

Supplement to Prediction of Infectious Disease Epidemics via Feature-Weighted Density Ensembles

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August 2017

In this supplement, we include additional figures and results.

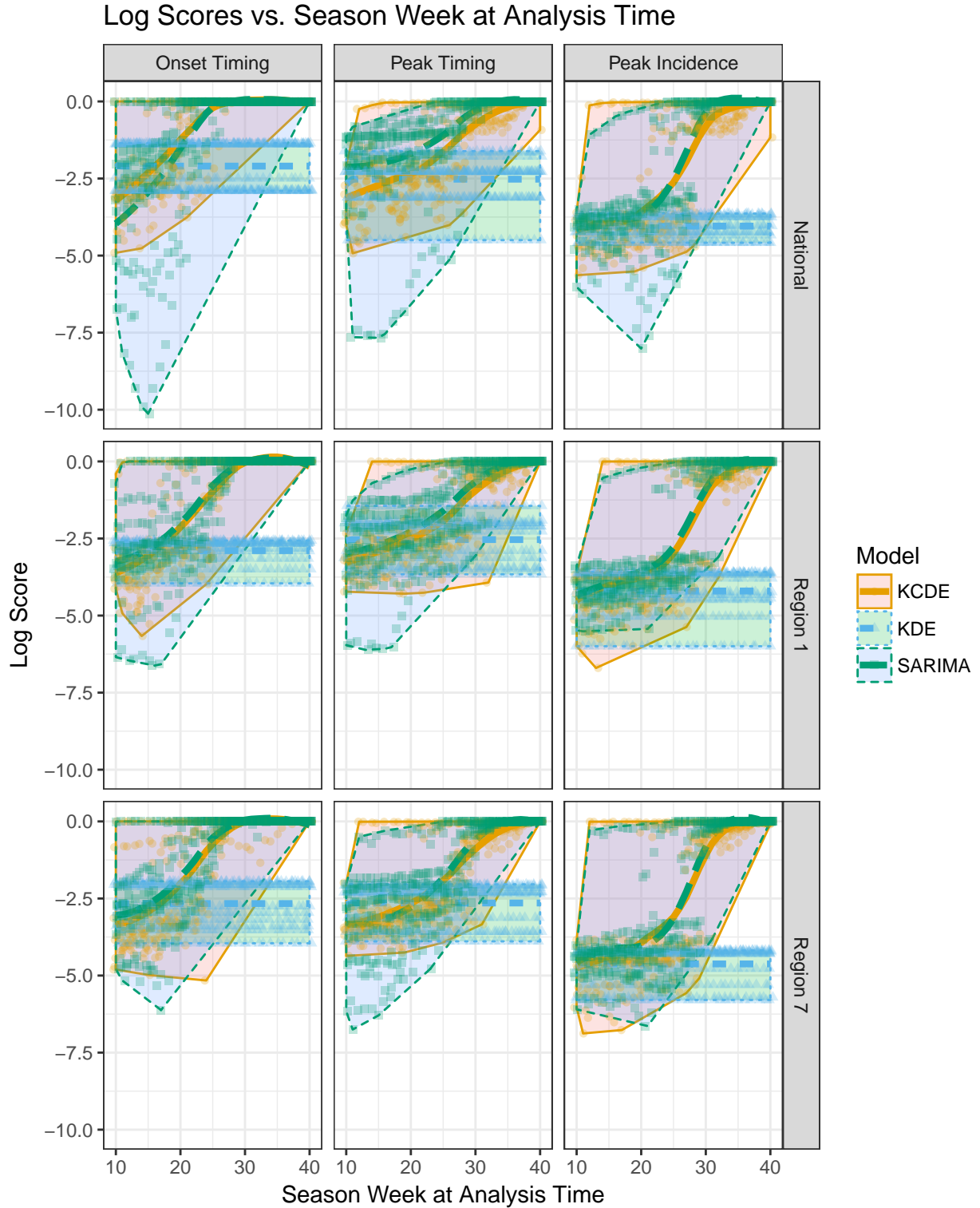
Component Model Log Scores and Weighting Features

Supplemental Figs 1, 2, and 3 illustrate the relationship between log scores and weighting features for predictions from the three component models made during the training phase in weeks before the season onset (for predictions of onset timing) or the season peak (for predictions of peak timing or peak incidence).

