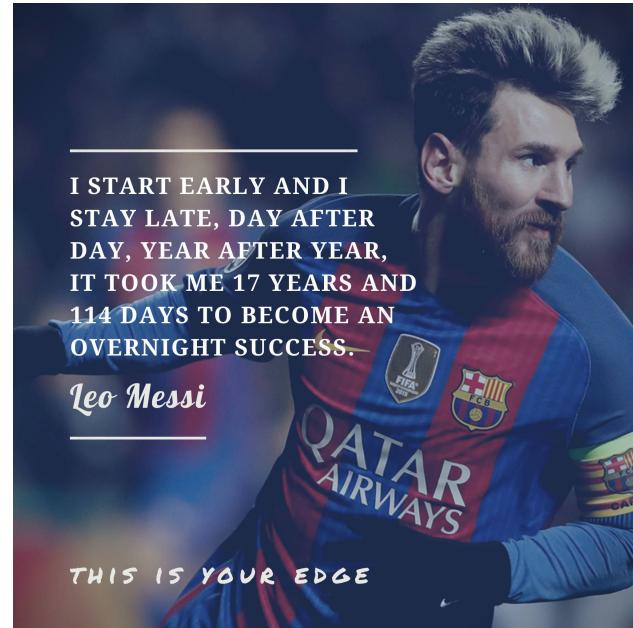


# TREES BASICS



Last class of  
Intermediate

## Today's content

- Trees intro
- Naming convention
- Tree traversal
  - Preorder
  - Inorder
  - Postorder
- Basic Tree problems

