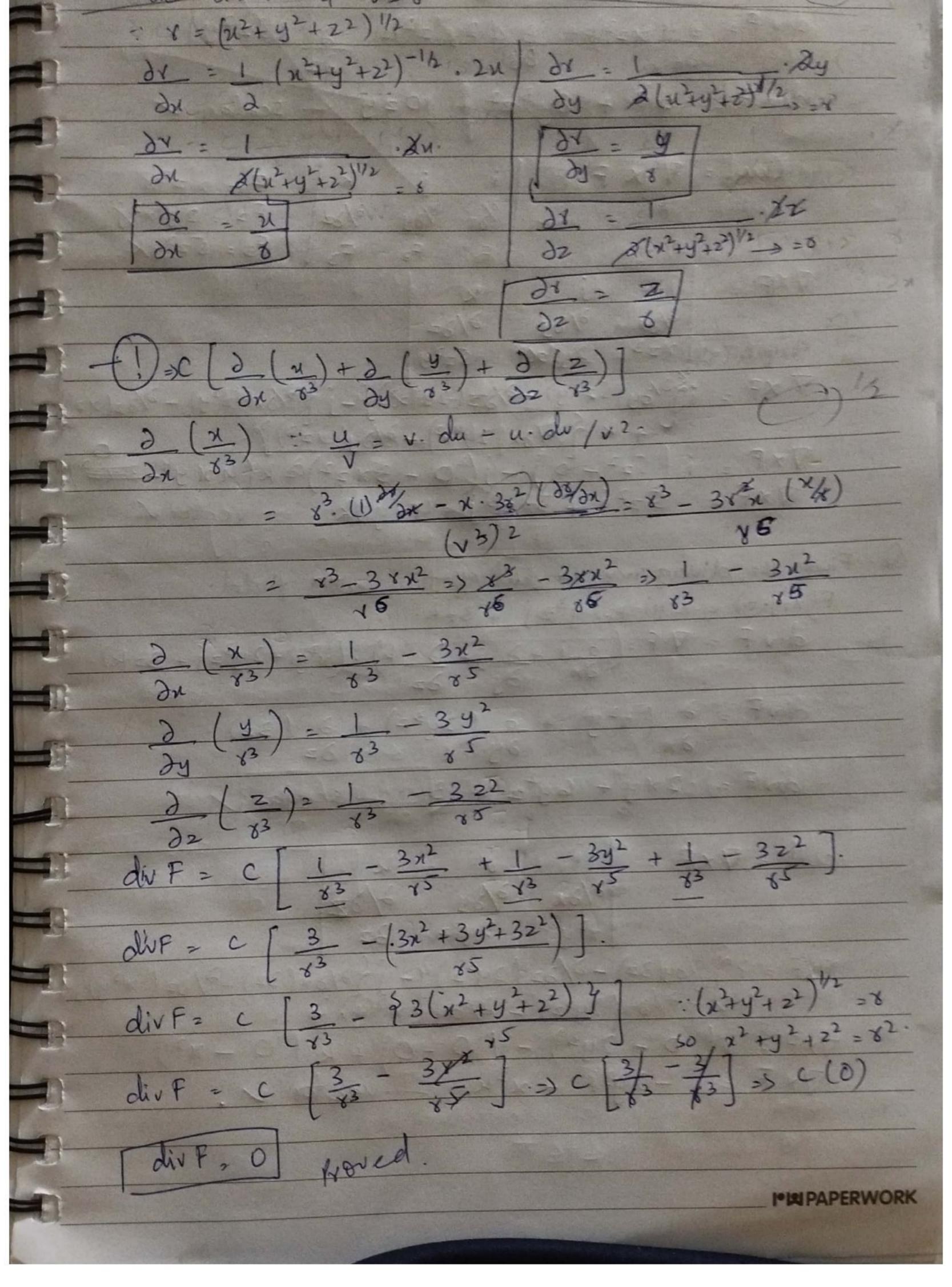
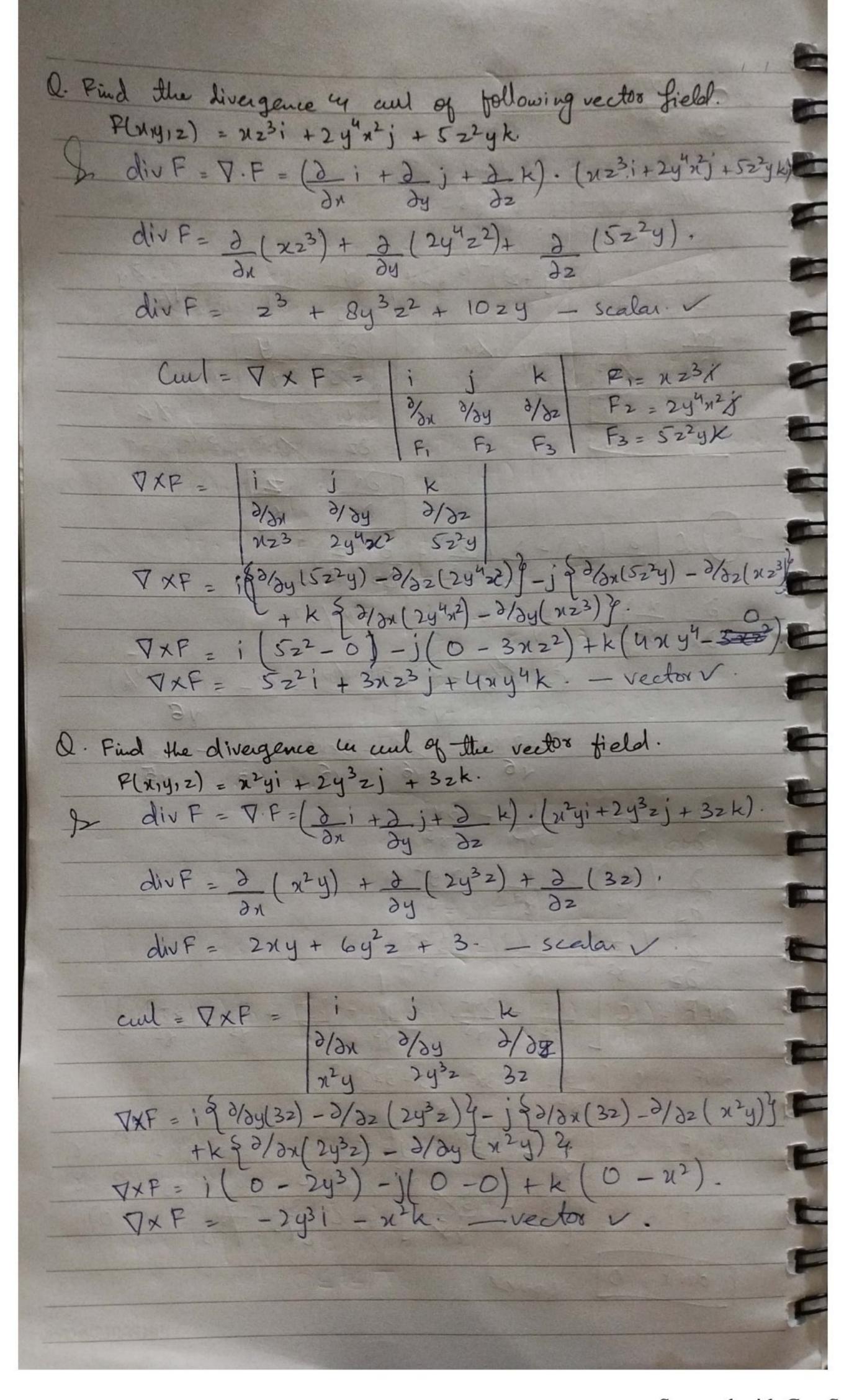
VECTOR FIELD: F(x,y) - f(x,y)i + g(x,y)j -> 2 space F(x,y,z)=f(x,y)+g(x,y)z)j+h(x,y,z)k -> 3 space Inverse square field. F(8) = C , 8 is readless vectors en e 15 a. ..P(x,y) = c .(xi+yj). 8 = 76i + 14j (x+y)3/2 x=xi+yj+zk. : F(x14,2) = c (xi+ yj+2+) (21+4+2)3/2 Inverse square fields are conservative in any region that does not contain the origin E.g.  $\phi(x,y) = -\frac{c}{(x^2+y^2)^{1/2}}$  is a patential function ∇Φ(x)y) = ∂Φ + ∂Φ j.  $= \frac{Cx}{(x^2+y^2)^{\frac{3}{2}}} + \frac{cy}{(x^2+y^2)^{\frac{3}{2}}}$ c (ni+ yj) Ex. Show that divergence of inverse squae field