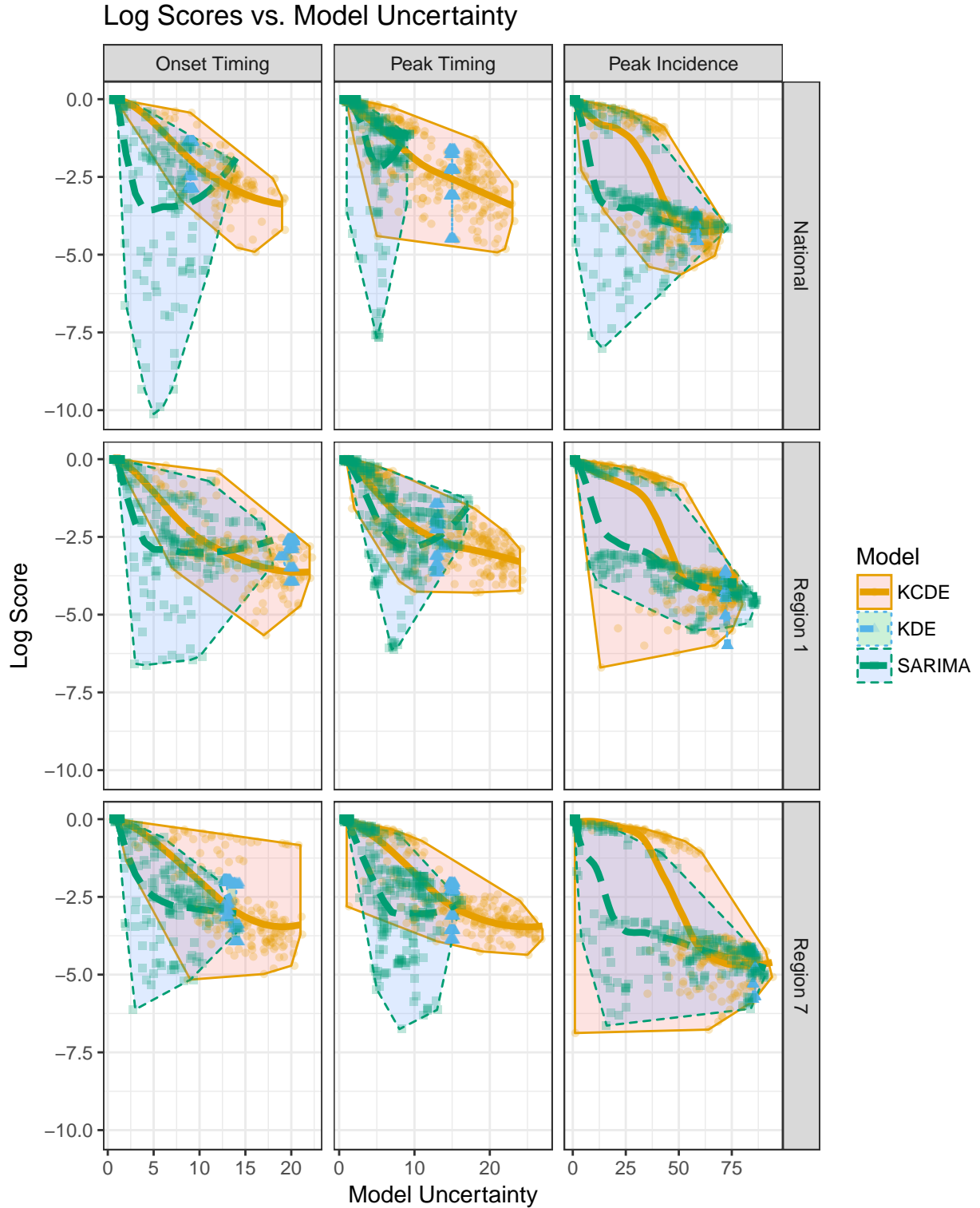
Estimated Mean Model Performance

Supplemental Fig ?? displays estimated mean log scores for each model and ensemble method in predictions made before the season onset or season peak. Supplemental Fig ??, ??, and ?? show estimates for the difference in mean log scores between the model with the highest estimated mean log score for each target and each other model. The point and 95% interval estimates are obtained from a mixed effects model with a separate fixed effect mean for the interaction of model and prediction target; random effects for each combination of region, season, model, and prediction target; and lag 1 autocorrelation nested within each combination of region, season, model, and prediction target. For predictions of onset timing, the only difference in model performance that is statistically significant is the difference between **CW** and **KDE**. For predictions of peak timing, the only difference that is statistically significant is between **SARIMA** and **KDE**. For predictions of peak incidence, none of the differences between the models are statistically significant.

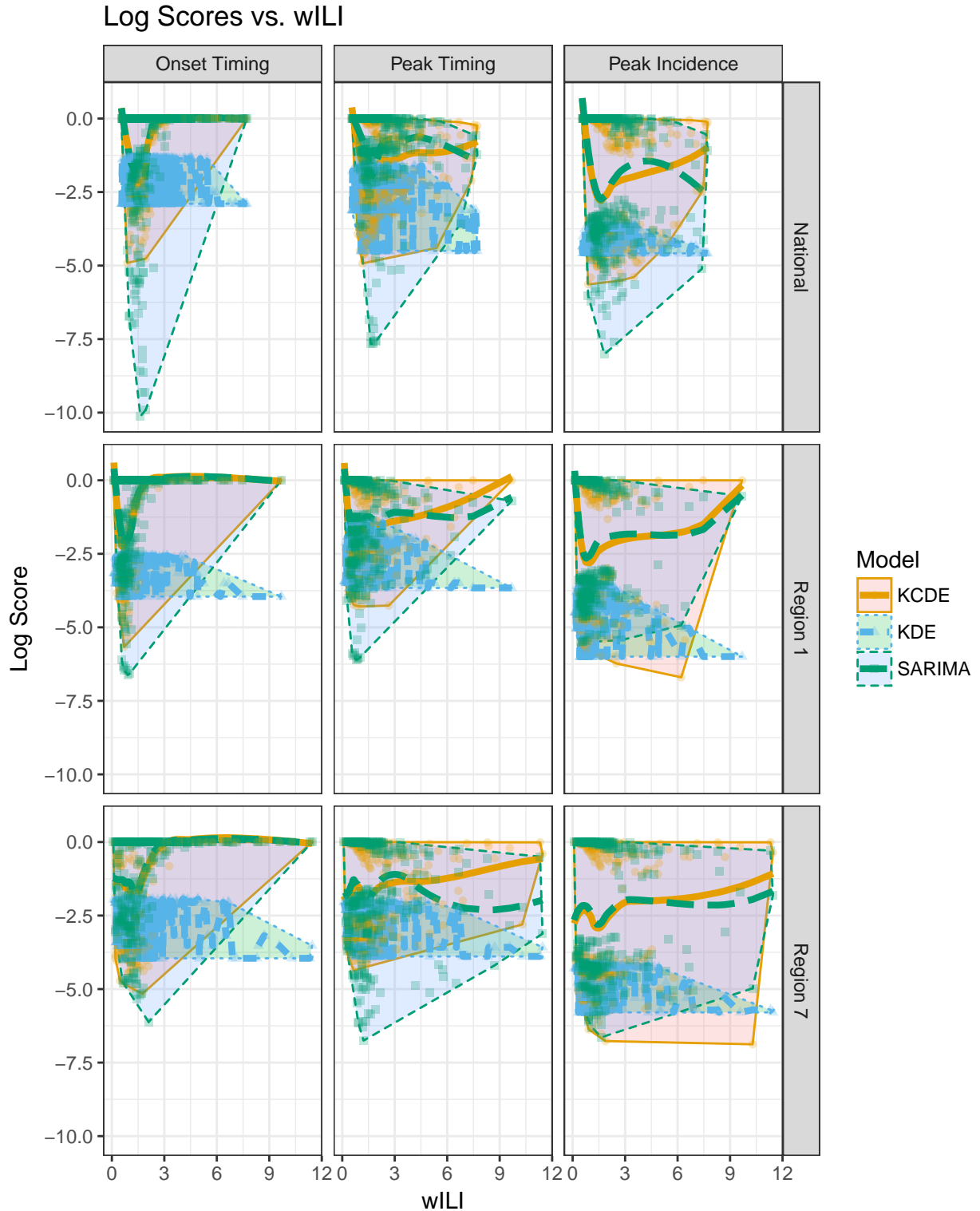
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## Joining, by = c("model", "prediction_target")
```



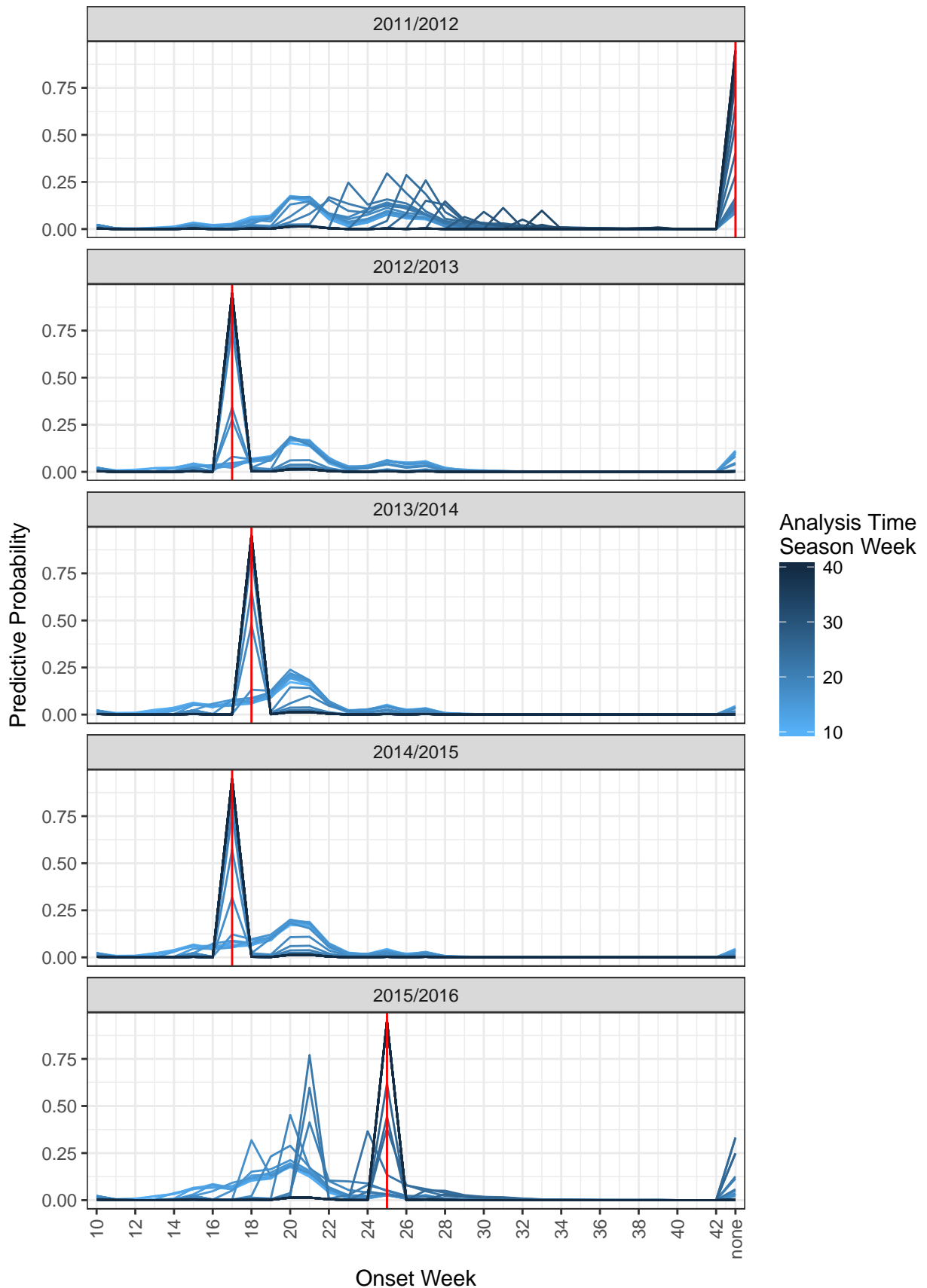
Supplemental Figure 1: Log scores achieved by each component model in each week of the season, summarizing across all seasons in both the training phase when all three component models produced predictions. The thick line is a smoothed estimate of mean log score at each week in the season; the shaded region indicates the convex hull of log scores achieved by each model; and the actual log scores achieved in each week are indicated with points.