## Linear Data Structure

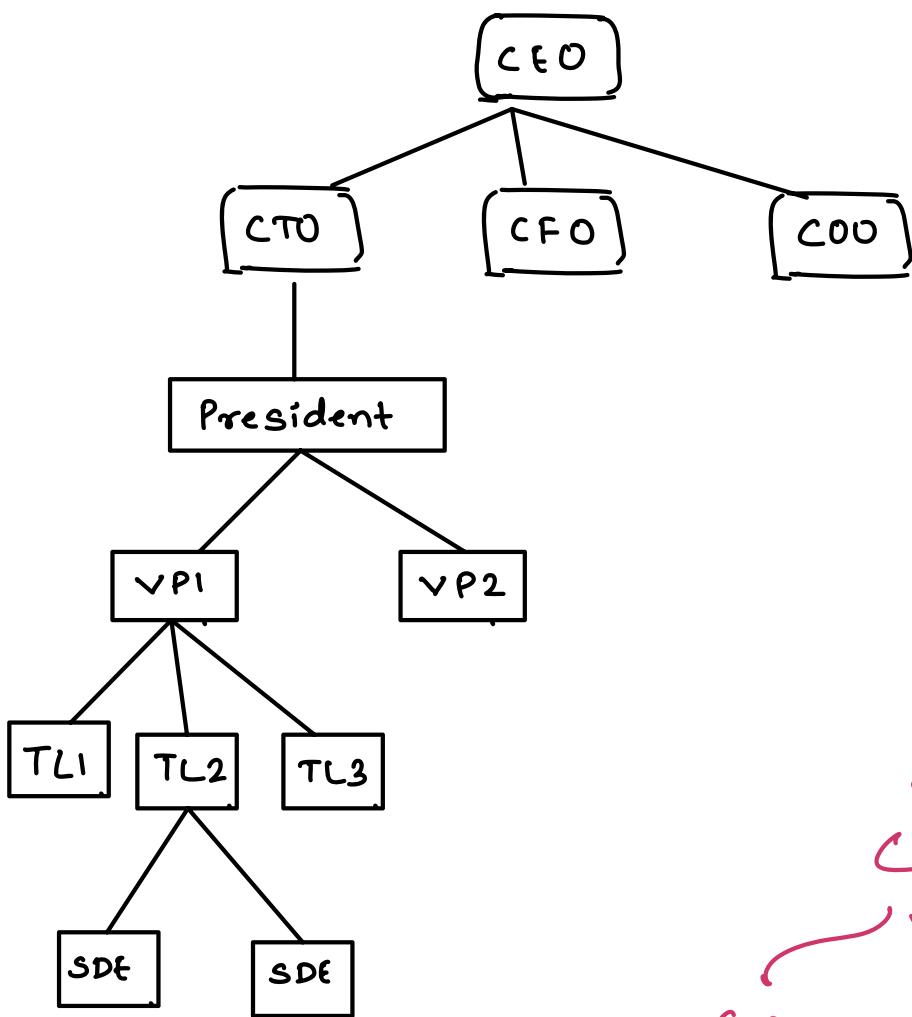
01. Array 

02. Linkedlist 

03. Stack

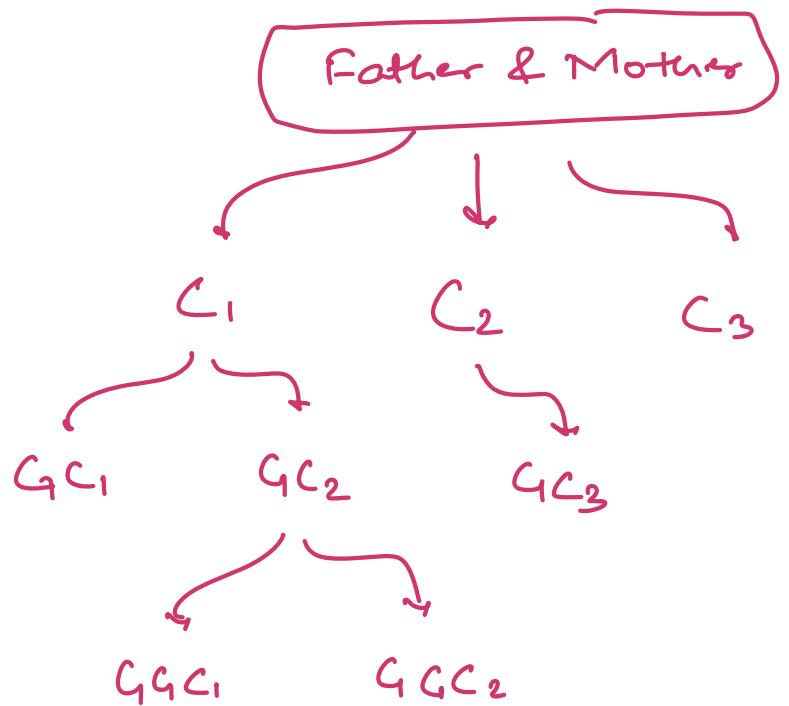


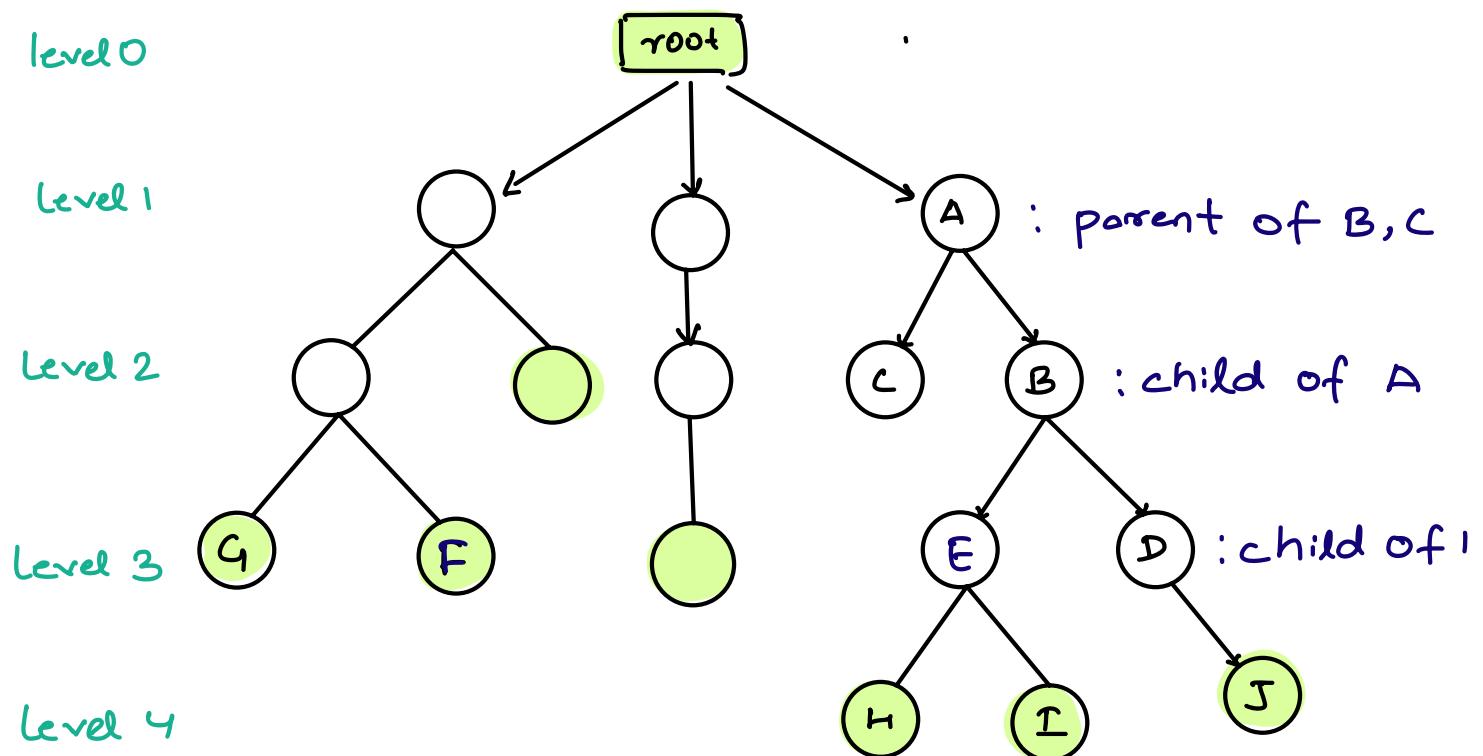
## Hierarchical Data Structure



File system

Family tree





$A \rightarrow D$     A is ancestor of D

D is descendant of A

$B \leftrightarrow C$ , siblings, since same parent

