

1 **Effects of Natural Variability of Seawater Temperature, Time Series Length,**
2 **Decadal Trend and Instrument Precision on the Ability to Detect**
3 **Temperature Trends**

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ABSTRACT

10 In South Africa 129 *in situ* temperature time series of 1 to 43 years are
11 used for investigations of the thermal characteristics of coastal seawater. They
12 are comprised of temperature recordings at precisions ranging from 0.5 °C to
13 0.001 °C and collected with handheld thermometers or underwater tempera-
14 ture recorders (UTRs). Using the naturally occurring range of seasonal sig-
15 nals, variability and temperature trends for 84 of these time series, the length,
16 decadal trend and data precision of each time series were systematically var-
17 ied before fitting generalized least squares (GLS) models to study the effect
18 these variables have on trend detection. We determined that the variables con-
19 tributing most to accurate trend detection in decreasing order are: the length
20 of the time series, the decadal trend, variance, amount of missing data and the
21 precision of the measurements. We found that time series at least 20 years
22 in length may be used tentatively for climate change research, but that time
23 series >30 years in length are preferable. The implication is that long-running
24 thermometer time series in this dataset, and others around the world, are more
25 useful for decadal scale climate change studies than the shorter, more precise
26 UTR time series. It is important to note that due to the nature of the dataset
27 used in this study, instrument drift was not able to be quantified.

28 1. Introduction

29 The roughly 3,000 km of South Africa's coastline is bordered by the Benguela and Agulhas cur-
30 rents (e.g. ??), which, in combination with other nearshore processes, affect the country's marine
31 coastal ecosystems (?). A thorough understanding of these coastal processes is provided by several
32 physical variables, of which temperature is one of the main determinants (e.g. ???). In order to
33 ensure a true representation of organisms' biological thermal limits, nearshore temperatures must
34 be accurately recorded and monitored. Some sources warn of the pitfalls in doing so *RWS: Add*
35 *references here showing which sources say using SST for the coast is inappropriate*, and a study
36 by ? showed that SST data have a warm bias as large as 6 °C when compared to coastal *in situ*
37 data. Nevertheless, a widespread approach in coastal ecological research is to use satellite and/or
38 model-generated temperature data as a representation of the sea surface temperature (SST) along
39 coastlines (e.g. ???), because apparently the dangers of applying gridded SSTs to the coast are not
40 widely known or in many places in the world there simply are no suitable *in situ* coastal tempera-
41 ture time series available. It is for this reason that we strongly recommended the use of *in situ* data
42 to support research conducted within 400 m from the shoreline.

43 Where records of *in situ* coastal seawater temperature do exist, the reliability of many of these
44 datasets that could be used in place of the remotely-sensed SST data remains to be verified. Users
45 of SST data benefit from it being refined through a number of well documented validation and
46 quality control processes (e.g. ???), whereas the standards and methods with which local *in situ*
47 data from a single dataset are collected and refined may differ greatly. For example, there are
48 currently seven organizations and/or governmental departments (hereafter referred to as bodies)
49 contributing coastal seawater temperature data to the South African Coastal Temperature Network
50 (SACTN). These bodies use different methods and instruments to collect their data as no national

51 standard has been set. One consequence of this methodological disparity is that two thirds of the
52 data were sampled with hand-held thermometers that are manually recorded at a data precision of
53 0.5 °C, as opposed to the current generation of Underwater Temperature Recorders (UTRs) with an
54 instrument precision of down to 0.001 °C. If these *in situ* data are to be used together *in lieu* of the
55 satellite-based SST data, it is important that the characteristics of the contributing data sources are
56 understood in terms of their ability to yield useful, reliable and accurate long-term measurements
57 for use in climate change studies.

58 This prompted us to examine the 129 *in situ* time series that comprise the SACTN. The range of
59 measurement precisions and statistical characteristics of this dataset were used to guide a series of
60 enquiry-driven analyses into the suitability of the time series to yield statistically significant and
61 accurate assessments of decadal temperature change. The length, decadal trend and data precision
62 of each time series were adjusted in a systematic manner, and forms the core of our analyses. Our
63 aim was to assess the effect that each of these variables has on the ability of a model to produce
64 a robust estimate of time series decadal trend. The effect gaps in the time series may have on the
65 fitting of models was also investigated as many of the time series used here have some missing
66 data scattered throughout, which is unavoidable for a 20+ year time series that is sampled by hand
67 by a single technician at each site.

68 The study provides a better understanding of some of the determinants of a time series that are
69 influential in the detection success of decadal trends in coastal ocean temperature time series.

70 2. Methods

71 *a. Data Sources*

72 Our study lies within the political borders of South Africa's coastline. The location of each point
73 of collection appears in Figure A1. Of these 129 time series, 43 are recorded with UTRs and the
74 other 86 with hand-held mercury thermometers. The oldest currently running time series began on
75 January 1st, 1972; there are 11 total time series that started in the 70s, 53 more started in the 80s,
76 34 began in the 90s, 18 in the 00s and 13 in the current decade.