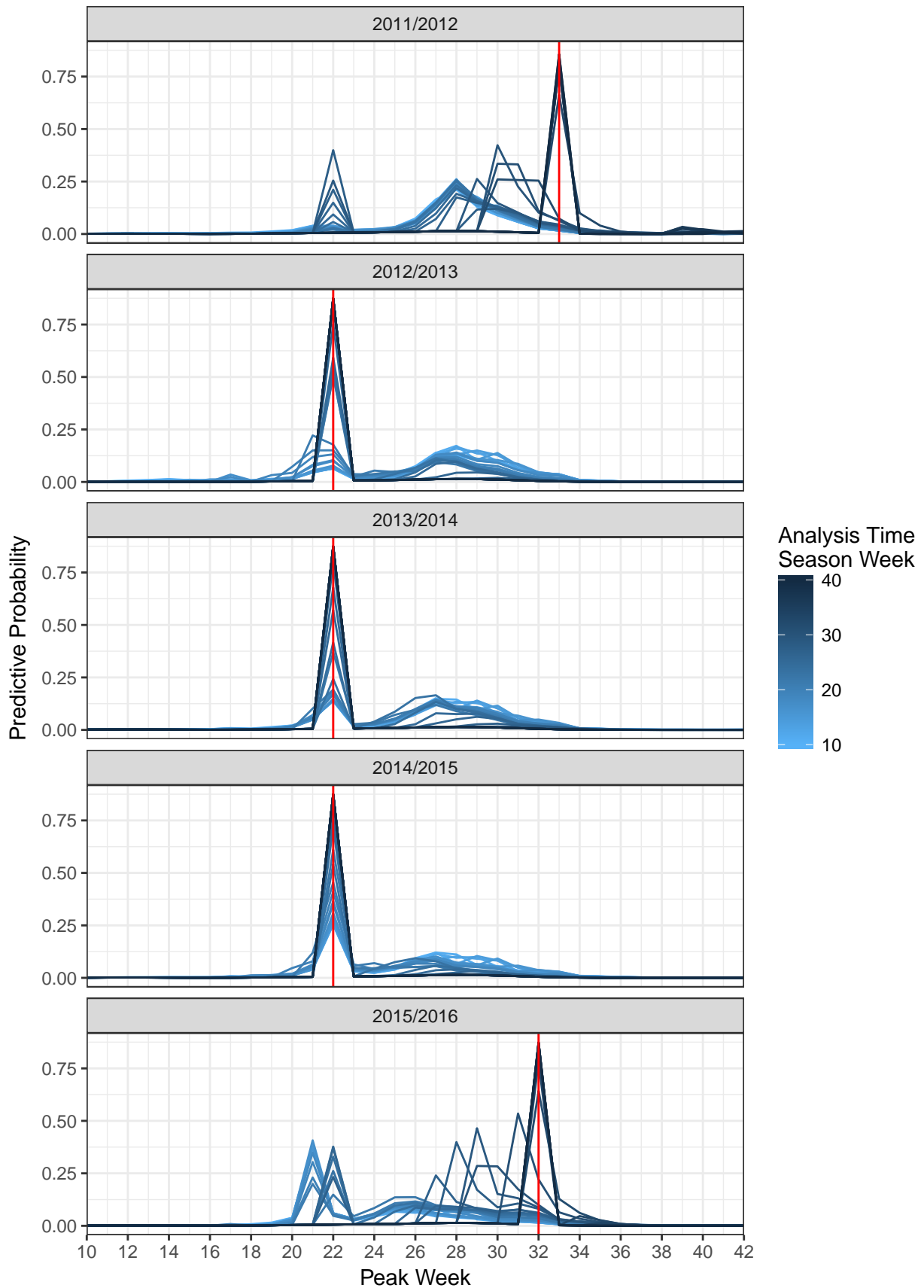
Supplemental Figure 2: Log scores achieved by each component model vs. model uncertainty as measured by the number of bins required to cover 90% of the predictive distribution. The plot summarizes results across all seasons in the training phase when all three component models produced predictions. The thick line is a smoothed estimate of mean log score at each value of model uncertainty; the shaded region indicates the convex hull of log scores achieved by each model; and the actual log scores achieved in each week are indicated with points. The KCDE and SARIMA models condition on all previously observed data within the current season, and generally have high certainty when the target event (season onset or season peak) has almost occurred or has already occurred.