D, E, F → Nodes at same level

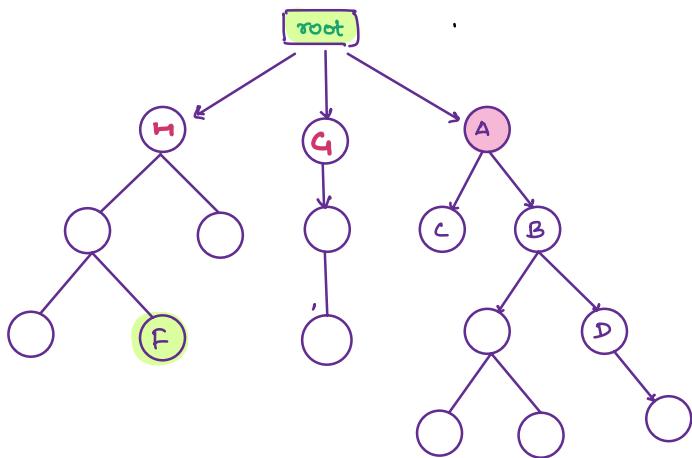
leaf nodes → Nodes with no child

Root → Node without parent

Obs 1 → there is only 1 root node

→ Root node is the ancestor/parent of all the nodes.

Height (node)  $\rightarrow$  length of longest path from node to any of its descendant leaf child