77 The data are collected using two different methods and a variety of instruments. Hand-held
78 mercury thermometers (which are being phased out in favor of alcohol thermometers or electronic
79 instruments) are used in some instances at the shoreline, and represent seawater temperatures at the
80 surface. At other places, predominantly along the country's east coast, data are collected with glass
81 thermometers from small boats at the location of shark nets along the coast (?). Whereas both types
82 of thermometers allow for a measurement precision of 0.1 °C, the recordings are written down at
83 a precision of 0.5 °C. Data at other localities are collected using delayed-mode instruments that
84 are permanently moored shallower than 10 m, but generally very close to the surface below the
85 low-water spring tide level.

86 Over the last 40+ years the electronic instruments used to measure coastal seawater temperatures
87 have changed and improved. The previous standard was the Onset Hobo UTR with a thermal
88 precision of 0.01 °C. The new standard currently being phased in is the Starmon Mini UTR. These
89 devices have a maximum thermal precision of $0.001\text{ °C} \pm 0.025\text{ °C}$ (<http://www.star-oddi.com/>).
90 Of the 43 UTR time series in this dataset, 30 were recorded at a precision of 0.001 °C for their
91 entirety, five UTR time series include older data that were recorded at a precision of 0.01 °C or

92 0.1 °C and so have been rounded down to match this level of precision. Eight additional UTR time
93 series have older data that were recorded at a precision of 0.1 °C.

94 The thermometer data are recorded manually and saved in an aggregated location at the head
95 offices of the collecting bodies. UTRs are installed and maintained by divers and data are retrieved
96 at least once annually. These data are digital and are downloaded to a hard drive at the respective
97 head offices of the collecting bodies.

98 *b. Data Management*

99 Each of the seven bodies contributing data to this study have their own method of data for-
100 matted. Steps are being taken towards a national standard as we move towards replacing all the
101 thermometer recordings with UTR devices; however, as of the writing of this article, one does not
102 yet exist. Data from each organization were formatted to a project-wide comma-separated values
103 (CSV) format with consistent column headers before any statistical analyses were performed. This
104 allowed for the same methodology to be used across the entire dataset, ensuring consistent analy-
105 sis. Before analysing the data they were scanned for any values above 35 °C or below 0 °C. These
106 data points were changed to NA, meaning ‘not available’, before including them in the SACTN
107 dataset.

108 All analyses and data management performed in this paper were conducted with R version 3.3.1
109 (2016-06-21) (?). The script and data used to conduct the analyses and create the tables and figures
110 in this paper may be found at https://github.com/schrob040/Trend_Analysis.

111 Any time series with a temporal precision greater than one day were averaged into daily values
112 before being aggregated into the SACTN. A series of additional checks were then performed (e.g.
113 removing long stretches in the time series without associated temperature recordings) and time
114 series shorter than five calendar years or collected at depths greater than 10 m were removed.

115 At the time of this analysis, this useable daily dataset consisted of 84 time series, consisting of
116 819,499 days of data; these data were then binned further to the 26,924 monthly temperature
117 values available for use in this study.

118 *c. Systematic Analysis of Time Series*

119 We used the 84 time series simply for their variance properties (comprised of seasonal, inter-
120 annual, decadal and noise components), which reflect that of the thermal environment naturally
121 present along the roughly 3,000 km of South African coastline. Linear trends that may have been
122 present in each time series were removed prior to the ensuing analysis by applying an ordinary
123 least squares regression and keeping the detrended residuals. In doing so we avoided the need to
124 simulate a series of synthetic time series, whose variance components may not have been fully
125 representative of that naturally present in coastal waters. These detrended time series represent a
126 range of time scales from 72 to 519 months in duration.

127 To each of the 84 detrended time series we artificially added linear decadal trends of 0.00°C to
128 $0.20^{\circ}\text{C dec}^{-1}$. In other words, we now had time series that captured the natural thermal variabil-
129 ities around the coast, but with their decadal trends known *a priori*. The range of decadal trends
130 was selected based around the global average of 0.124°C from ? and used in ?. Furthermore, in
131 order to represent the instrumental precision of the instruments used to collect these time series,
132 we rounded each of these (84 time series \times 5 decadal trends) to four levels of precision: 0.5°C ,
133 0.1°C , 0.01°C and 0.001°C . Consequently, we had a pool of 1,680 time series with which to
134 work.

135 To gain further insight into the effect of time series length on trend detection, each time series
136 was first shortened to a minimum length of 5 years, starting in January so that the timing of the
137 seasonal signal for each time series would be equitable. After fitting the model (see *Time Series*

138 *Model*, below) to all 1,680 of the shortened time series, the next year of data for each time series
139 was added and the models fitted again. This process was iterated until the full length of each time
140 series was attained. For example, if a time series consisted of 12 full years of data, it would require
141 160 models (8 iterations of increasing length \times 5 decadal trends \times 4 levels of precision); similarly,
142 720 models would be applied to a 40 year time series. Considering the 84 time series available,
143 the total number of individual models required to capture each combination of variables quickly
144 increased to 36,220.