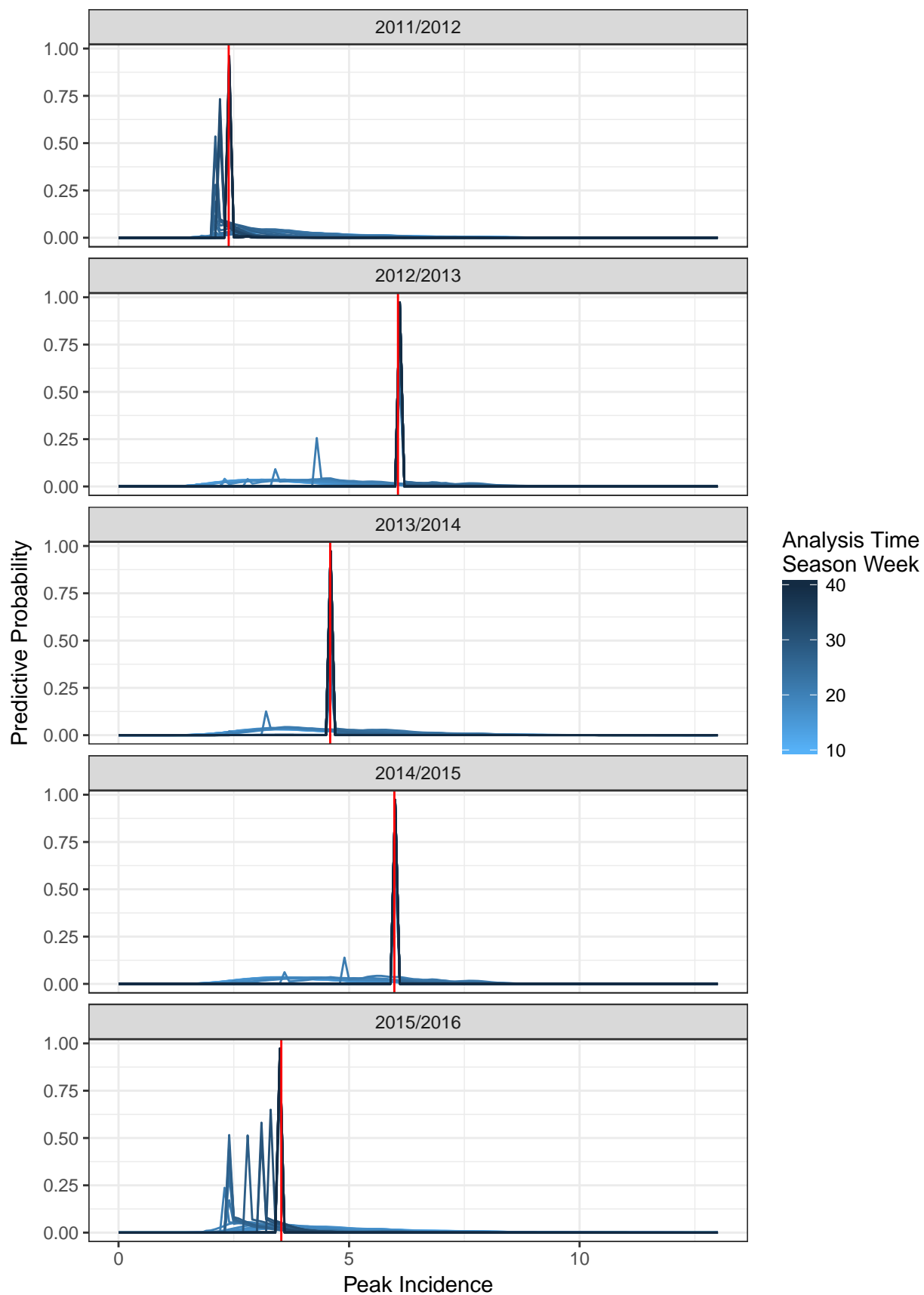
Supplemental Figure 3: Log scores achieved by each component model vs. wILI in the week of the season when predictions were made. The plot summarizes results across all seasons in the training phase when all three component models produced predictions. The thick line is a smoothed estimate of mean log score at each week in the season; the shaded region indicates the convex hull of log scores achieved