F(x,y,z) = c (xi+yj+zk) is zer

(x2+y2+z2)3/2 F(x, y, z)





Vector field again Q Confirm that "o" is a potential function or not. (i)  $\phi(x,y) = 2y^2 + 3x^2y - xy^3$ F(x,y)= 2xi+ 6yj +8zk. If F= VØ, it is a potential function else not ·  $\nabla \phi = (\frac{1}{2}i + \frac{1}{2}j) \phi (n,y)$ = \( \frac{1}{2} \) \( \left( 2y^2 + 3x^2y - xy^3 \).  $= \frac{\partial}{\partial x} i \left( 2y^2 + 3x^2y - xy^3 \right) + \frac{\partial}{\partial y} i \left( 2y^2 + 3x^2y - xy^3 \right).$ 0 + Bny- == 3 i + (4y + 3n2 - 3 my 2)j. since F + VO, & is not a potential O(x, y, z) = x sinz + y sinx + 2 siny  $F(x,y,z) = (\sin z + y\cos x)i + (\sin x + z\cos y)j + (\sin y + u\cos z)k.$   $F(x,y,z) = (\frac{\partial}{\partial x}i + \frac{\partial}{\partial y}j + \frac{\partial}{\partial z}k) \Phi(x,y,z)$ **PURIPAPERWORK** 

= (Sin 2 + y (0) x +0) i + (0+ Sin x + 2 cosy) j + (100 2 +0+ Siny) k. VQ = (Sinz + 9005x)1 + (Sinx + 2005y)1 + (Siny + x1052) K Since F = VØ, it is a potential function Consevative en Non-Conservative fields. F(x,y) = f(x,y)i+g(x,y)j. H if  $\partial f = \partial g$  (conservative) 24 dx else non-conservation 10it is valid for 2-space. F(x1412) = f(x1412) i + g(x1412) j + h(x14+2) k. if VXF =0 (conservative) else non-conservative 惍 X08 3-8 pace -Q. Whether the field is conservative or not. (i) F(x1y) = 2xy3 i+ (1+3x2y2)j  $4 + (x,y) = 2x^4y^3$   $g(x,y) = 1+3x^2y^2$  $\frac{\partial f}{\partial t} = 6 \pi y^2$