145 In order to deal with NAs present in some of the time series, we initially replaced these with
146 linearly interpolated temperature values. It turned out that this was a terrible idea because doing
147 so resulted in artificially increasing the goodness of fit of the detected trend: the degree to which
148 this ‘improvement’ occurs is proportional to the amount of interpolation applied and to the size of
149 the linear decadal trend added (see Appendix A). The analysis presented here therefore proceeded
150 with non-interpolated data only.

151 Our approach of fitting models to each of the semi-artificial time series that we generated allowed
152 us to study the effect that the relevant variables (time series length, natural variability, added
153 slope and level of measurement precision) has on the ability of the time series model to faithfully
154 detect the decadal thermal trend, which was known *a priori*. The primary results of interest in
155 these analyses were the significance (*p*-value) of the model fit, the accuracy of the decadal trend
156 determined by the GLS model as well as the error associated with the trend estimate.

157 *d. Time Series Model*

158 The selection of the appropriate model can greatly influence the ability to detect trends ? and
159 two broad approaches are widely used in climate change research (?). The first group of models
160 estimates linear trends, and although linearity may not reflect reality (*i.e.* trends are very frequently

161 non-linear), these models do provide the convenience of producing an easy to understand decadal
 162 trend (e.g. $0.10^{\circ}\text{C dec}^{-1}$) (?). The other group accommodates non-linear trajectories of temper-
 163 ature through time by the use of higher-degree polynomial terms or non-parametric smoothing
 164 splines, but the inconvenience comes from not being able to easily compare models among sites
 165 (insert refs here). Both groups of models can accommodate serially correlated error structures,
 166 which is often the cause for much criticism due to their effect on the uncertainty of the trend es-
 167 timates (insert refs here). For example, Generalized Least Squares (GLS; yielding estimates of
 168 linear trends) and Generalized Additive Mixed Models (GAMM; non-linear fitting with no trend
 169 estimate provided) can both capture various degrees of serial autocorrelation (??). Although our
 170 exploratory analysis assessed two parameterizations of each of the model groups, we opted to
 171 proceed here with a GLS equipped with a second-order autoregressive AR(2) correlation structure
 172 fitted using Restricted Maximum Likelihood (REML; ?):

$$y_t = \beta_0 + \beta_1 x_t + \varepsilon_t$$

173 where the second-order autoregressive errors are given by

$$\varepsilon_t = \phi_1 \varepsilon_{t-1} + \phi_2 \varepsilon_{t-2} + w_t$$

174 and the white noise series is

$$w_t \sim \text{iid } N(0, \sigma^2)$$

175 This is similar to that of the IPCC, although the latter uses an AR(1) error term. Another dif-
 176 ference from the IPCC approach is that we nested the autoregressive component within year. This
 177 modeling approach allowed us to assess how various properties of the detrended data sets would

178 affect the models' ability to detect trends – in other words, by comparing the estimates of the
179 trends themselves and how these deviate from the known trend.

180 3. Results

181 The resultant residual values from the base 84 detrended time series may be seen in Figure A2.

182 Important variables affecting the accuracy of the slope detected by the GLS model, in decreasing
183 order, are: i) time series length; ii) the size of the added decadal trend; iii) initial SD of the
184 time series (after detrending but prior to adding artificial slopes); iv) the amount of NA; and iv)
185 measurement precision. These variables influence the model fits in a systematic manner.

186 As would be expected, the size of the decadal trend estimated by the GLS increases in direct
187 proportion to the decadal trend which we added and therefore knew *a priori*. What is especially
188 noteworthy in this analysis is that time series of longer duration more often result in trend estimates
189 converging with the actual trend than those of shorter length (Figure A3). This effect is most
190 evident from around 30 years. Furthermore, how well the estimated model trend converges with
191 the actual trend is also very visible in the standard error (SE) of the trend estimate (Figure A4):
192 models fitted to short time series will always have modeled trends with larger SE compared to
193 longer ones. The strength of this correlation is $r = 0.56$ ($p < 0.001$) and it remains virtually
194 unchanged as the added decadal trend increases. The p -value of the fitted models also vary in
195 relation to time series duration and to the steepness of the added decadal trend (Figure A5). It is
196 usually the longer time series equipped with steeper decadal trends that are able to produce model
197 fits with estimated trends that are statistically significant. Note, however, that this p -value tests the
198 null hypothesis that the estimated trend is no different from $0\text{ }^{\circ}\text{C dec}^{-1}$ at $p \leq 0.05$, and *not* that the
199 slope is not different from the added trend. Taken together, these outcomes show that although our
200 GLS model can very often result in trend estimates that *approach* the true trend, it is seldom that

201 those estimates are statistically significant in the sense that the estimated trends differ statistically
202 from $0^{\circ}\text{C dec}^{-1}$.

