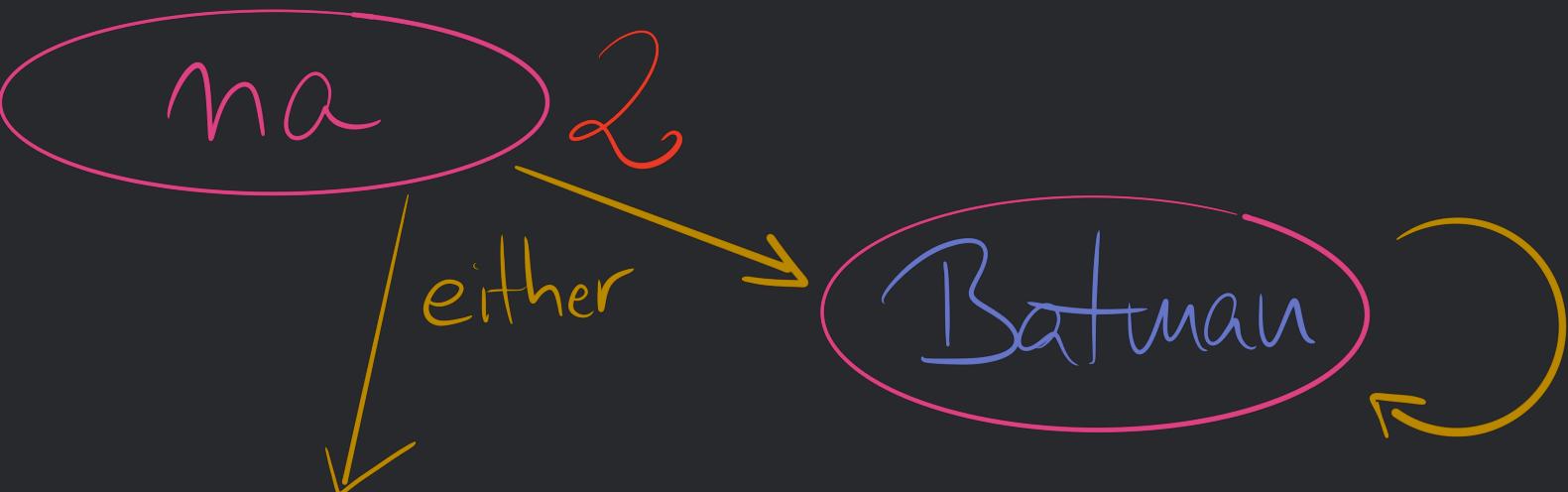
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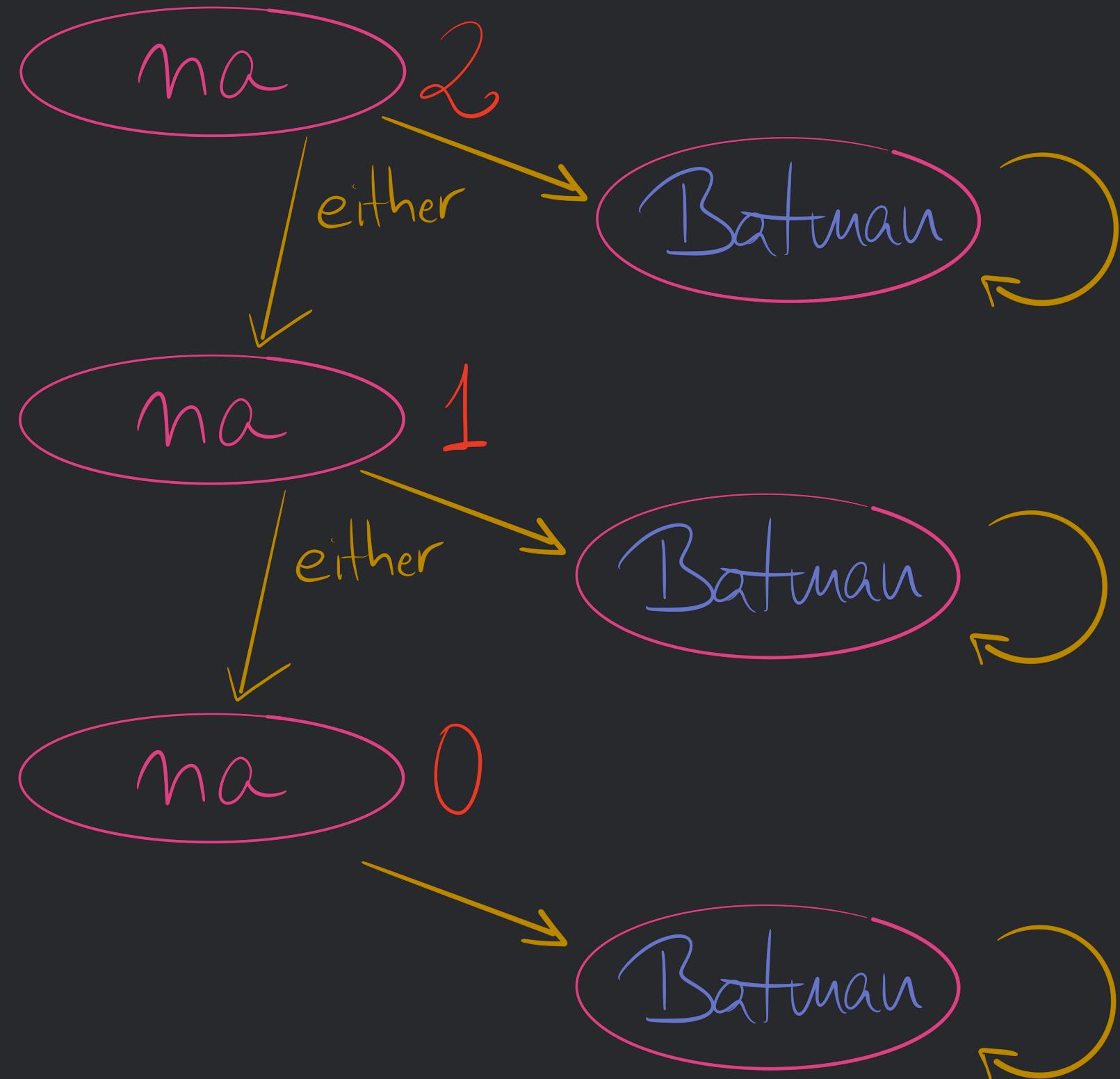
