

Advanced Petrophysics
PGE 381L, Fall 2023
Unique Number: 20215

Homework Assignment No. 8

November 16, 2023
Due on Thursday, December 4, 2023, before 11:00 PM

Name: _____

UT EID: _____

Objectives:

- a) To practice application of Young-Laplace equation to estimate capillary pressure
- b) To practice assessment and interpretation of capillary pressure
- c) To practice saturation-height analysis
- d) To understand trapping mechanisms

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Note: Please scan your homework assignment and upload it as one pdf file on the Canvas website before the deadline. Please name your homework document as follows:

PGE381L_2023_Fall_HW08_lastname_name.pdf

Example: PGE381L_2023_Fall_HW08_Heidari_Zoya.pdf

Question 1: This question can be considered as an application of Young-Laplace's equation in evaluation of oil migration in porous media. Figure 1 shows an oil blob being displaced by water at the pore scale in a reservoir. The blob has encountered a constriction at a pore throat. In order for the oil blob to pass through the constriction and be produced, a sufficiently high pressure gradient must be applied across the blob. If such a pressure gradient cannot be generated by the water injection, then the blob will be trapped as residual oil. The objective of this exercise is for you to calculate the pressure gradients necessary to mobilize the blob for a variety of situations to determine whether or not such gradients can be created under normal oilfield flow conditions. Answer the following questions:

Wetting phase	=	water
Oil-water interfacial tension	=	σ dynes/cm
Contact angle	=	θ°
Radius of pore body	=	R (cm)
Radius of pore throat	=	r (cm)
Length of blob	=	L (cm)

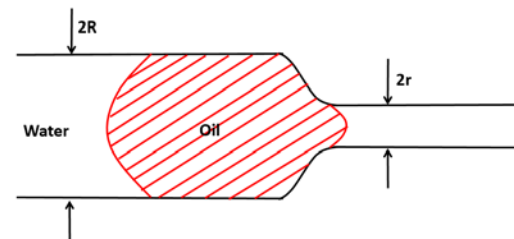


Figure 1

- a) Calculate the pressure gradients required for mobilization of the oil blob for an average sand and a very fine sand. Assume the following:

$$R = 5r$$

$$L = R$$

$$\theta = 0^\circ$$

$$\text{For average sand: } r = 0.005 \text{ cm}$$

$$\text{For very fine sand: } r = 0.001 \text{ cm}$$

$$\text{For a normal waterflood: } \sigma = 30 \text{ dynes/cm}$$

- b) Calculate the pressure gradients generated in a normal waterflood in rock types A and B (with an order of magnitude difference in permeability) using the following assumptions:

$$\text{Darcy velocity} = 1 \text{ ft/day}$$

$$\text{Water viscosity} = 1 \text{ cp}$$

$$\text{Effective permeability to water in rock type A} = 2 \text{ darcies}$$

$$\text{Effective permeability to water in rock type B} = 500 \text{ md}$$

Are these pressure gradients sufficient to mobilize the oil blob of part (a)?

- c) Repeat the calculations of part (b) for an enhanced waterflood in which a surfactant has been added to the injected water so as to reduce the oil-water interfacial tension to 0.01 dyne/cm. Comment on the effectiveness of the enhanced waterflood under normal oilfield flow conditions for rock types A and B.
- d) Compare the capillary numbers for the ordinary waterflood and the enhanced waterflood for rock types A and B. The capillary number is given by

$$N_c = \frac{\mu_w v}{\sigma}$$

where

N_c	=	capillary number
μ_w	=	water viscosity
v	=	darcy velocity
σ	=	water-oil interfacial tension

We will talk about capillary number later on in the class. In this assignment, I want you to get familiar with this unitless number and the way it is calculated.

Question 2: Figure 2 shows an upward migrating oil bubble from a source rock into a reservoir initially fully saturated with water. The migrating bubble has encountered a restriction at a pore throat of radius r_H . In order for migration to continue, the leading end of the bubble (A) must squeeze through the pore throat. Assume that ends A and B of the bubble are hemispherical with B having a radius r_B .

- a) Derive the condition necessary for the oil bubble to pass through the restriction and continue with its migration in terms of the following parameters:

$$\text{Water density} = \rho_w$$

$$\text{Oil Density} = \rho_o$$

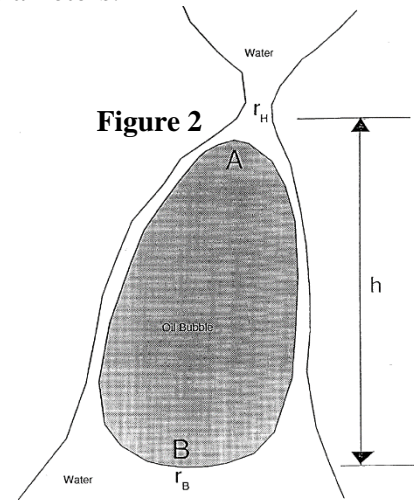
$$\text{Oil/water interfacial tension} = \sigma$$

$$\text{Gravitational acceleration} = g$$

$$\text{Pore throat radius} = r_H$$

$$\text{Bubble base radius} = r_B$$

$$\text{Height of bubble} = h$$



- b) Now assume the following quantitative reservoir properties and calculate the height the bubble must achieve in order to continue migration.