203 The variance of the detrended data is another variable that can affect model fitting, but its only
204 systematic influence concerns the SE of the trend estimate. Here, it acts in a manner that is entirely
205 consistent across all *a priori* trends (Figure A6). What we see is that as the variance of the data
206 increases (represented here as standard deviation, SD) the SE of the slope estimates increases too.
207 Moreover, it does so disproportionately more for time series of shorter duration. Again, as we
208 have seen with the estimated trend that converges to the true trend around 30 years, so too does
209 the initial SD of the data cease to be important in time series of around 3 decades in length.

210 The number of NAs permitted in any of our time series was limited to 15% per time series.
211 Twenty-five of the 84 time series have fewer than 1% NA. An additional 45 time series have up
212 to 5% NA, 10 have up to 10% NA and 4 have up to 15% NA. The mean number of NA for the data
213 is 2.65%. The relationship between %NA and the *p*-value of the models is shown in Figure A7.
214 At 2.5% or fewer NA their presence does not have any discernible effect on resultant *p*-values.
215 Progressively increasing the number of NAs above 5%, however, leads to a drastic improvement
216 of models fitted to series with no or gently increasing decadal trends (these generally have very
217 large *p*-values indicative of very poor fits, perhaps due to the presence of a very weak signal), and
218 a significant deterioration of models fitted to data with steep decadal trends (for these data, the
219 model generally fits better at low numbers of NAs, as suggested by the greater number *p*-values
220 that approach 0.05). In other words, the inclusion of missing values results in time series with no
221 added decadal trend to veer away from $0^{\circ}\text{C dec}^{-1}$ towards a situation where they may erroneously
222 appear to display a trend. On the other hand, time series that do indeed have decadal trends tend
223 to produce fits that are not significantly different from $0^{\circ}\text{C dec}^{-1}$.

224 Regarding the effect that the level of measurement precision has on the GLS models, we see
225 in Figure A8 that decreasing the precision from 0.001 °C to 0.01 °C has an undetectable effect
226 on any differences in the modeled trends. The Root Mean Square Error (RMSE) between the
227 slopes estimated from 0.001 °C and 0.01 °C data is 0.001. The correspondence between the slopes
228 estimated for data reported at 0.5 °C compared to that at 0.001 °C decreases to a RMSE of 0.03.

229 The effect of decreasing data measurement precision from 0.001 °C to 0.5 °C has almost no
230 appreciable effect on any of the measures of variance presented in this study. The effect of mea-
231 surement precision on the accuracy of the modeled slope, however, becomes very pronounced
232 going from 0.1 °C to 0.5 °C. This effect is larger on smaller decadal trends. For example, at a
233 trend of 0.05 °C dec⁻¹, the deviation from the true value of models fitted to data with a precision
234 of 0.1 °C is negligible; however, the accuracy of the fitted model on data recorded at a precision
235 of 0.5 °C with a real trend of 0.05 °C dec⁻¹ is 10.81% different on average (i.e. given a slope
236 of 0.05 °C dec⁻¹ the model detects slopes of 0.05540 °C dec⁻¹). This accuracy of the models
237 improves to an average difference of 6.44% with a slope of 0.10 °C dec⁻¹, 2.24% at 0.15 °C dec⁻¹
238 and decreases slightly to 2.30% at 0.20 °C dec⁻¹. A precision of 0.5 °C always provides clearly
239 less accurate modeled trends than at higher precisions; however, the current analysis did not high-
240 light one precision that consistently provides the most accurate estimate of the trends. This may
241 however become determinable in an analysis of synthetic data with variance structures that are
242 manipulated in a more consistent manner.

243 As the actual time series used to generate the data for this study are predominantly greater than
244 300 months in length and recorded at a data precision of 0.5 °C, we would be remiss not to inves-
245 tigate the interaction between the increase in accuracy provided by a lengthy time series, against
246 the decrease caused by a data precision of 0.5 °C. In other words, at what point does a model fitted
247 to a longer time series, with less precise measurements (e.g. those taken by thermometers and

reported at a precision of 0.5°C), become as accurate as a time series with more precise measurements (e.g. UTRs)? Figure A8 shows how varied the modeled trends become when a precision of 0.5°C is used, and we see here that when these low resolution time series have a shallow slope of $0.05^{\circ}\text{C dec}^{-1}$, a fitted model requires 24 months of additional data on average to have a comparable level of accuracy to a model fitted to data recorded at a precision of 0.1°C . This difference in length decreases to 16 months when a larger slope $0.20^{\circ}\text{C dec}^{-1}$ is used.

An analysis with a large number of variables as shown here is bound to have a medley of complex interactions between the various statistics being measured; however, much of the range seen in the results of the GLS models can be well explained by the influence of one independent variable, or two operating in concert, as we have shown above. The most important of these variables has clearly been length.

4. Discussion

The strongest finding of this analysis is that the accurate detection of long-term trends in time series primarily concerns the length of a dataset. But there is also a host of nuances resulting from time series length, the steepness of the decadal trend the model is asked to detect, the influence of the SD of a time series, the amount of missing values and the precision at which the data have been measured or recorded that interact with one-another and which must be considered.