$$\text{Height}(A) = 3$$

$$\text{Height}(G) = 2$$

$$\text{Height}(H) = 2$$

$$\text{Height}(F) = 0$$

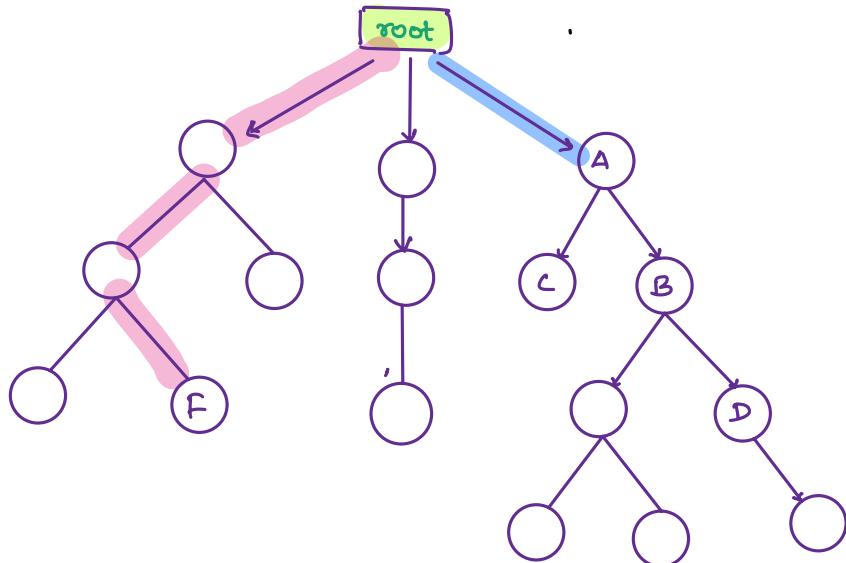
Height (root)

$\hookrightarrow 1 + \max \text{ height among the root children}$

$$\text{Height}(\text{node}) = 1 + \max \text{ height among node children}$$

$$\text{Height}(\text{leaf}) = 0$$

$\text{Depth}(\text{node}) \rightarrow$  length of the path from root node to given node



