AdvGeomec-Poli_Renato_HW5

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3.6 WP5: Poroelasticity

3.6.1 Exercise 1: Biot coefficient determination The file BiotCoeffExperiment.xlsx has data from a laboratory experiment on a reservoir sandstone that shows axial and radial deformations caused by alternating variations of confining stress P_c and pore pressure P_p .

- a. Plot pressure and stresses as a function of time.
- b. What are the dPc/dt and dPp/dt loading rates when either confining or pore pressure are increased??

The loading rates are approx. 5 psi/s.

- c. Fit a straight line to the data to obtain a unique relationship between ε_{vol} and σ_{mean} (effective), and calculate the bulk Biot coefficient α . Assuming isotropic elasticity and that the Poisson Ratio is 0.25, what is the Young's modulus?
- d. Plot together the volumetric strain with Terzaghi's and Biot's effective stresses.
- e. If permeability is k = 100 mD, the fluid is water, porosity is 0.28, and the sample length is 0.05 m with top and bottom drainage, what is the characteristic time for pore pressure diffusion T_{ch} ? How does it compare to the pressure/stress loading time? Would it be drained or undrained loading? Note: you need the diffusivity parameter for which you have to look up for properties of water.
- f. EXTRA: Use the theory of transverse isotropic poro-elasticity to figure out the stress paths needed to measure directly α_h and α_v .

```
# Support functions
import numpy as np
import matplotlib.pyplot as plt
import pandas as pd
plt.style.use('default') ## reset!
plt.style.use('paper.mplstyle')
df = pd.read_excel("BiotExp_fmt.xlsx")
df["Pp_psi_s"] = ( df.Pp_psi - df.Pp_psi.shift() ) / ( df.time_s - df.time_s.shift() )
df["Pp_psi_s"] = df.Pp_psi_s.rolling(20).mean()
df["Pc_psi_s"] = ( df.Pc_psi - df.Pc_psi.shift() ) / ( df.time_s - df.time_s.shift() )
df["Pc_psi_s"] = df.Pc_psi_s.rolling(20).mean()
df["strain_vol"] = 2*df.strain_rad + df.strain_ax
df["Sm_psi"] = ( 3*df.Pc_psi + df.Sd_psi ) / 3
df["Sm-Pp"] = df.Sm_psi - df.Pp_psi
# Optimize Biot
from scipy.optimize import minimize
from scipy.stats import linregress
def linreg_biot(alpha) :
    slope, intercept, r_value, p_value, std_err = linregress( df.strain_vol, (df.Sm_psi-alpha* df.Pp_psi) )
    return (1 - r_value**2 )**2
res = minimize( linreg_biot, 0.5 )
alpha = res.x[0]
df["Sm-alpha_Pp"] = df.Sm_psi - alpha* df.Pp_psi
slope, intercept, r_value, p_value, std_err = linregress(df.strain_vol,df["Sm-alpha_Pp"])
from IPython.display import display, Math, Latex
display(Latex(r"\newpage"))
print("### Find Biot coefficient and Young Modulus ###")
print(f"Biot = {alpha:.2f} minimizes gets to the most linear results (R^2 = {r_value**2:.2f}).")
nu = 0.25
K_Pa = slope * 6894.76
E_Pa = K_Pa * 3 * (1 - 2 * nu)
print(f"K = slope = \{slope: .1f\} psi = \{K_Pa/1e9: .2f\} GPa.")
print(f"E = Young Module = {slope:.1f} psi = {E_Pa/1e9:.2f} GPa.")
```

```
k_D = 0.1 \# Permeability
k_m2 = k_D * 9.869233e-13
phi = 0.28
L_m = 0.05/2
mu_Pa_s = 1e-3
Kf_Pa = 2.1e9 \# Pa - water bulk modulus
Ks_Pa = 38e9 # Pa - quarttz bulk modulus
M_Pa = 1 / ( (alpha - phi )/Ks_Pa + phi/Kf_Pa )
\label{eq:def:Diffusivity} \mbox{Diffusivity} = \mbox{k_m2} * \mbox{M_Pa} / \mbox{mu_Pa_s}
Tch_s = L_m**2 / Diffusivity
print("### Find Relaxation time ###")
print(f"Diffusivity: {Diffusivity: .3f} m2/s")
print(f"Tch: {Tch_s*1e3:.2f} ms")
print("As Tch << T_load, the experiment is DRAINED.")</pre>
fig, [[ax1, ax2], [ax3, ax4]] = plt.subplots(2,2)
fig.set_size_inches( 15, 10 )
ax.plot( df.time_s, df.Pp_psi, c='red', label="Pore Pressure $P_p$" )
ax.plot( df.time_s, df.Pc_psi, c='green',label="Confining Pressure $P_c$" )
ax.plot( df.time_s, df.Sd_psi, c='blue', label="Deviatoric stress $S_D$" )
ax.plot( df.time_s, df.Sm_psi, c='black',label="Mean Stress $S_m$" )
ax.set_ylim( 0,6000 )
ax.set_xlim( 0,3300 )
ax.set_xlabel("Time ($s$)")
ax.set_ylabel("Pressure ($psi$)")
ax.legend()
ax.plot( df.time_s, df.Pp_psi_s, c='red', label="Pore Pressure $P_p$" )
ax.plot( df.time_s, df.Pc_psi_s, c='green',label="Confining Pressure $P_c$" )
ax.set_xlim( 0,3300 )
ax.set_xlabel("Time ($s$)")
ax.set_ylabel("Change rate ($psi/s$)")
ax.legend()
ax.plot( df.strain_vol, df["Sm-Pp"], c='gray',label="$S_m-P_p$" )
#ax.set_xlim( 0,3300 )
ax.set_xlabel("Vol Strain ($\epsilon$)")
ax.set_ylabel("Sm - Pp ($psi$)")
ax.legend()
ax.plot( df.strain_vol, df["Sm-alpha_Pp"], c='orange',label=r"Biot ($S_m-\alpha P_p$)" )
ax.plot( df.strain_vol, df["Sm-Pp"], c='gray',label=r"Tersaghi ($S_m- P_p$)" )
#ax.set_xlim( 0,3300 )
ax.set_xlabel("Vol Strain ($\epsilon$)")
ax.set_ylabel(r"Effective stress ($psi$)")
ax.legend()
```

```
### Find Biot coefficient and Young Modulus ### Biot = 0.90 minimizes gets to the most linear results (R^2 = 0.98). K = slope = 462381.2 psi = 3.19 GPa. E = Young Module = 462381.2 psi = 4.78 GPa. ### Find Relaxation time ### Diffusivity: 0.660 m2/s Tch: 0.95 ms As Tch << T_load, the experiment is DRAINED.
```

10.00