Whereas time series with smaller variances (shown as SD in this study) generally produce model fits that are statistically significant (i.e. with decadal trends that are significantly different from $0^{\circ}\text{C dec}^{-1}$ at $p < 0.05$) and with smaller SE of the estimated trends after a shorter lengths of time, we also see that increasing a time series' length beyond 25 years, but preferably beyond 30 years, will increase the likelihood of detecting a decadal temperature change even in very variable data sets. Measuring temperature change in highly variable coastal environments, such as those

271 around the coast of South Africa and many temperate coastal environments globally (refs.), will
272 therefore benefit from access to the longest possible time series available. *Just wondering... do*
273 *time series around the east coast, where temps are generally less variable, converge sooner to*
274 *the actual trend than those along the south coast?.* The detection of long term trends require
275 long-term data. This finding is both positive and negative. The length of a time series needed for
276 climate change research is firmly under the control of the investigator with sufficient foresight and
277 perseverance to plan the installation and management of new instrument networks that will yield
278 usable results only after about three-quarters of a typical academic career has passed. Should
279 such data already exist, and considering the scarcity of such long-term records that are already
280 yielding benefits today, we must ensure that these sources of data are managed and curated with
281 great care and diligence as they are practically irreplaceable. For this reason, it is essential that
282 we understand the inherent strengths and weaknesses of such existing sources of data so that we
283 may fully maximize their utility and extract from them the model coefficients needed for climatic
284 research, and know their accuracy to the best of our ability. There are many time series < 20 years
285 in length that should be avoided, where possible, for trend analysis. These will mature with time
286 and their maintenance need to be ensured going forward.

287 Aside from length, the most powerful time series have measurements that are taken regularly.
288 The inclusion of too many missing values (NAs) in the data sets must be avoided. We have shown
289 that permitting more than 2.5% NAs into our time series has a drastic and significant influence on
290 the chance of committing a type I error (arriving at ‘false positive,’ i.e. detecting a trend when
291 none exists) for time series with no or very gentle decadal trends. On the other hand, the inclusion
292 of NAs in data sets with a decadal trend present tends to cause an increase in the probability of
293 committing a type 2 error (i.e. finding ‘false negatives’). Although our modern UTR data sets
294 have fewer NAs than we should be concerned about – therefore with a low chance of committing

295 type 1 or type 2 errors – the presence of NAs may seriously compromise some of the time series
296 that are still being collected by hand using hand-held thermometers.

297 We have demonstrated clearly that as the steepness of an expected decadal trend increases, the
298 ability for it to be modeled accurately increases, too. Our GLS model is generally not able to detect
299 trends that are significantly different from $0\text{ }^{\circ}\text{C dec}^{-1}$ unless a slope of $0.20\text{ }^{\circ}\text{C dec}^{-1}$ exists. Very
300 rarely were we able to produce significant model fits at shallower slopes. Finding significant
301 trends at $< 0.05\text{ }^{\circ}\text{C dec}^{-1}$ was not possible. *Rob, how long does a data set have to be for a*
302 *slope of $0.05\text{ }^{\circ}\text{C dec}^{-1}$ to be detected? Or of $0.05\text{ }^{\circ}\text{C dec}^{-1}$, which is around the global mean?.*
303 This finding is somewhat discouraging as most global analyses of decadal SST change based on
304 gridded SST products estimate a trend closer to $0.1\text{ }^{\circ}\text{C dec}^{-1}$ (refs.). This means that the trends
305 present in most time series representative of very variable coastal environments that exhibit the
306 same variance structure as that of our data are probably unlikely to be detected as significant, even
307 if they do indeed exist. In other words, the chance of committing a type 2 error is probably very
308 real for such systems, unless time series of XX years or longer are available.

309 One of the motivators for this paper was to investigate the effect measurement precision has on
310 a time series' ability to produce results useful for investigations of long-term climate change, and
311 to validate the use of the low precision $0.5\text{ }^{\circ}\text{C}$ thermometer data. Whereas the precision of these
312 data is below the current standard of $0.1\text{ }^{\circ}\text{C}$ required for climate change research (*ref. - I think it*
313 *is a WMO report of the 2000s; I'll find it*), the length of the thermometer time series makes them
314 a valuable asset. We have shown that the negative effect low precision has on the accuracy of a
315 model can be adjusted for with an additional 24 months of data. *Something needs to be said about*
316 *the effect of measurement precision prior to this paragraph, probably immediately before.* The
317 average length of the thermometer time series in the SACTN, from which the 84 time series used
318 in this study were drawn, is 349 months. The average length of the UTR time series is 167 months.

319 Given this difference in the lengths of the time series, even after correcting for the negative effect
320 of low measurement precision, at this point in time the time series collected with thermometers
321 are more useful for climate change research than the UTR time series within the SACTN.