$$\text{Depth}(A) = 1$$

$$\text{Depth}(F) = 3$$

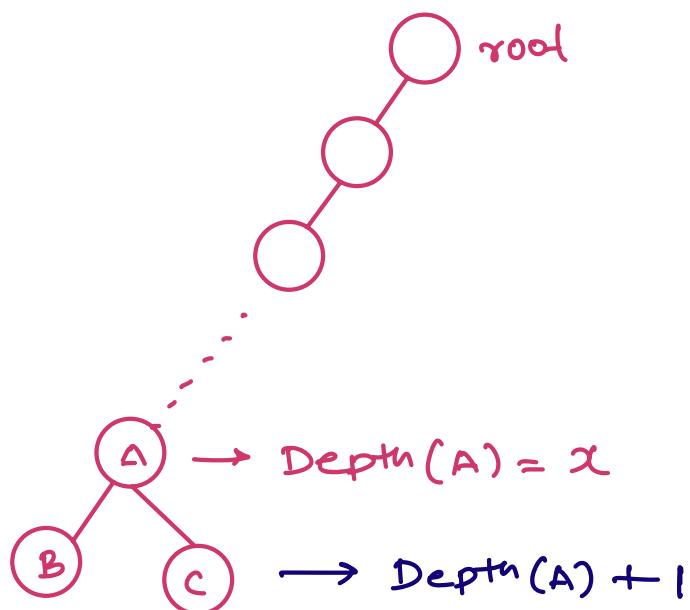
$$\text{Depth}(D) = 3$$

Height = Node to leaf

Depth = Node to root

Obs 1  $\rightarrow$  If depth of a node = d

$$\text{child}(\text{node}) = d + 1$$



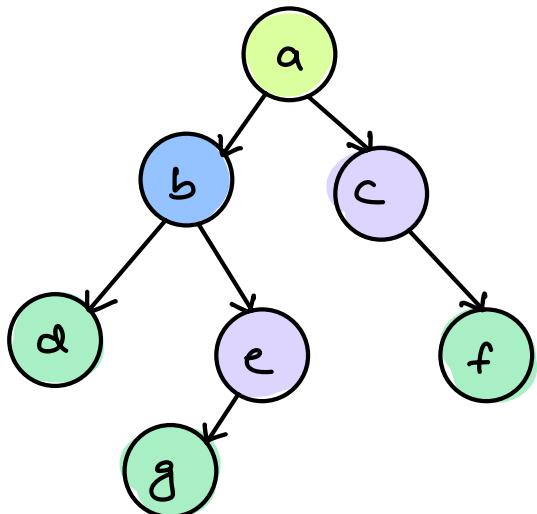
Obs 2  $\rightarrow$  depth of root = 0

$\text{depth}(\text{tree}) = \text{height}(\text{Tree}) = \text{Max level}$

## Binary Tree

↳ Every node is going to have at most 2 children

0, 1, 2, 3, 4  
✓      ✗      ✗



- root node
- node with 2 children
- node with 1 child
- leaf node

\* class Node

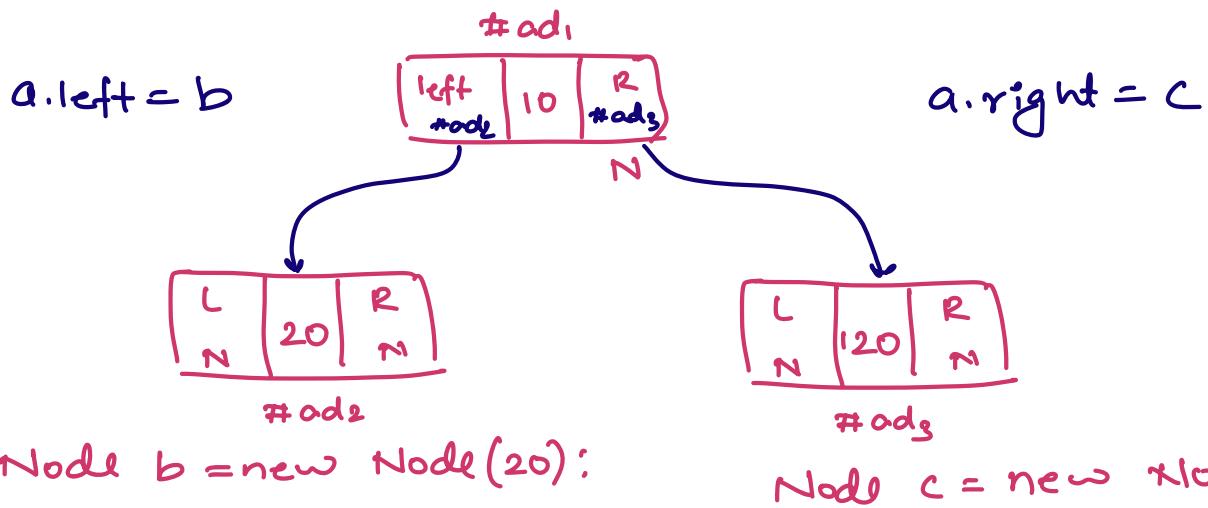
```
int data
Node left; // Obj reference
Node right; // Obj reference

Node (int d) {
    data=d
    left=null;
    right=null;
}
```

class Node

```
int data;
ArrayList<Node> children=new ArrayList();
Node (int d) {
    data=d;
}
```

Node a = new Node(10);



Obs → Given root node, we can traverse the complete tree.

Construction of trees → **Serialization & Deserialization**

of trees

For today's class, Assume we are given with completely constructed Tree

## Tree traversal

- 01. Preorder
- 02. Inorder
- 03. Postorder

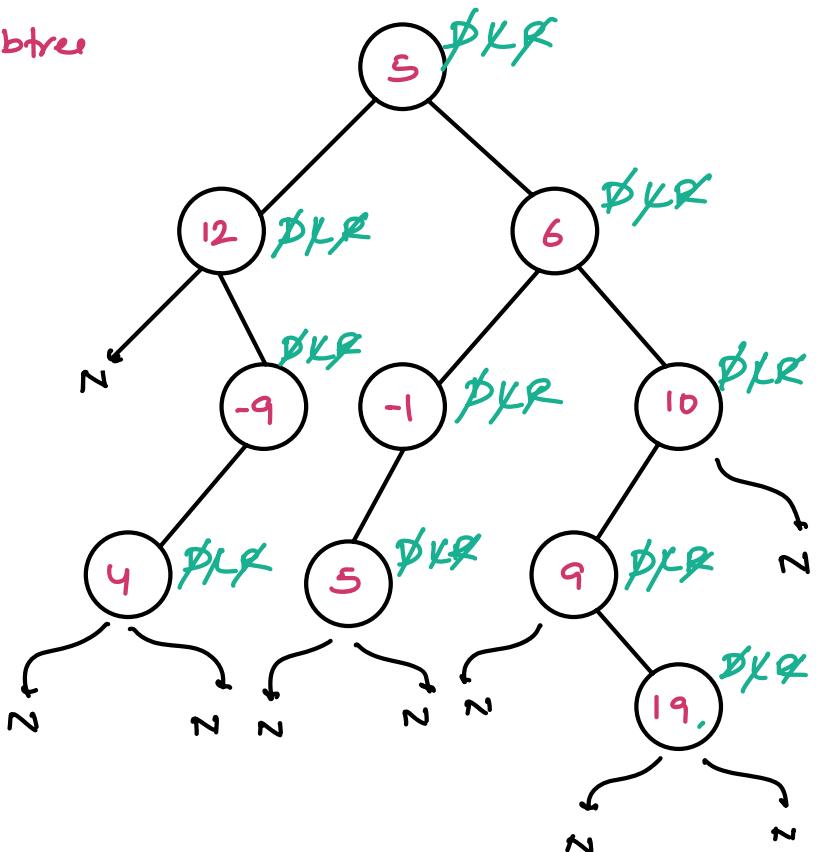
- Level order traversal
- Vertical order traversal
- Morris Inorder traversal