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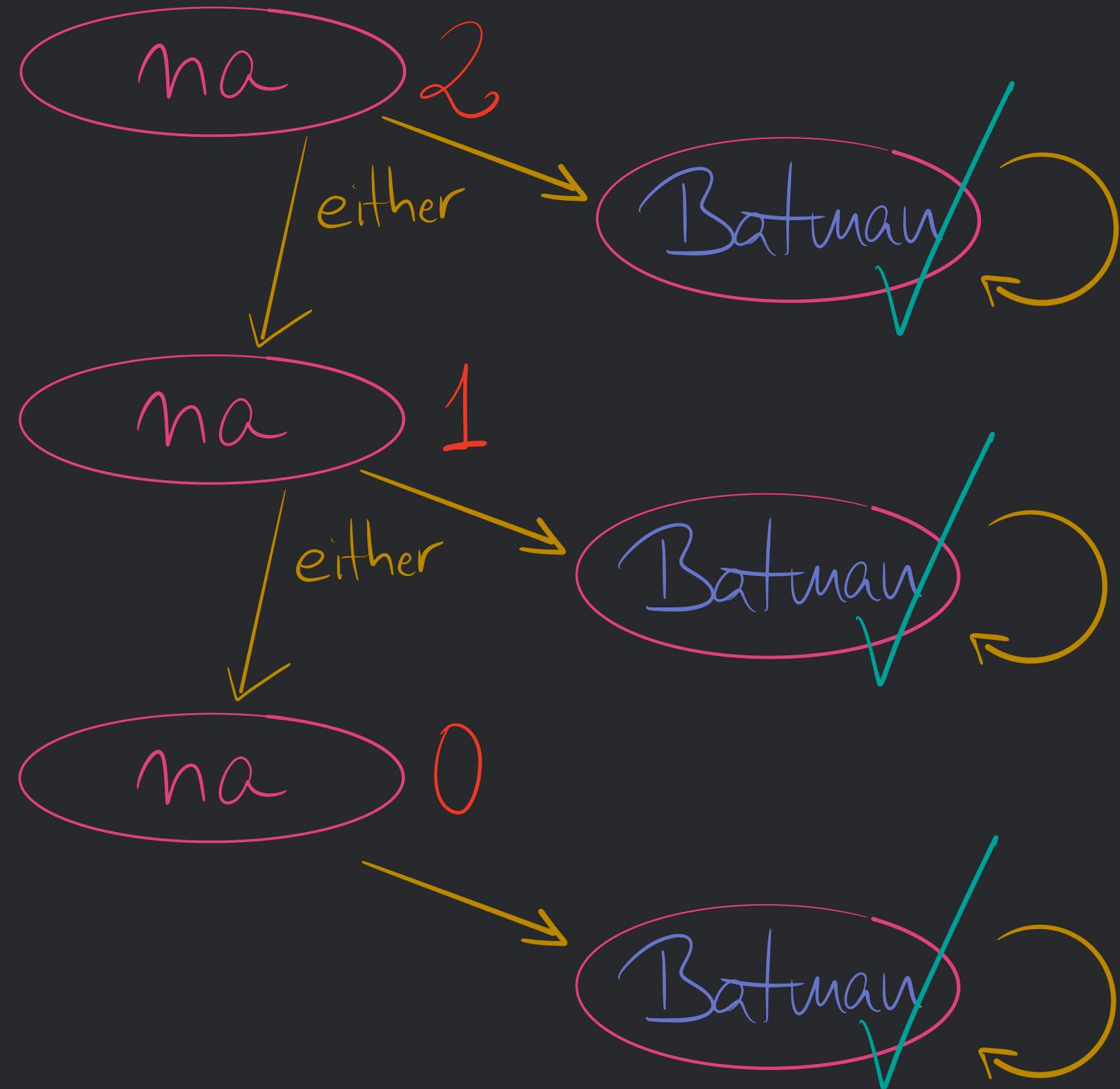
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```