322 We have reflected on the importance of the accuracy of the models, and not only on the impor-
323 tance of their of significance. Indeed, the p -value given for the slope in a model does not show
324 how well the model detects the true trend in the data (known *a-priori* in this study); rather, it
325 tells us if the detected trend is significantly different from $0^{\circ}\text{C dec}^{-1}$. This is not particularly
326 useful for applying the results of climate change research more broadly to biotic interests. That
327 a long term trend does exist, may be accurately detected by a model and related to an observed
328 change in the natural world – such as range expansion/contraction of coastal biota (cite: Bolton)
329 – is more important than whether or not the model can show if that trend is significantly different
330 from $0^{\circ}\text{C dec}^{-1}$ in a statistical sense. *I wonder if there is a way to test if the modeled slope is*
331 *statistically different from the know slope... Just wondering.*

332 *Not so sure what the point of this is, or what it actually means: I'm not really sure what good the*
333 *above paragraph is but I think it's pretty interesting and there is definitely something important to*
334 *be taken away from that finding.*

335 *Rob, did you not show me today that the precision does indeed have a role to play? below...*

336 The meta-data pertaining to these older temperature records and to those that came before, such
337 as the instrumentation used and the motivation behind the levels of precision at which the data
338 were recorded, have over time been lost, highlighting the issues of staff rotation in government
339 departments and the importance of implementing meta-data standards at a very early stage in any
340 monitoring programme. An additional issue with these older time series is that there has been no
341 effort to enforce instrument fidelity per site, and worse, the types of instruments (e.g. going from

mercury to alcohol thermometers) is not recorded. Therefore the effects that this may have on the time series cannot be quantified in this paper.

RWS: None of this text has been edited. I must still do so.

5. Conclusion

We draw several key conclusions:

1. There is not a significant relationship between the goodness of fit (R^2) of a linear model to a time series and the NA% of that time series when the NAs are filled in via linear interpolation. This is an important finding as it means that, within reason, linear interpolation may be used to fill gaps in a time series before applying any time series analysis methods.
2. Length has the largest effect on the goodness of fit (R^2) of the decadal trend and natural variability (SD) has the largest effect on the significance (p) of the trend detected.
3. There is a predictable decrease in the goodness of fit (R^2) of a linear model to the trend line of a time series as it extends from 10 to 20 years in length. The goodness of fit (R^2) then begins to increase once the time series becomes roughly 30+ years long. Analyses of time series at or under 10 years in length should be interpreted with extreme caution in spite of them often having strong R^2 values.
4. Within the first decade of a time series, if the temperatures within the last few months move strongly in the opposite direction from the prevailing trend, the linear model used to detect the trendline may show an abrupt change in direction (i.e. a positive trend can become negative and *vice versa*).

5. After the first decade of data, the changes detected in almost all trends for all 105 time series become more gradual; however, many trend lines still change direction over the course of the following two decades.
6. It is at these changes in direction that the p -values for the time series plummet, though generally they tend to follow the same pattern of becoming weaker and then slowly stronger over time, as we see in the R^2 values.
7. There is a slight linear decrease in R^2 as the natural thermal variability (SD) of seawater increases; however, the decrease in p -values is larger and more rapid.
8. A precision greater than $0.5\text{ }^{\circ}\text{C}$ is not required to confidently detect the long-term trend in a time series. This is an important consideration as many studies investigating the effects of climate change (e.g. ???) do use lower precision $0.1\text{ }^{\circ}\text{C}$ data. That being said, a precision of $0.001\text{ }^{\circ}\text{C}$ or $0.01\text{ }^{\circ}\text{C}$ is preferable over $0.5\text{ }^{\circ}\text{C}$. In fact, because the results from the higher precision of $0.001\text{ }^{\circ}\text{C}$ were almost identical to the $0.5\text{ }^{\circ}\text{C}$ tests, the higher precision is only necessary when one needs to identify trends at a precision of $0.01\text{ }^{\circ}\text{C}$ or greater (?). This finding means that older, lower precision data may be combined with newer higher precision data within the same time series without concern that the reduced overall data precision will have a large negative impact on the time series ability to detect decadal trends. Indeed, extending time series in this way will only serve to make them more dependable as length is the primary criteria through which one should initially assess a time series ability to detect climate change before refining ones assumptions with any statistical analyses.
9. Decreasing the precision of measurements to greater than $0.1\text{ }^{\circ}\text{C}$ has almost no appreciable effect on a time series ability to detect a long term trend, provided that the reported effect size matches the level of precision by the instruments.

385 We understand that time series of >30 years may be exceedingly rare. Therefore, while we
386 move forward as a scientific community investigating the issues of climate change, the increasing
387 length and continuity of any current and future time series must be ensured in order to construct and
388 maintain a clear understanding of the trends in changing temperature that are occurring throughout
389 Earth's oceans.

390 *Acknowledgments.* The authors would like to thank DAFF, DEA, EKZNSW, KZNSB, SAWS and
391 SAEON for contributing all of the raw data used in this study. Without it, this article and the
392 SACTN would not be possible. This research was supported by NRF Grant (CPRR14072378735).
393 The authors report no financial conflicts of interests. The data and analyses used in this paper may
394 be found at https://github.com/schrob040/Trend_Analysis.