by each model; and the actual log scores achieved in each week are indicated with points.



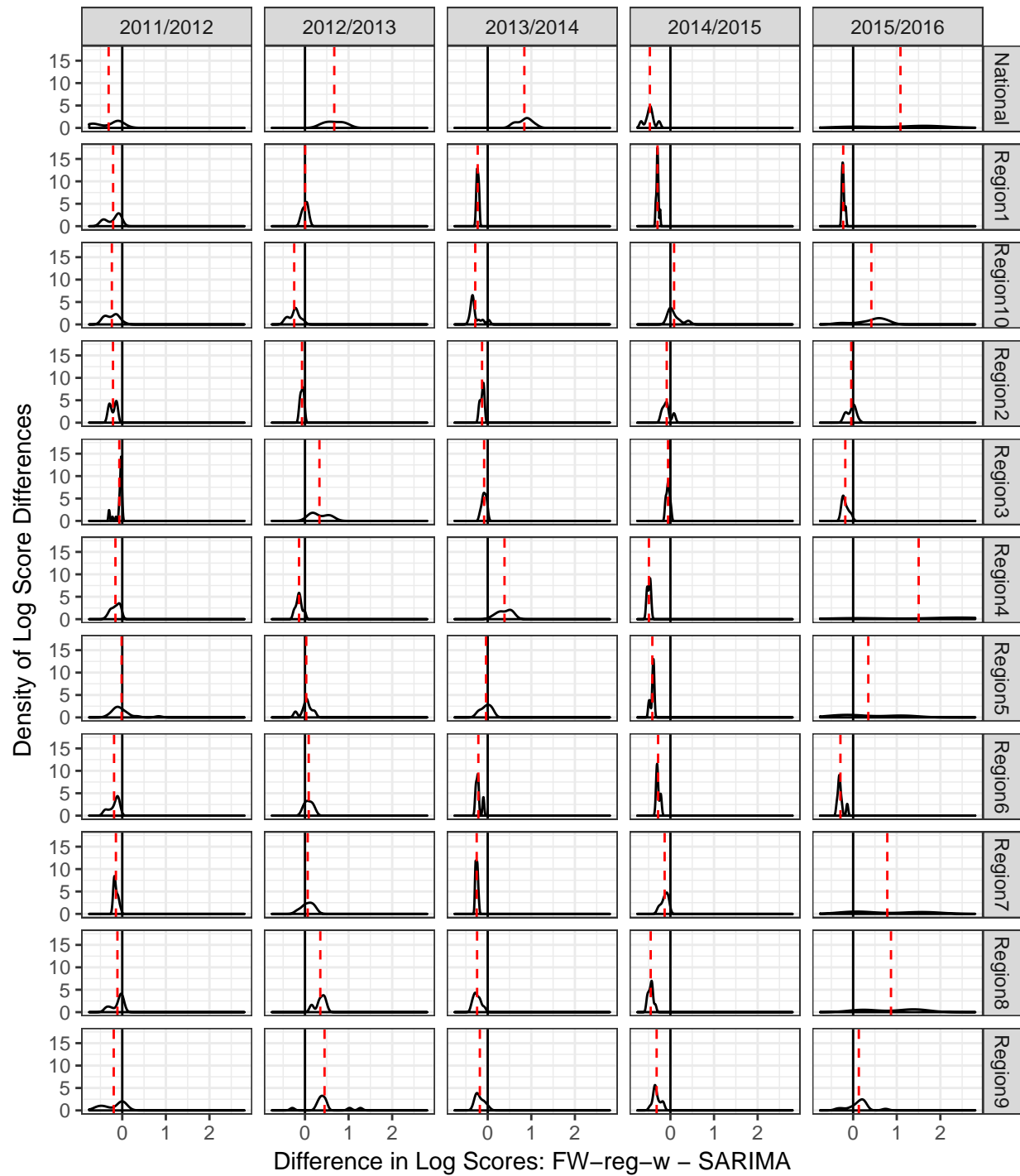
Supplemental Figure 4: Predictive distributions for onset timing at the national level from just the FW-reg-w method, faceted by season.



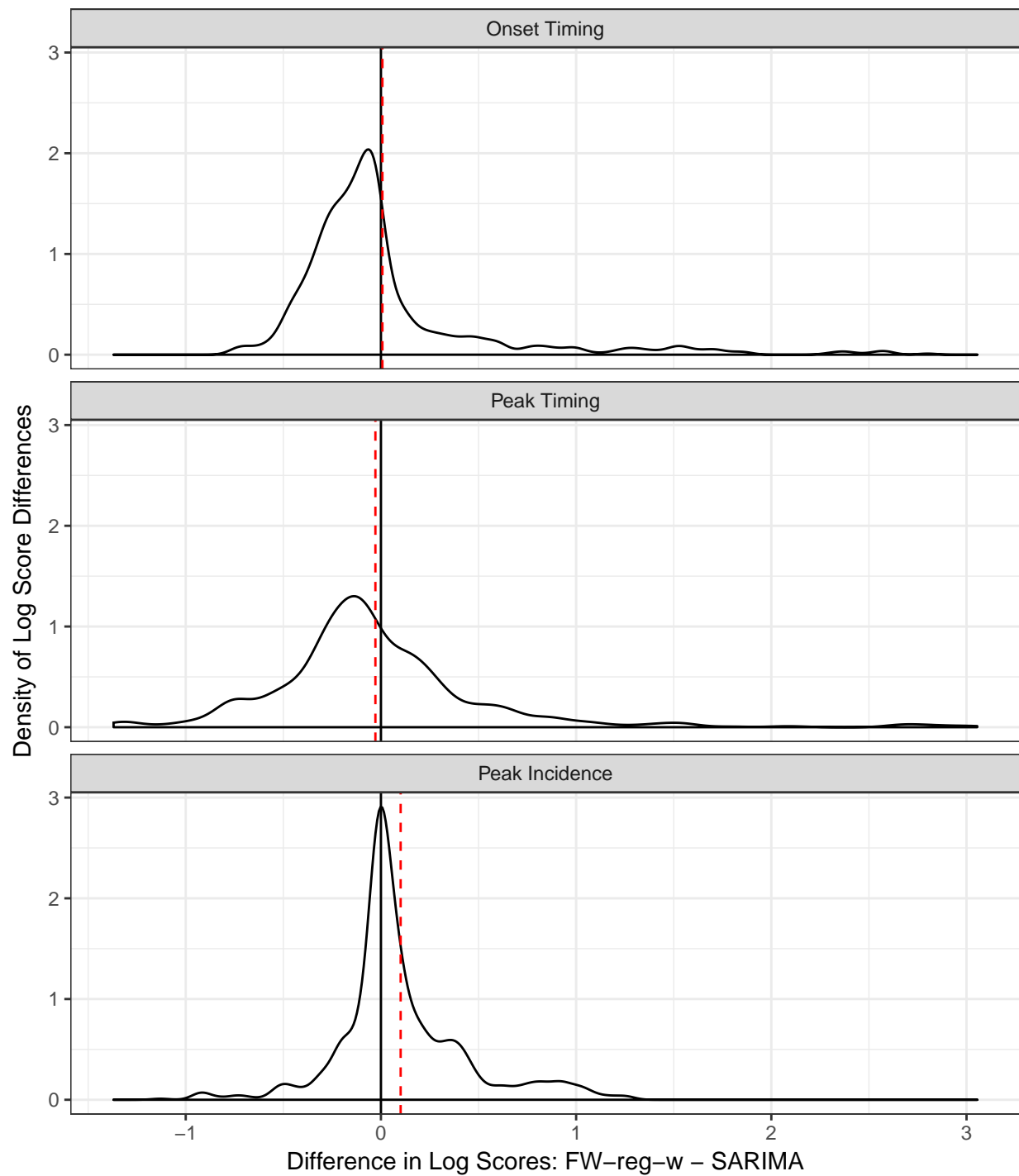
Supplemental Figure 5: Predictive distributions for peak timing at the national level from just the FW-reg-w method, faceted by season.