HOW WOULD THE
EQUIVALENT PLUSCAL
ALGORITHM LOOK LIKE?



```
(*--fair algorithm ThemeSong {
variables count = 2, s = "na";
{
    while (count > 0) {
        either {
            s := "Batman";
            count := 0;
        } or {
            s := "na";
            count := count - 1;
        }
    };
    if (count = 0) {
        s := "Batman";
    }
}
} -*-)
```



```

VARIABLES count, s, pc

vars == << count, s, pc >>

Init == /\ count = 2
      /\ s = "na"
      /\ pc = "ThemeSong"

ThemeSong == /\ pc = "ThemeSong"
            /\ IF count > 0
              THEN /\ \v /\ s' = "Batman"
                  /\ count' = 0
                  \v /\ s' = "na"
                  /\ count' = count - 1
                  /\ pc' = "ThemeSong"
            ELSE /\ IF count = 0
              THEN /\ s' = "Batman"
              ELSE /\ TRUE
                  /\ s' = s
                  /\ pc' = "Done"
                  /\ count' = count

Next == ThemeSong
       \v (pc = "Done" /\ UNCHANGED vars)

Spec == /\ Init /\ [] [Next]_vars /\ WF_vars(Next)

```



WE CAN 'EASILY' MODEL WHOLE
SYSTEMS USING PLUSCAL

LIKE...

WITH PLUSCAL WE CAN MODEL
CONCURRENT (OR NOT) SYSTEMS BY
USING process

```
variables actorInboxes = [ actor | -> <>> ];
triggered = FALSE;

procedure trigger(trigger_content="?")
  triggerLabel:
    triggered := TRUE;
    return;
}

fair process (actor = "actor")
variables currentMessage = <<"?", "no_content">>;
  kind = "?";
  content = "no_content";
{
  Send:
    actorInboxes["actor"] := Append(actorInboxes["actor"], <<"trigger", "foo">>);
  WaitForMessages:+
    while (TRUE) {
      if (actorInboxes["actor"] /= <>>) {
        currentMessage := Head(actorInboxes["actor"]);
        content := Head(Tail(currentMessage));
        kind := Head(currentMessage);
        actorInboxes["actor"] := Tail(actorInboxes["actor"]);
      };
      ProcessMessage:
        if (kind = "trigger") {
          call trigger(content);
        }
    }
}
```

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variables actorInboxes = [ actor | -> <>> ];
triggered = FALSE;

procedure trigger(trigger_content="?") {
    triggerLabel:
    triggered := TRUE;
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  WaitForMessages:+
    while (TRUE) {
      if (actorInboxes["actor"] /= <<>>) {
        currentMessage := Head(actorInboxes["actor"]);
        content := Head(Tail(currentMessage));
        kind := Head(currentMessage);
        actorInboxes["actor"] := Tail(actorInboxes["actor"]);
      };
      ProcessMessage:
        if (kind = "trigger") {
          call trigger(content);
        }
    }
}
```

A POSSIBLE CHECK ON THIS SYSTEM COULD THEN BE

Triggered == triggered = TRUE

Liveness == <>Triggered

A close-up photograph of a person wearing a dark balaclava and a grey hoodie. The person is looking directly at the camera with a neutral expression. The background is a plain, light-colored wall.

QUESTIONS?

THANKS!

FURTHER REFERENCES

DOWNLOADING THE TLA TOOLBOX

SPECIFYING SYSTEMS BY LESLIE LAMPORT^{SSL}

PRACTICAL TLA+ BY HILLEL WAYNE^{PTHW}

^{SSL} THIS IS THE MAIN REFERENCE FOR TLA+. AND ALTHOUGH IT CAN LOOK A BIT DENSE IT READS VERY WELL.

^{PTHW} THIS IS A LIGHTER FIRST REFERENCE, FOCUSED IN PLUSCAL (USING THE P SYNTAX). I STARTED WITH THIS BOOK, AND WITH IT YOU CAN EASILY GET ENOUGH PLUSCAL TO DEFINE YOUR SPECIFICATIONS AND VALIDATE YOUR MODELS

TLA+ VIDEO COURSE BY LESLIE LAMPORT^{TVC}

LEARN TLA ONLINE BOOK BY HILLEL WAYNE^{LTHW}

^{TVC} THIS IS A VIDEO COURSE BY LAMPORT. TOTAL OF AROUND 4 HOURS

^{LTHW} AN ONLINE BOOK BY HILLEL WAYNE COVERING PARTS OF PRACTICAL TLA+

EOF