395 APPENDIX A

396 **Effects of linear interpolation**

397 Blurb here about linear interpolation effects.... Figure A9. *RWS - This figure still needs to be*
398 *updated to the current standard. It is still a rough draft.*

399	LIST OF FIGURES	
400	Fig. 1. The location of each time series available for use in this study	21
401	Fig. 2. The effect of time series length on the ability of the GLS model to accurately detect the trend added to a	
402	time series	22
403	Fig. 3. The relationship between time series length and the standard error (SE) of the modelled trend	23
404	Fig. 4. The effect of the natural variation of a time series on the significance of the modelled trend	24
405	Fig. 5. The relationship between the effect of initial SD on the SE of a modelled trend	25
406	Fig. 6. The relationship between %NA and the significance of a fitted trend	26
407	Fig. 7. The minimal effect of rounding from	27
408	Fig. 8. Similar to Figure ??, this figure shows the effect missing data have on	28

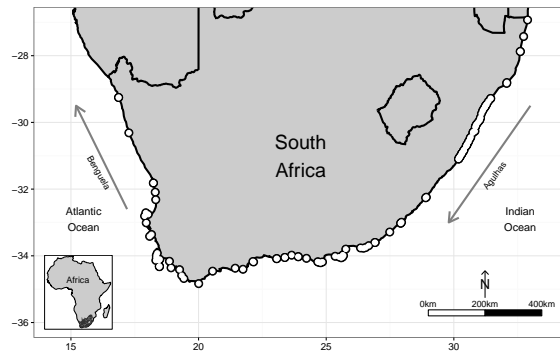


FIG. 1. The location of each time series available for use in this study.

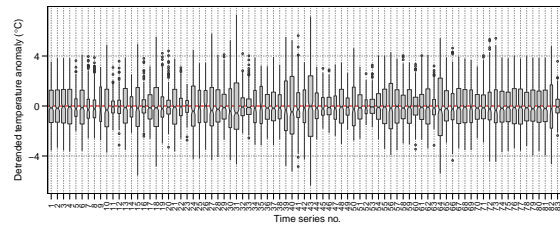


FIG. 2. Box and whisker plots of the base 84 time series used in this study after detrending but before changing the length, adding a decadal trend or rounding the data.

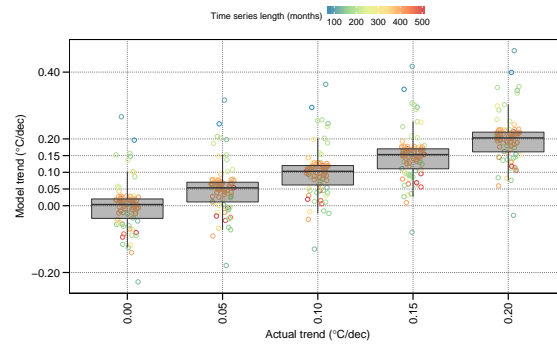


FIG. 3. The effect of time series length on the ability of the GLS model to accurately detect the trend added to each time series. The box-and-whisker plots show the first and third quartile as the extremities of the boxes, the median is shown as the horizontal line within each box, and the minima and maxima are indicated by the whiskers. Points indicate the spread of the actual data points and their colors are scaled according to the length of the time series.

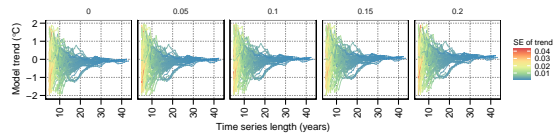


FIG. 4. The relationship between the length of a time series, the size of the modeled trend and its the standard error (SE). Each individual line shows the modeled trend for one of the 84 sites used in this analysis to which a model was fitted iteratively as the time series length was ‘grown’ from 5 years in length to the maximum duration available for the site.

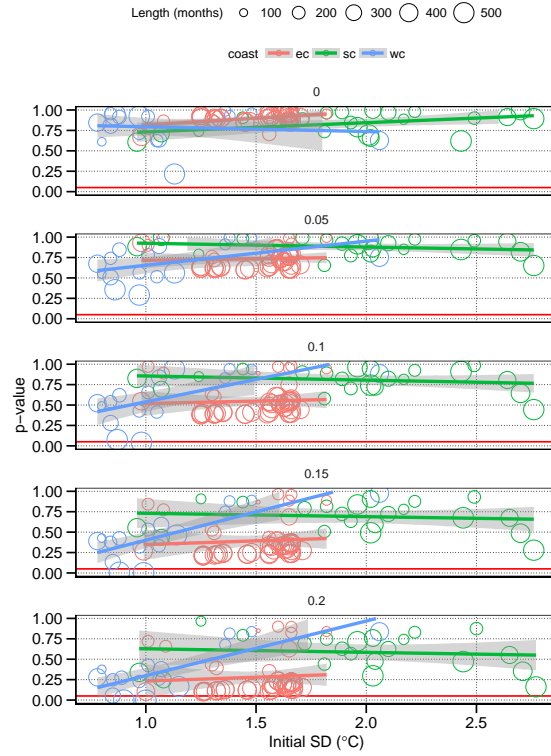


FIG. 5. The effect of the natural variation of a time series on the significance of the modelled trends estimated by the GLS. The size of the symbols are scaled proportionally to the time series length, with longer time series shown as larger circles.