$$\rho_w = 1.00 \text{ g/cm}^3$$

$$\rho_o = 0.8 \text{ g/cm}^3$$

$$\sigma = 35.0 \text{ dynes/cm}$$

$$g = 981 \text{ cm/s}^2$$

$$r_H = 0.0001 \text{ cm}$$

$$r_B = 0.01 \text{ cm}$$

Question 3: Figure 3 shows a microchannel placed horizontally on a chip. Assume that the microchannel has a circular shape with radius of r . Answer the following questions:

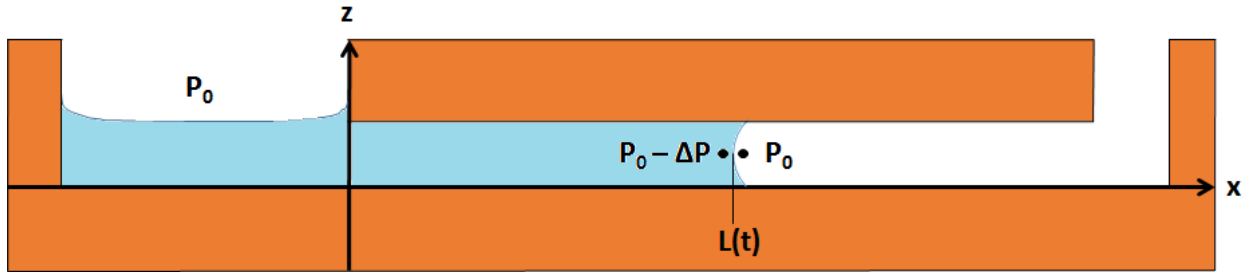


Figure 3: Schematic of a capillary-force micro-scale pump

- Derive an expression for $L(t)$ as a function of r , t , fluid viscosity (μ), surface tension (σ), and contact angle (θ).
- Derive an expression for the speed of fluid advancement in the horizontal microchannel.
- If you are asked to decide about the pump's material type, would you use Platinum or Plexiglas? Which one provides a higher pump efficiency?
HINT: Contact angle in the case of Platinum is smaller than the case of Plexiglas.

Question 4: The following data are given for the pore doublet model of Figure 7.73 in your textbook:

$$\begin{aligned} v_1 &= 1 \text{ ft/Day} \\ L &= 500 \text{ } \mu\text{m} \\ \mu &= 1 \text{ cp} \\ \sigma &= 30 \text{ dynes/cm} \\ \theta &= 0 \text{ degrees} \\ r_1 &= 50 \text{ } \mu\text{m} \\ r_2 &= 2.5 \text{ } \mu\text{m} \end{aligned}$$

Assume the capillaries are cylindrical tubes and that capillary tube 1 (with radius r_1) is larger than capillary tube 2 (with radius r_2). Answer the following questions:

- Calculate $(P_A - P_B)$ across capillary tube 1 in dynes/cm^2 . What percentage of this pressure difference is due to viscous pressure drop and what percentage is due to capillary pressure? Are you surprised by the degree of domination of one force over the other at the pore scale?
- Calculate the ratio v_2/v_1 . Which capillary tube will be displaced first, the larger tube or the smaller tube in this strongly water-wet medium?

Optional Bonus Questions:

Question 4: This is the same data set we will use in the class for practice (November 28th lecture). Please work on this example individually to make sure that you learn the concept we covered in the class.

Download the Excel file “PGE81L_HW_08_Data1” including the capillary pressure curves for the two layers of thickness 100 ft in a conventional reservoir. The water-oil density difference is 8.05 lb/ft³. Assume that the water-oil contact is at the bottom of the lower layer. Calculate the water saturation versus depth measured from the top to the bottom of the reservoir. Present the results of your calculations by plotting a graph of Depth versus Water Saturation, with Depth plotted on the vertical axis and Water Saturation plotted on the horizontal axis.

Question 5: Table 1 summarizes the results of a centrifuge drainage capillary pressure measurement along with other pertinent data about the experiment. Calculate and plot the drainage capillary pressure curve for the sample. Express your capillary pressure in psi.

Table 1: Centrifuge Data for Question 1

d	2.5	cm
L	7.35	cm
k	143	md
ϕ	19.0	%
V_p	7.04	cc
ρ_w	1.036	g/cc
ρ_o	0.822	g/cc
σ_{ow}	40	dynes/cm
θ	0	
r_1	8.25	cm
r_2	15.6	cm

RPM	V_w (cc)
520	0.0
800	1
860	1.5
920	2
1000	2.5
1100	2.9
1200	3.2
1400	3.6
1620	3.9
1800	4
2100	4.2

Question 6: Download the Excel file “PGE81L_HW_08_Data2” including mercury injection capillary pressure data obtained on a core sample. The core sample has a permeability of 3.86 md and a porosity of 13.2%. Answer the following questions.

- a) Plot S_w and S_{nw} versus pore throat radius on the same graph.
- b) Calculate the probability density function for the pore volume distribution and plot it on the same graph of S_w and S_{nw} versus pore throat radius. Use the 5-point central difference formula for calculating all derivatives.
- c) Calculate the probability density function for the pore radius distribution assuming a bundle of capillary tubes model for the porous medium. Compare this distribution with the pore volume distribution by plotting them on the same graph versus pore throat size. Comment on the pore structure of this sample.
- d) Estimate the absolute permeability of the sample from the mercury injection data. How does it compare with the lab measured permeability?

Question 7: Solve two questions of your choice from chapter 7 of your text book.