**Preorder** :  $D \ L \ R \rightarrow$  left subtree  
 data ↑ right subtree

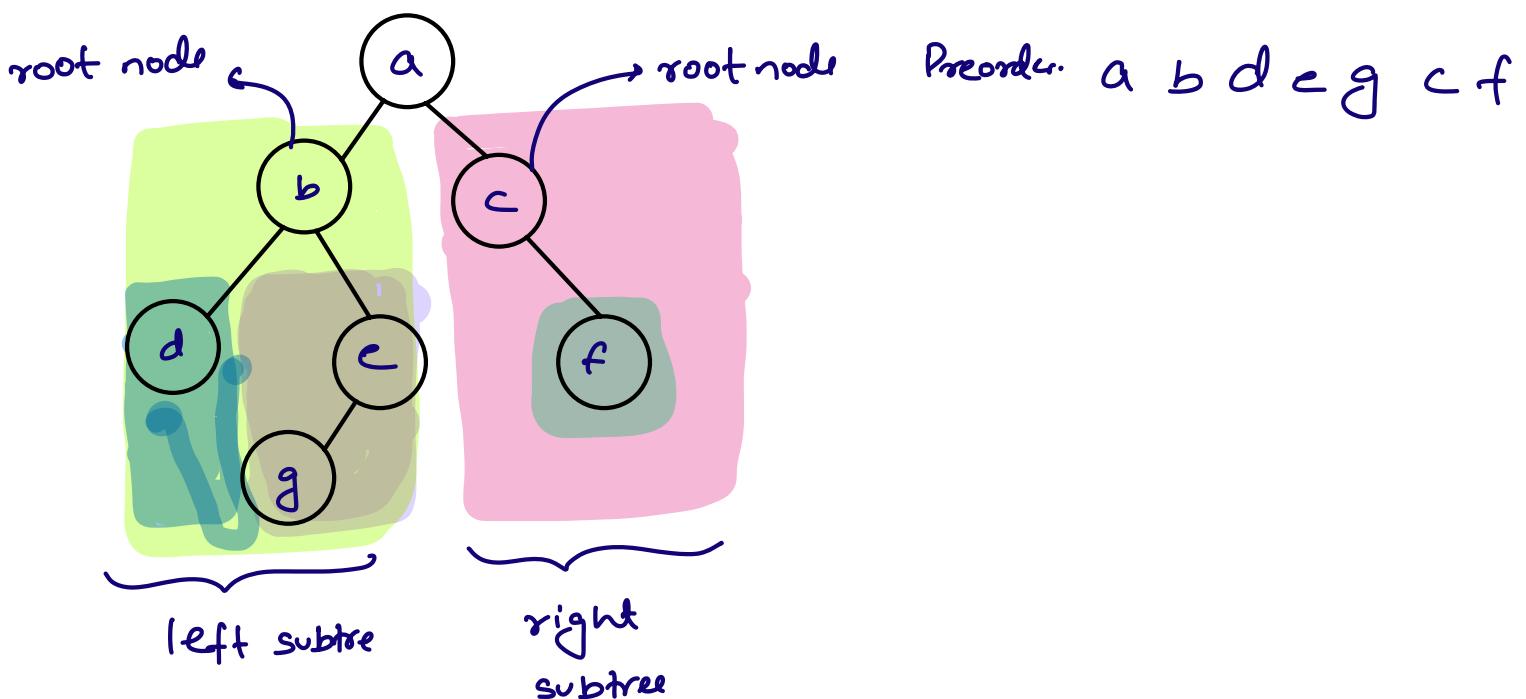
Steps 1 : point (root·data)