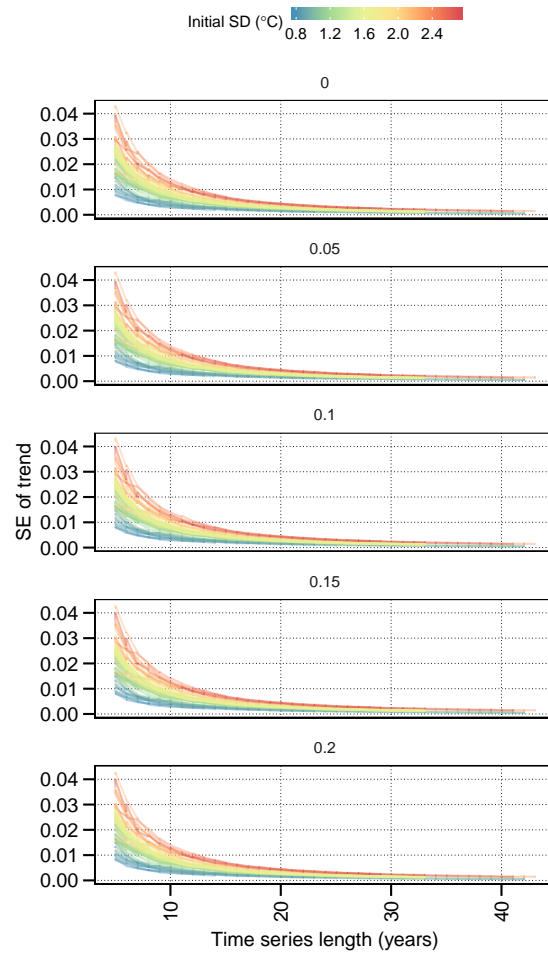


FIG. 6. The relationship between the effect of the initial SD of a time series on the SE of a modelled trend,
controlled for by the length of the time series.

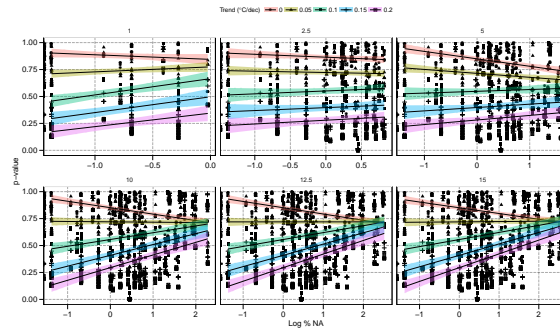


FIG. 7. The relationship between %NA and the significance of a fitted trend. Each panel shows the effect of an increasingly larger amount of missing values. The the fitted lines and 95% confidence intervals represent each of the five decadal trends assessed.

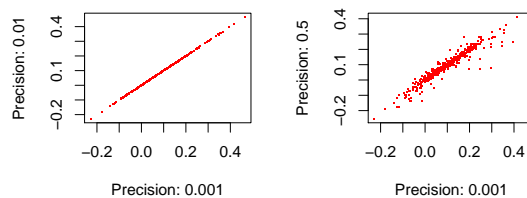


FIG. 8. The minimal effect of rounding from 0.001 °C to 0.01 °C may be seen in the panel on the right. The panel on the left shows that rounding from a precision of 0.001 °C to 0.5 °C has a more appreciable effect.

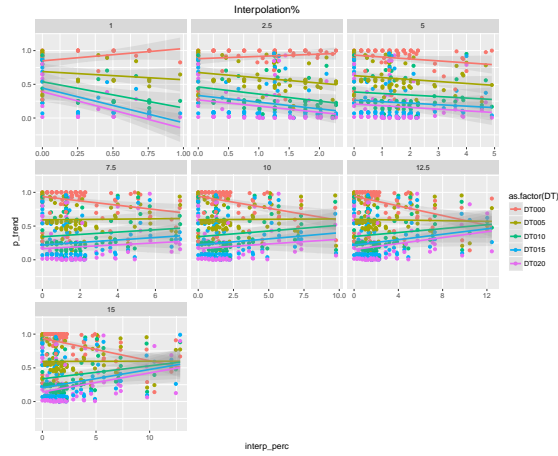


FIG. 9. Similar to Figure A7, this figure shows the effect missing data have on the significance of the slopes detected by GLS however; the missing values in the time series have been filled here via linear interpolation. The effect this has on the significance of the modeled trends is both immediate and dramatic. The behaviour of the quantity of interpolated data also differs from the effect of data left simply as NA. At lower levels of interpolation, missing data actually aid in the fitting of a more significant trend line. This phenomena reverses around 5%NA when the relationship becomes negative, meaning that as the amount of interpolated data increase, the significance of the fitted trend decreases.