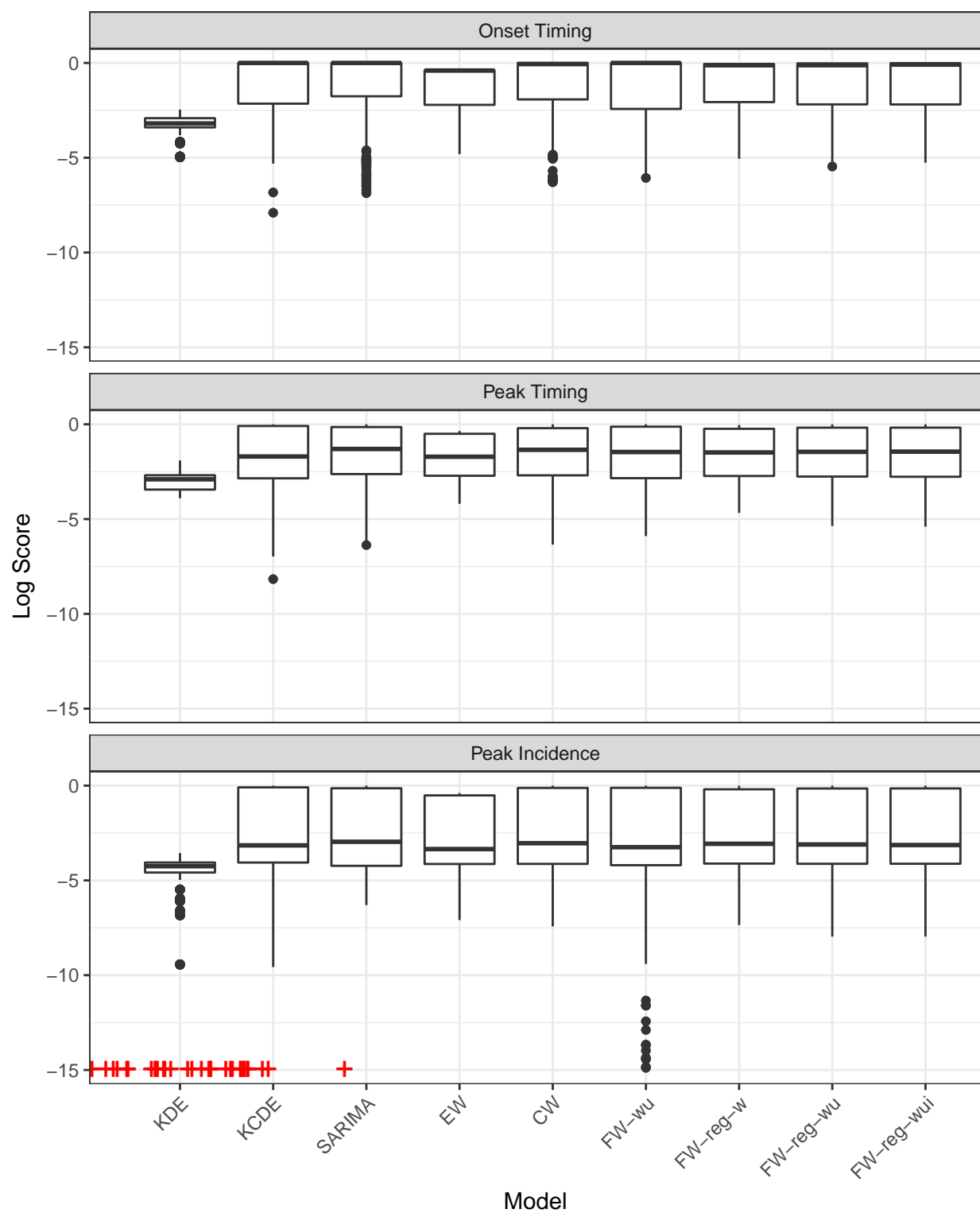
Supplemental Figure 6: Predictive distributions for peak incidence at the national level from just the FW-reg-w method, faceted by season.