Steps 2 : Go to left subtree  
 & point the entire  
 subtree in preorder

Steps 3 : Go to right subtree  
 & point the entire  
 subtree in preorder



Preorder = 5 12 -9 4 6 -1 5 10 9 19



```

void preorder ( Node root )
{
    if ( root == null ) return ;
    print ( root . data )
    preorder ( root . left )
    preorder ( root . right )
}

```

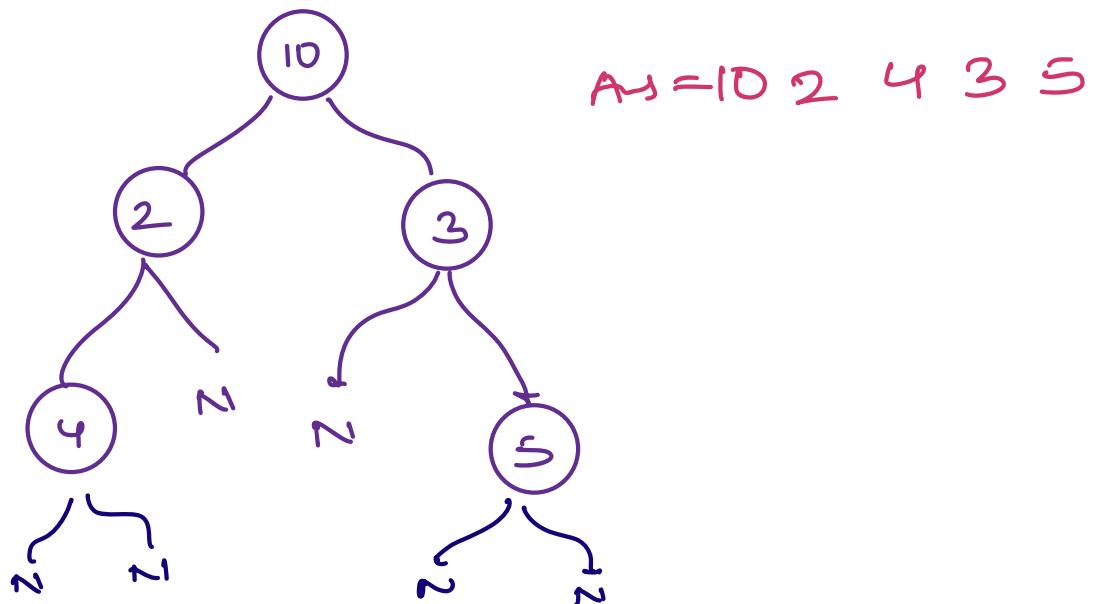
3

count of  
↑ nodes

TC :  $O(n)$

SC :  $O(h)$

height of tree



preorder(10)

x z b y

preorder(2)

y z b y

preorder(3)

x z b y

preorder(4)

x z b y

Preorder( Null )

① 2 3 4

reorder( Null )

① 2 3 4

Preorder( Null )

① 2 3 4

Preorder( Null )

① 2 3 4

preorder(5)

y z b y

reorder( Null )

① 2 3 4

Preorder( Null )

① 2 3 4

Preorder (D L R)

Inorder (L D R)  $\rightarrow$  4 2 10 3 5

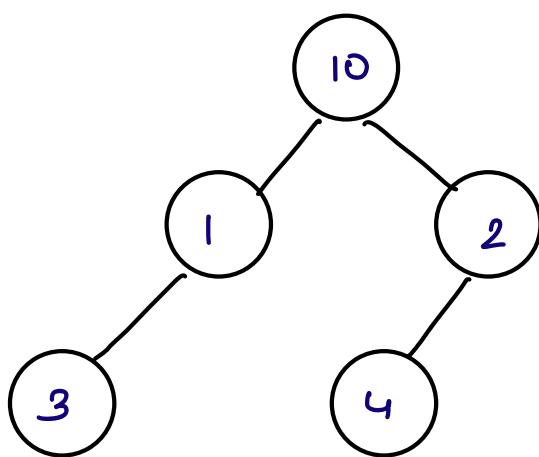
Postorder (L R D)  $\rightarrow$  4 2 5 3 10