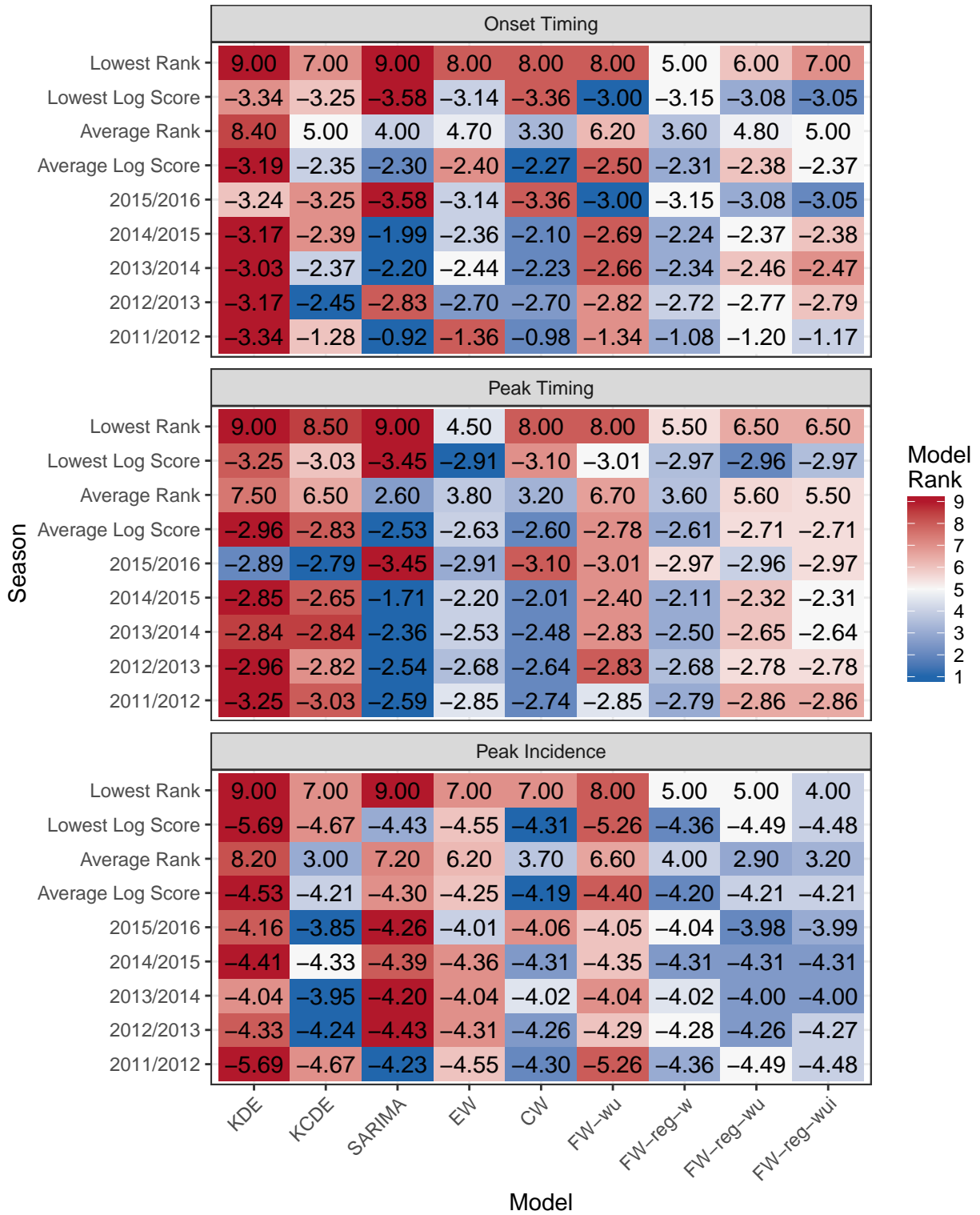
Supplemental Figure 7: Density plots representing the distribution of log score differences from predictions made by the FW-reg-w and SARIMA models for predictions of onset timing across all regions and test phase seasons. The horizontal axis represents the difference in log scores achieved by the FW-reg-w and SARIMA models for predictions made in a particular week; positive values indicate that FW-reg-w outperformed SARIMA for that prediction. The vertical line indicates the mean log score difference for all predictions made before the onset occurred in the given region and season.



Supplemental Figure 8: Density plots representing the distribution of log score differences from predictions made by the FW-reg-w and SARIMA models for predictions of each prediction target, aggregated across all regions and test phase seasons. The horizontal axis represents the difference in log scores achieved by the FW-reg-w and SARIMA models for predictions made in a particular week; positive values indicate that FW-reg-w outperformed SARIMA for that prediction. The vertical line indicates the mean log score difference for all predictions made before the onset or season peak occurred.



Supplemental Figure 9: Log scores across all regions, seasons, and season weeks represented in box plots. Log scores of negative infinity are represented with a cross at -15.



Supplemental Figure 10: Model performance ranked by mean log score within each of the five test seasons for predictions made before the target (season onset or peak) occurred. Averages are taken across all regions.

Table 1: Summary of average log scores and variance of log scores across all spatial units and test phase seasons for each method.

Model	Onset Timing		Peak Timing		Peak Incidence	
	Mean	Variance	Mean	Variance	Mean	Variance
KDE	-3.27	0.18	-3.00	0.25	-4.54	1.19
KCDE	-2.10	1.67	-2.85	0.51	-4.17	0.54
SARIMA	-2.04	2.24	-2.64	1.02	-4.27	0.41
EW	-2.17	1.12	-2.69	0.34	-4.22	0.28
CW	-2.00	1.80	-2.66	0.78	-4.16	0.29
FW-wu	-2.23	1.74	-2.80	0.63	-4.35	1.58
FW-reg-w	-2.03	1.45	-2.66	0.52	-4.16	0.30
FW-reg-wu	-2.11	1.51	-2.74	0.59	-4.18	0.36
FW-reg-wui	-2.10	1.49	-2.74	0.58	-4.17	0.35