Note :— Solve all these question using recursion  
without taking any global variable

(a) size (root)  $\rightarrow$  No. of nodes in tree

(b) sum (root)  $\rightarrow$  sum of nodes of tree

(c) Height (root)  $\rightarrow$  Height of complete tree



```

int size (root)           Ass - Given root , calculate &
{
    if (root==null) return 0      return the no. of nodes

    int l= size (root.left)
    int r= size (root.right)

    return l+r+1;
}

```

3

```

int sum (root)
{
    if (root==null) return 0

    int l= sum (root.left)
    int r= sum (root.right)

    return l+r+root.data;
}

```

3

Calculating height in terms of edges

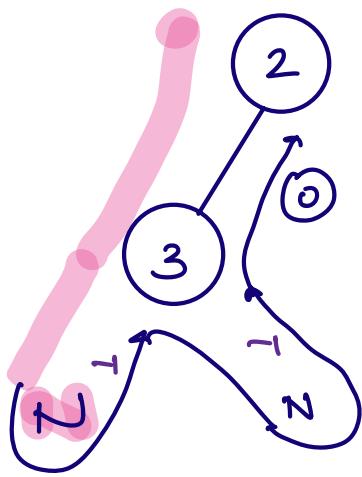
↳ Null return -1

Calculating height in terms of nodes

↳ Null return 0

```
int height (xroot)
{
    if (xroot == null) return -1
    int l = height (xroot.left)
    int r = height (xroot.right)
    return Math.max (l, r) + 1
}
```

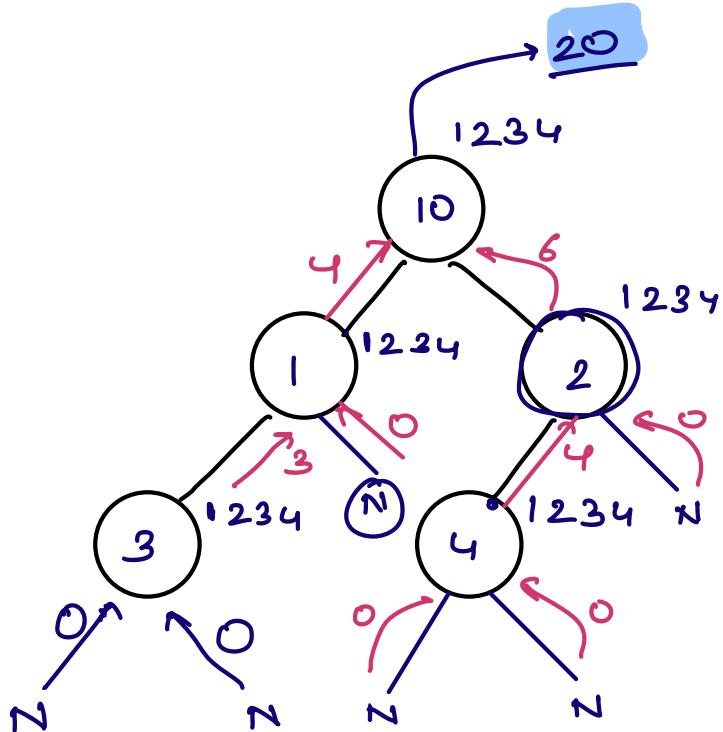
3



```

int sum (root)
{
    if (root == null) return 0
    int l = sum (root.left);
    int r = sum (root.right);
    return l + r + root.data;
}

```



$\left\{ \begin{array}{l} \text{if } (n/2 == 0) \text{ return } 0 \\ \text{int } a = \text{fun}(n-1) \\ \text{int } b = \text{func}(\text{Math.floor}(n/2)); \\ \text{return } a+b \end{array} \right.$

even no.  $\rightarrow O(1)$

$N=13 \rightarrow O(1)$

$N=14 \rightarrow \underline{\underline{O(\log N)}}$

